

# Lab 2

MOSFET Sizing and CS Amplifier  
(Xschem, NGSpice & ADT)

## Part 1: Sizing Chart

### Required Spec:

DC Gain	-10
Supply	2.5v
Current Consumption	10uA

### Analytic Calculations:

$$|A_v| \approx gmR_D = \frac{2I_D}{V_{ov}} = \frac{2V_{RD}}{V_{ov}}$$

*In Simulation  $V_{ov} \neq \frac{2I_D}{gm}$  all the time, Instead use  $V^* = \frac{2I_D}{gm}$*

$$|A_v| = \frac{2V_{RD}}{V^*}$$

**To get Large Output Swing: Assume CM output =  $V_{RD} = 1V$**

$$R = \frac{V_{RD}}{I_D} = \frac{1}{10\mu} = 100K\Omega \quad (\text{first design parameter calculated})$$

$$V_Q^* = \frac{2V_{RD}}{|A_v|} = 2 * \frac{1}{10} = 0.2 V$$

This concludes the initial Gain Calculation, We will use the obtained results on a ADT to get the remaining design parameters required to meet the Spec.

On ADT we assumed a relatively Length of 2um such that we are not affected by short channel effects, and get a high output resistance from the mosfet

### **V\* and Vov Overlaid vs VGS:**

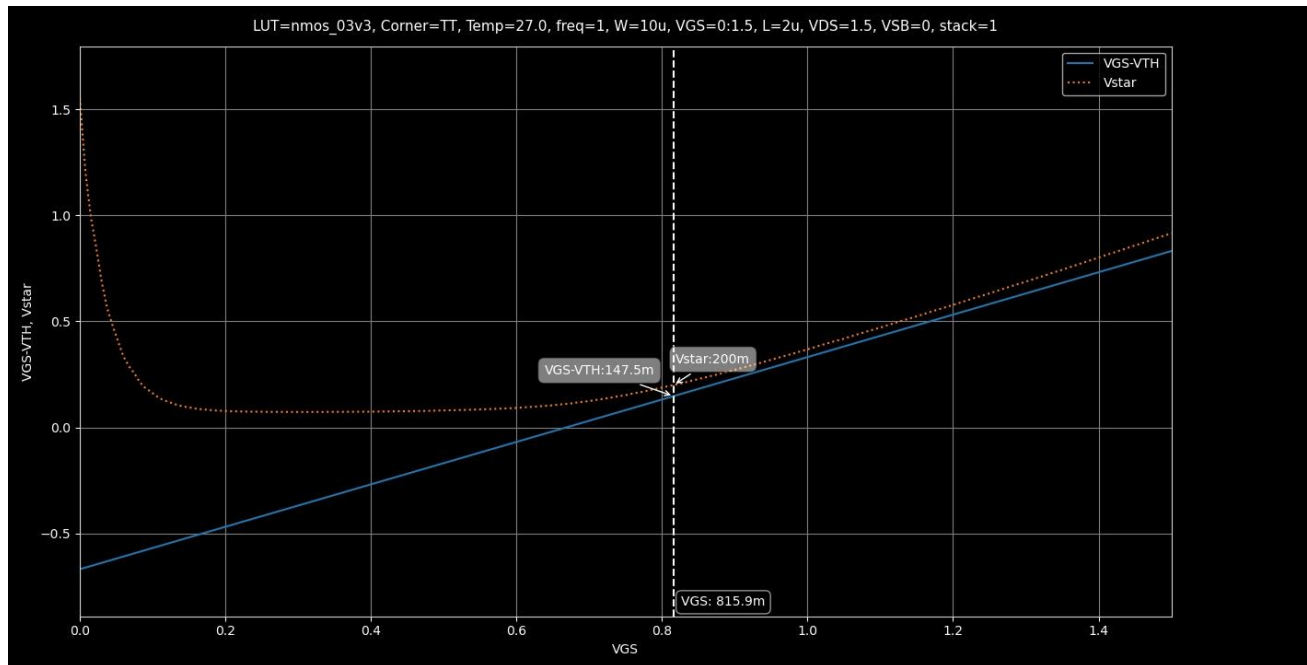


Figure 1 V\* and Vov vs VGS (ADT)

**Comment:** Vov and V\* are relatively close in value to each other at the beginning of the Strong Inversion region meaning the square law is relatively valid in that region. But for Deep Strong inversion (Large Vov) or weak inversion, the behavior is quite far despite using a Long Channel Length.

### **Locating $V_Q^*$ and $V_{GSQ}$ , $V_{ovQ}$ :**

$$@V_Q^* = 200mV, \quad V_{ovQ} = 147.5mV, \quad V_{GSQ} = 815.9mV$$

## Plotting $I_D$ , $g_m$ , $g_{ds}$ vs $V_{GS}$ :

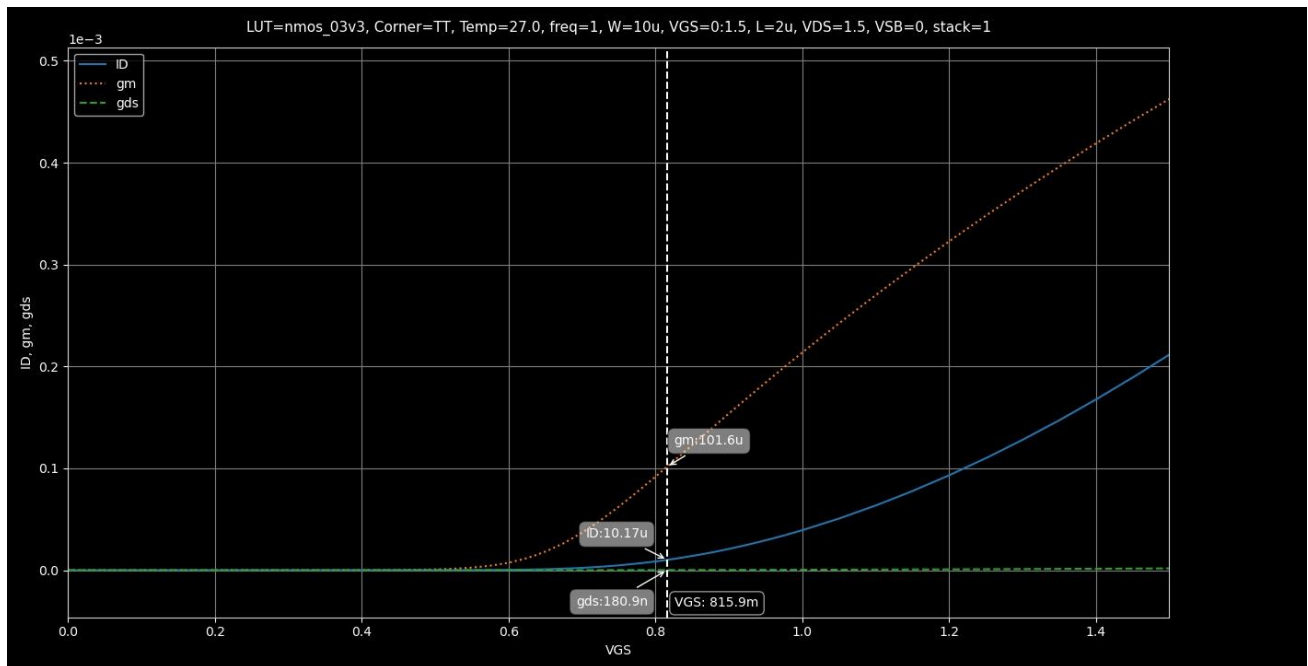


Figure 2  $I_D$ ,  $g_m$ ,  $g_{ds}$  vs  $V_{GS}$  and their corresponding values at  $V_{GSQ}$

<b>IDx</b>	10.17uA
<b>gm<sub>x</sub></b>	101.6uS
<b>gds<sub>x</sub></b>	180.9nS

## Getting the Value of $W$ , $I_{DQ}$ , $g_{mQ}$ , $g_{dsQ}$ :

We can get the required values for the design using cross multiplication since  $W$  and  $I$  are directly proportional to each other

$W$	$I_D$
<b>10 <math>\mu m</math></b>	$I_{DX} @ V_{Q*}$ (from the chart)
<b>?</b>	$I_{DQ} = 10 \mu A$ (from the specs)

But the easier approach would be to calculate them directly on ADT.



Figure 3 Calculated Parameters from ADT

**Verifying Gain:**

$$A_v = -gm(R_D // r_o) = -99.17\mu * \frac{100K * 5.66M}{100K + 5.66M} = -9.74 \approx -10$$

The parameters are correct!

**Final Parameter List:**

<b>W</b>	9.76 um
<b>L</b>	2 um
<b>gm</b>	99.17 uS
<b>gds</b>	176.7 nS
<b>ro</b>	5.66 MΩ
<b>R<sub>D</sub></b>	100 KΩ
<b>V<sub>gs</sub></b>	815.9 mV

## Part 2: CS Amplifier

What

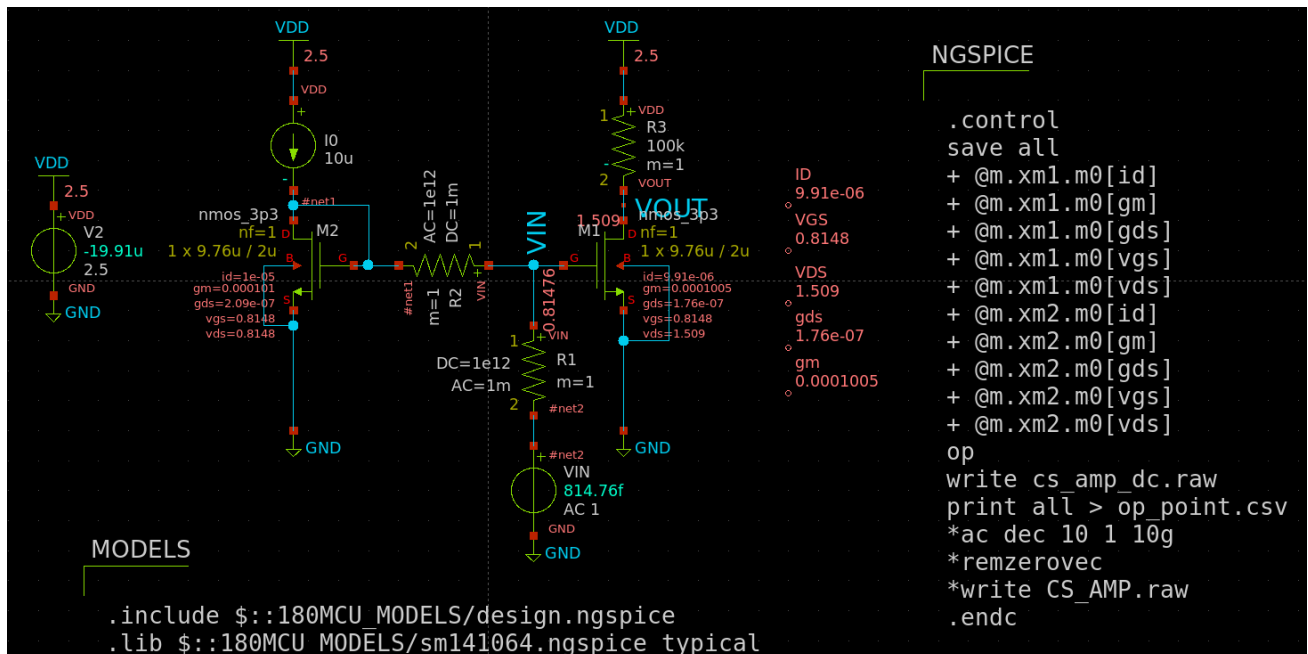


Figure 4 Testbench showcasing OP Points using all Required Methods

### Comparing Analytic and Simulation Results for OP Point:

Parameter	Simulation	Analytic
<b>Vgs</b>	814.8 mV	815.9 mV
<b>Id</b>	9.91 uA	10 uA
<b>gm</b>	100.5 uS	99.17 uS
<b>gds</b>	176 nS	176.7 nS
<b>ro</b>	5.68 MΩ	5.66 MΩ

The results are almost identical due to using a chart-based approach.

**Compare  $r_o$  and  $R_D$ . Is the assumption of ignoring  $r_o$  justified in this case? Do you expect the error to remain the same if we use min  $L$ ?**

$$R_D = 100\text{ K}\Omega, \quad r_o \approx 5.68\text{ M}\Omega, \quad r_o \gg R_D$$

Therefore, It is safe to neglect  $r_o$  in this case.

In case of using min  $L$ , Since  $r_o$  and  $L$  are directly proportional,  $r_o$  will massively decrease by decreasing  $L$  to a point where it is no longer valid to neglect it as it will have a value comparable with  $R_D$ .

- **Calculate the intrinsic gain of the transistor.**

$$\text{Intrinsic Gain } |A_v| = g_m * r_o = 100.5\mu * 5.68\text{M} = 570.84$$

- **Calculate the amplifier gain analytically. What is the relation ( $\ll$ ,  $<$ ,  $\approx$ ,  $>$ ,  $\gg$ ) between the amplifier gain and the intrinsic gain?**

$$\text{Amplifier Gain } |A_v| = g_m(R_D // r_o) = 100.5\mu * (100\text{K} // 5.68\text{M}) = 9.876 \ll 547.2$$

Amplifier Gain is much less than ( $\ll$ ) Intrinsic Gain.

## 2. AC Analysis:

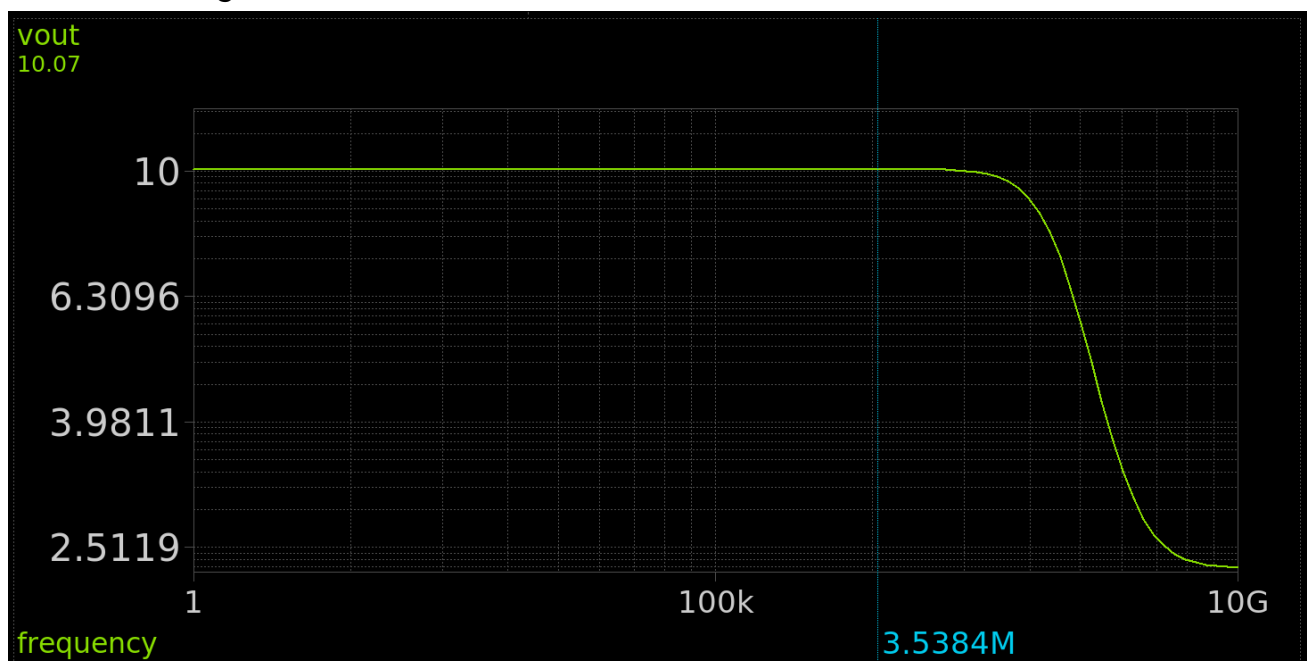


Figure 5 DC Gain from AC Analysis

Gain = 10.07, Agrees with Analytical Results and approximately equal to the required spec.

### 3. Gain Non-Linearity:

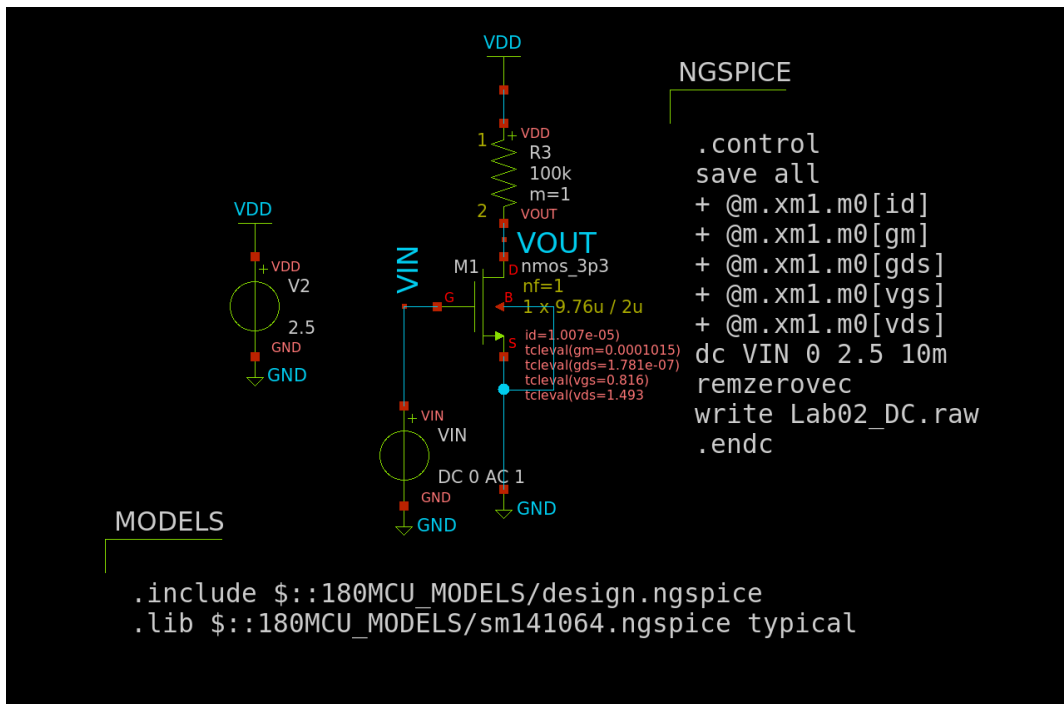


Figure 6 DC Testbench

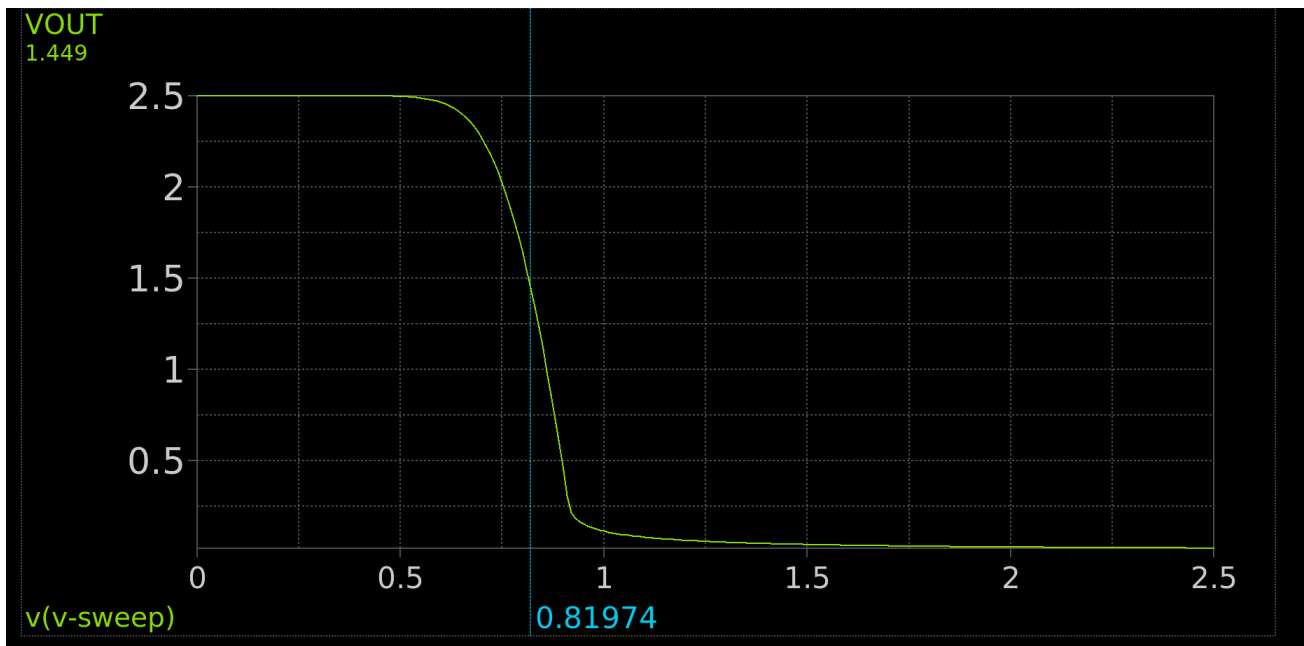


Figure 7 VIN vs VOUT Graph



**Comment:**

The relation between  $V_{IN}$  and  $V_{OUT}$  differs according to the region of operation of the transistor:

$V_{OUT}$  is given by  $V_{OUT} = V_{DD} - I_D \cdot R_D$

@  $V_{in} < V_{th}$ : Cutoff region,  $I_D = 0$  thus  $V_{OUT} = V_{DD}$

@  $V_{in} > V_{th}$  &  $V_{out} > V_{ov}$ : Saturation region, The relation is quadratic according to the Square Law.

Notice: Due to the big slope in that area, if a small signal is applied around the Operational point it could be approximated that the relation is linear in that case. Hence that's the preferred region to operate the amplifier but still the relation is not linear enough to consider the amplifier linear.

@  $V_{in} > V_{th}$  &  $V_{out} < V_{ov}$ : Triode Region, The relation is almost linear according to the triode current equation.

Though with a much smaller slope than the one in the saturation region.

## Derivative of VOUT vs VIN:

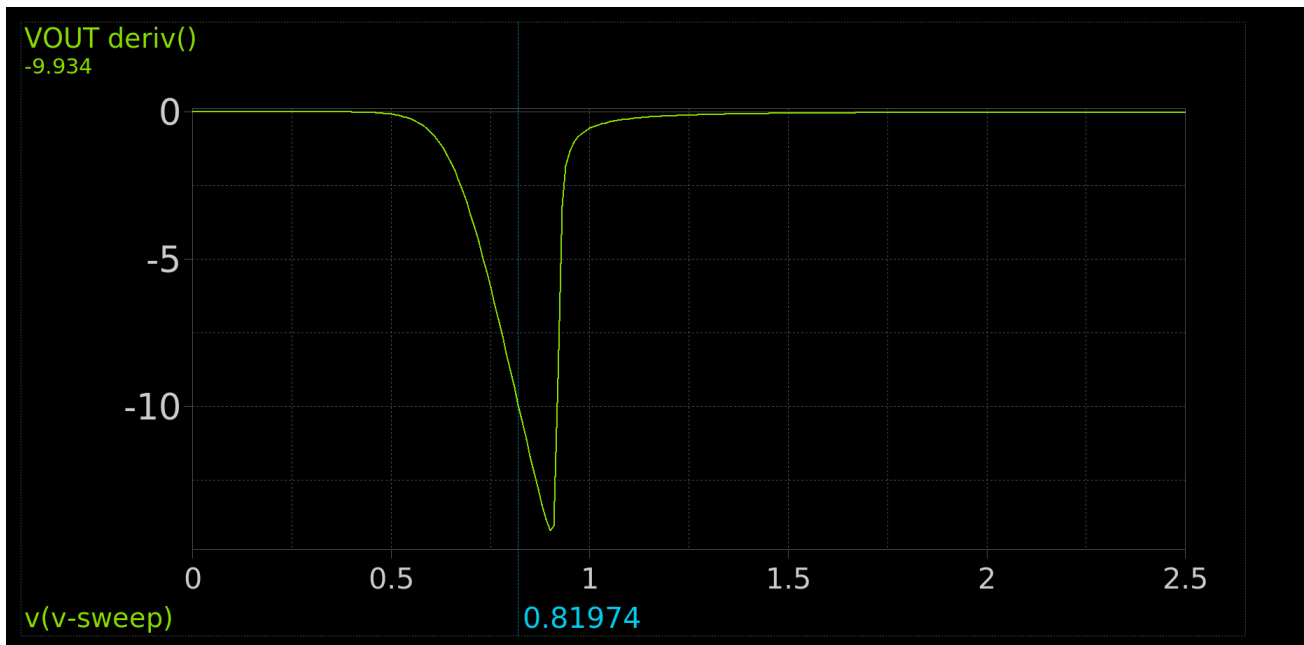


Figure 8 Derivative of VOUT vs VIN graph

### Is the Gain Linear?

Since  $V_{IN} = V_{GS}$ ,  $g_m = 2 \cdot I_D / V_{ov} = k \cdot V_{ov}$  depends on  $V_{GS}$  and the gain  $A_v = g_m \cdot R_d$  (Depends on  $g_m$ )

The Gain is the function of the input and as seen from the graph it is not linear. Though if zoomed in for a small signal it can be approximated to be linear in that case.

## 4. Transient Analysis:

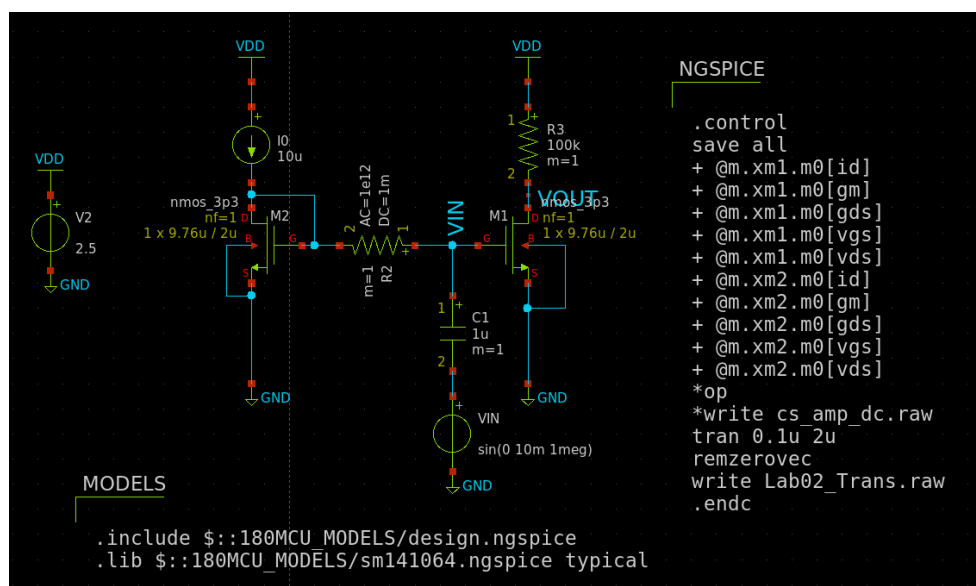


Figure 9 Transient Simulation Testbench

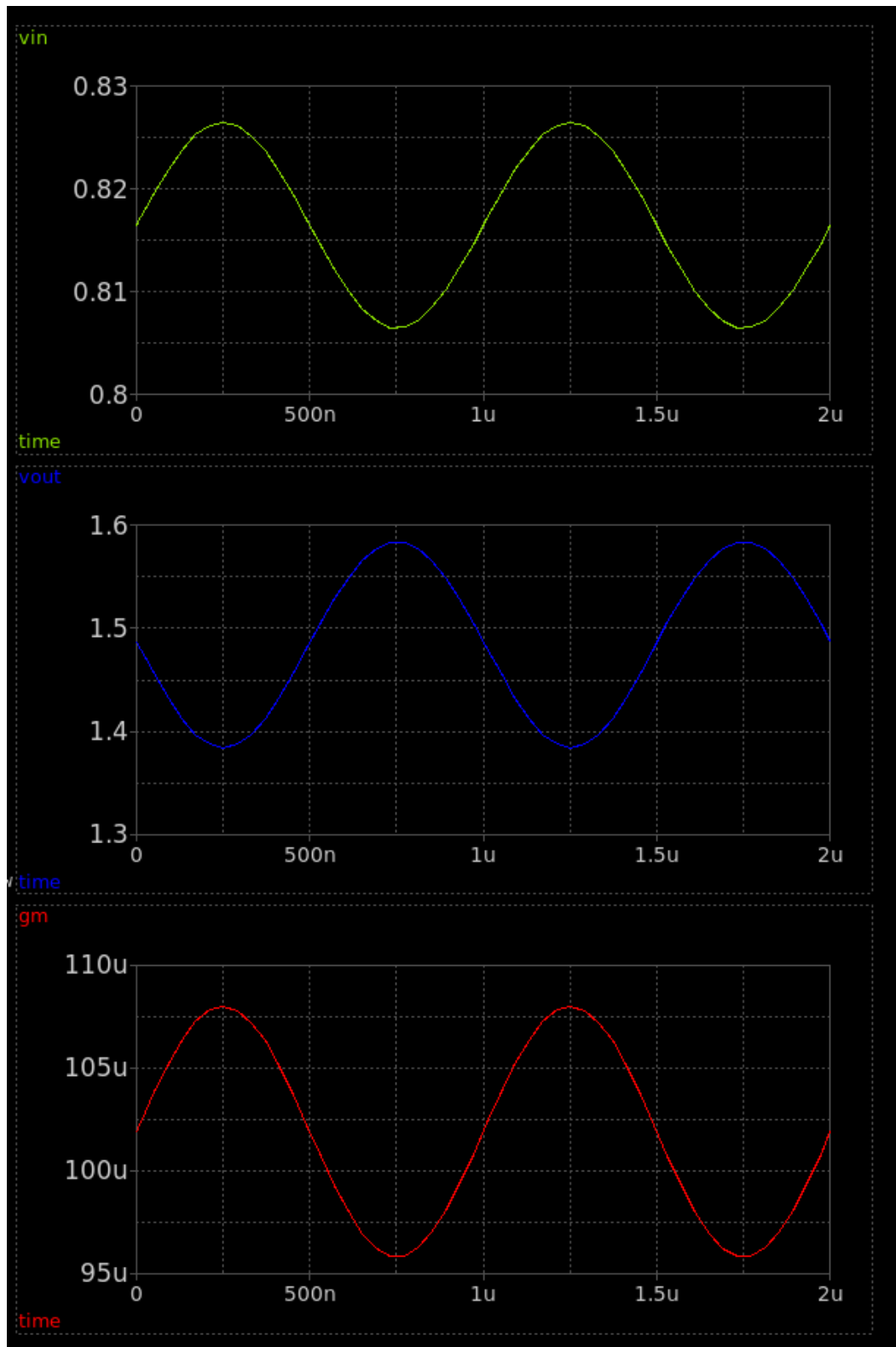


Figure 10  $V_{IN}$  (Green),  $V_{OUT}$  (Blue) and  $g_m$  (Red) vs Time

## Does gm vary with the input signal? What does that mean?

gm does vary across time as it is a function of the input. Which means the gain also varies with the input signal

## Is this amplifier linear? Comment.

No, The amplifier is not Linear.

While some linear behavior can be noticed on very small signals, those are merely approximations and do not show the entire picture. Vout varies with Vin which affects different parameters and makes the gain non-linear as well.

## 5. Gain Linearity (Negative Feedback):

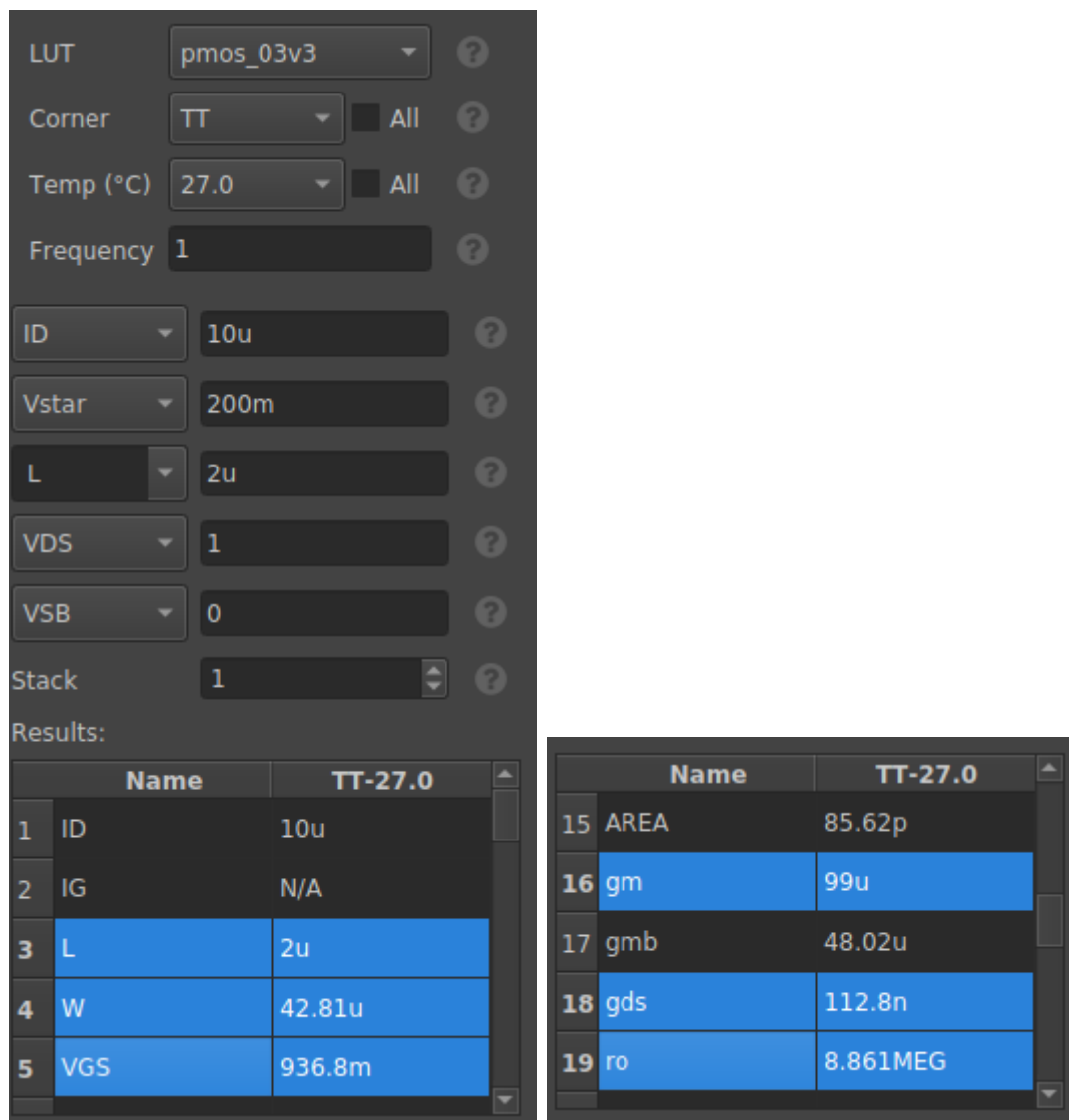


Figure 11 PMOS Sizing using ADT

$$L = 2\mu m, W = 42.81\mu m$$

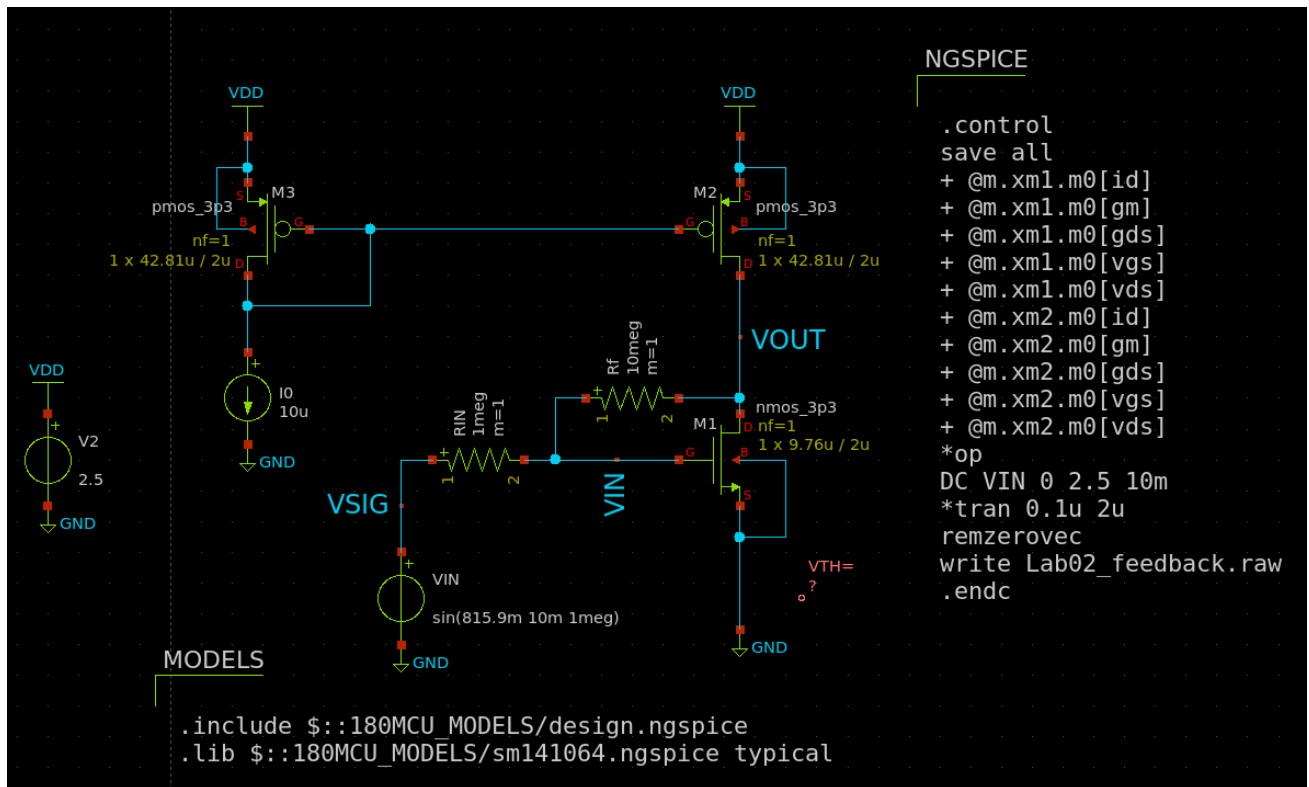
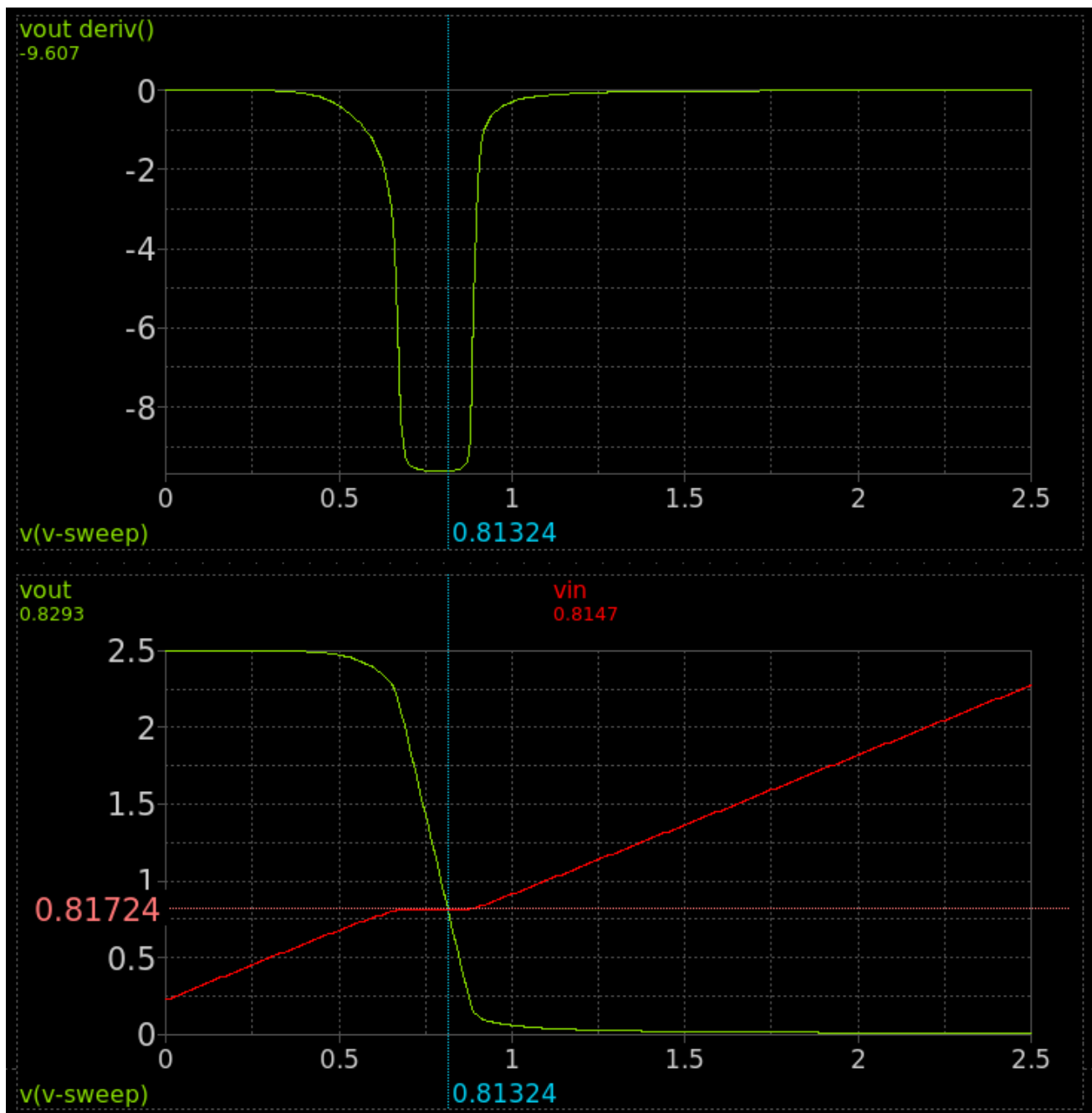


Figure 12 Negative Feedback Testbench

Choosing  $R_{sig}=1M\Omega$  as the gain is equal to  $R_f/R_{sig}$  thus choosing the appropriate  $R_{sig}$  to make the gain equal to -10 as required from the spec.

Figure 13 Gain,  $V_{IN}$  and  $V_{OUT}$  vs  $V_{SIG}$ 

**Report  $V_{IN}$  and  $V_{OUT}$  vs  $V_{SIG}$  (overlaid). At what voltage do the two curves cross? Why?**

The two curves cross paths at approximately  $V_{GS}$  of the Q-Point of the transistor, where  $V_{IN}$  equals  $V_{OUT}$  the transistor is considered to be diode connected. This is where the current produced by the NMOS and PMOS is equal each other.

## Is VOUT vs VSIG linear in the operating range of the amplifier? Why?

It is Linear, Due to the effect of negative feedback as it desensitizes the gain from the transistor parameters and makes it dependent only on the Rf resistor and the Rsig only

The negative feedback senses a change in voltage at the output node and return it to the input node by subtracting it thus returning the Gain to its original value and this cycle continue in the operating range sustaining a linear relation.

## Report the derivative of VOUT vs VSIG. The derivative is itself the small signal gain. Is the gain linear (independent of the input) in the operating range of the amplifier? Why?

As the transistor reaches its operating range. We can see a flat gain curve at approximately -10 which is the required gain from the circuit. The flat curve indicates the gain is linear and is independent of the input. Due to the negative feedback as mentioned previously

## VIN is almost constant in the operating range of the amplifier. What is its value? Why?

The Value of VIN is 817.224mV which is approximately equal to the bias VGS Calculated in the previous part, being constant show that the gain is also constant in that are. Due to the negative feedback as explained before.

## Analytically calculate the DC input range over which the gain is linear. Compare your analysis with the simulation result.

$$\text{Input Range} \approx \frac{V_{DD} - 2V^*}{|A_v|} = \frac{2.5 - 2 * 0.2}{10} = 0.21V$$

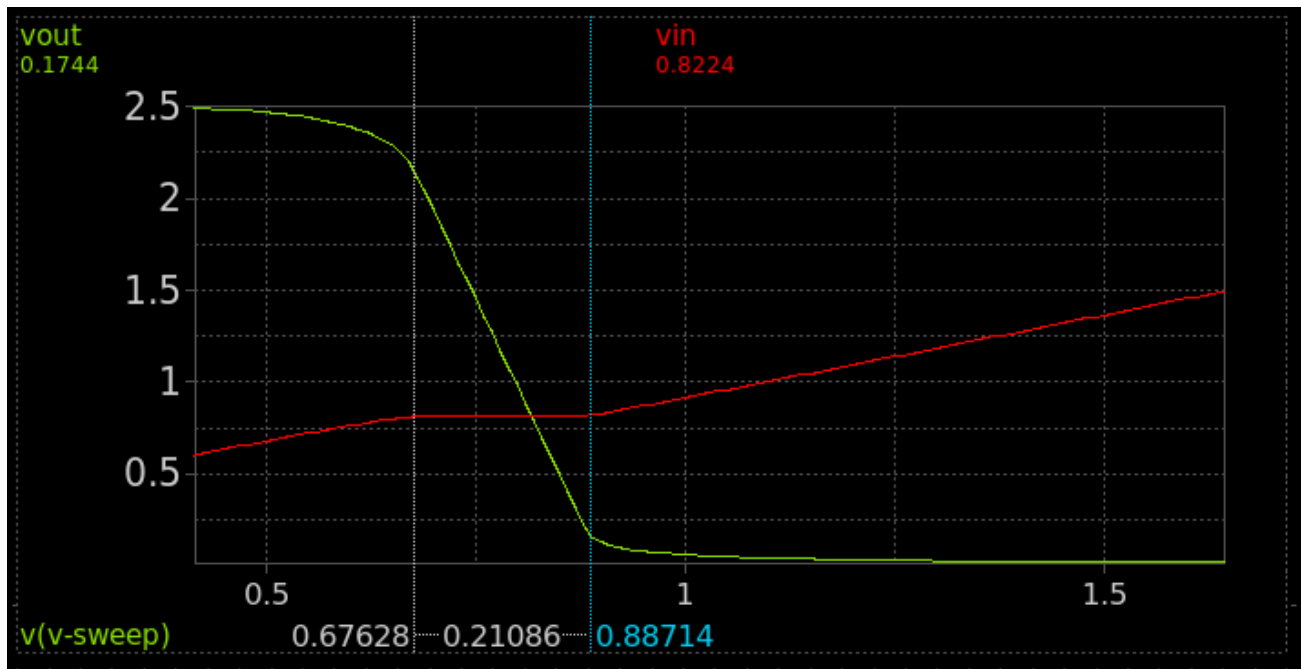


Figure 14 Input Range from Simulation

Simulation results = 0.21086V, Hand Analysis = 0.21V. Approximately equal!

## GM vs Time (Transient Analysis)

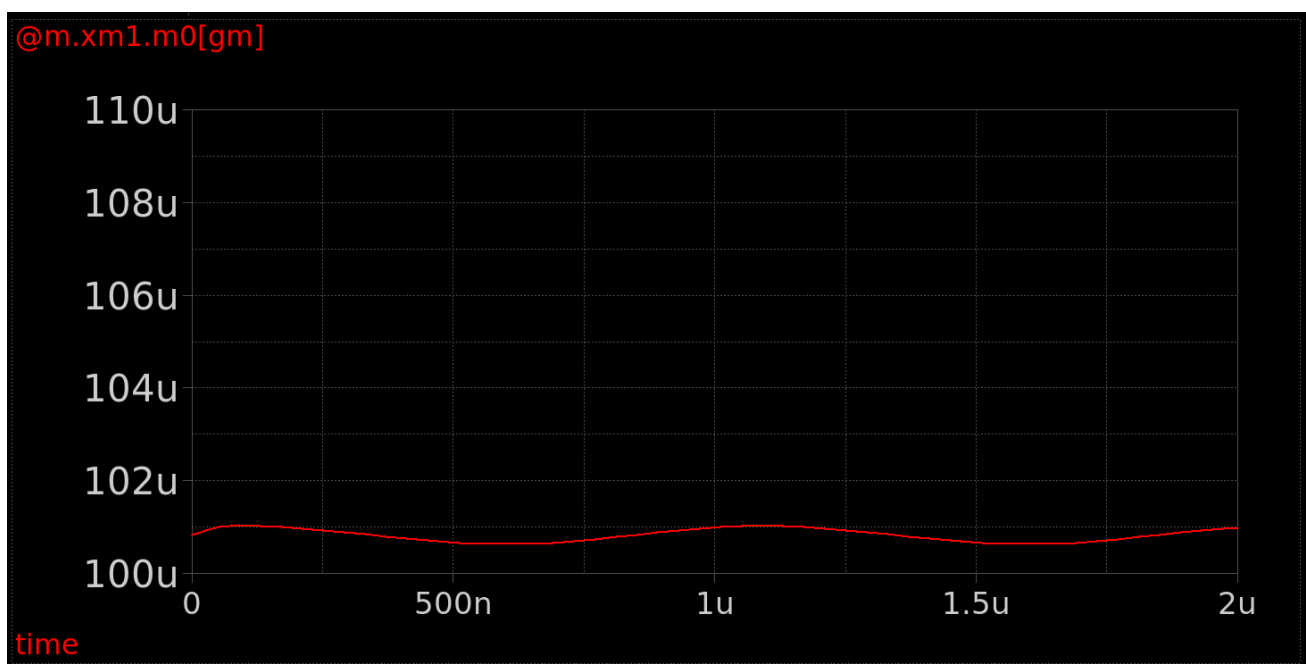


Figure 15 gm vs Time

Compared to figure 10, we can see gm varies at a much smaller range around the 101uS point compared to the bigger variation seen in figure 10, This small variation can be considered approximately Constant in this case.