

# 1. Bag of visual words model: recognizing object categories

# Problem: Image Classification

## Given:

- positive training images containing an object class, and



- negative training images that don't



## Classify:

- a test image as to whether it contains the object class or not



?

# Weakly-supervised learning

- Learn model from a set of training images containing object instances



- Know if image contains object or not
- But no segmentation of object or manual selection of features

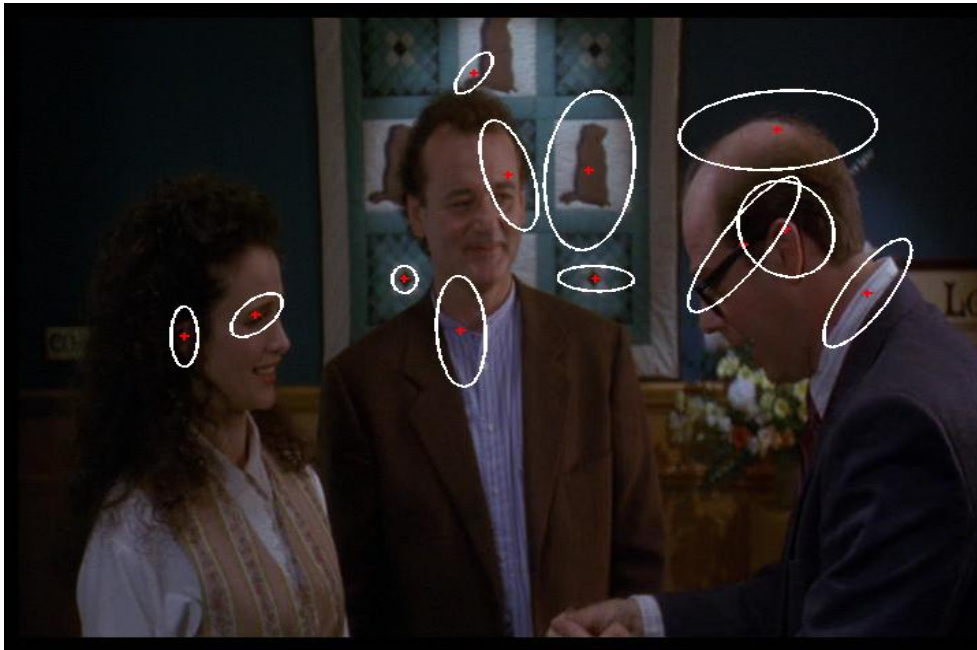
# Three stages:

1. Represent each training image by a vector
  - Use a bag of visual words representation
2. Train a classifier to discriminate vectors corresponding to positive and negative training images
  - Use a Support Vector Machine (SVM) classifier
3. Apply the trained classifier to the test image

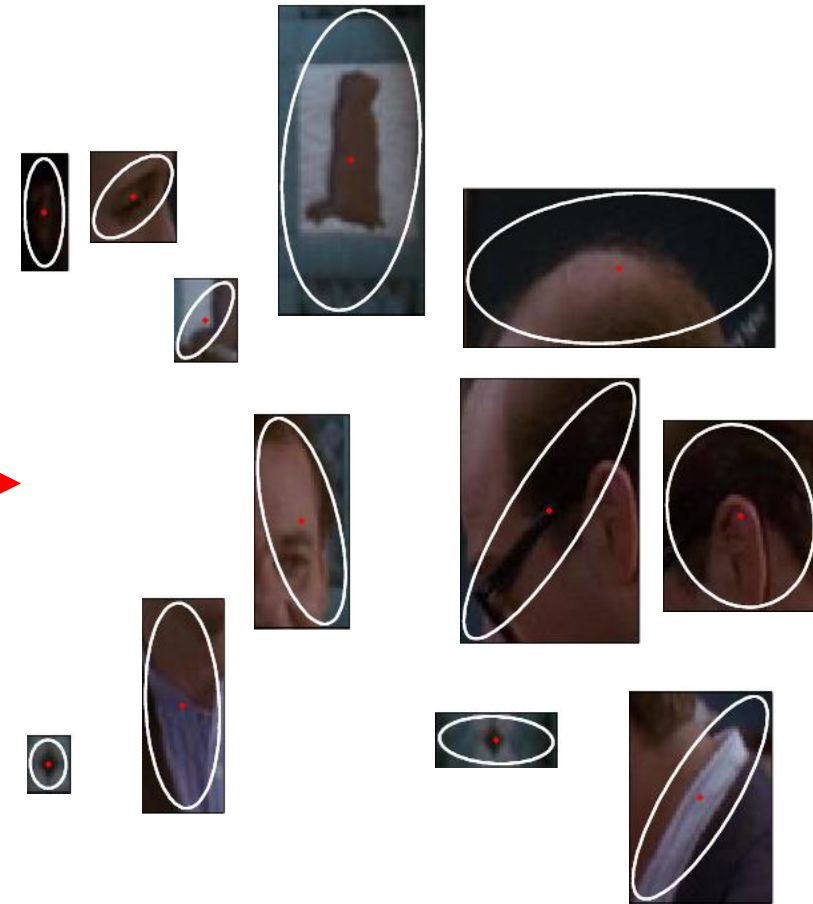
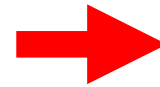
# Representation: Bag of visual words

Visual words are 'iconic' image patches or fragments

- represent the frequency of word occurrence
- but not their position

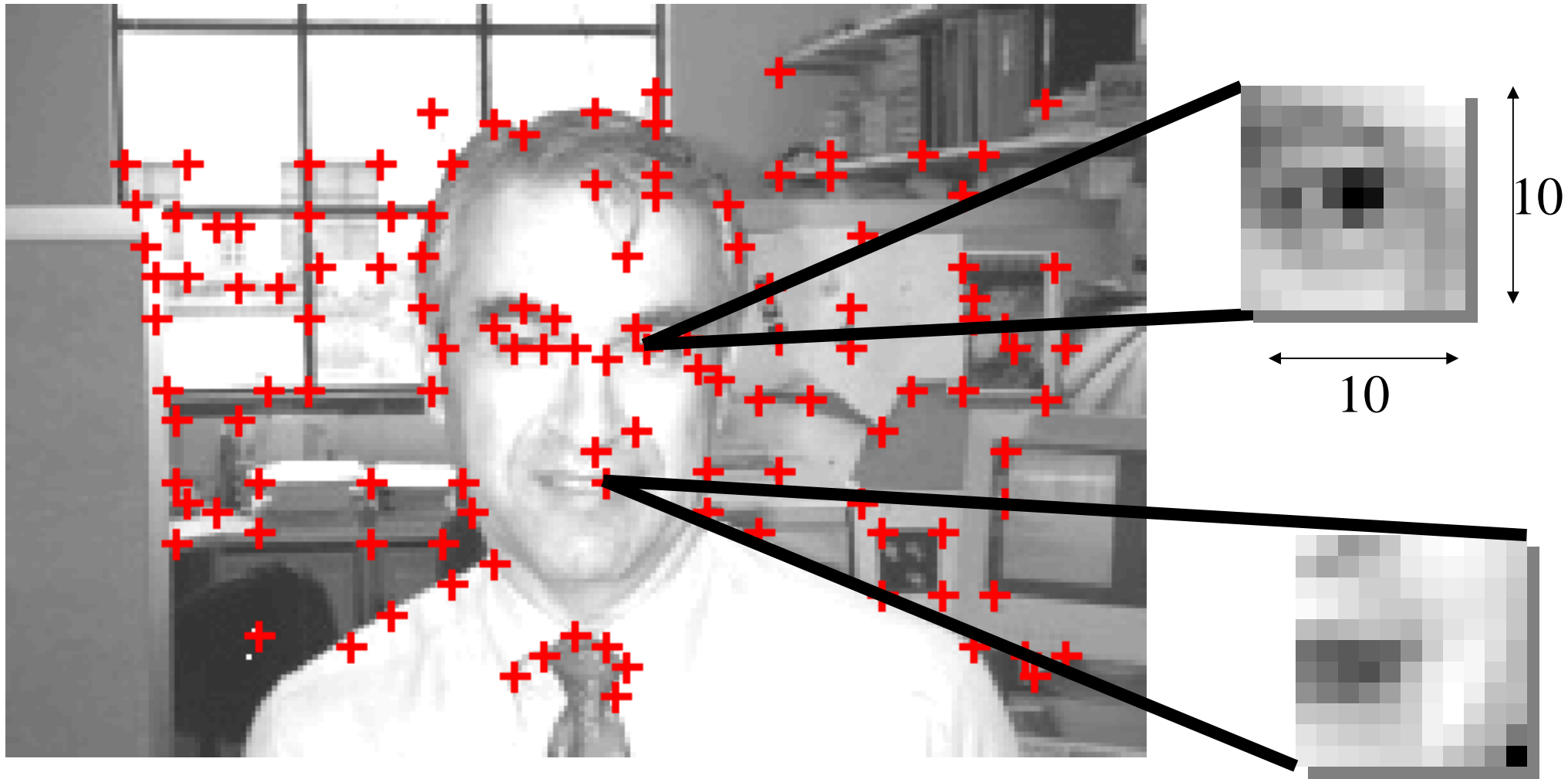


Image



Collection of visual words

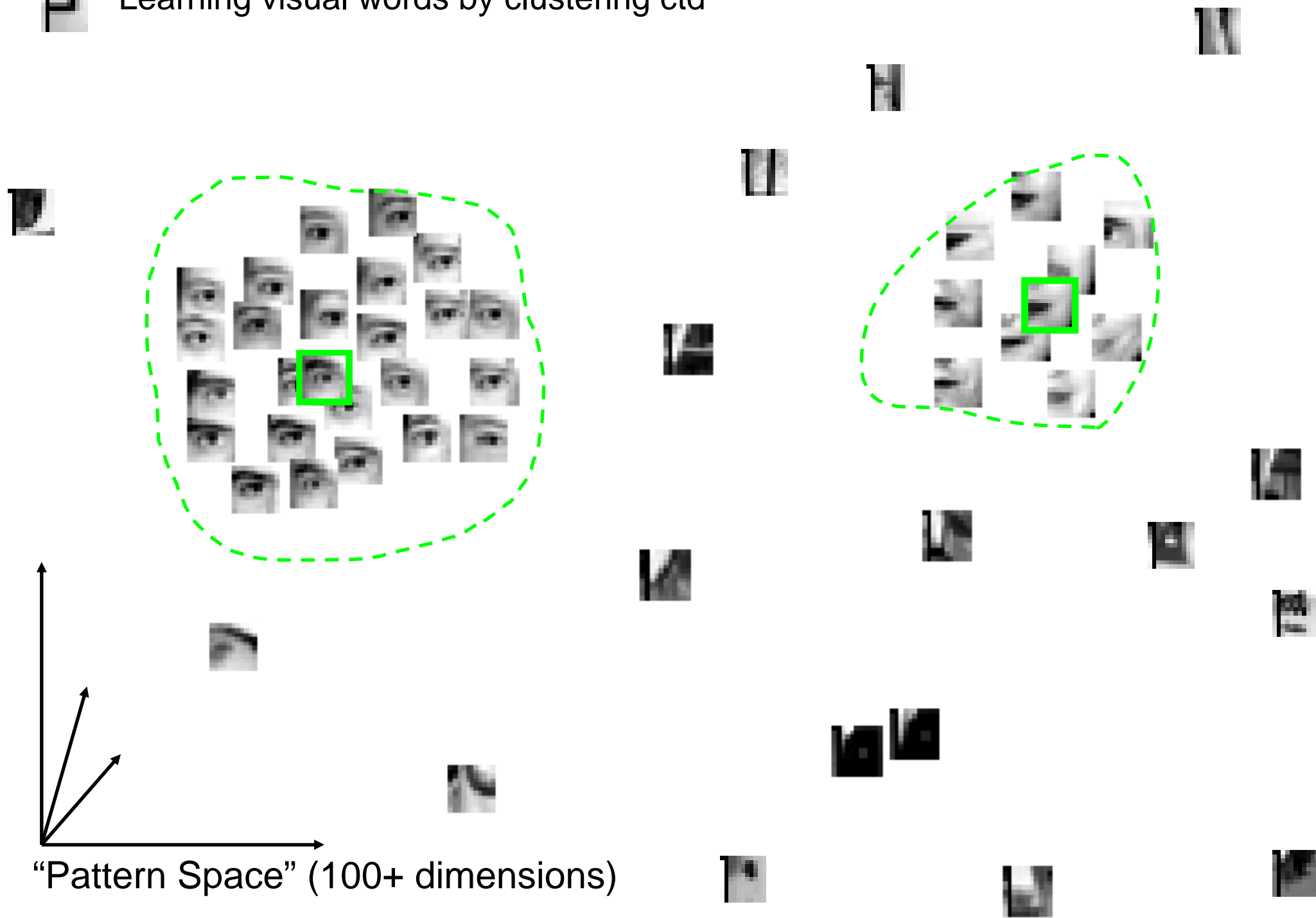
## Example: Learn visual words by clustering



- Interest point features: textured neighborhoods are selected
- produces 100-1000 regions per image

Weber, Welling & Perona 2000

# Learning visual words by clustering ctd

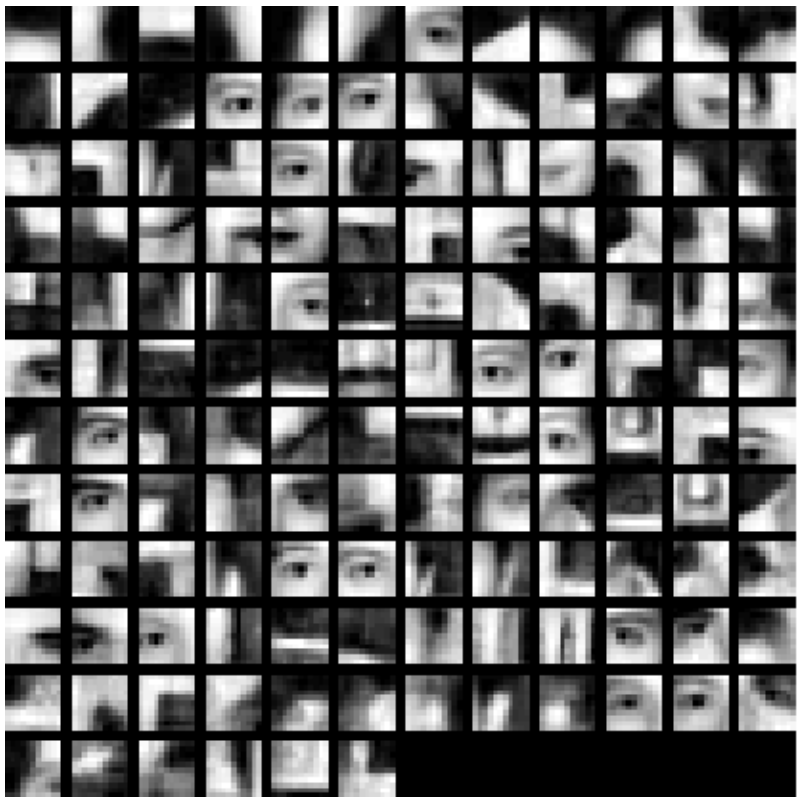
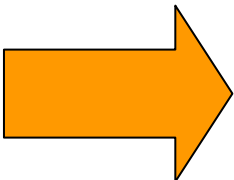




Example of visual words learnt by clustering faces



100-1000 images

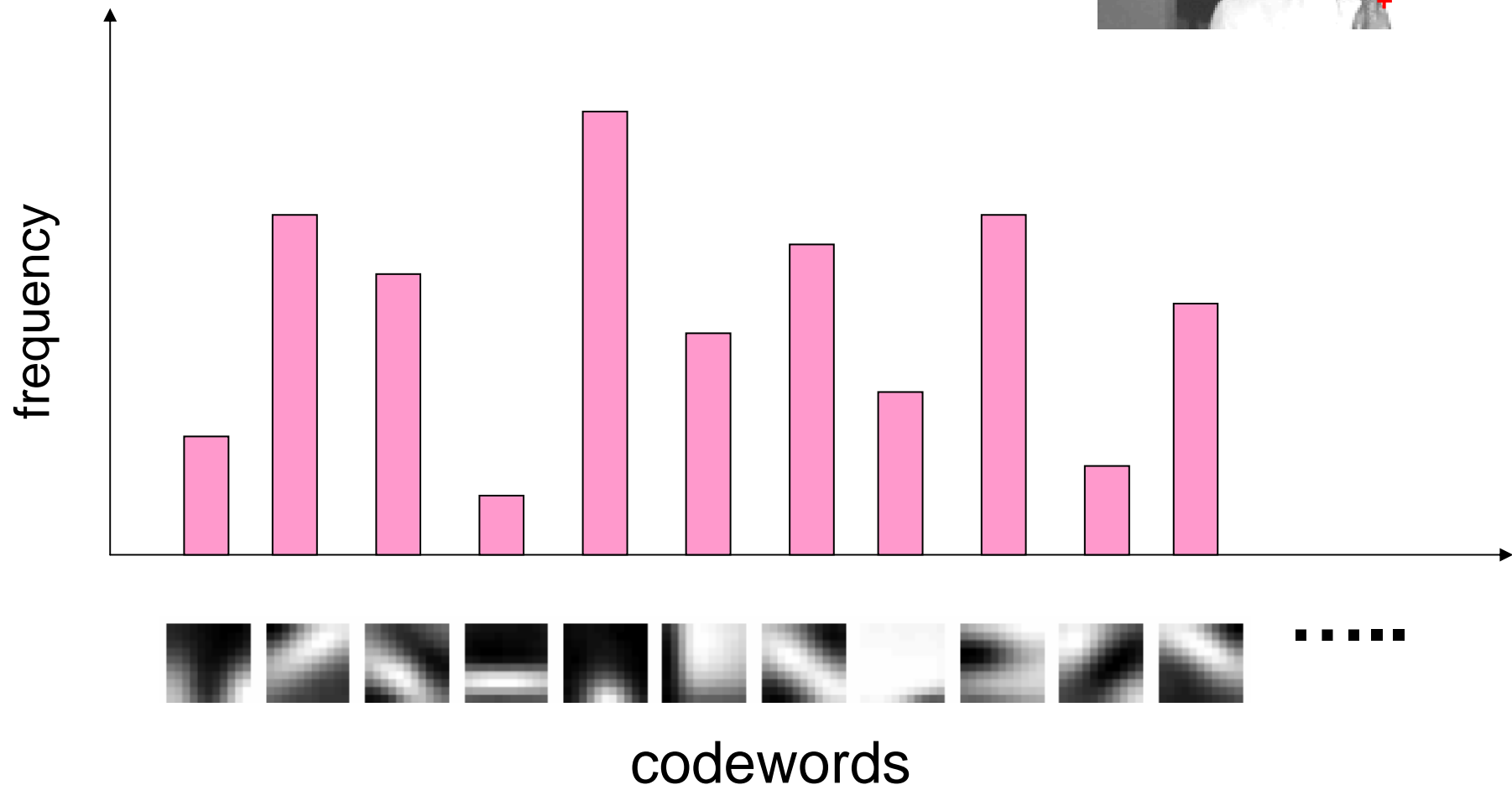
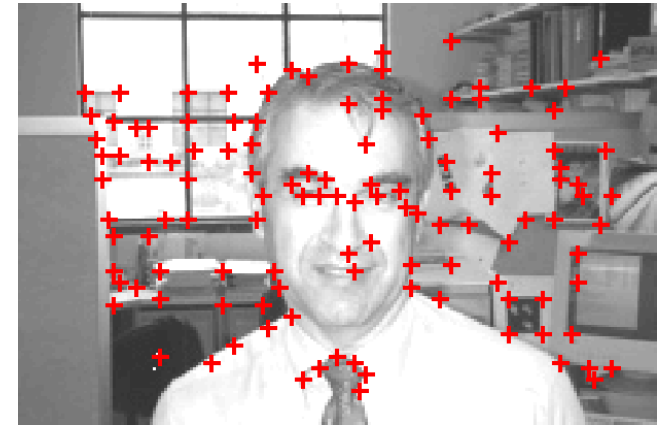


~100 visual words

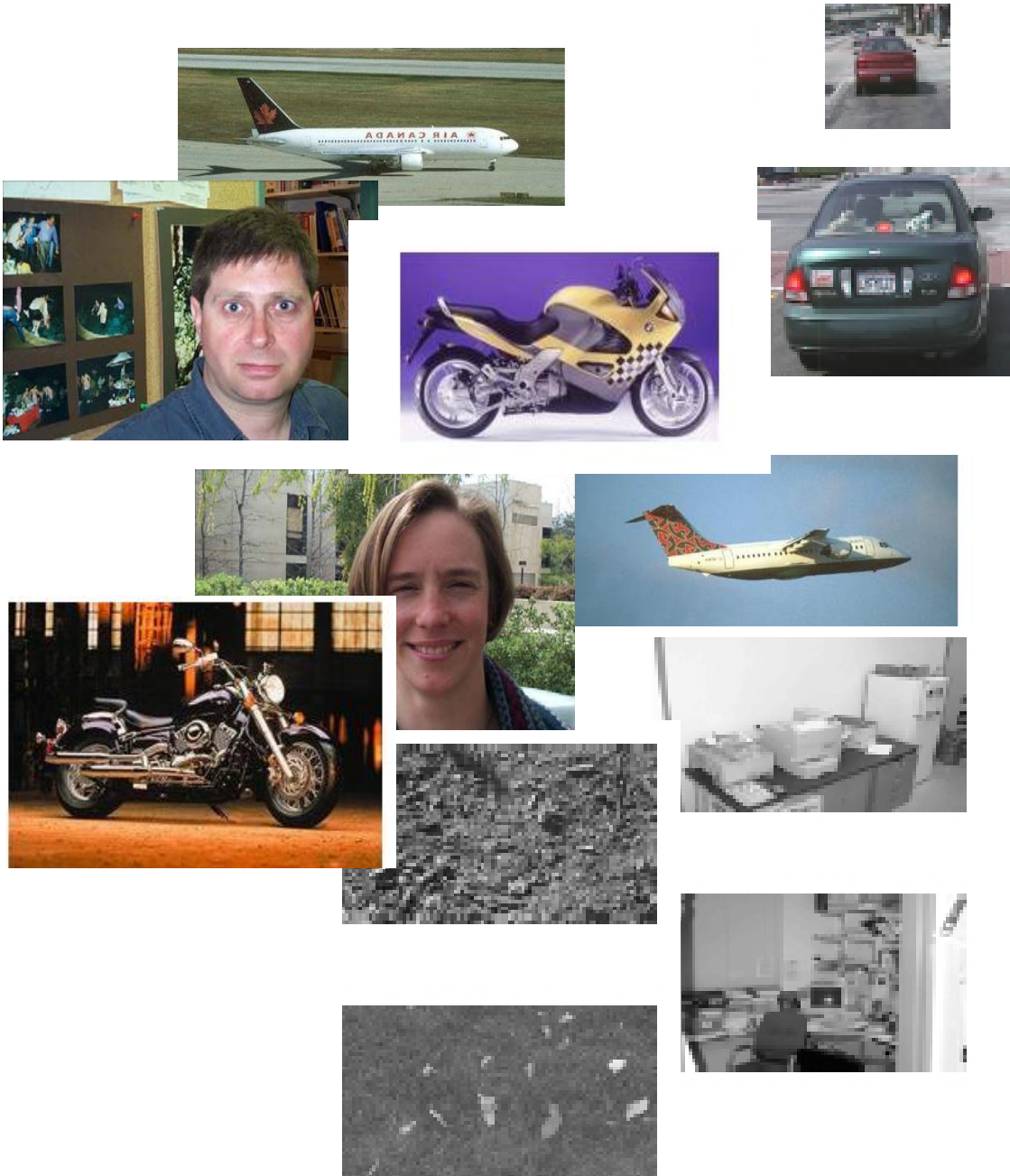


# Image representation – normalized histogram

- detect interest point features
- find closest visual word to region around detected points
- record number of occurrences, but not position



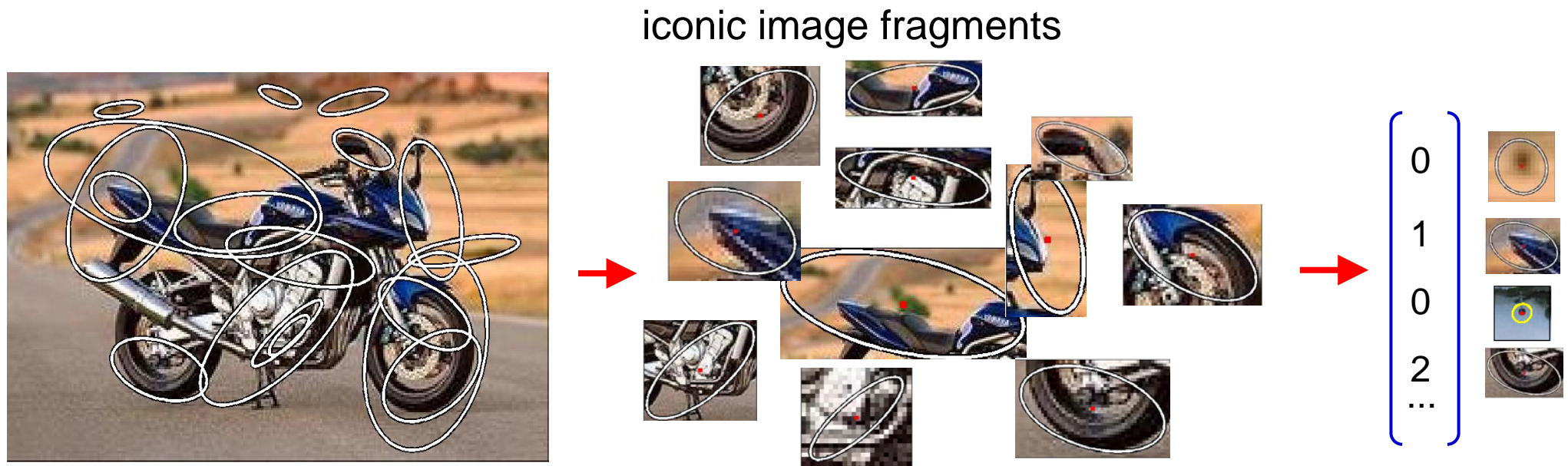
# Example Image collection: four object classes + background



Faces	435
Motorbikes	800
Airplanes	800
Cars (rear)	1155
Background	900
<b>Total:</b>	<b>4090</b>

The “Caltech 5”

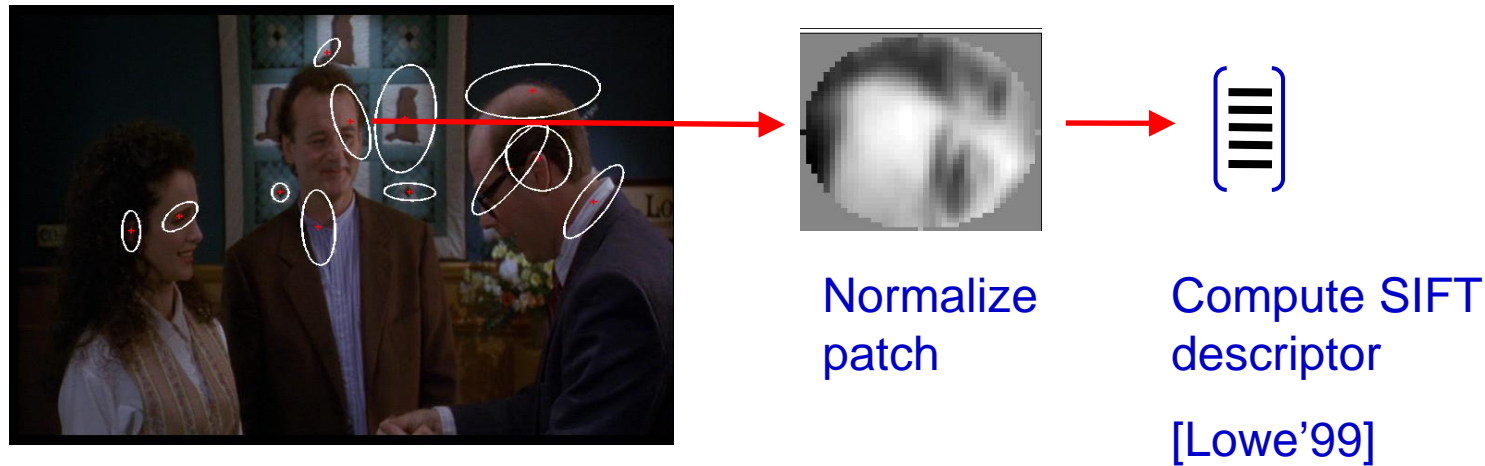
# Represent an image as a histogram of visual words



## Bag of words model

- Detect affine covariant regions
- Represent each region by a SIFT descriptor
- Build visual vocabulary by k-means clustering (K~1,000)
- Assign each region to the nearest cluster centre

# Visual vocabulary for affine covariant patches

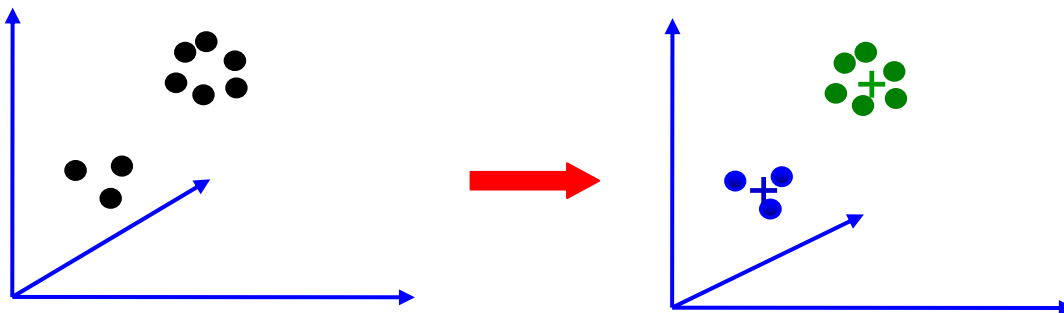


Detect patches

[Mikolajczyk and Schmid '02]

[Matas et al. '02]

Vector quantize descriptors from a set of training images using k-means



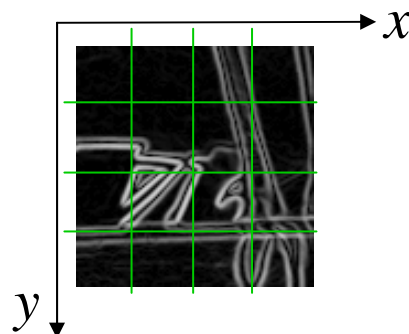
# Descriptors – SIFT [Lowe'99]

distribution of the gradient over an image patch

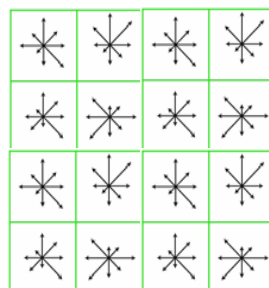
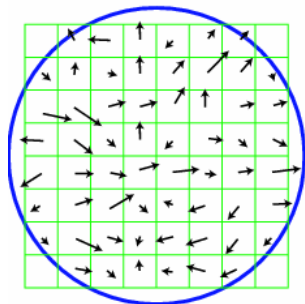
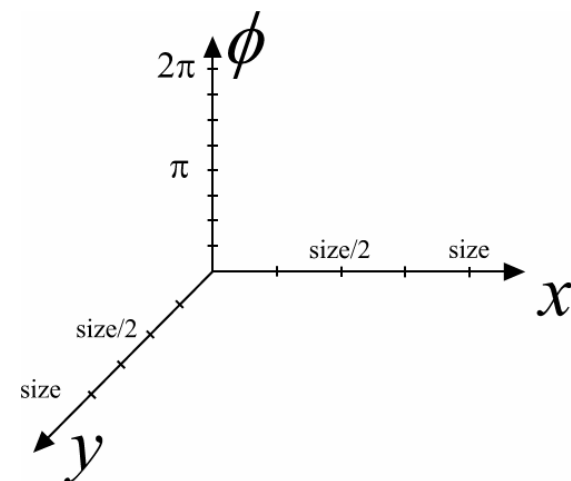
image patch



gradient



3D histogram

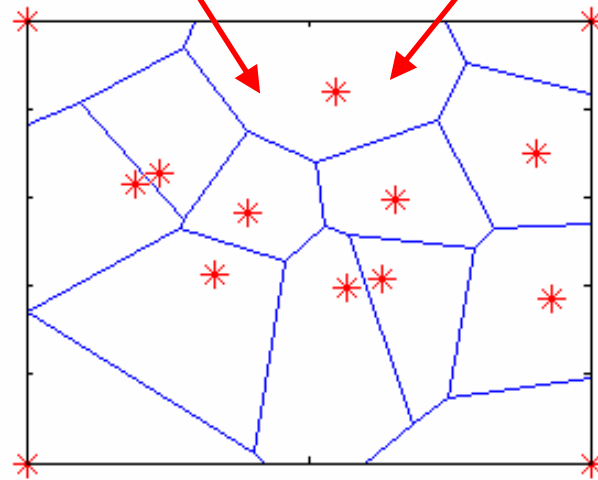


4x4 location grid and 8 orientations (128 dimensions)

very good performance in image matching [Mikolaczyk and Schmid'03]



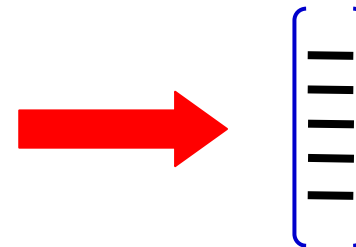
# Vector quantize the descriptor space (SIFT)



The same visual word

Each image: assign all detections to their visual words

- gives bag of visual word representation
- normalized histogram of word frequencies
- also called 'bag of key points'





# Visual words from affine covariant patches

Vector quantize SIFT descriptors to a vocabulary of iconic “visual words”.

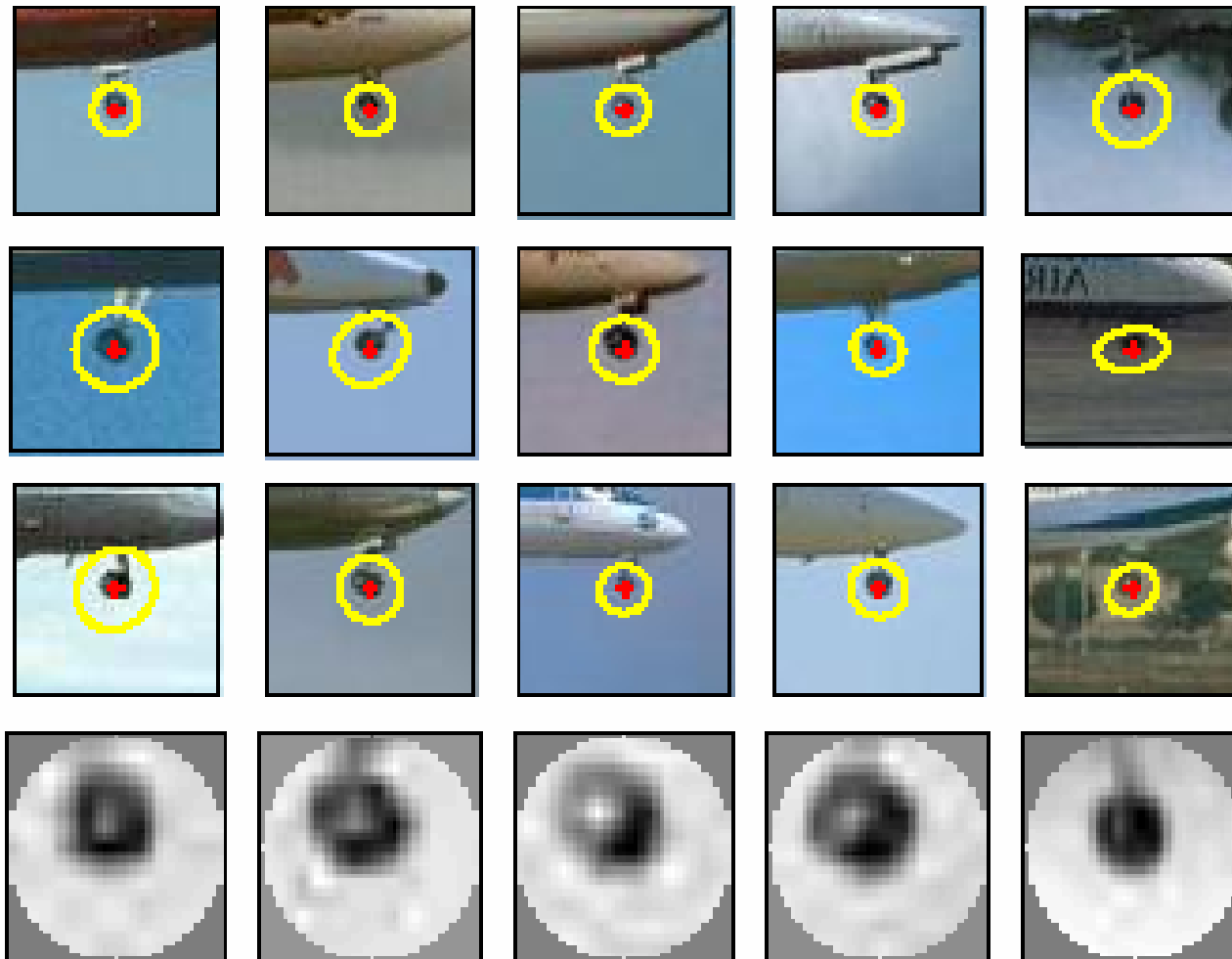
Design of descriptors makes these words invariant to:

- illumination
- affine transformations (viewpoint)

Size (granularity) of vocabulary is an important parameter

- fine grained – represent model instances
- coarse grained – represent object categories

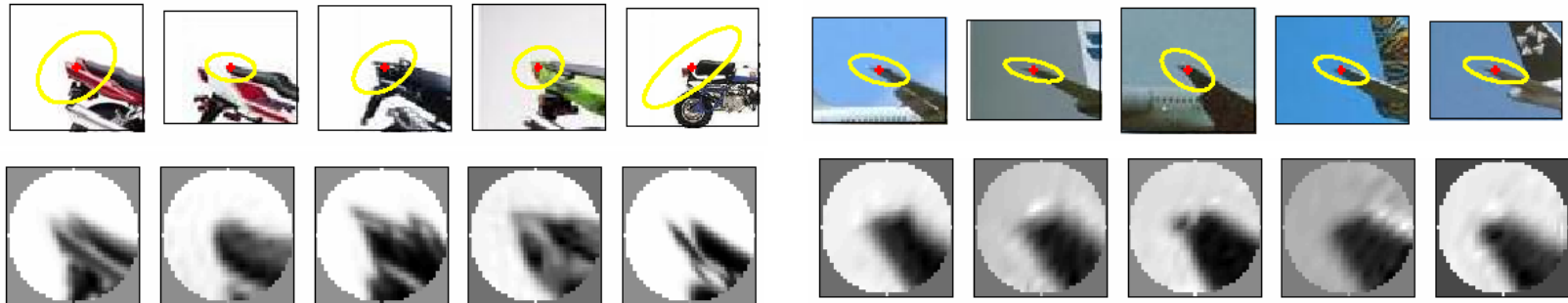
# Examples of visual words



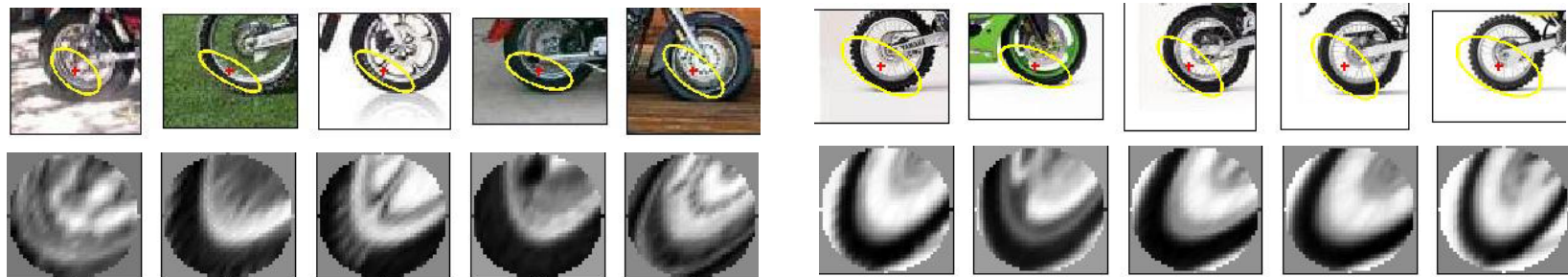
# More visual words



# Visual synonyms and polysemy



**Visual Polysemy:** Single visual word occurring on different (but locally similar) parts on different object categories.



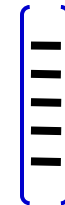
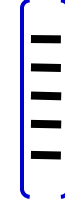
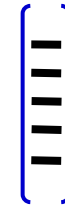
**Visual Synonyms:** Two different visual words representing a similar part of an object (wheel of a motorbike).

Training data: vectors are histograms, one from each training image

positive



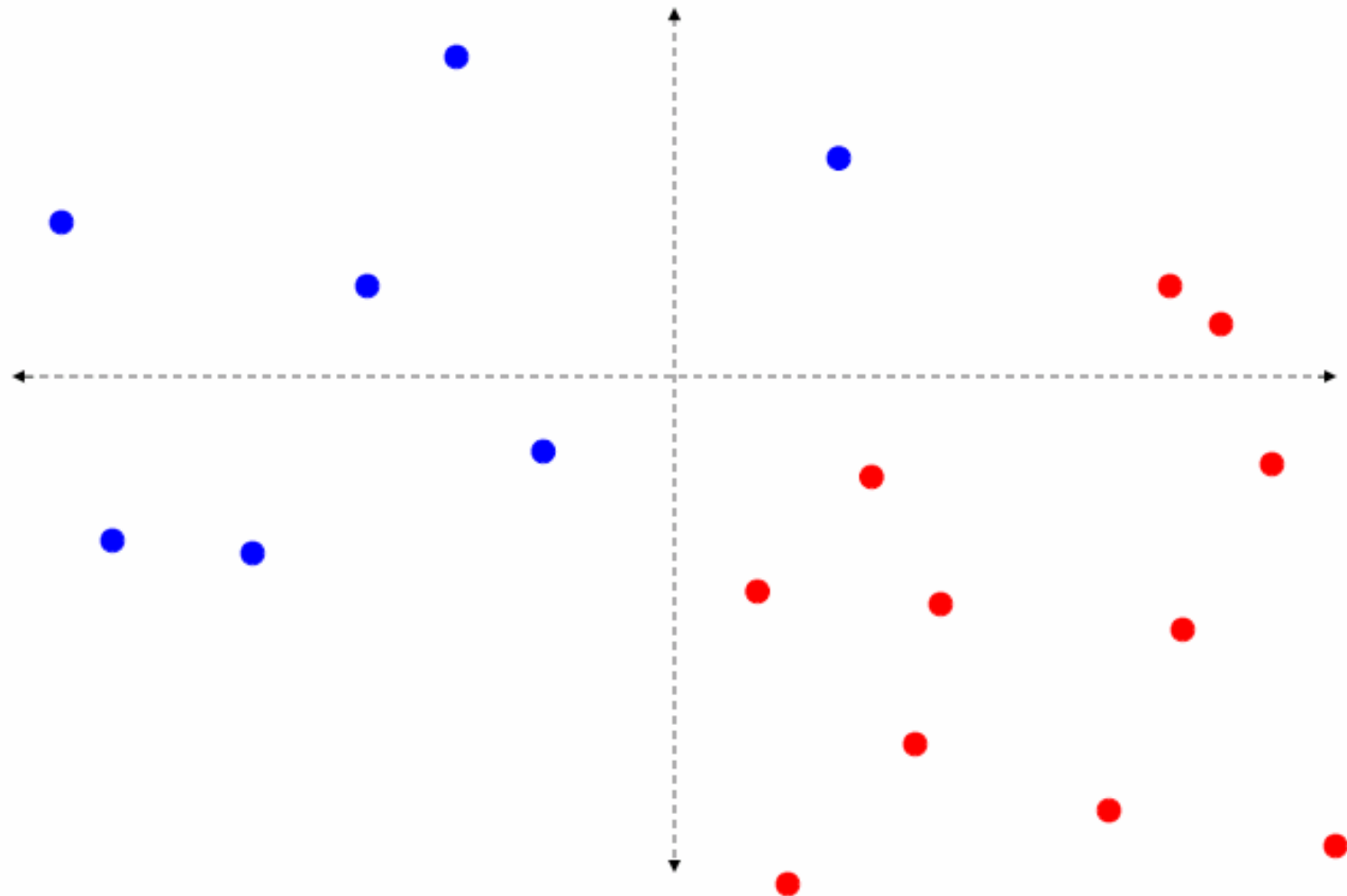
negative



Train classifier, e.g. SVM

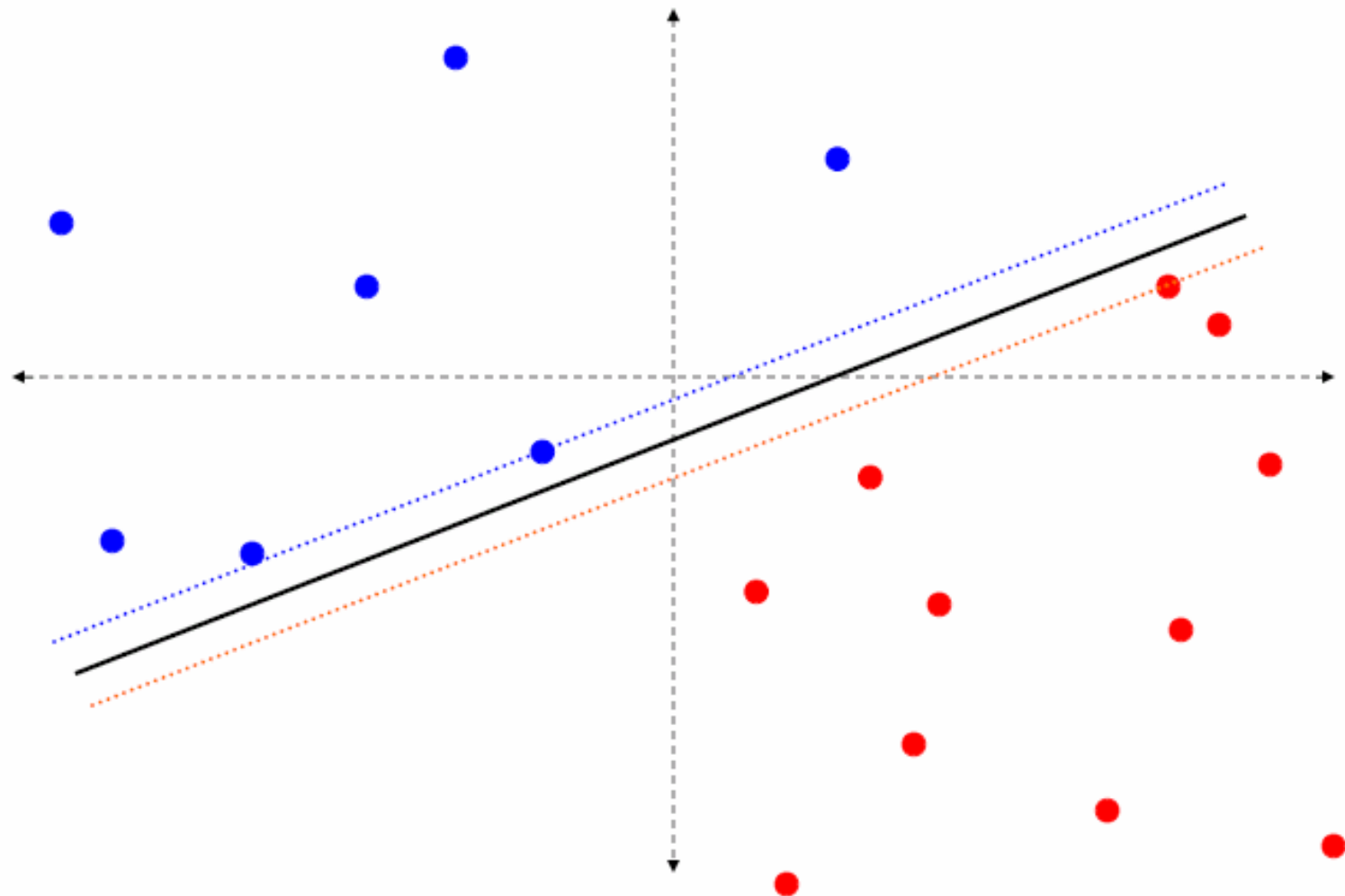
# The Binary Classification Problem

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# A Separating Hyperplane

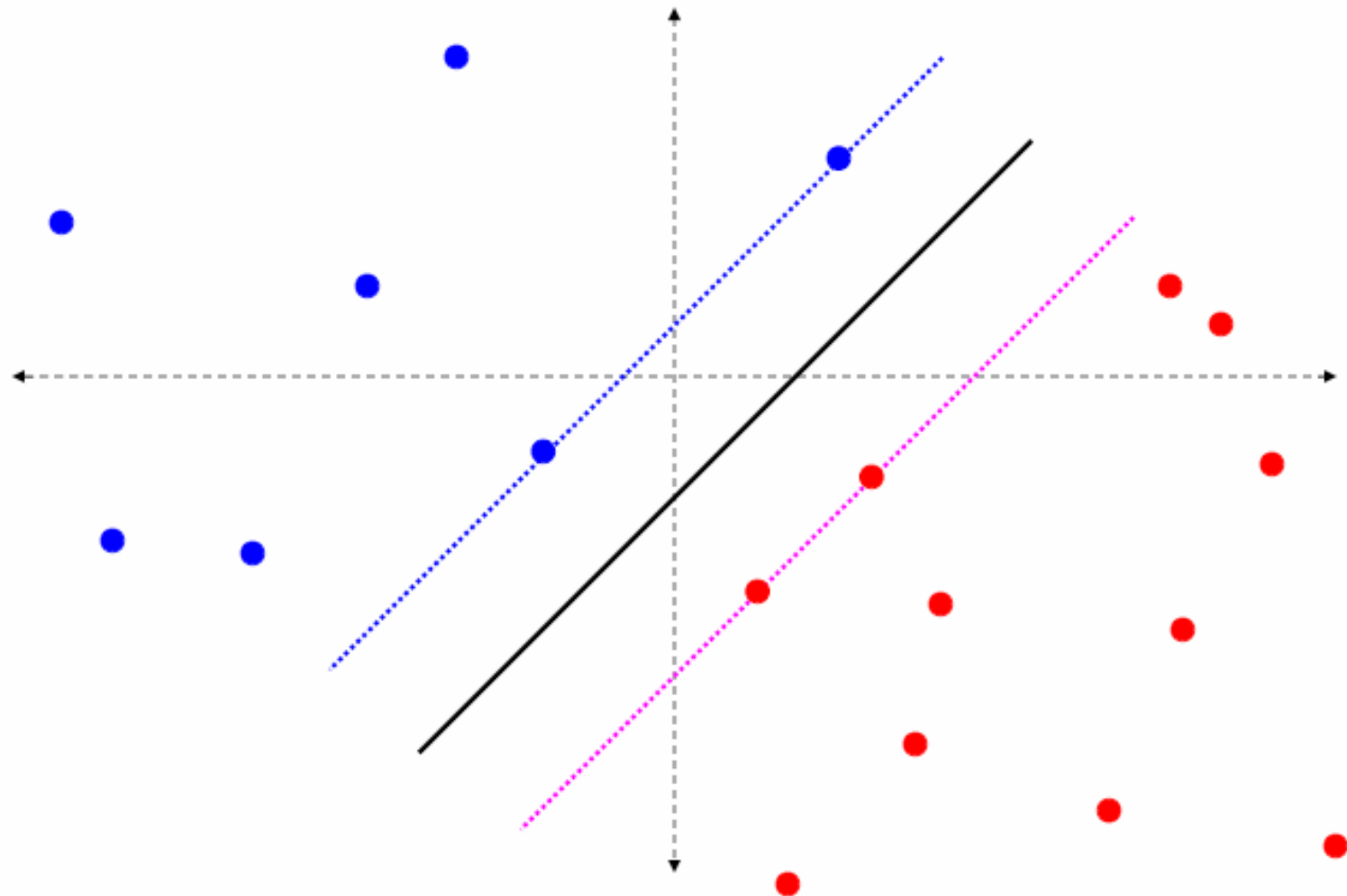
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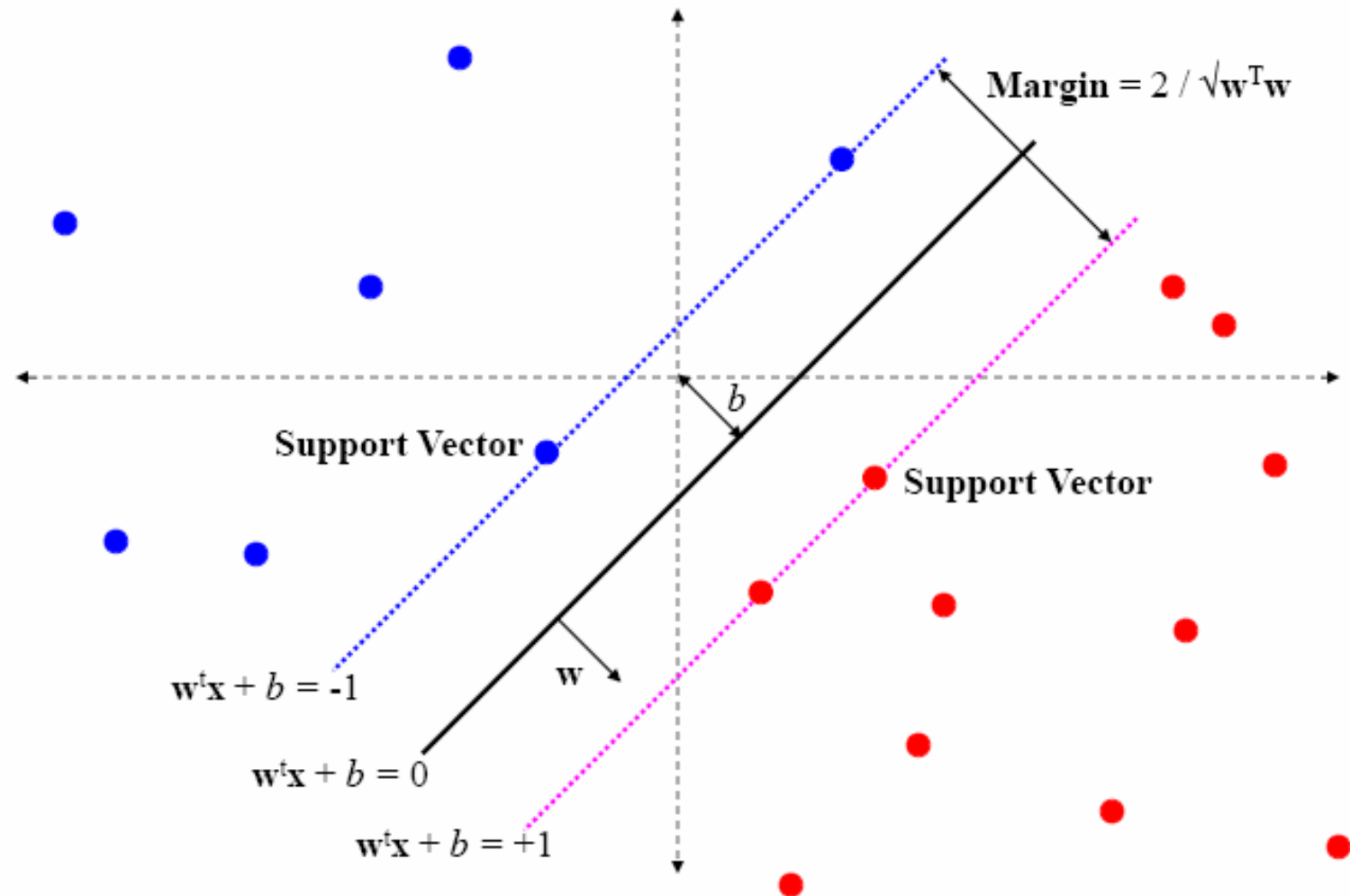


# Maximal Margin Hyperplane

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# SVM Terminology




# SVM classifier with kernels

$N$  = size of training data

$$f(\mathbf{x}) = \sum_i^N \alpha_i k(\mathbf{x}_i, \mathbf{x}) + b$$

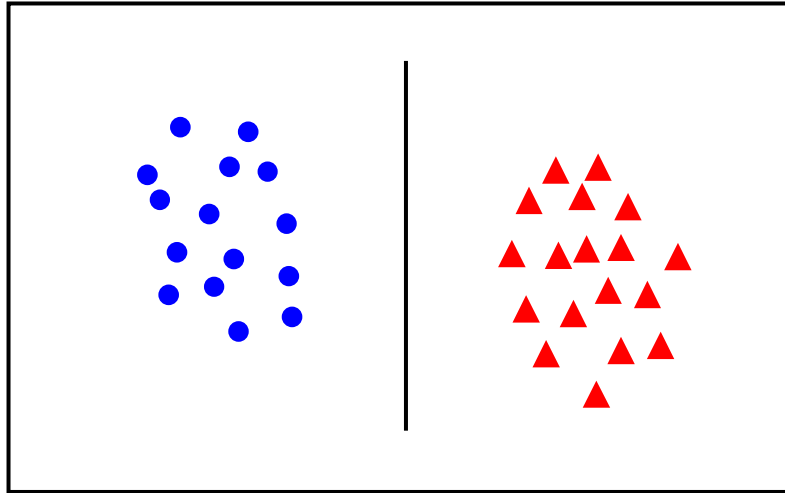
weight (may be zero)      support vector



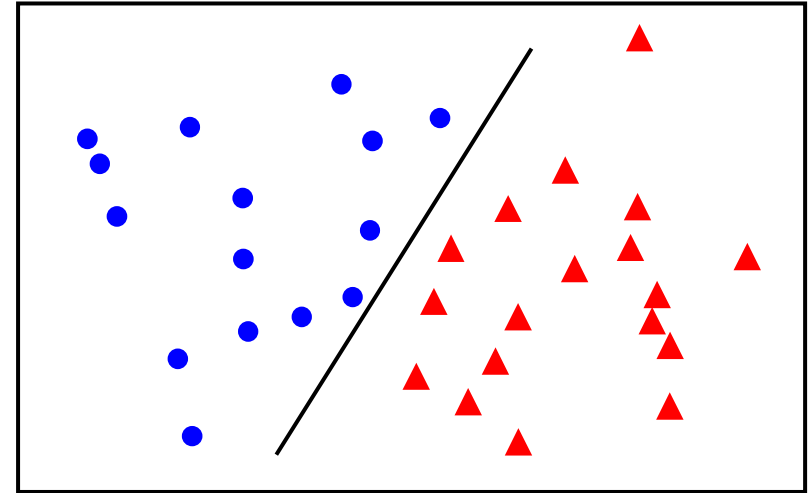
$$f(\mathbf{x}) \begin{cases} \geq 0 & \text{positive class} \\ < 0 & \text{negative class} \end{cases}$$

# Linear separability

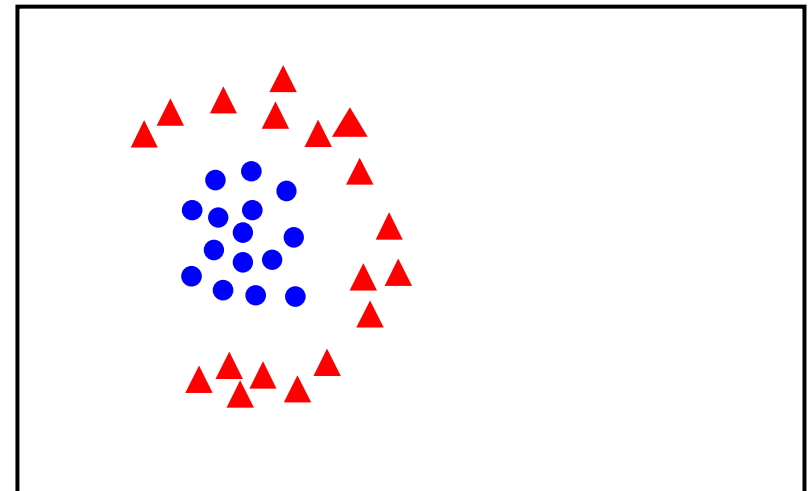
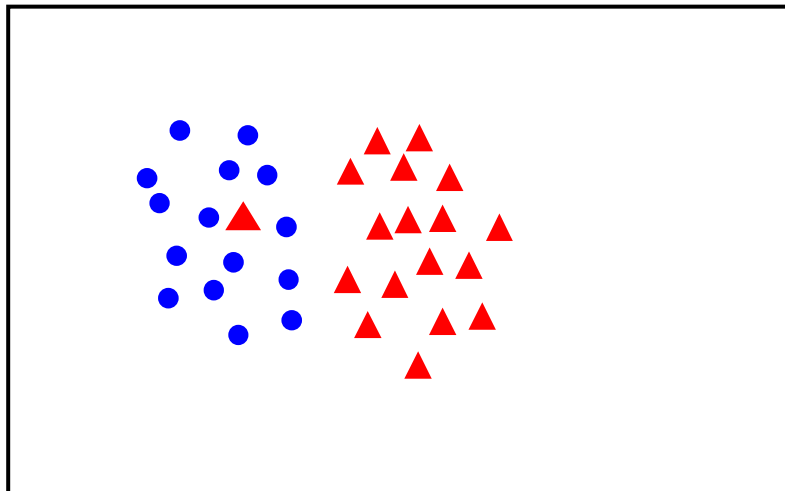
linearly  
separable



linear kernel sufficient



not  
linearly  
separable



use non-linear kernel

# Some popular kernels

- Linear:  $K(\mathbf{x}, \mathbf{y}) = \mathbf{x}^\top \mathbf{y}$
- Polynomial:  $K(\mathbf{x}, \mathbf{y}) = (\mathbf{x}^\top \mathbf{y} + c)^n$
- Radial basis function:  $K(\mathbf{x}, \mathbf{y}) = e^{-\gamma \|\mathbf{x} - \mathbf{y}\|^2}$
- Chi-squared:  $K(\mathbf{x}, \mathbf{y}) = e^{-\gamma \chi^2(\mathbf{x}, \mathbf{y})}$   
where  $\chi^2(\mathbf{x}, \mathbf{y}) = \sum_j \frac{(x_j - y_j)^2}{x_j + y_j}$

# Advantage of linear kernels – at test time

$N$  = size of training data

$$f(\mathbf{x}) = \sum_i^N \alpha_i k(\mathbf{x}_i, \mathbf{x}) + b$$

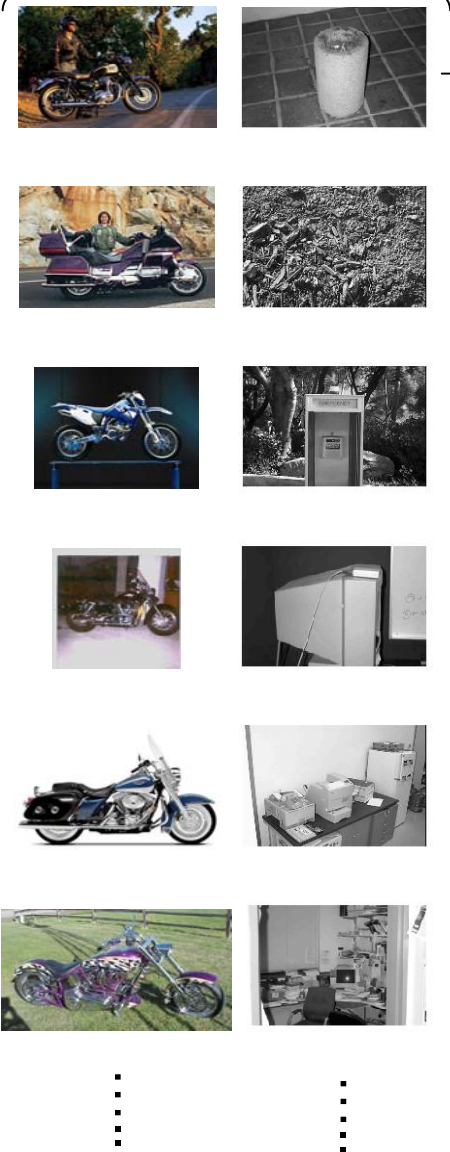
$$f(\mathbf{x}) = \sum_i^N \alpha_i \mathbf{x}_i^\top \mathbf{x} + b$$

$$= \mathbf{w}^\top \mathbf{x} + b$$

Independent of size of training data

# Current Paradigm for learning an object category model

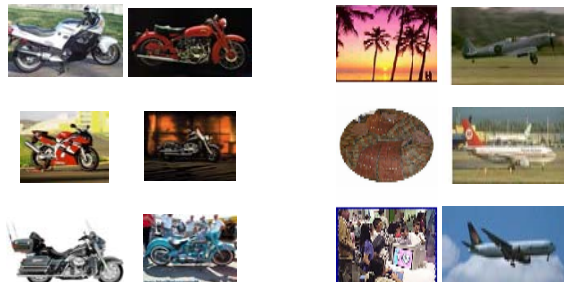
Manually gathered training images



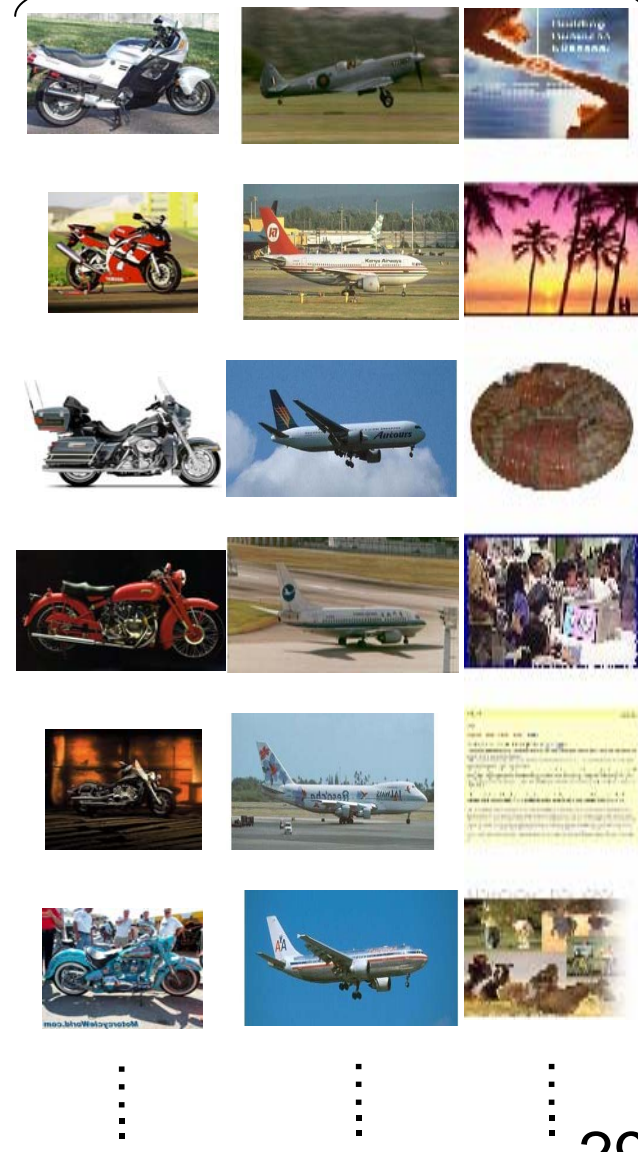
Visual words

Learn a visual category model

Evaluate classifier / detector



Test images





# Example: weak supervision

## Training

- 50% images
- No identification of object within image

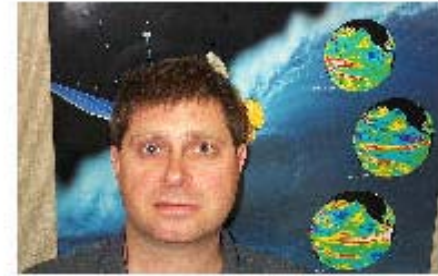
Motorbikes



Airplanes



Frontal Faces



## Testing

- 50% images
- Simple object present/absent test

Cars (Rear)



Background



## Learning

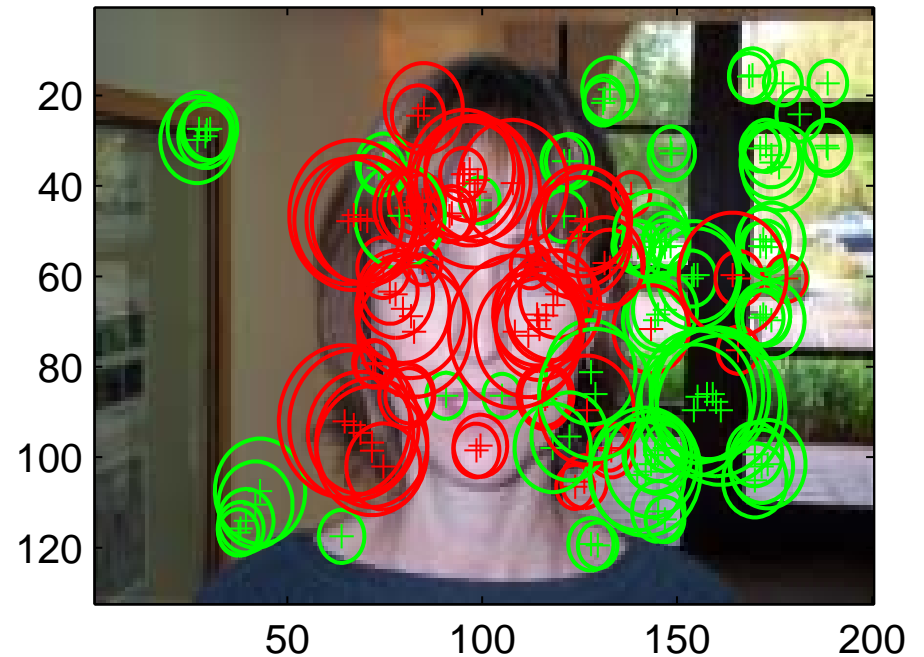
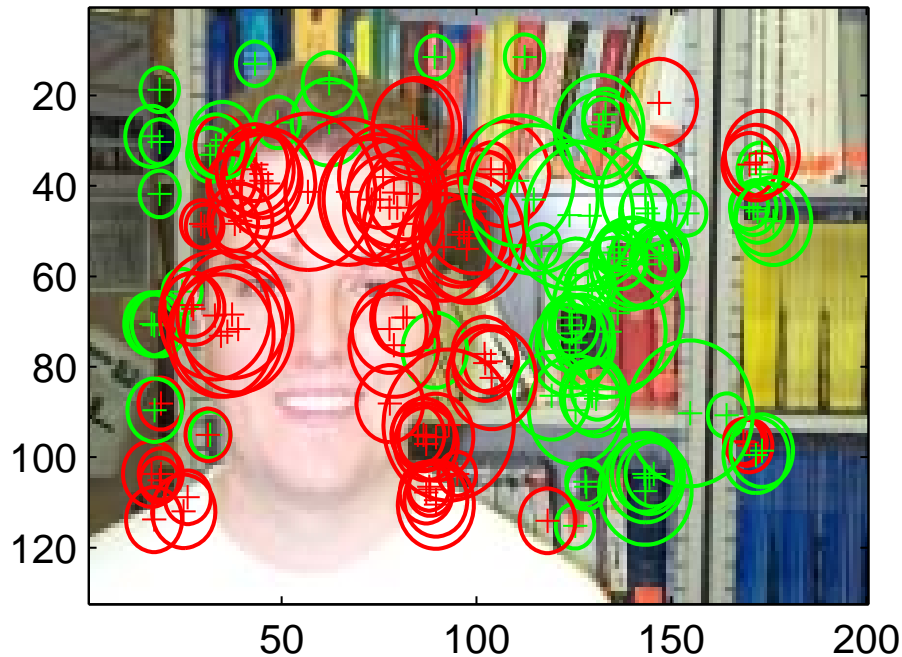
- SVM classifier
- Gaussian kernel using  $\chi^2$  as distance between histograms



## Result

- Between 98.3 – 100% correct, depending on class

# Localization according to visual word probability

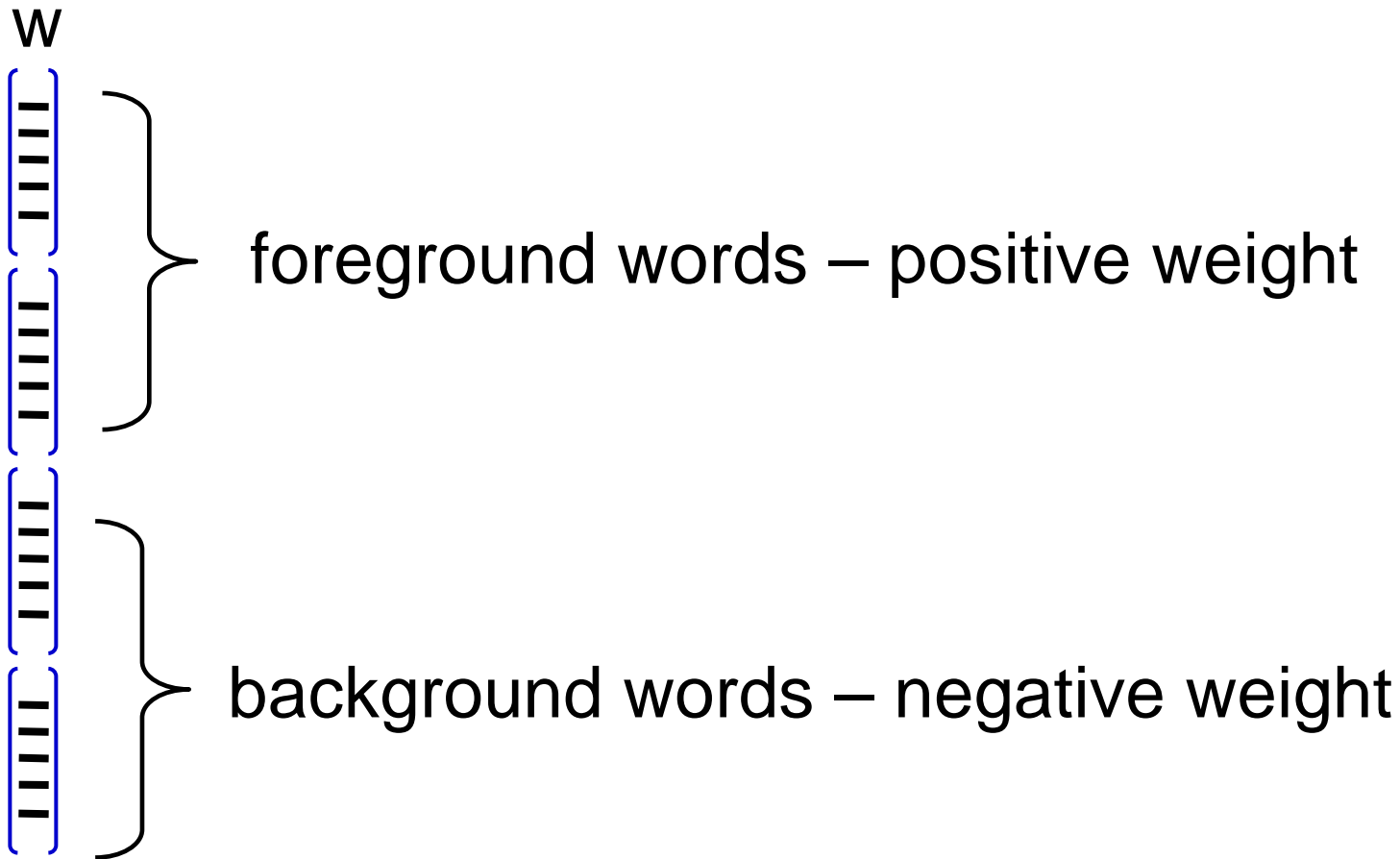
sparse segmentation



-  foreground word more probable
-  background word more probable

# Why does SVM learning work?

- Learns foreground and background visual words



# Bag of visual words summary

- Advantages:

- largely unaffected by position and orientation of object in image
- fixed length vector irrespective of number of detections
- Very successful in classifying images according to the objects they contain
- Still requires further testing for large changes in scale and viewpoint

- Disadvantages:

- No explicit use of configuration of visual word positions
- Poor at **localizing** objects within an image