

Linear Regression Method:

$$y = a + bt$$

Given	y_t	t	$y_t \cdot t$	t^2
	26	1	26	1
	28	2	56	4
	29	3		

$$\sum y_t = na + b \sum t$$

$$\sum y_t \cdot t = a \sum t + b \sum t^2$$

find out a and b

and calculate n th day by $y = a + bt$

→ can handle trend data

→ Moving Avg only for applied in constant data.

* Exponential Smoothing

model where the prediction is weighted sum of past observations

→ Use exponentially ↓ weights for past obsen-

3 type

① Single Exponential Smoothing (ETS)

- Without trends or seasonality

- Smoothing factor (α) → control the rate at which the influence of the observation at prior time stems decay exponentially

Large (α) → model pay attention mainly to most recent observation → Fast Comp

Small (α) → more of history taken into account
→ Slow Computation

Given

t	A _t	F _t
1	39	
2	44	
3	40	
4	45	
5	38	
6	43	
7	39	

$$F_{t+1} = F_t + \alpha (A_t - F_t)$$

or

$$F_{t+1} = \alpha A_t + (1-\alpha) F_t$$

• Let $\alpha = 0.2$

$$F_{t+1} = 0.2 A_t + 0.8 F_t$$

• Let $F_1 = A_1$

$$F_8 = 0.2 A_7 + 0.8 F_7$$

2) Double Exponential Smoothing

or

Holt's method \rightarrow Charles Holt

\rightarrow extension of Simple Exponential smoothing that explicitly adds support for trends.

(α, β)

\hookrightarrow smoothing factor for slope (handle trend)

\hookrightarrow smoothing factor for level

$$F_{t+1} = a_t + b_t$$

$$a_t = \alpha A_t + (1-\alpha) F_t$$

$$b_t = \beta (a_t - a_{t-1}) + (1-\beta) b_{t-1}$$

Let $\alpha = 0.2$

$\beta = 0.3$

$$a_1 = A_1 = 26, \quad b_1 = \frac{A_6 - A_1}{5} = \frac{35 - 26}{5}$$

$$\text{series} = 26, 28, 29, 31, 32, 35$$