N-Dimensional Lists (ndlist)

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https://github.com/ambaker1/ndlist

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Abstract

The "ndlist" package is a pure-Tcl package for tensor manipulation and processing. This package is also a Tin package, and can be loaded in as shown below:

Example 1: Installing and loading "ndlist"

Code

package require tin
tin add -auto ndlist https://github.com/ambaker1/ndlist install.tcl
tin import ndlist

1-Dimensional Lists (Vectors)

Lists are foundational to Tcl, so in addition to providing utilities for ND-lists, this package also provides utilities for working with 1D-lists, or vectors.

Range Generator

The command *range* simply generates a list of integer values. This can be used in conjunction with the Tcl foreach loop to simplify writing "for" loops. There are two ways of calling this command, as shown below.

```
range $n
range $start $stop <$step>
```

\$n Number of indices, starting at 0 (e.g. 3 returns 0 1 2).

\$start Starting value. \$stop Stop value.

\$step Step size. Default 1 or -1, depending on direction of start to stop.

```
Example 2: Integer range generation

Code:

puts [range 3]
puts [range 0 2]
puts [range 10 3 -2]

Output:

0 1 2
0 1 2
10 8 6 4
```

```
Example 3: Simpler for-loop

Code:
   foreach i [range 3] {
      puts $i
   }

Output:
   0
   1
   2
```

Logical Indexing

The command find returns the indices of non-zero elements of a boolean list, or indices of elements that satisfy a given criterion. Can be used in conjunction with nget to perform logical indexing.

find \$list <\$op \$scalar>

\$list List of values to compare.

\$op Comparison operator. Default "!=".

\$scalar Comparison value. Default 0.

Example 4: Filtering a list

Code:

```
set x \{0.5 \ 2.3 \ 4.0 \ 2.5 \ 1.6 \ 2.0 \ 1.4 \ 5.6\} puts [nget x \ [find \ x > 2]]
```

Output:

2.3 4.0 2.5 5.6

Linear Interpolation

The command *linterp* performs linear 1D interpolation. Converts input to "double".

linterp \$x \$xList \$yList

\$x Value to query in \$xList

\$xList List of x points, strictly increasing

\$yList List of y points, same length as **\$xList**

Example 5: Linear interpolation

Code:

```
puts [linterp 2 {1 2 3} {4 5 6}]
puts [linterp 8.2 {0 10 20} {2 -4 5}]
```

Output:

5.0 -2.92

Vector Generation

The command *linspace* can be used to generate a vector of specified length and equal spacing between two specified values. Converts input to "double"

linspace \$n \$start \$stop

\$n Number of points \$start Starting value \$stop End value

Example 6: Linearly spaced vector generation

Code:

puts [linspace 5 0 1]

Output:

0.0 0.25 0.5 0.75 1.0

The command *linsteps* generates intermediate values given an increment size and a sequence of targets. Converts input to "double".

linsteps \$step \$x1 \$x2 ...

\$step Maximum step size \$x1 \$x2 ... Targets to hit.

Example 7: Intermediate value vector generation

Code:

puts [linsteps 0.25 0 1 0]

Output:

0.0 0.25 0.5 0.75 1.0 0.75 0.5 0.25 0.0

Functional Mapping

The command lapply simply applies a command over each element of a list, and returns the result. Basic math operators can be mapped over a list with the command lop.

lapply \$command \$list \$arg ...

lop \$list \$op \$arg...

\$list List to map over.

\$command prefix to map with.

\$op Math operator (see ::tcl::mathop documentation).

\$arg ... Additional arguments to append to command after each list element.

Example 8: Applying a math function to a list

Code:

Add Tcl math functions to the current namespace path
namespace path [concat [namespace path] ::tcl::mathfunc]
puts [lapply abs {-5 1 2 -2}]

Output:

5 1 2 2

Mapping Over Two Lists

The commands lapply and lop only map over one list. The commands lapply2 and lop2 allow you to map, element-wise, over two lists. List lengths must be equal.

lapply2 \$command \$list1 \$list2 \$arg ...

lop2 \$list1 \$op \$list2 \$arg...

\$list1 \$list2 Lists to map over, element-wise.

\$command Prefix to map with.

\$op Math operator (see ::tcl::mathop documentation).

\$arg ... Additional arguments to append to command after list elements.

Example 9: Mapping over two lists

Code:

lapply puts [lapply2 {format "%s %s"} {hello goodbye} {world moon}]

Output:

hello world goodbye moon

Example 10: Adding two lists together

Code:

puts [lop2 {1 2 3} + {2 3 2}]

Output:

3 5 5

List Math

The Tcl command lmap allows you to loop over an arbitrary number of lists in parallel, evaluating a script at each iteration, and collecting the results of each loop iteration into a new list. The command lexpr is an extension of this concept, just calling lmap and passing the input through the Tcl expr command.

lexpr \$varList \$list <\$varList \$list ...> \$expr

\$varList ... List(s) of variables to iterate with.

\$list ... List(s) to iterate over.

\$expr Tcl expression to evaluate at every loop iteration.

```
Example 11: Filtering a list

Code:

set numbers [range 10]
set odds [lexpr x $numbers {$x % 2 ? $x : [continue]}]; # only odd numbers
puts $odds

Output:

1 3 5 7 9
```

```
Example 12: Adding three lists together

Code:

set x {1 2 3}
set y {2 9 2}
set z {5 -2 0}
puts [lexpr xi $x yi $y zi $z {$xi + $yi + $zi}]

Output:
8 9 5
```

List Statistics

The commands max, min, sum, product, mean, median, variance, and stdev compute the maximum, minimum, sum, product, mean, median, variance, and standard deviation of values in a list. For more advanced statistics, check out the Tcllib math::statistics package.

max \$list
min \$list

sum \$list

product \$list

mean \$list

median \$list

variance \$list <\$pop>

stdev \$list <\$pop>

\$list List (at least length 1) to compute statistic of.

\$pop Compute population statistic instead of sample statistic. Default false.

Example 13: List Statistics

```
Code:
    set list {-5 3 4 0}
    foreach stat {max min sum product mean median variance stdev} {
        puts [list $stat [$stat $list]]
}

Cutput:
    max 4
    min -5
    sum 2
    product 0
    mean 0.5
    median 1.5
    variance 16.3333333333332
    stdev 4.041451884327381
```

Vector Algebra

The dot product of two equal length vectors can be computed with dot. The cross product of two vectors of length 3 can be computed with cross.

dot \$a \$b

cross \$a \$b

\$a First vector.
\$b Second vector.

Example 14: Dot and cross product Code: set x {1 2 3} set y {-2 -4 6} puts [dot \$x \$y] puts [cross \$x \$y] Output: 8 24 -12 0

The norm, or magnitude, of a vector can be computed with norm.

norm \$a <\$p>

\$a Vector to compute norm of.

\$p Norm type. 1 is sum of absolute values, 2 is euclidean distance, and Inf is

absolute maximum value. Default 2.

```
Example 15: Normalizing a vector

Code:

set x {3 4}

set x [lop $x / [norm $x]]

puts $x

Output:

0.6 0.8
```

For more advanced vector algebra routines, check out the Tcllib math::linearalgebra package.

2-Dimensional Lists (Matrices)

A matrix is a two-dimensional list, or a list of row vectors. This is consistent with the format used in the Tellib math::linearalgebra package. See the example below for how matrices are interpreted.

$$A = \begin{bmatrix} 2 & 5 & 1 & 3 \\ 4 & 1 & 7 & 9 \\ 6 & 8 & 3 & 2 \\ 7 & 8 & 1 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} 9 \\ 3 \\ 0 \\ -3 \end{bmatrix}, \quad C = \begin{bmatrix} 3 & 7 & -5 & -2 \end{bmatrix}$$

Example 16: Matrices and vectors

```
Code:
```

```
set A \{\{2\ 5\ 1\ 3\}\ \{4\ 1\ 7\ 9\}\ \{6\ 8\ 3\ 2\}\ \{7\ 8\ 1\ 4\}\} set B \{9\ 3\ 0\ -3\} set C \{\{3\ 7\ -5\ -2\}\}
```

Identity Matrix

The command eye generates an identity matrix of a specified size.

eye \$n

\$n

Size of identity matrix

Example 17: Generating an identity matrix

Code:

puts [eye 3]

Output:

{1 0 0} {0 1 0} {0 0 1}

Matrix Transpose

The command *transpose* simply swaps the rows and columns of a matrix.

transpose \$A

\$A

Matrix to transpose, nxm.

Returns an mxn matrix.

```
Example 18: Transposing a matrix

Code:

puts [transpose {{1 2} {3 4}}]

Output:
{1 3} {2 4}
```

Matrix Multiplication

The command *matmul* performs matrix multiplication for two matrices. Inner dimensions must match.

matmul \$A \$B

\$A Left matrix, nxq.

\$B Right matrix, qxm.

Returns an nxm matrix (or the corresponding dimensions from additional matrices)

```
Example 19: Multiplying a matrix

Code:

puts [matmul {{2 5 1 3} {4 1 7 9} {6 8 3 2} {7 8 1 4}} {9 3 0 -3}]

Output:

24 12 72 75
```

For more advanced matrix algebra routines, check out the Tcllib math::linearalgebra package.

Iteration Tools

The commands zip zips two lists into a list of tuples, and zip3 zip three lists into a list of triples. Lists must be the same length.

zip \$a \$b

\$a \$b \$c

Lists to zip together.

```
Example 20: Zipping lists

Code:

puts [zip {A B C} {1 2 3}]
puts [zip3 {Do Re Mi} {A B C} {1 2 3}]

Output:

{A 1} {B 2} {C 3}
{Do A 1} {Re B 2} {Mi C 3}
```

The command *cartprod* computes the Cartesian product of an arbitrary number of vectors, returning a matrix where the columns correspond to the input vectors and the rows correspond to all the combinations of the vector elements.

```
cartprod $list1 $list2 ...
```

\$list1 \$list2 ... Lists, or vectors, to take Cartesian product of.

```
Example 21: Cartesian product

Code:

puts [cartprod {A B C} {1 2 3}]

Output:

{A 1} {A 2} {A 3} {B 1} {B 2} {B 3} {C 1} {C 2} {C 3}
```

N-Dimensional Lists (Tensors)

A ND-list is defined as a list of equal length (N-1)D-lists, which are defined as equal length (N-2)D-lists, and so on until (N-N)D-lists, which are scalars of arbitrary size. This definition is flexible, and allows for different interpretations of the same data. For example, the list "1 2 3" can be interpreted as a scalar with value "1 2 3", a vector with values "1", "2", and "3", or a matrix with row vectors "1", "2", and "3".

The command *ndlist* validates that the input is a valid ND-list. If the input value is "ragged", as in it has inconsistent dimensions, it will throw an error. In general, if a value is a valid for N dimensions, it will also be valid for dimensions 0 to N-1. All other ND-list commands assume a valid ND-list.

ndlist \$nd \$value

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$value List to interpret as an ndlist

Shape and Size

The commands *nshape* and *nsize* return the shape and size of an ND-list, respectively. The shape is a list of the dimensions, and the size is the product of the shape.

nshape \$nd \$ndlist <\$axis>

nsize \$nd \$ndlist

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist ND-list to get dimensions of.

\$axis Axis to get dimension along. Blank for all.

Example 22: Getting shape and size of an ND-list

```
Code:
   set A [ndlist 2D {{1 2 3} {4 5 6}}]
   puts [nshape 2D $A]
   puts [nsize 2D $A]
```

Output:

2 3

6

Initialization

The command nfull initializes a valid ND-list of any size filled with a single value.

nfull \$value \$n ...

\$value Value to repeat

\$n ... Shape (list of dimensions) of ND-list.

Example 23: Generate ND-list filled with one value

Code:

```
puts [nfull foo 3 2]; # 3x2 matrix filled with "foo"
puts [nfull 0 2 2 2]; # 2x2x2 tensor filled with zeros
```

Output:

```
{foo foo} {foo foo} {foo foo} {{0 0} {0 0}} {{0 0}}
```

The command nrand initializes a valid ND-list of any size filled with random values between 0 and 1.

nrand \$n ...

\$n ... Shape (list of dimensions) of ND-list.

Example 24: Generate random matrix

Code:

```
expr \{srand(0)\}; # resets the random number seed (for the example) puts [nrand 1 2]; # 1x2 matrix filled with random numbers
```

Output:

{0.013469574513598146 0.3831388500440581}

Repeating and Expanding

The command *nrepeat* repeats portions of an ND-list a specified number of times.

```
nrepeat $ndlist $n ...
```

\$value Value to repeat

\$n ... Repetitions at each level.

```
Example 25: Repeat elements of a matrix

Code:

puts [nrepeat {{1 2} {3 4}} 1 2]

Output:

{1 2 1 2} {3 4 3 4}
```

The command *nexpand* repeats portions of an ND-list to expand to new dimensions. New dimensions must be divisible by old dimensions. For example, 1x1, 2x1, 4x1, 1x3, 2x3 and 4x3 are compatible with 4x3.

```
nexpand $ndlist $n ...
```

\$ndlist ND-list to expand.

\$n ... New dimensions of ND-list.

```
Example 26: Expand an ND-list to new dimensions
```

Code:

```
puts [nexpand {1 2 3} 3 2]
puts [nexpand {{1 2}} 2 4]
```

Output:

```
{1 1} {2 2} {3 3}
{1 2 1 2} {1 2 1 2}
```

Flattening and Reshaping

The command *nreshape* reshapes a vector into a compatible shape. Vector length must equal ND-list size.

nreshape \$vector \$n ...

\$vector Vector (1D-list) to reshape.

\$n ... Shape (list of dimensions) of ND-list.

Example 27: Reshape a vector to a matrix

Code:

puts [nreshape {1 2 3 4 5 6} 2 3]

Output:

{1 2 3} {4 5 6}

The inverse is *nflatten*, which flattens an ND-list to a vector, which can be then used with *nreshape*.

nflatten \$nd \$ndlist

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist ND-list to flatten.

Example 28: Reshape a matrix to a 3D tensor

Code:

set x [nflatten 2D {{1 2 3 4} {5 6 7 8}}]
puts [nreshape \$x 2 2 2]

Output:

{{1 2} {3 4}} {{5 6} {7 8}}

Index Notation

This package provides generalized N-dimensional list access/modification commands, using an index notation parsed by the command ::ndlist::ParseIndex, which returns the index type and an index list for the type.

::ndlist::ParseIndex \$n \$input

\$start:\$step:\$stop Stepped range of indices (e.g. 0:2:-2 or 2:3:end).

\$iList of indices (e.g. {0 end-1 5} or 3).

\$i. Single index with a dot, "flattens" the ndlist (e.g. 0. or end-3.).

Additionally, indices get passed through the ::ndlist::Index2Integer command, which converts the inputs "end", "end±integer", "integer±integer" and negative wrap-around indexing (where -1 is equivalent to "end") into normal integer indices. Note that this command will return an error if the index is out of range.

::ndlist::Index2Integer \$n \$index

\$n Number of elements in list.

\$index Single index.

```
Example 29: Index Notation

Code:

set n 10
puts [::ndlist::ParseIndex $n *]
puts [::ndlist::ParseIndex $n 1:8]
puts [::ndlist::ParseIndex $n 0:2:6]
puts [::ndlist::ParseIndex $n {0 5 end-1}]
puts [::ndlist::ParseIndex $n end.]

Output:

A {}
R {1 8}
L {0 2 4 6}
L {0 5 8}
S 9
```

Access

Portions of an ND-list can be accessed with the command nget, using the index parser ::ndlist::ParseIndex for each dimension being indexed. Note that unlike the Tcl lindex and lrange commands, nget will return an error if the indices are out of range.

```
nget $ndlist $i ...
```

\$ndlist ND-list value.

\$i ... Index inputs, parsed with ::ndlist::ParseIndex. The number of index argu-

ments determines the interpreted dimensions.

```
Example 30: ND-list access

Code:

set A {{1 2 3} {4 5 6} {7 8 9}}

puts [nget $A 0 *]; # get row matrix

puts [nget $A 0.*]; # flatten row matrix to a vector

puts [nget $A 0:1 0:1]; # get matrix subset

puts [nget $A end:0 end:0]; # can have reverse ranges

puts [nget $A {0 0 0} 1.]; # can repeat indices

Output:

{1 2 3}

1 2 3

{1 2} {4 5}

{9 8 7} {6 5 4} {3 2 1}

2 2 2
```

Modification

A ND-list can be modified by reference with *nset*, and by value with *nreplace*, using the index parser ::ndlist::ParseIndex for each dimension being indexed. Note that unlike the Tcl lset and lreplace commands, the commands nset and nreplace will return an error if the indices are out of range. If all the index inputs are "*" except for one, and the replacement list is blank, it will delete values along that axis by calling nremove. Otherwise, the replacement ND-list must be expandable to the target index dimensions.

nset \$varName \$i ... \$sublist

nreplace \$ndlist \$i ... \$sublist

\$varName Variable that contains an ND-list (must exist).

\$ndlist ND-list to modify.

\$i ... Index inputs, parsed with ::ndlist::ParseIndex. The number of index inputs

determines the interpreted dimensions.

\$sublist Replacement list, or blank to delete values.

Example 31: Replace range with a single value

Code:

puts [nreplace [range 10] 0:2:end 0]

Output:

0 1 0 3 0 5 0 7 0 9

Example 32: Swapping matrix rows

Code:

```
set a \{\{1\ 2\ 3\}\ \{4\ 5\ 6\}\ \{7\ 8\ 9\}\} nset a \{1\ 0\} * [nget \{0\ 1\} *]; # Swap rows and columns (modify by reference) puts \{a
```

Output:

{4 5 6} {1 2 3} {7 8 9}

Removal

The command *nremove* removes portions of an ND-list at a specified axis.

nremove \$nd \$ndlist \$i <\$axis>

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist ND-list to modify.

\$i Index input, parsed with ::ndlist::ParseIndex.

\$axis Axis to remove at. Default 0.

Example 33: Filtering a list by removing elements

```
Code:
```

set x [range 10]
puts [nremove \$x [find \$x > 4]]

Output:

0 1 2 3 4

Example 34: Deleting a column from a matrix

Code:

set a {{1 2 3} {4 5 6} {7 8 9}} puts [nremove \$a 2 1]

Output:

{1 2} {4 5} {7 8}

Insertion and Concatenation

The command *ninsert* allows you to insert an ND-list into another ND-list at a specified index and axis, as long as the ND-lists agree in dimension at all other axes. If "end" or "end-integer" is used for the index, it will insert after the index. Otherwise, it will insert before the index.

ninsert \$nd \$ndlist1 \$index \$ndlist2 <\$axis>

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist1 \$ndlist2 ND-lists to combine. \$index Index to insert at.

\$axis Axis to insert at (default 0).

The command nstack is shorthand for inserting at "end", and concatenates two ND-lists.

nstack \$nd \$ndlist1 \$ndlist2 <\$axis>

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist1 \$ndlist2 ND-lists to concatenate.

\$axis Axis to concatenate at (default 0).

Example 35: Inserting a column into a matrix

```
Code:
```

```
set matrix {{1 2} {3 4} {5 6}}
set column {A B C}
puts [ninsert 2D $matrix 1 $column 1]
```

Output:

{1 A 2} {3 B 4} {5 C 6}

Example 36: Concatenate tensors

```
Code:
```

```
set x [nreshape {1 2 3 4 5 6 7 8 9} 3 3 1]
set y [nreshape {A B C D E F G H I} 3 3 1]
puts [nstack 3D $x $y 2]
```

Output:

 $\{\{1\ A\}\ \{2\ B\}\ \{3\ C\}\}\ \{\{4\ D\}\ \{5\ E\}\ \{6\ F\}\}\ \{\{7\ G\}\ \{8\ H\}\ \{9\ I\}\}\}$

Changing Order of Axes

The command *nswapaxes* is a general purpose transposing function that swaps the axes of an ND-list. For simple matrix transposing, the command *transpose* can be used instead.

nswapaxes \$ndlist \$axis1 \$axis2

\$ndlist ND-list to manipulate.

\$axis1 \$axis2 Axes to swap.

The command *nmoveaxis* moves a specified source axis to a target position. For example, moving axis 0 to position 2 would change "i,j,k" to "j,k,i".

nmoveaxis \$ndlist \$source \$target

\$ndlist ND-list to manipulate.

\$source Source axis.
\$target Target position.

The command *npermute* is more general purpose, and defines a new order for the axes of an ND-list. For example, the axis list "1 0 2" would change "i,j,k" to "j,i,k".

npermute \$ndlist \$axis ...

\$ndlist ND-list to manipulate.

\$axis ... List of axes defining new order.

Example 37: Changing tensor axes

Code:

```
set x {{{1 2} {3 4}} {{5 6} {7 8}}}
set y [nswapaxes $x 0 2]
set z [nmoveaxis $x 0 2]
puts [lindex $x 0 0 1]
puts [lindex $y 1 0 0]
```

puts [lindex \$z 0 1 0]

Output:

- 2
- 2
- 2

ND Functional Mapping

The command *napply* simply applies a command over each element of an ND-list, and returns the result. Basic math operators can be mapped over an ND-list with the command *nop*, which is a special case of *napply*, using the ::tcl::mathop namespace.

napply \$nd \$command \$ndlist \$arg ...

nop \$nd \$ndlist \$op \$arg...

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist ND-list to map over.

\$command prefix to map with.

\$op Math operator (see ::tcl::mathop documentation).

\$arg ... Additional arguments to append to command after ND-list element.

Example 38: Chained functional mapping over a matrix Code: napply 2D puts [napply 2D {format %.2f} [napply 2D expr {{1 2} {3 4}} + 1]] Output: 2.00 3.00 4.00 5.00

```
Example 39: Element-wise operations

Code:

puts [nop 1D {1 2 3} + 1]
puts [nop 2D {{1 2 3} {4 5 6}} > 2]

Output:

2 3 4
{0 0 1} {1 1 1}
```

Mapping Over Two ND-lists

The commands *napply* and *nop* only map over one ND-list. The commands *napply2* and *nop2* allow you to map, element-wise, over two ND-lists. If the input lists have different shapes, they will be expanded to their maximum dimensions with *nexpand* (if compatible).

napply2 \$nd \$command \$ndlist1 \$ndlist2 \$arg ...

nop2 \$nd \$ndlist1 \$op \$ndlist2 \$arg...

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$ndlist1 \$ndlist2 ND-lists to map over, element-wise.

\$command Command prefix to map with.

\$op Math operator (see ::tcl::mathop documentation).

\$arg ... Additional arguments to append to command after ND-list elements.

```
Example 40: Format columns of a matrix

Code:

set data {{1 2 3} {4 5 6} {7 8 9}}

set formats {{%.1f %.2f %.3f}}

puts [napply2 2D format $formats $data]

Output:

{1.0 2.00 3.000} {4.0 5.00 6.000} {7.0 8.00 9.000}
```

```
Example 41: Adding matrices together

Code:

set A {{1 2} {3 4}}

set B {{4 9} {3 1}}

puts [nop2 2D $A + $B]

Output:

{5 11} {6 5}
```

Reducing an ND-list

3 7 11 15

The command nreduce combines nmoveaxis and napply to reduce an axis of an ND-list with a function that reduces a vector to a scalar, like max or sum.

nreduce \$nd \$command \$ndlist <\$axis>

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$command Prefix to map with.

\$ndlist ND-list to map over.

\$axis Axis to reduce. Default 0.

```
Example 42: Matrix row and column statistics

Code:

set x {{1 2} {3 4} {5 6} {7 8}}

puts [nreduce 2D max $x]; # max of each column

puts [nreduce 2D max $x 1]; # max of each row

puts [nreduce 2D sum $x]; # sum of each column

puts [nreduce 2D sum $x 1]; # sum of each row

Cutput:

7 8

2 4 6 8

16 20
```

Generalized N-Dimensional Mapping

The command *nmap* is a general purpose mapping function for N-dimensional lists in Tcl, and the command *nexpr* a special case for math expressions. If multiple ND-lists are provided for iteration, they must be expandable to their maximum dimensions. The actual implementation flattens all the ND-lists and calls the Tcl *lmap* command, and then reshapes the result to the target dimensions. So, if "continue" or "break" are used in the map body, it will return an error.

```
nmap $nd $varName $ndlist <$varName $ndlist ...> $body
```

nexpr \$nd \$varName \$ndlist <\$varName \$ndlist ...> \$expr

\$nd Rank of ND-list (e.g. 2D, 2d, or 2 for a matrix).

\$varName Variable name to iterate with.

\$ndlist ND-list to iterate over.

\$body Tcl script to evaluate at every loop iteration.

\$expr Tcl expression to evaluate at every loop iteration.

```
Example 43: Expand and map over matrices

Code:

set phrases [nmap 2D greeting {{hello goodbye}} subject {world moon} {
    list $greeting $subject
}]
    napply 2D puts $phrases

Output:

hello world
    goodbye world
    hello moon
    goodbye moon
```

```
Example 44: Adding two matrices together, element-wise

Code:

set x {{1 2} {3 4}}
set y {{4 1} {3 9}}
set z [nexpr 2D xi $x yi $y {$xi + $yi}]
puts $z

Output:
{5 3} {6 13}
```

Command Index

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