

# 25 Most important Mathematical

## Definitions in Data Science



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#### 1) Gradient Descent

$$\theta_{j+1} = \theta_j - \alpha \nabla J(\theta_j)$$

#### 2) Normal distribution

$$\left| heta_{j+1} = heta_j - lpha 
abla J( heta_j) 
ight| \left| f(x|\mu, \sigma^2) = rac{1}{\sigma \sqrt{2\pi}} \exp\left(-rac{(x-\mu)^2}{2\sigma^2}
ight) 
ight| \left| z = rac{x-\mu}{\sigma} 
ight|$$

$$z = \frac{x - \mu}{\sigma}$$

$$\sigma(x) = rac{1}{1+e^{-x}}$$

$$\operatorname{Correlation} = rac{\operatorname{Cov}(X,Y)}{\operatorname{Std}(X) \cdot \operatorname{Std}(Y)}$$

#### 6) Cosine Similarity

similarity = 
$$\frac{A \cdot B}{\|A\| \|B\|}$$

#### 7) Naive Bayes

$$P(y|x_1,\ldots,x_n) = rac{P(y)\prod_{i=1}^n P(x_i|y)}{P(x_1,\ldots,x_n)}$$

#### 8) MLE

$$\operatorname{argmax}_{\theta} \prod_{i=1}^{n} P(x_i | \theta)$$

$$\hat{\beta} = (X^T X)^{-1} X^T y$$

#### 10) F1 Score

$$\frac{2 \cdot P \cdot R}{P + R}$$

#### 11) RelU

$$\max(0, x)$$

#### 12) Softmax

$$P(y=j|x) = rac{e^{x^Tw_j}}{\sum_{k=1}^K e^{x^Tw_k}}$$

$$P(y=j|x) = rac{e^{x^T w_j}}{\sum_{k=1}^K e^{x^T w_k}} \; igg| \; R^2 = 1 - rac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - ar{y})^2}$$

#### 14) MSE

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

#### 15) MSE + L2 Reg

$$ext{MSE} = rac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \left[ \int ext{MSE}_{ ext{regularized}} = rac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \lambda \sum_{j=1}^p eta_j^2 
ight]$$

#### 16) Eigen vectors

$$Av = \lambda v$$

#### 17) Entropy

$$ext{Entropy} = -\sum_i p_i \log_2(p_i)$$

#### 18) KMeans

$$\operatorname{argmin}_{S} \sum_{i=1}^{k} \sum_{x \in S_{i}} \|x - \mu_{i}\|^{2}$$

### 19) KL Divergence

$$\operatorname{argmin}_{S} \sum_{i=1}^{k} \sum_{x \in S_{i}} \|x - \mu_{i}\|^{2} \qquad D_{\operatorname{KL}}(P\|Q) = \sum_{x \in \mathcal{X}} P(x) \log \left(\frac{P(x)}{Q(x)}\right)$$

#### 20) Log-loss

$$-rac{1}{N} \sum_{i=1}^{N} \left( y_i \log(\hat{y}_i) + (1-y_i) \log(1-\hat{y}_i) 
ight)$$

$$-rac{1}{N}\sum_{i=1}^{N}\left(y_{i}\log(\hat{y}_{i})+(1-y_{i})\log(1-\hat{y}_{i})
ight)\Bigg[\prod_{w,b}rac{1}{2}\|w\|^{2}+C\sum_{i=1}^{n}\max(0,1-y_{i}(w\cdot x_{i}-b))\Bigg]$$

### 22) Linear regression

$$y=eta_0+eta_1x_1+eta_2x_2+\ldots+eta_nx_n+\epsilon$$

### 23) SVD

$$A = U\Sigma V^T$$

#### 24) Lagrange multiplier

$$\max f(x) \; ; \; g(x) = 0$$
  $L(x,\lambda) = f(x) - \lambda * g(x)$ 

#### 25) What will you add?

# Machine Learning Hyperparameters



ML Algorithms		Hyperparameters
Linear Regression		<ul><li>L1/L2 Penalty • Fit Intercept</li><li>Solver</li></ul>
Logistic Regression		<ul><li>L1/L2 Penalty • Class Weight</li><li>Solver</li></ul>
Naive Bayes	$P(A B) = \frac{P(B A)P(A)}{P(B)}$	<ul><li>Alpha</li><li>Binarize</li><li>Fit Prior</li></ul>
Decision Tree		<ul><li>Criterion</li><li>Min Sample</li><li>Max Depth</li><li>Split</li></ul>
Random Forest		<ul> <li>Criterion</li> <li>Max Depth</li> <li>Max Features</li> </ul>
Gradient Boosted Trees		<ul> <li>Criterion</li> <li>Max Depth</li> <li>N Estimators</li> <li>Min Sample Split</li> <li>Learning Rate</li> </ul>
Principal Component	PC2 PC1	N Component
K-Nearest Neighbor		N Neighbors Algorithm ('kd_tree', 'brute')
K-Means		N Clusters     Max Iter     Init
Dense Neural Networks	Input (X) Output (0) Hidden (H1) Hidden (H2)	<ul> <li>Hidden Layer Sizes • Solver</li> <li>Activation • Alpha</li> <li>Droput • Learning rate</li> </ul>