

# Data Structures (part 2)

*Dataframes*

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PSICOSTAT

# A type of data structure you are already familiar with

	A	B	C	D	E	F	G	H	I
1	Year	Type of course	Title	Teacher	Hours	ECTS	Mandatory	Delivery	Language
2	1	METHODOLOGY	CURRENT ISSUES IN STATISTICAL INFERENCE FOR	MASSIMILIANO PASTORE	10	2	YES	IN PERSON	ENGLISH
3	1	METHODOLOGY	LINEAR AND MIXED EFFECT MODELS WITH SPSS	JEFF KIESNER	15	3	NO	IN PERSON	ENGLISH
4	1	METHODOLOGY	BASICS OF STATISTICAL INFERENCE WITH R	UMBERTO GRANZIOL	20	4	YES	IN PERSON	ENGLISH
5	1	PROGRAMMING	BASICS OF R FOR DATA SCIENCE	ENRICO TOFFALINI	10	2	YES	IN PERSON	ENGLISH
6	1	METHODOLOGY	PSYCHOLOGICAL MEASUREMENT	LUCA STEFANUTTI	15	3	YES	IN PERSON	ENGLISH
7	1	METHODOLOGY	POWER AND DESIGN ANALYSIS	GIANMARCO ALTOE	5	1	YES	IN PERSON	ENGLISH
8	1	METHODOLOGY	EVALUATION OF OUTLIERS AND INFLUENTIAL	GIANMARCO ALTOE	5	1	NO	IN PERSON	ENGLISH
9	1	METHODOLOGY	QUESTIONABLE MEASUREMENT PRACTICES AND	TATIANA MARCI	5	1	YES	IN PERSON	ENGLISH
10	1	METHODOLOGY	DATA VISUALISATION WITH GGLOT2	MICHELE VICOVARO	5	1	NO	IN PERSON	ENGLISH
11	1	SOFT SKILLS	CRAFTING EFFECTIVE SCIENTIFIC	FILIPPO GAMBAROTA	5	1	NO	IN PERSON	ENGLISH
12	1	PROGRAMMING	BASICS OF MATLAB FOR DATA SCIENCE	LUCA STEFANUTTI	10	2	NO	IN PERSON	ENGLISH
13	1	PROGRAMMING	BASICS OF PYTHON FOR DATA SCIENCE	ENRICO TOFFALINI	10	2	NO	IN PERSON	ENGLISH
14	2-3	SOFT SKILLS	ADVANCING RESEARCH PARADIGMS: OPEN	GIULIA CALIGNANO	5	1	NO	IN PERSON	ENGLISH
15	2-3	THEMATIC COURSE	NEUROPSYCHOLOGY OF VISION	LUCA BATTAGLINI	5	1	NO	IN PERSON	ENGLISH
16	2-3	METHODOLOGY	METHODOLOGY IN NEUROSCIENCES	SIMONE CUTINI	10	2	NO	IN PERSON	ENGLISH
17	2-3	METHODOLOGY	BAYESIAN DATA ANALYSIS IN PSYCHOLOGICAL	MASSIMILIANO PASTORE	10	2	NO	IN PERSON	ENGLISH
18	2-3	METHODOLOGY	GENERALISED LINEAR MODELS	FILIPPO GAMBAROTA	15	3	NO	IN PERSON	ENGLISH
19	2-3	METHODOLOGY	STRUCTURAL EQUATION MODELING	TOMMASO FERACO	20	4	NO	IN PERSON	ENGLISH
20	2-3	METHODOLOGY	CONDUCTING SYSTEMATIC REVIEWS	ENRICO SELLA	5	1	NO	IN PERSON	ENGLISH
21	2-3	METHODOLOGY	INTRODUCTION TO ITEM RESPONSE THEORY	MARINA OTTAVIA EPIFANIA	15	3	NO	IN PERSON	ENGLISH
22	2-3	SOFT SKILLS	HOW TO WIN RESEARCH GRANTS	CHRISTIAN AGRILLO	5	1	NO	IN PERSON	ENGLISH
23	2-3	SOFT SKILLS	CAREER COUNSELING	NICOLA CELLINI	10	2	NO	IN PERSON	ENGLISH
24	2-3	SOFT SKILLS	OUTSIDE ACADEMIA	ALESSIA BASTIANELLI	5	1	NO	IN PERSON	ENGLISH
25	2-3	METHODOLOGY	INTRODUCTION TO META-ANALYSIS WITH	GIANMARCO ALTOE	5	1	NO	IN PERSON	ENGLISH
26	2-3	METHODOLOGY	DATA SIMULATION IN PSYCHOLOGICAL STUDIES	MASSIMILIANO PASTORE	10	2	NO	IN PERSON	ENGLISH
27	2-3	SOFT SKILLS	PUBLISHING IN HIGH-IMPACT JOURNALS	MARA CADINU	15	3	NO	IN PERSON	ENGLISH
28	2-3	THEMATIC COURSE	PSYCHONEUROENDOCRINOLOGY	JEFF KIESNER	5	1	NO	IN PERSON	ENGLISH
29	2-3	PROGRAMMING	BASICS OF LINUX FOR DATA SCIENCE	FRANCESCO VESPIGNANI	5	1	NO	IN PERSON	ENGLISH

# A type of data structure you are already familiar with

here is how I would import it in R ([download here](#)), and display the first few rows:

```
library(readxl)
df = data.frame(read_excel("data/Courses40Cycle.xlsx"))
head(df)
```

	Year	TypeOfCourse	Title					
1	1	METHODOLOGY	CURRENT ISSUES IN STATISTICAL INFERENCE FOR PSYCHOLOGY					
2	1	METHODOLOGY	LINEAR AND MIXED EFFECT MODELS WITH SPSS					
3	1	METHODOLOGY	BASICS OF STATISTICAL INFERENCE WITH R					
4	1	PROGRAMMING	BASICS OF R FOR DATA SCIENCE					
5	1	METHODOLOGY	PSYCHOLOGICAL MEASUREMENT					
6	1	METHODOLOGY	POWER AND DESIGN ANALYSIS					
	Teacher	Hours	ECTS	Mandatory	Attendance	DeliveryMethod	Language	
1	MASSIMILIANO PASTORE	10	2		YES	IN PERSON	ENGLISH	
2	JEFF KIESNER	15	3		NO	IN PERSON	ENGLISH	
3	UMBERTO GRANZIOL	20	4		YES	IN PERSON	ENGLISH	
4	ENRICO TOFFALINI	10	2		YES	IN PERSON	ENGLISH	
5	LUCA STEFANUTTI	15	3		YES	IN PERSON	ENGLISH	
6	GIANMARCO ALTOE	5	1		YES	IN PERSON	ENGLISH	

# Dataframes as collections of vectors

In fact, **dataframes** are just collections (lists) of **vectors of different types**, all with the same length. Each column in a dataframe is a vector (a variable):

df\$Teacher	
[1]	"MASSIMILIANO PASTORE" "JEFF KIESNER"
[3]	"UMBERTO GRANZIOL" "ENRICO TOFFALINI"
[5]	"LUCA STEFANUTTI" "GIANMARCO ALTOE"
[7]	"GIANMARCO ALTOE" "TATIANA MARCI"
[9]	"MICHELE VICOVARO" "FILIPPO GAMBAROTA"
[11]	"LUCA STEFANUTTI" "ENRICO TOFFALINI"
[13]	"GIULIA CALIGNANO" "LUCA BATTAGLINI"
[15]	"SIMONE CUTINI" "MASSIMILIANO PASTORE"
[17]	"FILIPPO GAMBAROTA" "TOMMASO FERACO"
[19]	"ENRICO SELLA" "MARINA OTTAVIA EPIFANIA"
[21]	"CHRISTIAN AGRILLO" "NICOLA CELLINI"
[23]	"ALESSIA BASTIANELLI" "GIANMARCO ALTOE"
[25]	"MASSIMILIANO PASTORE" "MARA CADINU"
[27]	"JEFF KIESNER" "FRANCESCO VESPIGNANI"
df\$Hours	
[1]	10 15 20 10 15 5 5 5 5 5 10 10 5 5 10 10 15 20 5 15 5 10 5 5
10	
[26]	15 5 5

# Basic Functions on Dataframes

To know the names of all variables in a dataframe, use the **names()** function:

```
names(df)

[1] "Year"           "TypeOfCourse"    "Title"
[4] "Teacher"        "Hours"           "ECTS"
[7] "MandatoryAttendance" "DeliveryMethod"  "Language"
```

Use the **dim()** function to view the dimensions of a dataframe:

```
# first value is number of rows, second is number of columns (variables)
dim(df)

[1] 28  9
```

Alternatively, you can use **nrow()** and **ncol()**:

```
nrow(df) # number of rows

[1] 28
```

```
ncol(df) # number of columns

[1] 9
```

# Basic Functions on Dataframes

The **str()** function provides a quick overview of the structure of a dataframe, including its dimensions, variables, their data types, and first few observations:

```
str(df)

'data.frame':  28 obs. of  9 variables:
 $ Year          : chr  "1" "1" "1" "1" ...
 $ TypeOfCourse  : chr  "METHODODOLOGY" "METHODODOLOGY" "METHODODOLOGY"
 "PROGRAMMING" ...
 $ Title         : chr  "CURRENT ISSUES IN STATISTICAL INFERENCE FOR
 PSYCHOLOGY" "LINEAR AND MIXED EFFECT MODELS WITH SPSS" "BASICS OF STATISTICAL
 INFERENCE WITH R" "BASICS OF R FOR DATA SCIENCE" ...
 $ Teacher       : chr  "MASSIMILIANO PASTORE" "JEFF KIESNER" "UMBERTO
 GRANZIOL" "ENRICO TOFFALINI" ...
 $ Hours         : num  10 15 20 10 15 5 5 5 5 5 ...
 $ ECTS          : num  2 3 4 2 3 1 1 1 1 1 ...
 $ MandatoryAttendance: chr  "YES" "NO" "YES" "YES" ...
 $ DeliveryMethod : chr  "IN PERSON" "IN PERSON" "IN PERSON" "IN PERSON"
 ...
 $ Language      : chr  "ENGLISH" "ENGLISH" "ENGLISH" "ENGLISH" ...
```

# Accessing Elements in Dataframes

The “\$” (dollar) operator is essential to access variables in a dataframe:

The screenshot shows an R console window with the following content:

```
>  
>  
> df$
```

Annotations for the console output:

- Name of the dataframe object followed by "\$"**: Points to `df$`.
- Type of the highlighted variable**: Points to `<character>`.
- Length of the highlighted variable (vector)**: Points to `[28]`.
- Pointing a variable highlights it**: Points to the `Teacher` variable in the list.
- A preview of the content**: Points to the text `chr [1:28] "MASSIMILIANO PASTORE" "JEFF KIESNER" "UMBERTO GRANZIOL" "ENRICO TOFFALINI" ...`.
- A list of all variables (vectors) composing this dataframe**: Points to the list of variables: `Year`, `TypeOfCourse`, `Title`, `Teacher`, `Hours`, `ECTS`, `MandatoryAttendance`, `DeliveryMethod`, and `Language`.

Variable	Type
<code>Year</code>	<code>[df]</code>
<code>TypeOfCourse</code>	<code>[df]</code>
<code>Title</code>	<code>[df]</code>
<code>Teacher</code>	<code>[df]</code>
<code>Hours</code>	<code>[df]</code>
<code>ECTS</code>	<code>[df]</code>
<code>MandatoryAttendance</code>	<code>[df]</code>
<code>DeliveryMethod</code>	<code>[df]</code>
<code>Language</code>	<code>[df]</code>

# Accessing and Working with Elements in Dataframes

As an exercise, let's check whether ECTS is actually always  $\text{Hours} \cdot 5$

We may use many different, increasingly sophisticated, strategies:

$$\text{df\$Hours} / \text{df\$ECTS}$$

[1] 5

```
(df$Hours / df$ECTS) == 5
```

```
[1] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
TRUE TRUE TRUE
```

```
[16] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
TRUE
```

```
sum( (df$Hours / df$ECTS) == 5)
```

[1] 28

```
sum( (df$Hours / df$ECTS) == 5) == nrow(df)
```

```
[1] TRUE
```

```
sum((df$Hours / df$ECTS) != 5)
```

[1] 0



# Accessing and Working with Elements in Dataframes

Variables in a dataframe can be manipulated like any other vector:

```
log(df$Hours)
[1] 2.302585 2.708050 2.995732 2.302585 2.708050 1.609438 1.609438 1.609438
[9] 1.609438 1.609438 2.302585 2.302585 1.609438 1.609438 2.302585 2.302585
[17] 2.708050 2.995732 1.609438 2.708050 1.609438 2.302585 1.609438 1.609438
[25] 2.302585 2.708050 1.609438 1.609438
```

Also, new variables can easily be created and added at any time:

```
df$newVar = log(df$Hours)
names(df)
[1] "Year"           "TypeOfCourse"   "Title"
[4] "Teacher"        "Hours"          "ECTS"
[7] "MandatoryAttendance" "DeliveryMethod" "Language"
[10] "newVar"

df$newVar
[1] 2.302585 2.708050 2.995732 2.302585 2.708050 1.609438 1.609438 1.609438
[9] 1.609438 1.609438 2.302585 2.302585 1.609438 1.609438 2.302585 2.302585
[17] 2.708050 2.995732 1.609438 2.708050 1.609438 2.302585 1.609438 1.609438
[25] 2.302585 2.708050 1.609438 1.609438
```

# Indexing Elements in a Dataframe

In addition to using the “\$” (dollar) operator, you can directly access a variable of a dataframe using **indexing** with **square brackets []**:

```
df[ , "Hours"]  
[1] 10 15 20 10 15 5 5 5 5 5 10 10 5 5 10 10 15 20 5 15 5 10 5 5  
10  
[26] 15 5 5
```

Notice the comma “,” above.

Unlike vectors, dataframes must be indexed by **both row and column**. In the example above, we’re specifying only the desired column (“Hours”), leaving the row index blank before the comma , This selects all rows for the column named “Hours”. Remember that blank index means “all”. Importantly, the “,” must always be there when indexing dataframes!

# Indexing Elements in a Dataframe - Examples

```
df[ 1 , "Hours"]
```

```
[1] 10
```

```
df[ 1:5 , "Hours"]
```

```
[1] 10 15 20 10 15
```

```
df[ 1 , c("Teacher","Hours","TypeOfCourse")]
```

```
      Teacher Hours TypeOfCourse  
1 MASSIMILIANO PASTORE      10  METHODOLOGY
```

```
df[ 1:5 , c("Teacher","Hours","TypeOfCourse")]
```

```
      Teacher Hours TypeOfCourse  
1 MASSIMILIANO PASTORE      10  METHODOLOGY  
2           JEFF KIESNER      15  METHODOLOGY  
3    UMBERTO GRANZIOL      20  METHODOLOGY  
4    ENRICO TOFFALINI      10  PROGRAMMING  
5      LUCA STEFANUTTI      15  METHODOLOGY
```

```
df[ 1 , c(4, 5, 2)]
```

```
      Teacher Hours TypeOfCourse  
1 MASSIMILIANO PASTORE      10  METHODOLOGY
```

# Indexing and Modifying Elements in a Dataframe

Editing/modifying elements in a dataframe is similar to what you do in vectors

```
dx = data.frame(name = letters[1:10],  
                score = rnorm(10))
```

dx

	name	score
1	a	1.262954285
2	b	-0.326233361
3	c	1.329799263
4	d	1.272429321
5	e	0.414641434
6	f	-1.539950042
7	g	-0.928567035
8	h	-0.294720447
9	i	-0.005767173
10	j	2.404653389

```
dx[3:5, "score"] = NA
```

dx

	name	score
1	a	1.262954285
2	b	-0.326233361
3	c	NA
4	d	NA
5	e	NA
6	f	-1.539950042
7	g	-0.928567035
8	h	-0.294720447
9	i	-0.005767173
10	j	2.404653389

# Indexing and Modifying Elements in a Dataframe

Editing/modifying elements in a dataframe is similar to what you do in vectors

```
dx = data.frame(name = letters[1:10],  
                score = rnorm(10))
```

dx

	name	score
1	a	1.262954285
2	b	-0.326233361
3	c	1.329799263
4	d	1.272429321
5	e	0.414641434
6	f	-1.539950042
7	g	-0.928567035
8	h	-0.294720447
9	i	-0.005767173
10	j	2.404653389

```
dx$score = dx$score * 10
```

dx

	name	score
1	a	12.62954285
2	b	-3.26233361
3	c	13.29799263
4	d	12.72429321
5	e	4.14641434
6	f	-15.39950042
7	g	-9.28567035
8	h	-2.94720447
9	i	-0.05767173
10	j	24.04653389

# Indexing and Modifying Elements in a Dataframe

Editing/modifying elements in a dataframe is similar to what you do in vectors

```
dx = data.frame(name = letters[1:10],  
                score = rnorm(10))
```

dx

	name	score
1	a	1.262954285
2	b	-0.326233361
3	c	1.329799263
4	d	1.272429321
5	e	0.414641434
6	f	-1.539950042
7	g	-0.928567035
8	h	-0.294720447
9	i	-0.005767173
10	j	2.404653389

```
dx$score = round( 100 + d
```

dx

	name	score
1	a	119
2	b	95
3	c	120
4	d	119
5	e	106
6	f	77
7	g	86
8	h	96
9	i	100
10	j	136

# Indexing and Modifying Elements in a Dataframe

Assigning a single value to a column replaces the value for all rows (this is unlike vectors)

```
dx = data.frame(name = letters[1:10],  
                 score = rnorm(10))
```

dx

	name	score
1	a	1.262954285
2	b	-0.326233361
3	c	1.329799263
4	d	1.272429321
5	e	0.414641434
6	f	-1.539950042
7	g	-0.928567035
8	h	-0.294720447
9	i	-0.005767173
10	j	2.404653389

```
dx$score = 3
```

dx

	name	score
1	a	3
2	b	3
3	c	3
4	d	3
5	e	3
6	f	3
7	g	3
8	h	3
9	i	3
10	j	3

# Indexing Dataframes by Logical Conditions

Just like for vectors, you can use **logical conditions** for indexing a dataframe.

How do you extract **only the rows** related to "MASSIMILIANO PASTORE"?

```
head(df)
```

	Year	TypeOfCourse						Title
1	1	METHODOLOGY	CURRENT ISSUES IN STATISTICAL INFERENCE FOR PSYCHOLOGY					
2	1	METHODOLOGY	LINEAR AND MIXED EFFECT MODELS WITH SPSS					
3	1	METHODOLOGY	BASICS OF STATISTICAL INFERENCE WITH R					
4	1	PROGRAMMING	BASICS OF R FOR DATA SCIENCE					
5	1	METHODOLOGY	PSYCHOLOGICAL MEASUREMENT					
6	1	METHODOLOGY	POWER AND DESIGN ANALYSIS					
		Teacher	Hours	ECTS	Mandatory	Attendance	DeliveryMethod	Language
1		MASSIMILIANO PASTORE	10	2		YES	IN PERSON	ENGLISH
2		JEFF KIESNER	15	3		NO	IN PERSON	ENGLISH
3		UMBERTO GRANZIOL	20	4		YES	IN PERSON	ENGLISH
4		ENRICO TOFFALINI	10	2		YES	IN PERSON	ENGLISH
5		LUCA STEFANUTTI	15	3		YES	IN PERSON	ENGLISH
6		GIANMARCO ALTOE	5	1		YES	IN PERSON	ENGLISH
	newVar							
1	0	202505						



# Indexing Dataframes by Logical Conditions

Just like for vectors, you can use **logical conditions** for indexing a dataframe.

Let's consider this logical condition:

```
df$Teacher == "MASSIMILIANO PASTORE"
```

```
[1]  TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
[13] FALSE FALSE FALSE  TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
[25]  TRUE FALSE FALSE FALSE
```

Let's use it to extract some dataframe rows:

```
df[df$Teacher == "MASSIMILIANO PASTORE" , ] # some rows by condition ,
```

```
      Year TypeOfCourse                                     Title
1        1  METHODOLOGY CURRENT ISSUES IN STATISTICAL INFERENCE FOR PSYCHOLOGY
16     2-3  METHODOLOGY          BAYESIAN DATA ANALYSIS IN PSYCHOLOGICAL RESEARCH
25     2-3  METHODOLOGY          DATA SIMULATION IN PSYCHOLOGICAL STUDIES
      Teacher Hours ECTS MandatoryAttendance DeliveryMethod Language
1 MASSIMILIANO PASTORE    10      2                YES      IN PERSON  ENGLISH
16 MASSIMILIANO PASTORE    10      2                NO      IN PERSON  ENGLISH
25 MASSIMILIANO PASTORE    10      2                NO      IN PERSON  ENGLISH
      newVar
1    2.302585
16  2.302585
25  2.302585
```

# Indexing Elements in a Dataframe - A Summary

	[ , "Type"]	[ , "Teacher"]		[ , "Hours"]
[1 , ]	"METHODODOLOGY"	"MASSIMILIANO PASTORE"		10
[2 , ]	"METHODODOLOGY"	"JEFF KIESNER"		15
[3 , ]	"METHODODOLOGY"	"UMBERTO GRANZIOL"	...	20
[4 , ]	"PROGRAMMING"	"ENRICO TOFFALINI"		10
	...	...		...
[28 , ]	"PROGRAMMING"	"FRANCESCO VESPIGNANI"	...	5

# Subset

Base function **subset()** can also be used as an alternative to indexing

```
subset(df, Teacher == "MASSIMILIANO PASTORE", select=c("Teacher", "Hours", "TypeOfCourse"))
```

	Teacher	Hours	TypeOfCourse
1	MASSIMILIANO PASTORE	10	METHODOLOGY
16	MASSIMILIANO PASTORE	10	METHODOLOGY
25	MASSIMILIANO PASTORE	10	METHODOLOGY

```
df[df$Teacher == "MASSIMILIANO PASTORE" , c("Teacher", "Hours", "TypeOfCourse")]
```

	Teacher	Hours	TypeOfCourse
1	MASSIMILIANO PASTORE	10	METHODOLOGY
16	MASSIMILIANO PASTORE	10	METHODOLOGY
25	MASSIMILIANO PASTORE	10	METHODOLOGY

However, indexing with **[ ]** is more “computationally focused”, computationally faster (especially if working with large datasets), and more similar to programming in other languages (e.g., **Python**), so should probably be favoured by data scientists!

# Combine Two Dataframes Using `rbind()`

Imagine you have two datasets collected by two students, each including different participants:

df1			
	subjName	age	accuracy
1	Julie	12	0.92
2	Tommy	10	0.78
3	Phil	10	0.85

  

df2			
	subjName	age	accuracy
1	Amber	9	0.87
2	Max	13	0.90

Our goal is to get one single dataset including all participant's data for the final analysis. Of course, you could combined these files manually outside R (e.g., in Excel). However, it's simpler and more efficient to do this directly in R using `rbind()`

# Combine Two Dataframes Using `rbind()`

```
dfTotal = rbind(df1, df2)
```

```
dfTotal
```

	subjName	age	accuracy
1	Julie	12	0.92
2	Tommy	10	0.78
3	Phil	10	0.85
4	Amber	9	0.87
5	Max	13	0.90

**Important:** for `rbind()` to work, the two to-be-combined dataframes must:

- have the **exact same number of columns**;
- the **column names must be identical** (remember that R is case-sensitive).

# Merge Two Dataframes Using `merge()`

Another frequent case is having data collected from the **same participants** across **different dataframes**, and having to analyze all information together:

df1

	subjName	age
1	Julie	12
2	Amber	9
3	Tommy	10
4	Phil	10

df2

	subjName	accuracy	time
1	Julie	0.92	1203
2	Tommy	0.78	3302
3	Phil	0.85	994
4	Amber	0.87	1163

# Merge Two Dataframes Using `merge()`

You can merge the two dataframes into a single, comprehensive dataframe:

```
dfTotal = merge(df1, df2, by="subjName")
```

```
dfTotal
```

	subjName	age	accuracy	time
1	Amber	9	0.87	1163
2	Julie	12	0.92	1203
3	Phil	10	0.85	994
4	Tommy	10	0.78	3302

**Important:** `merge()` will work even if some or even all values that should be used for merging do not match... but in that case part of or all data will be lost

# Contingency Tables

The `table()` function, which counts frequencies, can also be used on dataframes. Importantly, it can also create **contingency tables** when applied to multiple variables at once

```
table(df$Hours) # just counts frequencies
```

```
5 10 15 20
13 8 5 2
```

```
table(df$TypeOfCourse, df$Hours) # creates contingency table
```

```
           5 10 15 20
METHODOLOGY 6  4  4  2
PROGRAMMING  1  3  0  0
SOFT SKILLS  4  1  1  0
THEMATIC COURSE 2  0  0  0
```