

USD/RUB Brent

Alexander Cherkashin

9 2015 .

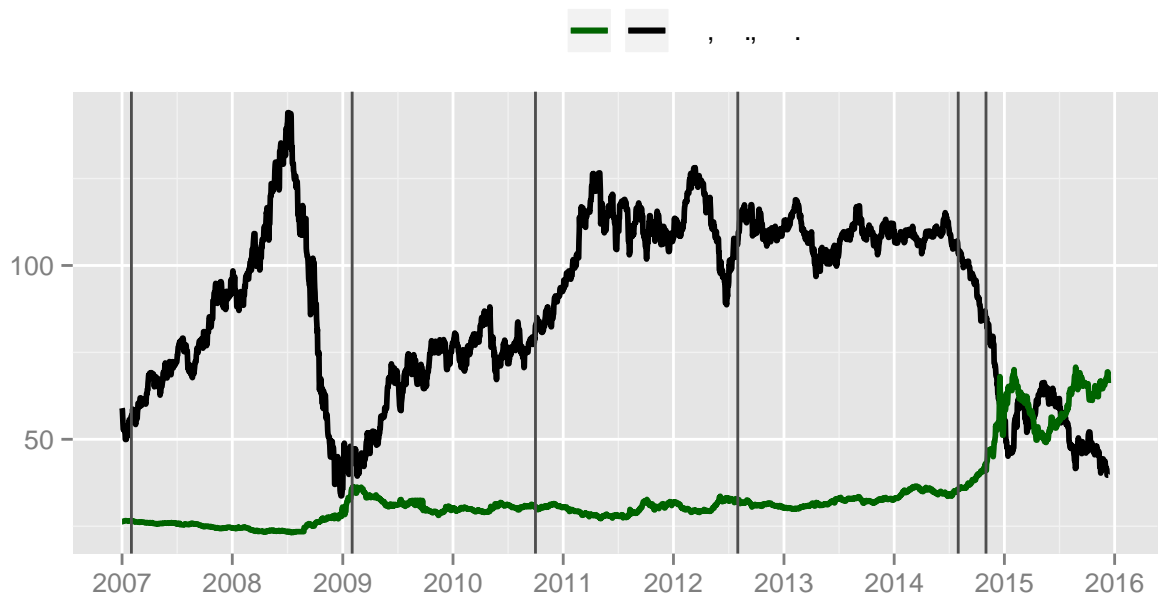
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 , , ¹ ² Brent 2007 . , X , - () .
 , ³ . “+” - , “-” - . 2013 .
 , . , 2007 2008 , . , 2009 , .
 , : , . - , , .

¹ Yahoo: <https://beta.finance.yahoo.com/quote/USDRUB%3DX/news>

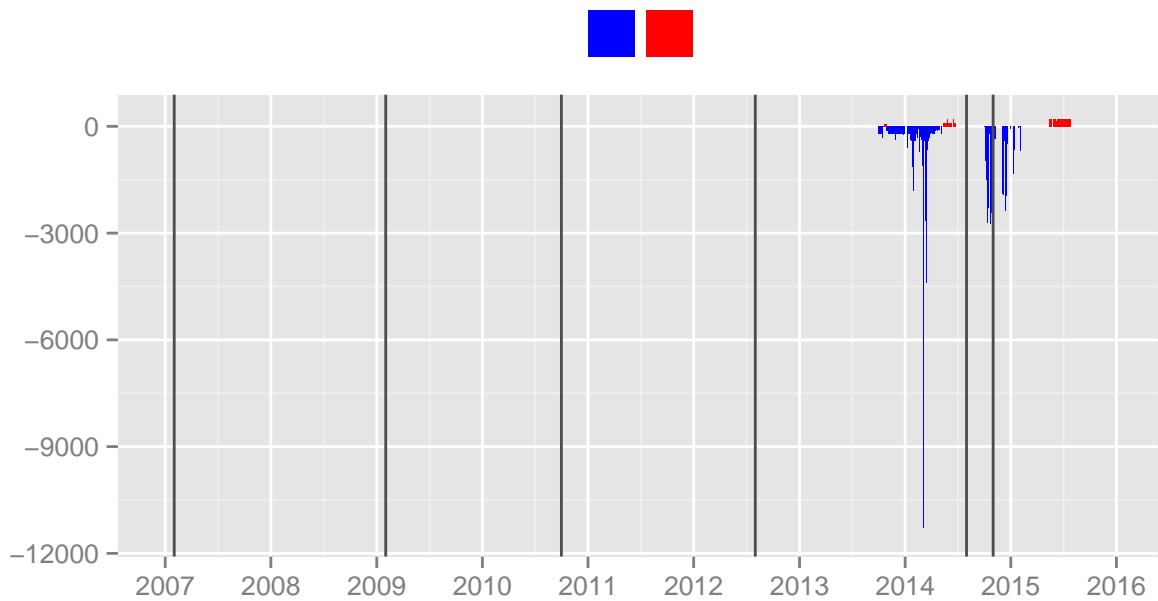
² The Federal Reserve Bank of St. Louis: <https://research.stlouisfed.org/fred2/series/DCOILBRENTU>

³ : http://www.cbr.ru/hd_base/default.aspx?prtid=valint_day&pid=idkp_br&sid=ITM_45393

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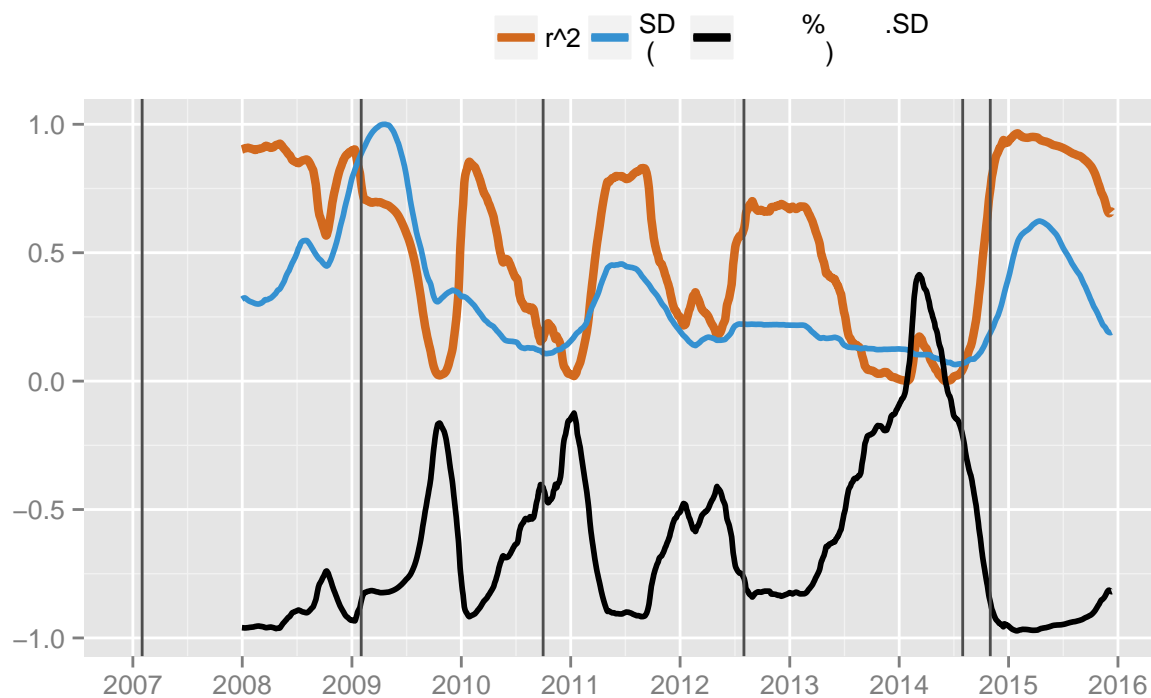
.USD



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 4 , , , , : - . Naive method. , .

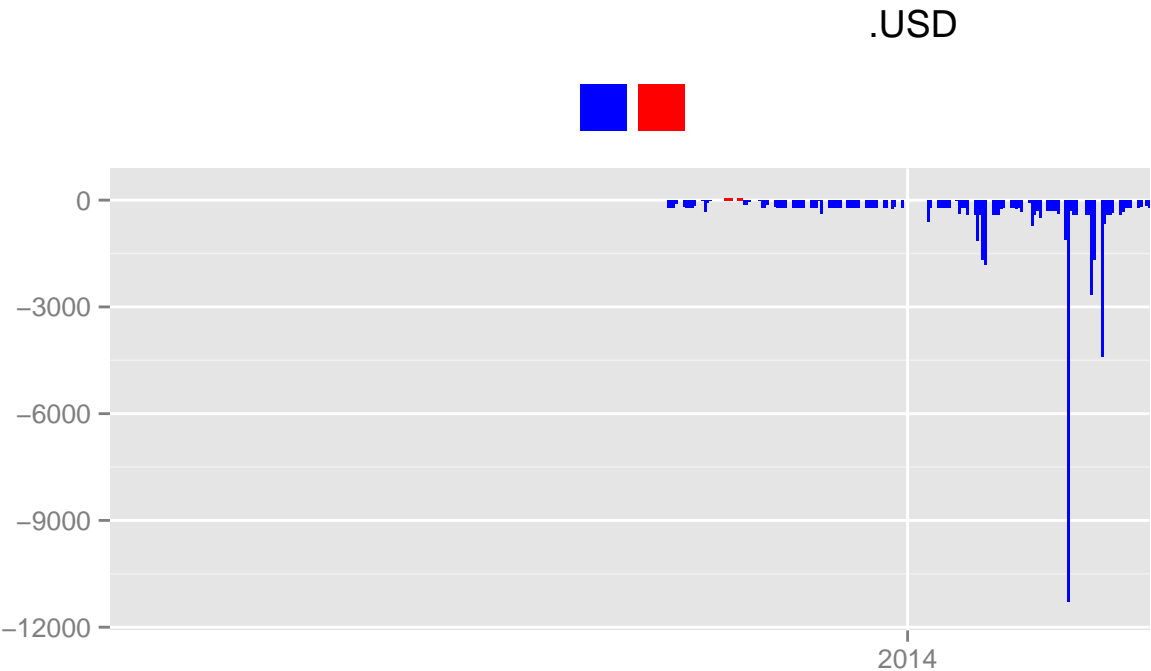
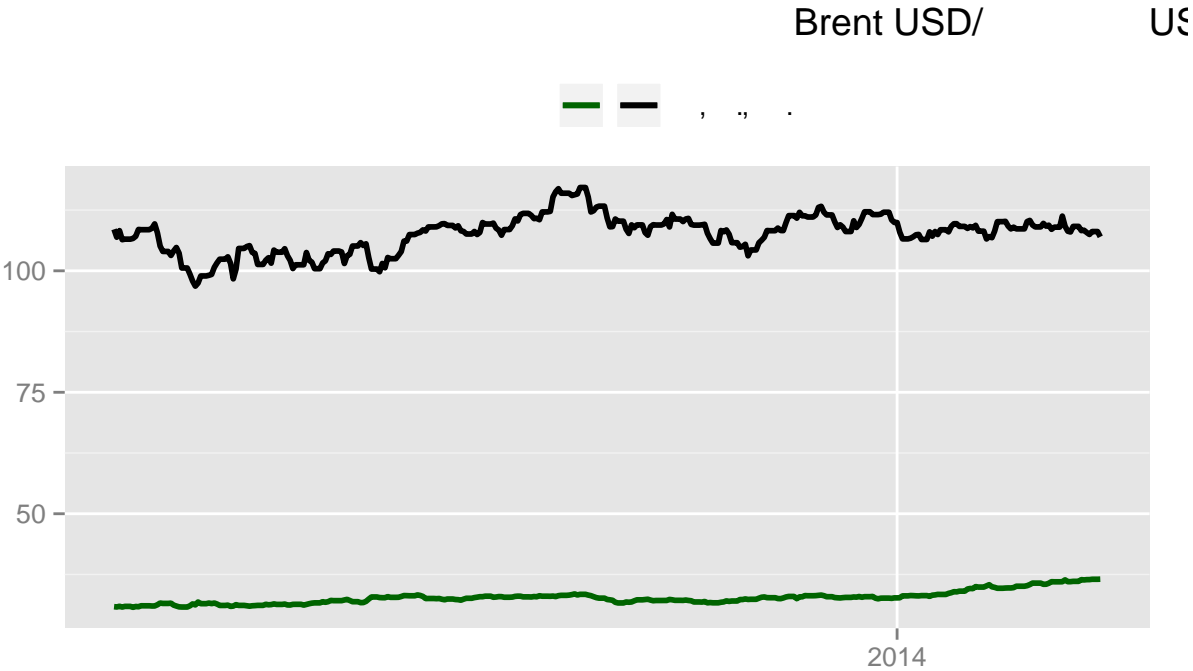
“” . - , .
 : Bias-variance tradeoff. - (- “”) “” - .
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 r^{26} . , . 1 - 100% , 0 - - .



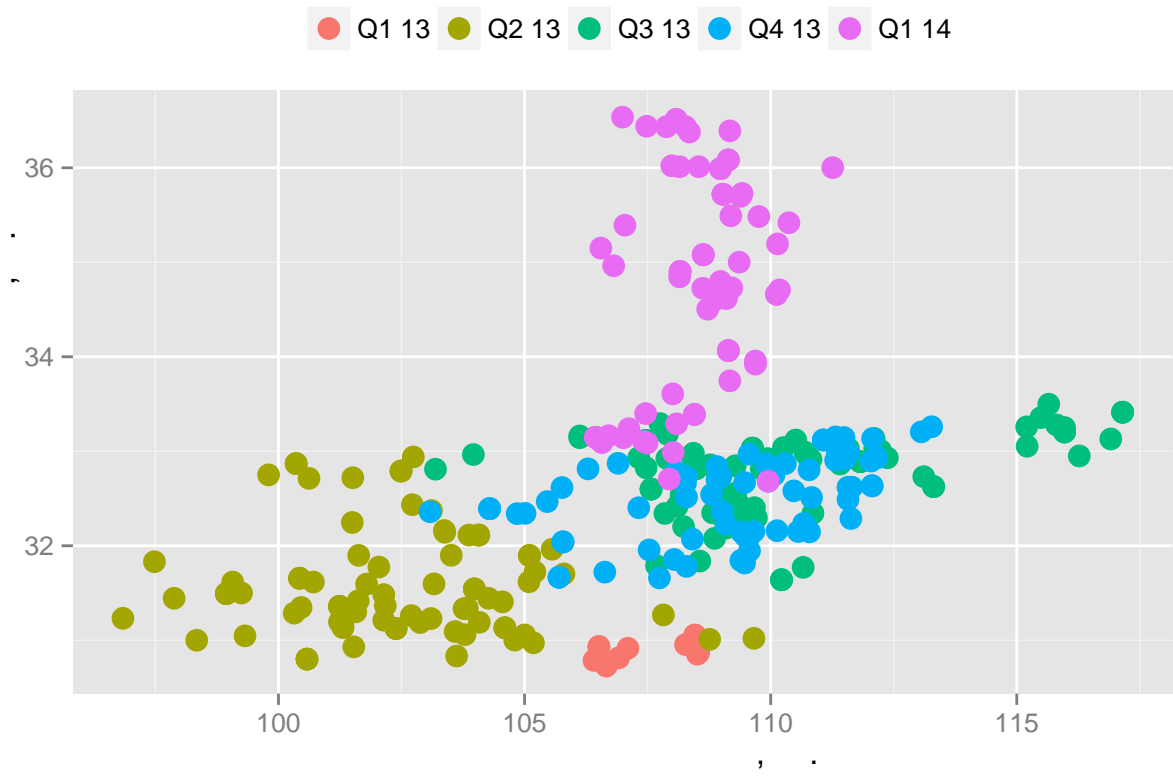
, . , - . , , , “” () , - r^2 . , : - , . , .
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⁵: . $Y = b \cdot \log(X)$. - , - . : , .
⁶ .
⁷ , , “ ” , , . , , .

(18 2013 17 2014) :



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2013 , , : - . ⁸ 2014 - : .
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⁸ , - , .

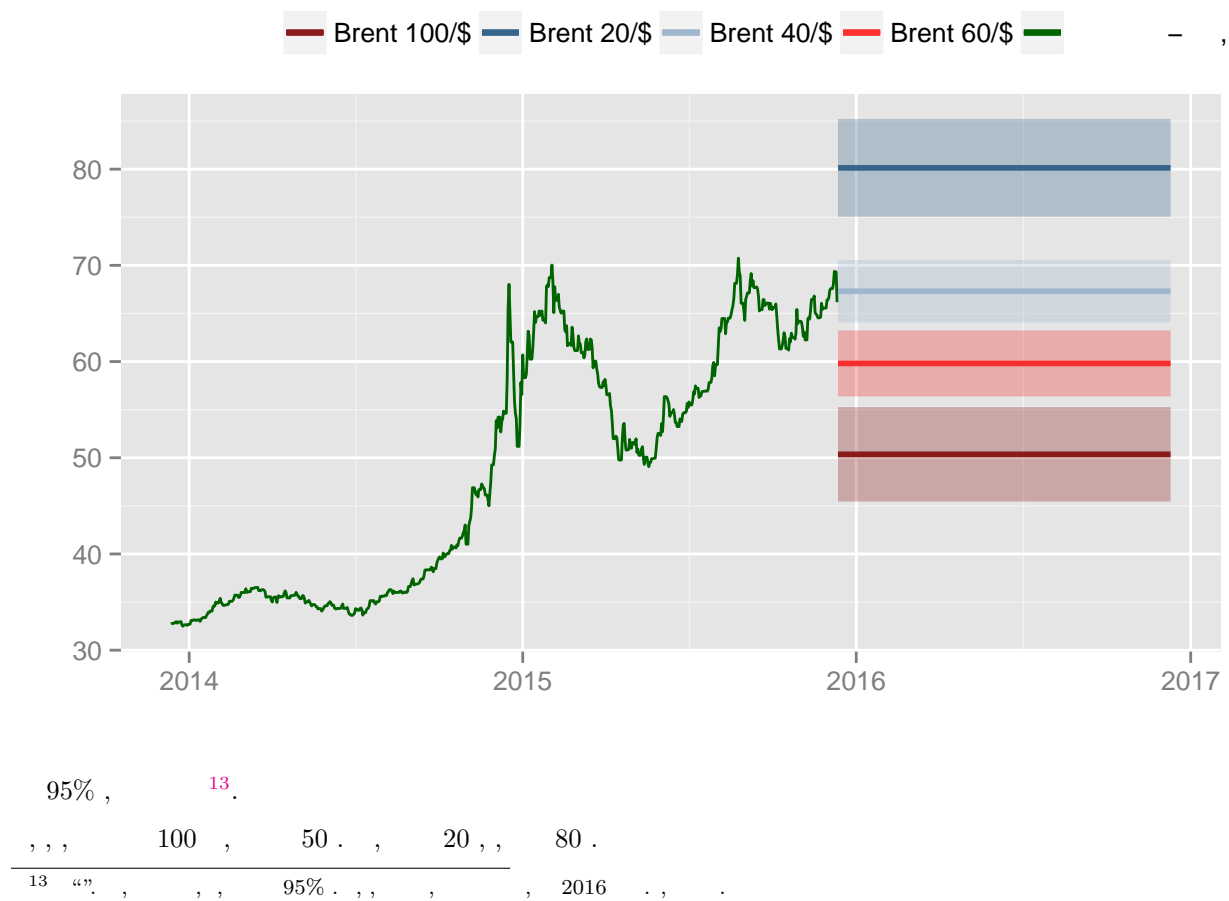


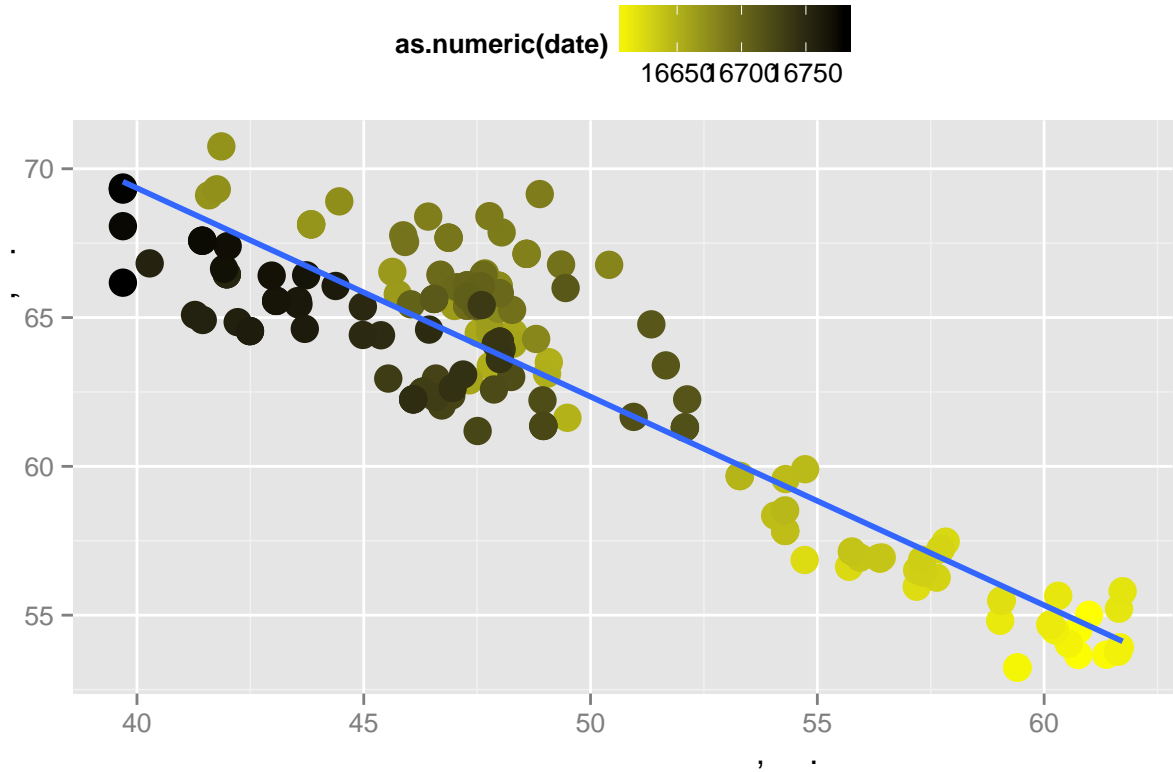
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 , , , , . , 2007 2015 2 (9 8%). , , - , 8% ¹² .
 - Brent 20, 40 60 . 90 . , .

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, , - 8% . , .

“” . , , .

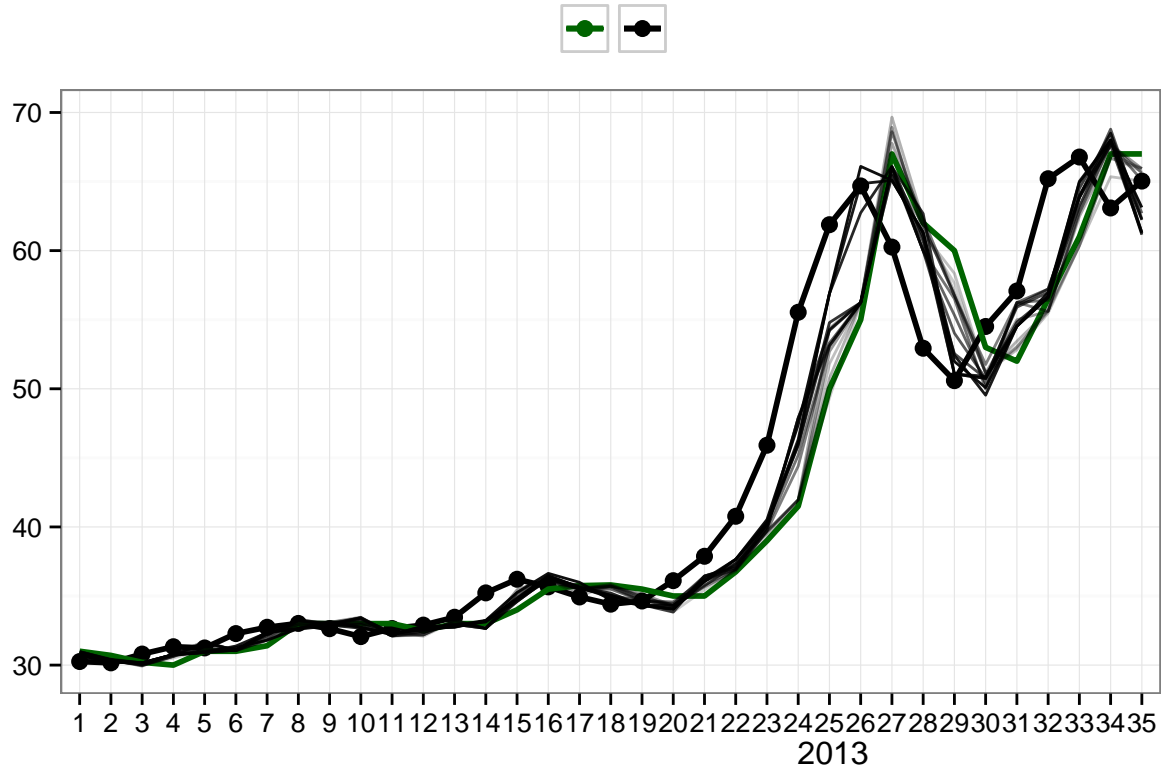
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1-, 2-, ..., 15- M-1 (,).

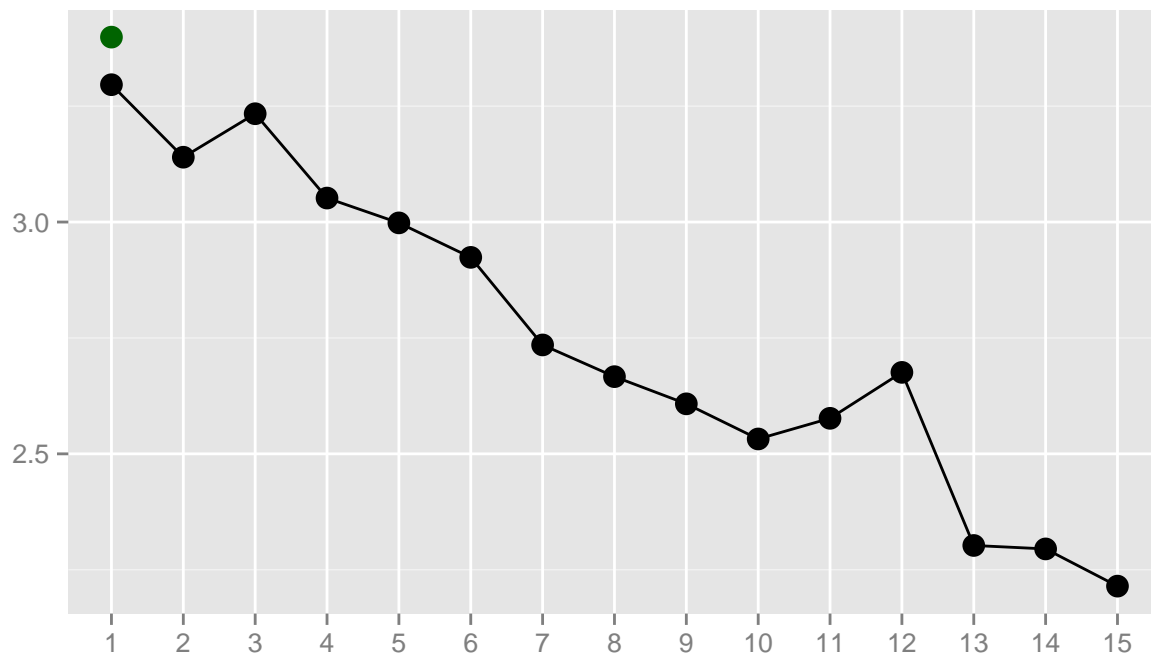
35 2013 2015. 35 .

, . , , . M-1 (), -2 ().

35 2013 . - , - , - , 1 15 ; - 1, - 15.



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 , , “ ” 11:30.

Table 1: 1. USD/RUB , - , . , 4 .

| | | | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 | .10 | .11 | .12 | .13 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .13 | 30.26 | 31.00 | 30.81 | 30.81 | 30.81 | 30.84 | 30.99 | 30.82 | 30.91 | 30.97 | 30.97 | 30.97 | 30.87 | 30.75 | 30.73 |
| .13 | 30.16 | 30.70 | 30.37 | 30.37 | 30.37 | 30.37 | 30.37 | 30.37 | 30.37 | 30.37 | 30.37 | 30.42 | 30.36 | 30.25 | 30.25 |
| .13 | 30.80 | 30.20 | 30.02 | 30.00 | 30.00 | 30.00 | 29.93 | 30.12 | 29.96 | 30.05 | 30.16 | 30.16 | 30.16 | 30.16 | 30.17 |
| .13 | 31.33 | 30.00 | 30.51 | 30.64 | 30.64 | 30.64 | 30.79 | 30.70 | 30.62 | 30.76 | 30.76 | 30.76 | 30.76 | 30.76 | 30.75 |
| .13 | 31.24 | 31.00 | 31.08 | 31.11 | 31.12 | 31.39 | 31.72 | 31.62 | 31.62 | 31.62 | 31.61 | 31.21 | 31.00 | 30.88 | 30.93 |
| .13 | 32.28 | 31.00 | 31.04 | 31.04 | 31.04 | 31.04 | 31.04 | 31.04 | 31.08 | 31.08 | 31.08 | 31.08 | 31.08 | 31.08 | 31.08 |
| .13 | 32.74 | 31.40 | 31.80 | 31.80 | 31.80 | 32.05 | 31.83 | 31.98 | 32.14 | 32.24 | 32.24 | 32.24 | 32.32 | 32.40 | 32.40 |
| .13 | 33.02 | 33.00 | 32.71 | 32.85 | 32.95 | 33.22 | 33.16 | 33.22 | 33.22 | 33.22 | 33.32 | 33.08 | 32.91 | 32.59 | 32.64 |
| .13 | 32.63 | 33.00 | 33.03 | 32.97 | 33.10 | 33.10 | 33.10 | 32.88 | 32.94 | 32.98 | 32.94 | 32.86 | 32.86 | 32.86 | 32.89 |
| .13 | 32.06 | 33.00 | 33.25 | 33.25 | 33.25 | 33.37 | 33.47 | 33.39 | 33.43 | 33.43 | 33.43 | 33.32 | 33.06 | 32.96 | 32.67 |
| .13 | 32.65 | 33.00 | 32.48 | 32.30 | 32.30 | 32.12 | 32.10 | 32.10 | 32.10 | 32.29 | 32.30 | 32.36 | 32.36 | 32.21 | 32.21 |
| .13 | 32.89 | 32.50 | 32.08 | 32.18 | 32.18 | 32.18 | 32.18 | 32.35 | 32.45 | 32.38 | 32.55 | 32.55 | 32.55 | 32.66 | 32.81 |
| .14 | 33.46 | 33.00 | 33.19 | 33.19 | 33.15 | 33.25 | 33.26 | 33.11 | 32.95 | 32.95 | 32.95 | 32.78 | 32.78 | 32.73 | 32.75 |
| .14 | 35.23 | 33.00 | 32.66 | 32.66 | 32.66 | 32.66 | 32.66 | 32.66 | 32.66 | 32.66 | 32.66 | 33.15 | 33.21 | 33.21 | 33.21 |
| .14 | 36.21 | 34.00 | 35.18 | 35.18 | 35.18 | 35.23 | 35.45 | 34.96 | 34.73 | 34.60 | 34.60 | 34.60 | 34.76 | 34.80 | 34.76 |

| | | | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 | .10 | .11 | .12 | .13 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .14 | 35.66 | 35.50 | 36.18 | 36.18 | 36.18 | 36.38 | 36.32 | 36.08 | 36.13 | 36.26 | 36.26 | 36.26 | 36.26 | 36.40 | 36.49 |
| .14 | 34.93 | 35.75 | 35.61 | 35.02 | 35.25 | 35.52 | 35.50 | 35.50 | 35.50 | 35.47 | 35.55 | 35.75 | 35.56 | 35.62 | 35.62 |
| .14 | 34.41 | 35.80 | 35.72 | 35.72 | 35.72 | 35.72 | 35.72 | 35.84 | 35.66 | 35.50 | 35.03 | 35.03 | 35.03 | 35.03 | 35.21 |
| .14 | 34.64 | 35.50 | 34.74 | 34.74 | 34.89 | 35.01 | 35.14 | 34.90 | 34.66 | 34.66 | 34.66 | 34.33 | 34.37 | 34.32 | 34.32 |
| .14 | 36.11 | 35.00 | 33.84 | 34.23 | 34.25 | 34.19 | 34.32 | 34.32 | 34.32 | 34.57 | 34.43 | 34.08 | 33.84 | 34.06 | 34.06 |
| .14 | 37.88 | 35.00 | 35.44 | 35.73 | 35.73 | 35.73 | 35.66 | 35.80 | 36.11 | 36.25 | 36.45 | 36.45 | 36.45 | 36.05 | 36.09 |
| .14 | 40.77 | 36.75 | 36.93 | 37.29 | 37.35 | 37.32 | 36.80 | 36.92 | 36.92 | 36.92 | 37.09 | 37.03 | 37.17 | 37.38 | 37.65 |
| .14 | 45.91 | 39.00 | 39.38 | 39.66 | 39.55 | 39.70 | 39.70 | 39.70 | 39.98 | 39.74 | 39.98 | 39.98 | 40.21 | 40.21 | 40.21 |
| .14 | 55.54 | 41.50 | 41.96 | 41.96 | 41.96 | 41.96 | 41.96 | 44.40 | 45.19 | 47.88 | 47.88 | 47.88 | 45.89 | 45.95 | 46.34 |
| .15 | 61.88 | 50.00 | 49.32 | 51.81 | 50.77 | 54.38 | 52.69 | 53.11 | 53.11 | 53.11 | 53.31 | 54.21 | 54.28 | 54.79 | 56.89 |
| .15 | 64.68 | 55.00 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 56.24 | 62.74 |
| .15 | 60.26 | 67.00 | 68.93 | 68.93 | 69.66 | 67.77 | 65.45 | 68.61 | 66.04 | 66.04 | 66.04 | 65.78 | 65.45 | 66.06 | 66.10 |
| .15 | 52.93 | 62.00 | 61.27 | 61.27 | 62.22 | 62.36 | 61.87 | 61.85 | 59.99 | 59.99 | 59.99 | 59.99 | 60.66 | 62.68 | 60.96 |
| .15 | 50.59 | 60.00 | 57.65 | 58.35 | 56.99 | 56.75 | 56.75 | 56.75 | 56.52 | 55.33 | 54.03 | 52.54 | 51.07 | 51.07 | 51.07 |
| .15 | 54.51 | 53.00 | 51.14 | 51.14 | 51.14 | 51.14 | 51.14 | 51.76 | 49.98 | 50.36 | 50.75 | 50.75 | 50.75 | 50.75 | 50.91 |
| .15 | 57.08 | 52.00 | 52.97 | 52.82 | 53.44 | 53.06 | 54.99 | 56.25 | 56.25 | 56.25 | 56.04 | 55.91 | 54.82 | 54.53 | 54.53 |
| .15 | 65.20 | 56.50 | 55.84 | 55.48 | 55.66 | 55.60 | 55.60 | 55.60 | 56.41 | 57.22 | 57.22 | 56.98 | 56.67 | 56.67 | 56.67 |
| .15 | 66.77 | 61.00 | 60.35 | 60.35 | 60.35 | 62.47 | 62.92 | 62.72 | 63.86 | 63.84 | 63.84 | 63.84 | 64.50 | 63.21 | 65.02 |
| .15 | 63.09 | 67.00 | 66.72 | 65.35 | 66.68 | 67.01 | 67.69 | 67.69 | 67.69 | 68.49 | 68.79 | 67.62 | 68.50 | 68.01 | 68.01 |
| .15 | 65.03 | 67.00 | 65.74 | 65.03 | 65.94 | 65.94 | 65.94 | 65.62 | 65.10 | 62.71 | 62.29 | 61.30 | 61.30 | 61.30 | 61.15 |

Table 2: 2. , 4.

| | | | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 | .10 | .11 | .12 | .13 |
|-----|-------|--------|--------|--------|--------|--------|--------|--------|--------|-------|-------|-------|-------|-------|-------|
| .13 | 30.26 | 0.74 | 0.55 | 0.55 | 0.55 | 0.58 | 0.74 | 0.57 | 0.65 | 0.71 | 0.71 | 0.71 | 0.61 | 0.49 | 0.49 |
| .13 | 30.16 | 0.54 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.26 | 0.20 | 0.09 | 0.09 |
| .13 | 30.80 | -0.60 | -0.78 | -0.80 | -0.80 | -0.80 | -0.87 | -0.68 | -0.84 | -0.75 | -0.64 | -0.64 | -0.64 | -0.64 | -0.64 |
| .13 | 31.33 | -1.33 | -0.82 | -0.69 | -0.69 | -0.69 | -0.54 | -0.63 | -0.71 | -0.57 | -0.57 | -0.57 | -0.57 | -0.57 | -0.57 |
| .13 | 31.24 | -0.24 | -0.16 | -0.13 | -0.12 | 0.15 | 0.48 | 0.38 | 0.38 | 0.38 | 0.37 | -0.03 | -0.24 | -0.36 | -0.36 |
| .13 | 32.28 | -1.28 | -1.24 | -1.24 | -1.24 | -1.24 | -1.24 | -1.24 | -1.20 | -1.20 | -1.20 | -1.20 | -1.20 | -1.20 | -1.20 |
| .13 | 32.74 | -1.34 | -0.94 | -0.94 | -0.94 | -0.69 | -0.90 | -0.76 | -0.60 | -0.50 | -0.50 | -0.50 | -0.41 | -0.34 | -0.34 |
| .13 | 33.02 | -0.02 | -0.31 | -0.16 | -0.07 | 0.20 | 0.14 | 0.21 | 0.21 | 0.21 | 0.31 | 0.07 | -0.10 | -0.43 | -0.43 |
| .13 | 32.63 | 0.37 | 0.40 | 0.34 | 0.46 | 0.46 | 0.46 | 0.25 | 0.30 | 0.35 | 0.31 | 0.23 | 0.23 | 0.23 | 0.23 |
| .13 | 32.06 | 0.94 | 1.18 | 1.18 | 1.19 | 1.31 | 1.40 | 1.33 | 1.37 | 1.37 | 1.37 | 1.26 | 1.00 | 0.90 | 0.90 |
| .13 | 32.65 | 0.35 | -0.16 | -0.35 | -0.35 | -0.52 | -0.55 | -0.55 | -0.55 | -0.35 | -0.35 | -0.28 | -0.29 | -0.43 | -0.43 |
| .13 | 32.89 | -0.39 | -0.82 | -0.71 | -0.71 | -0.71 | -0.71 | -0.54 | -0.44 | -0.51 | -0.35 | -0.35 | -0.35 | -0.23 | -0.23 |
| .14 | 33.46 | -0.46 | -0.27 | -0.27 | -0.32 | -0.22 | -0.20 | -0.35 | -0.51 | -0.51 | -0.51 | -0.69 | -0.68 | -0.73 | -0.73 |
| .14 | 35.23 | -2.23 | -2.57 | -2.57 | -2.57 | -2.57 | -2.57 | -2.57 | -2.57 | -2.57 | -2.57 | -2.07 | -2.02 | -2.02 | -2.02 |
| .14 | 36.21 | -2.21 | -1.03 | -1.03 | -1.03 | -0.98 | -0.76 | -1.25 | -1.48 | -1.61 | -1.61 | -1.61 | -1.45 | -1.42 | -1.42 |
| .14 | 35.66 | -0.16 | 0.52 | 0.52 | 0.52 | 0.72 | 0.66 | 0.42 | 0.46 | 0.60 | 0.60 | 0.60 | 0.60 | 0.74 | 0.74 |
| .14 | 34.93 | 0.82 | 0.67 | 0.09 | 0.32 | 0.58 | 0.57 | 0.57 | 0.57 | 0.54 | 0.62 | 0.82 | 0.63 | 0.69 | 0.69 |
| .14 | 34.41 | 1.39 | 1.31 | 1.31 | 1.31 | 1.31 | 1.31 | 1.43 | 1.25 | 1.09 | 0.63 | 0.63 | 0.63 | 0.63 | 0.63 |
| .14 | 34.64 | 0.86 | 0.10 | 0.10 | 0.25 | 0.37 | 0.50 | 0.27 | 0.02 | 0.02 | 0.02 | -0.31 | -0.27 | -0.32 | -0.32 |
| .14 | 36.11 | -1.11 | -2.27 | -1.88 | -1.86 | -1.92 | -1.79 | -1.79 | -1.79 | -1.54 | -1.69 | -2.04 | -2.28 | -2.05 | -2.05 |
| .14 | 37.88 | -2.88 | -2.43 | -2.15 | -2.15 | -2.15 | -2.22 | -2.08 | -1.77 | -1.63 | -1.43 | -1.43 | -1.43 | -1.83 | -1.83 |
| .14 | 40.77 | -4.02 | -3.84 | -3.48 | -3.42 | -3.45 | -3.97 | -3.85 | -3.85 | -3.85 | -3.68 | -3.74 | -3.60 | -3.40 | -3.40 |
| .14 | 45.91 | -6.91 | -6.53 | -6.25 | -6.37 | -6.22 | -6.22 | -6.22 | -5.93 | -6.17 | -5.93 | -5.93 | -5.70 | -5.70 | -5.70 |
| .14 | 55.54 | -14.04 | -13.58 | -13.58 | -13.58 | -13.58 | -13.58 | -11.14 | -10.35 | -7.66 | -7.66 | -7.66 | -9.65 | -9.59 | -9.59 |
| .15 | 61.88 | -11.88 | -12.56 | -10.07 | -11.11 | -7.50 | -9.18 | -8.77 | -8.77 | -8.77 | -8.57 | -7.67 | -7.60 | -7.08 | -7.08 |
| .15 | 64.68 | -9.68 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 | -8.45 |
| .15 | 60.26 | 6.74 | 8.67 | 8.67 | 9.41 | 7.52 | 5.19 | 8.35 | 5.79 | 5.79 | 5.79 | 5.53 | 5.19 | 5.80 | 5.80 |

| | | | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 | .10 | .11 | .12 | . |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|
| .15 | 52.93 | 9.07 | 8.34 | 8.34 | 9.29 | 9.43 | 8.94 | 8.91 | 7.06 | 7.06 | 7.06 | 7.06 | 7.73 | 9.75 | 8.3 |
| .15 | 50.59 | 9.41 | 7.06 | 7.76 | 6.40 | 6.16 | 6.16 | 6.16 | 5.93 | 4.74 | 3.44 | 1.95 | 0.48 | 0.48 | 0.3 |
| .15 | 54.51 | -1.51 | -3.37 | -3.37 | -3.37 | -3.37 | -3.37 | -2.75 | -4.53 | -4.15 | -3.76 | -3.76 | -3.76 | -3.76 | -3.3 |
| .15 | 57.08 | -5.08 | -4.11 | -4.26 | -3.64 | -4.02 | -2.09 | -0.83 | -0.83 | -0.83 | -1.04 | -1.17 | -2.26 | -2.55 | -2.3 |
| .15 | 65.20 | -8.70 | -9.36 | -9.73 | -9.55 | -9.60 | -9.60 | -9.60 | -8.79 | -7.98 | -7.99 | -8.22 | -8.54 | -8.54 | -8.3 |
| .15 | 66.77 | -5.77 | -6.43 | -6.43 | -6.43 | -4.31 | -3.86 | -4.06 | -2.91 | -2.94 | -2.94 | -2.94 | -2.28 | -3.57 | -1.3 |
| .15 | 63.09 | 3.91 | 3.63 | 2.26 | 3.59 | 3.92 | 4.60 | 4.60 | 4.60 | 5.40 | 5.71 | 4.53 | 5.41 | 4.92 | 4.3 |
| .15 | 65.03 | 1.97 | 0.70 | 0.00 | 0.91 | 0.91 | 0.91 | 0.59 | 0.06 | -2.33 | -2.74 | -3.74 | -3.74 | -3.74 | -3.3 |