# N-Dimensional Lists (ndlist)

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https://github.com/ambaker1/ndlist

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#### Abstract

In Tcl, everything is a string, and most things are lists. This package expands on this, by proposing a new paradigm for Tcl: everything is an ND-list.

This package is also a Tin package, and can be loaded in as shown below:

#### Example 1: Installing and loading "ndlist"

#### Code:

package require tin 2.1
tin autoadd ndlist https://github.com/ambaker1/ndlist install.tcl
tin import ndlist

# 1-Dimensional Lists (Vectors)

Lists are foundational to Tcl, so in addition to providing utilities for ND-lists, this package also provides utilities for working with 1D-lists, or vectors.

# Range Generator

The command *range* simply generates a list of integer values. This can be used in conjunction with the Tcl foreach loop to simplify writing "for" loops. There are two ways of calling this command, as shown below.

```
range $n
range $start $stop <$step>
```

\$n Number of indices, starting at 0 (e.g. 3 returns 0 1 2).

\$start Starting value. \$stop Stop value.

**\$step** Step size. Default 1 or -1, depending on direction of start to stop.

```
Example 2: Integer range generation

Code:

puts [range 3]
puts [range 0 2]
puts [range 10 3 -2]

Output:

0 1 2
0 1 2
10 8 6 4
```

```
Example 3: Simpler for-loop

Code:
   foreach i [range 3] {
      puts $i
   }

Output:
   0
   1
   2
```

# Logical Indexing

The command find returns the indices of non-zero elements of a boolean list, or indices of elements that satisfy a given criterion. Can be used in conjunction with nget to perform logical indexing.

#### find \$list <\$op \$scalar>

\$list List of values to compare.

**\$op** Comparison operator. Default "!=".

**\$scalar** Comparison value. Default 0.

#### Example 4: Filtering a list

#### Code:

```
set x {0.5 2.3 4.0 2.5 1.6 2.0 1.4 5.6}
puts [nget $x [find $x > 2]]
```

#### Output:

2.3 4.0 2.5 5.6

### Linear Interpolation

The command *linterp* performs linear 1D interpolation. Converts input to double.

#### linterp \$x \$xList \$yList

\$x Value to query in \$xList

**\$xList** List of x points, strictly increasing

**\$yList** List of y points, same length as **\$xList** 

#### Example 5: Linear interpolation

#### Code:

```
puts [linterp 2 {1 2 3} {4 5 6}]
puts [linterp 8.2 {0 10 20} {2 -4 5}]
```

#### Output:

5.0 -2.92

#### Vector Generation

The command *linspace* can be used to generate a vector of specified length and equal spacing between two specified values. Converts input to double.

#### linspace \$n \$start \$stop

\$n Number of points \$start Starting value \$stop End value

#### Example 6: Linearly spaced vector generation

Code:

puts [linspace 5 0 1]

Output:

0.0 0.25 0.5 0.75 1.0

The command *linsteps* generates intermediate values given an increment size and a sequence of targets. Converts input to double.

#### linsteps \$step \$x1 \$x2 ...

\$step Maximum step size \$x1 \$x2 ... Targets to hit.

#### Example 7: Intermediate value vector generation

Code:

puts [linsteps 0.25 0 1 0]

Output:

0.0 0.25 0.5 0.75 1.0 0.75 0.5 0.25 0.0

## Functional Mapping

The command lapply simply applies a command over each element of a list, and returns the result. The command lapply2 maps element-wise over two equal length lists.

#### lapply \$command \$list \$arg ...

#### lapply2 \$command \$list1 \$list2 \$arg ...

\$list List to map over.

\$list1 \$list2 Lists to map over, element-wise.

\$command Command prefix to map with.

**\$arg** ... Additional arguments to append to command after list elements.

#### Example 8: Applying a math function to a list

#### Code:

# Add Tcl math functions to the current namespace path
namespace path [concat [namespace path] ::tcl::mathfunc]
puts [lapply abs {-5 1 2 -2}]

Output:

5 1 2 2

#### Example 9: Mapping over two lists

#### Code:

lapply puts [lapply2 {format "%s %s"} {hello goodbye} {world moon}]

Output:

hello world goodbye moon

#### List Statistics

The commands max, min, sum, product, mean, median, stdev and pstdev compute the maximum, minimum, sum, product, mean, median, sample and population standard deviation of values in a list. For more advanced statistics, check out the Tellib math::statistics package.

```
max $list

min $list

sum $list

product $list

mean $list

median $list

stdev $list
```

\$list

List to compute statistic of.

```
Example 10: List Statistics

Code:

set list {-5 3 4 0}
foreach stat {max min sum product mean median stdev pstdev} {
 puts [list $stat [$stat $list]]
}

Output:

max 4
min -5
sum 2
product 0
mean 0.5
median 1.5
stdev 4.041451884327381
pstdev 3.5
```

# Vector Algebra

The dot product of two equal length vectors can be computed with dot. The cross product of two vectors of length 3 can be computed with cross.

# dot \$a \$b

#### cross \$a \$b

\$a First vector.
\$b Second vector.

The norm, or magnitude, of a vector can be computed with *norm*.

#### norm \$a <\$p>

\$a Vector to compute norm of.

\$p Norm type. 1 is sum of absolute values, 2 is euclidean distance, and Inf is

absolute maximum value. Default 2.

# Example 11: Dot and cross product

Code:

set x {1 2 3}
set y {-2 -4 6}
puts [dot \$x \$y]
puts [cross \$x \$y]

#### Output:

8 24 -12 0

For more advanced vector algebra routines, check out the Tcllib math::linearalgebra package.

# 2-Dimensional Lists (Matrices)

A matrix is a two-dimensional list, or a list of row vectors. This is consistent with the format used in the Tellib math::linearalgebra package. See the example below for how matrices are interpreted.

$$A = \begin{bmatrix} 2 & 5 & 1 & 3 \\ 4 & 1 & 7 & 9 \\ 6 & 8 & 3 & 2 \\ 7 & 8 & 1 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} 9 \\ 3 \\ 0 \\ -3 \end{bmatrix}, \quad C = \begin{bmatrix} 3 & 7 & -5 & -2 \end{bmatrix}$$

```
Example 12: Matrices and vectors
Code:
  # Define matrices, column vectors, and row vectors
  set A {{2 5 1 3} {4 1 7 9} {6 8 3 2} {7 8 1 4}}
  set B {9 3 0 -3}
  set C \{\{3\ 7\ -5\ -2\}\}
  # Print out matrices (join with newline to print out each row)
  puts "A ="
  puts [join $A \n]
  puts "B ="
  puts [join $B \n]
 puts "C ="
 puts [join $C \n]
Output:
  2 5 1 3
  4 1 7 9
  6 8 3 2
 7 8 1 4
  3
  0
 -3
 C =
  3 7 -5 -2
```

# Combining Matrices

The commands stack and augment can be used to combine matrices, row or column-wise.

```
stack $mat1 $mat2 ...
```

```
augment $mat1 $mat2 ...
```

\$mat1 \$mat2 ... Arbitrary number of matrices to stack/augment (number of columns/rows must match)

The command *block* combines a matrix of matrices into a block matrix.

#### block \$matrices

\$matrices

Matrix of matrices.

```
Code:
    set A [stack {{1 2}} {{3 4}}]
    set B [augment {1 2} {3 4}]
    set C [block [list [list $A $B] [list $B $A]]]
    puts $A
    puts $B
    puts [join $C \n]; # prints each row on a new line

Output:
    {1 2} {3 4}
    {1 3} {2 4}
    1 2 1 3
    3 4 2 4
    1 3 1 2
    2 4 3 4
```

# Matrix Transpose

The command transpose simply swaps the rows and columns of a matrix.

#### transpose \$A

\$A

Matrix to transpose, nxm.

Returns an mxn matrix.

# Example 14: Transposing a matrix Code: puts [transpose {{1 2} {3 4}}] Output: {1 3} {2 4}

# Matrix Multiplication

The command matmul performs matrix multiplication for two matrices. Inner dimensions must match.

#### matmul \$A \$B

\$A

Left matrix, nxq.

\$В

Right matrix, qxm.

Returns an nxm matrix (or the corresponding dimensions from additional matrices)

#### Example 15: Multiplying a matrix

Code:

puts [matmul {{2 5 1 3} {4 1 7 9} {6 8 3 2} {7 8 1 4}} {9 3 0 -3}]

Output:

24 12 72 75

# Miscellaneous Linear Algebra Routines

The command eye generates an identity matrix.

#### eye \$n

\$n

Size of identity matrix

The command *outerprod* takes the outer product of two vectors,  $\mathbf{a} \otimes \mathbf{b} = \mathbf{a} \mathbf{b}^T$ .

#### outerprod \$a \$b

\$a \$b

Vectors with lengths n and m. Returns a matrix, shape nxm.

The command kronprod takes the Kronecker product of two matrices, as shown in Eq. (1).

#### kronprod \$A \$B

\$A \$B

Matrices, shapes nxm and pxq. Returns a matrix, shape (np)x(mq).

$$\mathbf{A} \otimes \mathbf{B} = \begin{bmatrix} a_{11}\mathbf{B} & \dots & a_{1n}\mathbf{B} \\ \vdots & \ddots & \vdots \\ a_{n1}\mathbf{B} & \dots & a_{nn}\mathbf{B} \end{bmatrix}$$
 (1)

```
Example 16: Outer product and Kronecker product

Code:

set A [eye 3]
set B [outerprod {1 2} {3 4}]
set C [kronprod $A $B]
puts [join $C \n]; # prints out each row on a new line

Output:

3 4 0 0 0 0
6 8 0 0 0 0
0 0 3 4 0 0
0 0 6 8 0 0
0 0 0 0 3 4
0 0 0 0 6 8
```

For more advanced matrix algebra routines, check out the Tcllib math::linearalgebra package.

#### Iteration Tools

The commands zip zips two lists into a list of tuples, and zip3 zip three lists into a list of triples. Lists must be the same length.

```
zip $a $b
```

\$a \$b \$c

Lists to zip together.

```
Example 17: Zipping and unzipping lists

Code:

# Zipping
set x [zip {A B C} {1 2 3}]
set y [zip3 {Do Re Mi} {A B C} {1 2 3}]
puts $x
puts $y
# Unzipping (using transpose)
puts [transpose $x]

Output:

{A 1} {B 2} {C 3}
{Do A 1} {Re B 2} {Mi C 3}
{A B C} {1 2 3}
```

The command *cartprod* computes the Cartesian product of an arbitrary number of vectors, returning a matrix where the columns correspond to the input vectors and the rows correspond to all the combinations of the vector elements.

```
cartprod $a $b ...
```

**\$a \$b** ... Arbitrary number of vectors to take Cartesian product of.

```
Example 18: Cartesian product

Code:

puts [cartprod {A B C} {1 2 3}]

Output:

{A 1} {A 2} {A 3} {B 1} {B 2} {B 3} {C 1} {C 2} {C 3}
```

# N-Dimensional Lists (Tensors)

All Tcl values are ND-lists. An ND-list is defined as a list of equal length (N-1)D-lists, which are defined as equal length (N-2)D-lists, and so on until 0D-lists, which are simply strings that either have no list representation or are of list length 1. This definition is flexible, and allows for different interpretations of the same data. For example, the list "1 2 3" can be interpreted as a scalar with value "1 2 3", a vector with values "1", "2", and "3", or a matrix with row vectors "1", "2", and "3". In general, if a value is a valid for N dimensions, it will also be valid for dimensions 0 to N-1.

The command *ndims* returns the rank of an ND-list, and the command *ndims\_multiple* returns the rank that is compatible with multiple ND-lists. By default, it automatically determines the rank for the data, but if a rank is provided, it will validate that the ND-list or ND-lists are compatible with the provided rank.

# ndims \$ndlist <\$rank>

# ndims\_multiple \$ndlists <\$rank>

**\$ndlist** ND-list.

**\$ndlists** List of ND-lists.

\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

```
Example 19: Rank of an ND-list

Code:
    set x {1}
    set y {1 2 {hello world}}; # note that this is not a valid 2D list
    set z {{1 2 3} {4 5 6}}
    puts [ndims $x]; # 0
    puts [ndims $y]; # 1
    puts [ndims $z]; # 2
    # the only rank that works for x, y, and z is 1
    puts [ndims_multiple [list $x $y $z]]; # 1

Output:

0
1
2
1
```

# Shape and Size

The commands *nshape* and *nsize* return the shape and size of an ND-list, respectively. The shape is a list of the dimensions, and the size is the product of the shape.

```
nshape $ndlist <$rank>
```

#### nsize \$ndlist <\$rank>

**\$ndlist** ND-list to get shape/size of.

\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

```
Example 20: Getting shape and size of an ND-list
Code:
 # Create a 3D list
 set x {{{1 2} {3 4} {5 6}} {{7 8} {9 10} {11 12}}}
 # Get the shape and size for different rank interpretations
 puts [list [nshape $x] [nsize $x]]; # auto-rank (3)
 puts [list [nshape $x 1] [nsize $x 1]]; # rank 1
 puts [list [nshape $x 2] [nsize $x 2]]; # rank 2
 puts [list [nshape $x 3] [nsize $x 3]]; # rank 3
 puts [list [nshape $x 4] [nsize $x 4]]; # rank 4
Output:
 {2 3 2} 12
 2 2
 {2 3} 6
 {2 3 2} 12
 {2 3 2 1} 12
```

#### Initialization

The command nfull initializes a valid ND-list of any size filled with a single value.

# nfull \$value \$n ...

**\$value** Value to repeat

**\$n** ... Shape (list of dimensions) of ND-list.

#### Example 21: Generate ND-list filled with one value

#### Code:

```
puts [nfull foo 3 2]; # 3x2 matrix filled with "foo"
puts [nfull 0 2 2 2]; # 2x2x2 tensor filled with zeros
```

#### Output:

```
{foo foo} {foo foo} {foo foo} {{0 0} {0 0}} {{0 0}}
```

The command nrand initializes a valid ND-list of any size filled with random values between 0 and 1.

#### nrand \$n ...

**\$n** ... Shape (list of dimensions) of ND-list.

#### Example 22: Generate random matrix

#### Code:

```
expr \{srand(0)\}; # resets the random number seed (for the example) puts [nrand 1 2]; # 1x2 matrix filled with random numbers
```

#### Output:

{0.013469574513598146 0.3831388500440581}

# Repeating and Expanding

The command *nrepeat* repeats portions of an ND-list a specified number of times.

```
nrepeat $ndlist $n ...
```

**\$value** Value to repeat

**\$n...** Repetitions at each level.

```
Example 23: Repeat elements of a matrix

Code:

puts [nrepeat {{1 2} {3 4}} 1 2]

Output:

{1 2 1 2} {3 4 3 4}
```

The command *nexpand* repeats portions of an ND-list to expand to new dimensions. New dimensions must be divisible by old dimensions. For example, 1x1, 2x1, 4x1, 1x3, 2x3 and 4x3 are compatible with 4x3.

```
nexpand $ndlist $n ...
```

**\$ndlist** ND-list to expand.

**\$n . . .** New shape of ND-list. If -1 is used, it keeps that axis the same.

#### Example 24: Expand an ND-list to new dimensions

```
Code:
```

```
puts [nexpand {1 2 3} -1 2]
puts [nexpand {{1 2}} 2 4]
```

#### Output:

```
{1 1} {2 2} {3 3}
{1 2 1 2} {1 2 1 2}
```

## Padding and Extending

The command *npad* pads an ND-list along its axes by a specified number of elements.

#### npad \$ndlist \$value \$n ...

\$ndlistND-list to pad.\$valueValue to pad with.

**\$n** ... Number of elements to pad.

#### Example 25: Padding an ND-list with zeros

#### Code.

```
set a {{1 2 3} {4 5 6} {7 8 9}}
puts [npad $a 0 2 1]
```

#### Output:

{1 2 3 0} {4 5 6 0} {7 8 9 0} {0 0 0 0} {0 0 0 0}

The command *nextend* extends an ND-list to a new shape by padding.

#### nextend \$ndlist \$value \$n ...

\$ndlistND-list to extend.\$valueValue to pad with.

**\$n** ... New shape of ND-list. To keep the shape at an axis, use -1.

#### Example 26: Extending an ND-list to a new shape with a filler value

#### Code:

```
set a {hello hi hey howdy}
puts [nextend $a world -1 2]; # -1 preserves size at axis 0
```

#### Output:

{hello world} {hi world} {hey world} {howdy world}

# Flattening and Reshaping

The command nflatten flattens an ND-list to a vector.

#### nflatten \$ndlist <\$rank>

**\$ndlist** ND-list to flatten.

\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

#### Example 27: Reshape a matrix to a 3D tensor

#### Code:

```
set x [nflatten {{1 2 3 4} {5 6 7 8}}]
puts [nreshape $x 2 2 2]
```

#### Output:

```
{{1 2} {3 4}} {{5 6} {7 8}}
```

The command *nreshape* reshapes a vector into specified dimensions. Sizes must be compatible.

#### nreshape \$vector \$n ...

**\$vector** Vector (1D-list) to reshape.

\$n ... Shape of ND-list. One axis may be dynamic, denoted with -1.

#### Example 28: Reshape a vector to a matrix with three columns

#### Code.

```
puts [nreshape {1 2 3 4 5 6} -1 3]
```

#### Output:

{1 2 3} {4 5 6}

#### Index Notation

This package provides generalized N-dimensional list access/modification commands, using an index notation parsed by the command ::ndlist::ParseIndex, which returns the index type and an index list for the type.

#### ::ndlist::ParseIndex \$n \$input

```
$n Number of elements in list.
$input Index input. Options are shown below:
: All indices
$start:$stop Range of indices (e.g. 0:4 or 1:end-2).
$start:$step:$stop Stepped range of indices (e.g. 0:2:-2 or 2:3:end).
$iList List of indices (e.g. {0 end-1 5} or 3).
$i* Single index with a asterisk, "flattens" the ndlist (e.g. 0* or end-3*).
```

Additionally, indices get passed through the ::ndlist::Index2Integer command, which converts the inputs "end", "end-integer", "integer±integer" and negative wrap-around indexing (where -1 is equivalent to "end") into normal integer indices. Note that this command will return an error if the index is out of range.

```
::ndlist::Index2Integer $n $index
```

\$n Number of elements in list.

**\$index** Single index.

```
Example 29: Index Notation

Code:

set n 10

puts [::ndlist::ParseIndex $n :]

puts [::ndlist::ParseIndex $n 1:8]

puts [::ndlist::ParseIndex $n 0:2:6]

puts [::ndlist::ParseIndex $n 60 5 end-1}]

puts [::ndlist::ParseIndex $n end*]

Output:

A {}

R {1 8}

L {0 2 4 6}

L {0 5 8}

S 9
```

#### Access

Portions of an ND-list can be accessed with the command nget, using the index parser ::ndlist::ParseIndex for each dimension being indexed. Note that unlike the Tcl lindex and lrange commands, nget will return an error if the indices are out of range.

```
nget $ndlist $i ...
```

\$ndlist

ND-list value.

\$i ...

Index inputs, parsed with ::ndlist::ParseIndex.

```
Example 30: ND-list access

Code:

set A {{1 2 3} {4 5 6} {7 8 9}}

puts [nget $A 0:]; # get row matrix

puts [nget $A 0*:]; # flatten row matrix to a vector

puts [nget $A 0:1 0:1]; # get matrix subset

puts [nget $A end:0 end:0]; # can have reverse ranges

puts [nget $A {0 0 0} 1*]; # can repeat indices

Coutput:

{1 2 3}

1 2 3

{1 2} {4 5}

{9 8 7} {6 5 4} {3 2 1}

2 2 2
```

#### Modification

A ND-list can be modified by reference with *nset*, and by value with *nreplace*, using the index parser ::ndlist::ParseIndex for each dimension being indexed. Note that unlike the Tcl lset and lreplace commands, the commands nset and nreplace will return an error if the indices are out of range. If all the index inputs are ":" except for one, and the replacement list is blank, it will delete values along that axis by calling nremove. Otherwise, the replacement ND-list must be expandable to the target index dimensions.

If using the "= \$expr" notation, it will call *nexpr*, where "self" is the ND-list or indexed range being modified and "rank" is "auto" if no index arguments are provided, otherwise it is equal to the number of index arguments minus the number of single index (S) arguments (see ::ndlist::ParseIndex).

```
nset $varName $i ... ($sublist | = $expr)
```

# nreplace \$ndlist \$i ... (\$sublist | = \$expr)

**\$varName** Variable that contains an ND-list.

**\$ndlist** ND-list to modify.

**\$i** ... Index inputs, parsed with ::ndlist::ParseIndex.

**\$sublist** Replacement list, or blank to delete values.

**\$expr** Expression to evaluate and replace values with. Indexed range can be

accessed with "Q." for convenience.

```
Example 31: ND-list modification

Code:

# Swap rows in a matrix (by reference)
set a {{1 2 3} {4 5 6} {7 8 9}}
nset a {{1 0} : [nget $a {0 1} :]
puts $a

# Element-wise operation on portion of vector (by value)
set b [range 10]
puts [nreplace $b 0:2:end = {@. + 10}]

Output:
{4 5 6} {1 2 3} {7 8 9}
10 1 12 3 14 5 16 7 18 9
```

## Removal

The command *nremove* removes portions of an ND-list at a specified axis.

#### nremove \$ndlist \$i <\$axis>

**\$ndlist** ND-list to modify.

\$i Index input, parsed with ::ndlist::ParseIndex.

**\$axis** Axis to remove at. Default 0.

#### Example 32: Filtering a list by removing elements

```
Code:
```

```
set x [range 10]
puts [nremove $x [find $x > 4]]
```

#### Output:

0 1 2 3 4

#### Example 33: Deleting a column from a matrix

#### Code:

```
set a {{1 2 3} {4 5 6} {7 8 9}} puts [nremove $a 2 1]
```

#### Output:

{1 2} {4 5} {7 8}

#### Insertion and Concatenation

The command *ninsert* inserts an ND-list into another ND-list at a specified index and axis. The ND-lists must agree in dimension at all other axes. If "end" or "end-integer" is used for the index, it will insert after the index. Otherwise, it will insert before the index. The command *ncat* is shorthand for inserting at "end", and concatenates two ND-lists.

#### ninsert \$ndlist1 \$index \$ndlist2 <\$axis> <\$rank>

#### ncat \$ndlist1 \$ndlist2 <\$axis> <\$rank>

\$axis Axis to insert/concatenate at (default 0).

\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

#### Example 34: Inserting a column into a matrix

#### Code:

```
set matrix {{1 2} {3 4} {5 6}}
set column {A B C}
puts [ninsert $matrix 1 $column 1 2]
```

#### Output:

{1 A 2} {3 B 4} {5 C 6}

#### Example 35: Concatenate tensors

#### Code:

```
set x [nreshape {1 2 3 4 5 6 7 8 9} 3 3 1]
set y [nreshape {A B C D E F G H I} 3 3 1]
puts [ncat $x $y 2 3]
```

#### Output:

 $\{\{1\ A\}\ \{2\ B\}\ \{3\ C\}\}\ \{\{4\ D\}\ \{5\ E\}\ \{6\ F\}\}\ \{\{7\ G\}\ \{8\ H\}\ \{9\ I\}\}\}$ 

# Changing Order of Axes

The command *nswapaxes* is a general purpose transposing function that swaps the axes of an ND-list. For simple matrix transposing, the command *transpose* can be used instead.

#### nswapaxes \$ndlist \$axis1 \$axis2

**\$ndlist** ND-list to manipulate.

\$axis1 \$axis2 Axes to swap.

The command *nmoveaxis* moves a specified source axis to a target position. For example, moving axis 0 to position 2 would change "i,j,k" to "j,k,i".

#### nmoveaxis \$ndlist \$source \$target

**\$ndlist** ND-list to manipulate.

\$source Source axis.
\$target Target position.

The command *npermute* is more general purpose, and defines a new order for the axes of an ND-list. For example, the axis list "1 0 2" would change "i,j,k" to "j,i,k".

#### npermute \$ndlist \$axis ...

**\$ndlist** ND-list to manipulate.

**\$axis** ... List of axes defining new order.

# Example 36: Changing tensor axes

#### Code:

```
set x {{{1 2} {3 4}} {{5 6} {7 8}}}
set y [nswapaxes $x 0 2]
set z [nmoveaxis $x 0 2]
puts [lindex $x 0 0 1]
```

puts [lindex \$y 1 0 0]
puts [lindex \$z 0 1 0]

#### Output:

2

2

2

# ND Functional Mapping

The command *napply* applies a command over each element of an ND-list, and returns the result. The commands *napply2* maps element-wise over two ND-lists. If the input lists have different shapes, they will be expanded to their maximum dimensions with *nexpand* (if compatible).

#### napply \$command \$ndlist <\$suffix> <\$rank>

#### napply2 \$command \$ndlist1 \$ndlist2 <\$suffix> <\$rank>

**\$ndlist** ND-list to map over.

\$ndlist1 \$ndlist2 ND-lists to map over, element-wise.
\$command Command prefix to map with.

\$suffix Additional arguments to append after ND-list elements. Default blank.
\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

# Example 37: Chained functional mapping over a matrix

#### Code:

napply puts [napply {format %.2f} [napply expr {{1 2} {3 4}} {+ 1}]]

#### Output:

2.00

3.00

4.00

5.00

#### Example 38: Format columns of a matrix

#### Code:

set data {{1 2 3} {4 5 6} {7 8 9}}
set formats {{%.1f %.2f %.3f}}
puts [napply2 format \$formats \$data]

#### Output:

{1.0 2.00 3.000} {4.0 5.00 6.000} {7.0 8.00 9.000}

## Reducing an ND-list

The command nreduce combines nmoveaxis and napply to reduce an axis of an ND-list with a function that reduces a vector to a scalar, like max or sum.

#### nreduce \$command \$ndlist <\$axis> <\$suffix> <\$rank>

\$command prefix to map with.

**\$ndlist** ND-list to map over.

**\$axis** Axis to reduce. Default 0.

\$suffix Additional arguments to append after ND-list elements. Default blank.
\$rank Rank of ND-list (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

#### Example 39: Matrix row and column statistics

```
Code:
```

```
set x {{1 2} {3 4} {5 6} {7 8}}
puts [nreduce max $x]; # max of each column
puts [nreduce max $x 1]; # max of each row
puts [nreduce sum $x]; # sum of each column
puts [nreduce sum $x 1]; # sum of each row
```

#### Output:

7 8 2 4 6 8 16 20 3 7 11 15

## Generalized N-Dimensional Mapping

The command *nmap* is a general purpose mapping function for N-dimensional lists in Tcl. If multiple ND-lists are provided for iteration, they must be expandable to their maximum dimensions. The actual implementation flattens all the ND-lists and calls the Tcl *lmap* command, and then reshapes the result to the target dimensions. So, if "continue" or "break" are used in the map body, it will return an error. If rank is not specified, it will automatically determine the rank using *ndims\_multiple* and the referenced ND-lists.

#### nmap <\$rank> \$varName \$ndlist <\$varName \$ndlist ...> \$body

\$rank Rank (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

**\$varName** Variable name to iterate with.

**\$ndlist** ND-list to iterate over.

\$body Tcl script to evaluate at every loop iteration.

#### Example 40: Expand and map over matrices

#### Code:

```
set phrases [nmap 2 greeting {{hello goodbye}} subject {world moon} {
    list $greeting $subject
}]
napply puts $phrases {} 2
```

#### Output:

hello world goodbye world hello moon goodbye moon

# Loop Index Access

The iteration indices of nmap can be accessed with the commands i, j, and k. The commands j and k are simply shorthand for i with axes 1 and 2.

# i <\$axis>

j

K

\$axis

Dimension to access mapping index at. Default 0.

If -1, returns the linear index of the loop.

```
Example 41: Finding index tuples that match criteria

Code:

set x {{1 2 3} {4 5 6} {7 8 9}}
set indices {}
```

```
set indices {}
nmap xi $x {
   if {$xi > 4} {
      lappend indices [list [i] [j]]
   }
}
puts $indices
```

Output:

{1 1} {1 2} {2 0} {2 1} {2 2}

# Element-wise operations

The command *neval* maps over ND-arrays using *nmap*, but without the need to specify looping variables, and the command *nexpr* is a special case that passes input through the Tcl *expr* command. ND-lists can be referred to with "@ref", where "ref" is the name of the variable storing the ND-list. If an ND-list is provided as "self", it can be referred to with "@." for convenience. Additionally, portions of an ND-list can be mapped over with the notation "@ref(\$i,...)", where "\$i,..." are raw index arguments (does not do any substitution). If rank is not specified, it will automatically determine the rank using *ndims\_multiple* and the referenced/indexed ND-lists.

#### neval \$body <\$self> <\$rank>

#### nexpr \$expr <\$self> <\$rank>

\$body Script to evaluate, with "@ref" notation for ND-list references.

**\$expr** Expression to evaluate, with "@ref" notation for ND-list references.

\$self ND-list to refer to with "@.". Default blank.

\$rank Rank (e.g. 2 for matrix) or "auto" for auto-rank. Default "auto".

```
Example 42: Get distance between elements in a vector

Code:

set x {1 2 4 7 11 16}

puts [nexpr {@x(1:end) - @x(0:end-1)}]

Output:

1 2 3 4 5
```

```
Example 43: Outer product of two vectors

Code:

set x {1 2 3}
set y {{4 5 6}}
puts [nexpr {@x * @y}]

Output:
{4 5 6} {8 10 12} {12 15 18}
```

# File Import/Export

The commands readFile and writeFile perform simple data import/export, while the commands readMatrix and writeMatrix dynamically convert files to matrix format and matrices to the specified file format (e.g. file extension .csv will call conversion functions mat2csv and csv2mat).

```
readFile <$option $value ...> <-newline> $file
```

#### readMatrix <\$option \$value ...> <-newline> \$file

**\$option \$value ...** File configuration options, see Tcl fconfigure command.

-newline Option to read the final newline if it exists.

**\$file** File to read data from.

```
writeFile <$option $value ...> <-nonewline> $file $data
```

```
writeMatrix <$option $value ...> <-nonewline> $file $data
```

**\$option \$value ...** File configuration options, see Tcl fconfigure command.

-nonewline Option to not write a final newline.

\$file File to write data to.
\$data Data to write to file.

#### Example 44: File import/export

```
Code:
```

```
# Export matrix to file (converts to csv)
writeMatrix example.csv {{foo bar} {hello world}}
# Read CSV file
puts [readFile example.csv]
puts [readMatrix example.csv]; # converts from csv to matrix
```

file delete example.csv

#### Output:

foo,bar hello,world

{foo bar} {hello world}

#### Data Conversions

The commands mat2txt and txt2mat convert between matrix and space-delimited text, where new-lines separate rows. Escaping of spaces and newlines is consistent with Tcl rules for valid lists.

#### mat2txt \$mat

#### txt2mat \$txt

Matrix value. \$mat

Space-delimited values. \$txt

The commands mat2csv and csv2mat convert between matrix and CSV-formatted text, where new lines separate rows. Commas and newlines are escaped with quotes, and quotes are escaped with double-quotes.

#### mat2csv \$mat

#### csv2mat \$csv

Matrix value. \$mat

Comma-separated values. \$csv

#### Example 45: Data conversions

```
Code:
```

```
set matrix {{A B C} {{hello world} foo,bar {"hi"}}}
puts {TXT format:}
puts [mat2txt $matrix]
puts {CSV format:}
puts [mat2csv $matrix]
```

#### Output:

```
TXT format:
A B C
{hello world} foo,bar {"hi"}
CSV format:
A,B,C
hello world, "foo, bar", """hi"""
```

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