```
Last login: Wed Feb 14 13:23:25 on ttys004 carbon: $ utop
```

Welcome to utop version 2.0.2 (using OCaml version 4.06.0)

Type #utop_help for help about using utop.

```
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sqr_desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
 | Tri of tri desc
 | Sqr of sqr_desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
utop # Nothing ;;
- : 'a maybe = Nothing
utop # Just 6 ;;
- : int maybe = Just 6
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
```

```
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sqr_desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri desc
 | Sgr of sgr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sgr
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
utop # divide 5 2 ;;
- : int maybe = Just 2
utop # divide 56 2 ;;
- : int maybe = Just 28
utop # divide 56 0 ::
- : int maybe = Nothing
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ_desc = coord * float
type tri desc = coord * coord * coord
type sgr desc = coord * coord * coord * coord
```

```
type shape =
   Circ of circ desc
  | Tri of tri_desc
  | Sqr of sqr_desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sgr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri desc
  I Sar of sar desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sgr
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
val l1 : 'a myList = Nil
val l2 : int myList = Cons (1, Cons (2, Cons (3, Nil)))
```

```
-( 15:50:10 )-< command 9 >------{ counter: 0 }-
utop # (3, Nil) ;;
-: int * 'a myList = (3, Nil)
utop # [] ;;
- : 'a list = []
-( 15:54:41 )-< command 11 >----
                                 _____{ counter: 0 }-
utop # Cons (3, Nil) ;;
- : int myList = Cons (3, Nil)
utop # 1::[];;
-: int list = [1]
-( 15:55:04 )-< command 13 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri_desc = coord * coord * coord
type sqr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  Tri of tri desc
 | Sgr of sgr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
```

```
-( 15:56:37 )-< command 14 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri_desc = coord * coord * coord
type sqr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri_desc
  | Sgr of sgr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val l2 : int myList = Cons (1, Cons (2, Cons (3, Nil)))
-( 15:59:05 )-< command 15 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
```

```
type sqr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
   Tri of tri desc
  | Sqr of sqr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val l2 : int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
utop # sumList l2 ;;
-: int = 6
-( 16:03:59 )-< command 17 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ_desc = coord * float
type tri_desc = coord * coord * coord
type sqr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri_desc
  | Sqr of sqr_desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
```

```
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Noe of 'a * 'a btree * 'a btree
val treeAmin : int btree =
 Noe (1, Noe (2, Empty, Empty), Noe (3, Empty, Empty))
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sqr_desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri desc
  | Sar of sar desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sgr
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
```

```
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Node of 'a * 'a btree * 'a btree
val treeAmin : int btree =
 Node (1, Node (2, Empty, Empty),
  Node (3, Empty, Empty))
val sumTree : int btree -> int = <fun>
utop # sumTree treeAmin ;;
- : int = 6
-( 16:11:37 )-< command 20 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sgr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri_desc
  | Sqr of sqr_desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sgr
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
```

```
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val l2 : int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Node of 'a * 'a btree * 'a btree
val treeAmin : int btree =
 Node (1, Node (2, Empty, Empty),
  Node (3, Empty, Empty))
val sumTree : int btree -> int = <fun>
val tstr : string btree =
 Node ("a", Node ("Hello", Empty, Empty),
  Node ("Why?", Empty, Empty))
val concatTree : string btree -> string = <fun>
utop # concatTree tstr ;;
- : string = "HelloaWhy?"
utop # List.map string_of_int [1;2;3] ;;
- : string list = ["1"; "2"; "3"]
utop # treeAmin
- : int btree =
Node (1, Node (2, Empty, Empty), Node (3, Empty, Empty))
utop # treeMap string_of_int treeAmin ;;
Error: Unbound value treeMap
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri_desc = coord * coord * coord
type sqr_desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
```

```
| Tri of tri_desc
  | Sqr of sqr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sgr
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Node of 'a * 'a btree * 'a btree
val treeAmin : int btree =
 Node (1, Node (2, Empty, Empty),
   Node (3, Empty, Empty))
val sumTree : int btree -> int = <fun>
val tstr : string btree =
 Node ("a", Node ("Hello", Empty, Empty),
  Node ("Why?", Empty, Empty))
val concatTree : string btree -> string = <fun>
val treeMap : ('a \rightarrow 'b̄) \rightarrow 'a btree \rightarrow 'b btree = <fun>
-( 16:18:43 )-< command 26 >------{ counter: 0 }-
utop # treeMap string of int treeAmin ;;
- : string btree =
Node ("1", Node ("2", Empty, Empty),
Node ("3", Empty, Empty))
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
```

```
type circ desc = coord * float
type tri desc = coord * coord * coord
type sqr_desc = coord * coord * coord * coord
type shape =
    Circ of circ desc
  | Tri of tri_desc
  | Sqr of sqr_desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Node of 'a * 'a btree * 'a btree
val treeAmin : int btree =
  Node (1, Node (2, Empty, Empty),
   Node (3, Empty, Empty))
val sumTree : int btree -> int = <fun>
val tstr : string btree =
  Node ("a", Node ("Hello", Empty, Empty),
   Node ("Why?", Empty, Empty))
val concatTree : string btree -> string = <fun>
val treeMap: ('a -> 'b) -> 'a btree -> 'b btree = <fun>
val treeFold:
  ('a ->
   ('a btree -> 'a btree) ->
   ('a btree -> 'a btree) -> 'a btree) ->
  'a btree -> 'a btree -> 'a btree = <fun>
-( 16:18:50 )-< command 28 >------{ counter: 0 }-
utop # treeFold (fun a b c \rightarrow a + \underline{b} + c) 0 treeAmin ;;
Error: This expression has type int btree -> int btree
       but an expression was expected of type int
```

```
-( 16:25:06 )-< command 29 >------{ counter: 0 }-
utop # #use "inductive.ml";;
type color = Red | Green | Blue
type weekday = Mon | Tue | Wed | Thu | Fri | Sat | Sun
type boolean = True | False
val isRed : color -> bool = <fun>
val isWorkday : weekday -> bool = <fun>
type intorstr = Int of int | Str of string
type coord = float * float
type circ desc = coord * float
type tri desc = coord * coord * coord
type sqr desc = coord * coord * coord * coord
type shape =
   Circ of circ desc
  | Tri of tri_desc
  | Sgr of sgr desc
val isRect : shape -> bool = <fun>
File "inductive.ml", line 35, characters 2-74:
Warning 8: this pattern-matching is not exhaustive.
Here is an example of a case that is not matched:
Sqr _
val area : shape -> float = <fun>
type 'a maybe = Nothing | Just of 'a
val divide : int -> int -> int maybe = <fun>
val listHd : 'a list -> 'a option = <fun>
type 'a myList = Nil | Cons of 'a * 'a myList
type intList = IntNil | IntCons of int * intList
type ('a, 'b) dictionary = ('a * 'b) list
val l1 : 'a myList = Nil
val 12: int myList = Cons (1, Cons (2, Cons (3, Nil)))
val sumList : int myList -> int = <fun>
type 'a btree = Empty | Node of 'a * 'a btree * 'a btree
val treeAmin : int btree =
 Node (1, Node (2, Empty, Empty),
   Node (3, Empty, Empty))
val sumTree : int btree -> int = <fun>
val tstr : string btree =
 Node ("a", Node ("Hello", Empty, Empty),
  Node ("Why?", Empty, Empty))
val concatTree : string btree -> string = <fun>
val treeMap: ('a -> 'b) -> 'a btree -> 'b btree = <fun>
```

```
val treeFold :
    ('a -> 'b -> 'b -> 'b) -> 'b -> 'a btree -> 'b = <fun>
-( 16:25:34 ) -< command 30 > ______ { counter: 0 } -
utop # treeFold (fun a b c -> a + b + c) 0 treeAmin ;;
- : int = 6
-( 16:25:51 ) -< command 31 > _____ { counter: 0 } -
utop # treeAmin
;;
- : int btree =
Node (1, Node (2, Empty, Empty), Node (3, Empty, Empty))
-( 16:25:53 ) -< command 32 > _____ { counter: 0 } -
utop #
Arg Array ArrayLabels Assert_failure Bigarray Blue Buffe
```