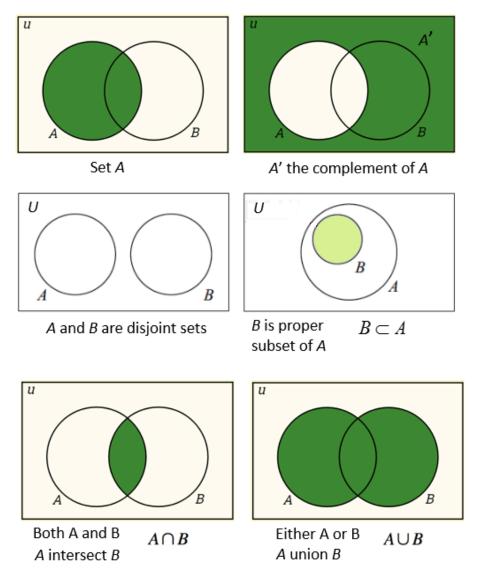
Set Theory

Cantor's defintion of a set

A set is a collection of definite and seperate objects. These objects are called elements of the set.



An empty set is denoted by $\{\ \}$, it is an unique set with no elements.

Ordered tuples

An ordered n-tuple is defined by $(x_1, x_2, ..., x_n)$

An ordered pair is defined by (x_1, x_2)

An ordered triple is defined by (x_1, x_2, x_3)

Rule: (a,b) = (c,d) iff (in and only if) (a=c), (b=d)

Cartesian products

The Cartesian product $A_1\times A_2\times ...\times A_n$ of ordered n-tuples $(a_1,a_2,...,a_n)|(a_1\in A_1)\wedge (a_2\in A_2)\wedge ...\wedge (a_n\in A_n)$

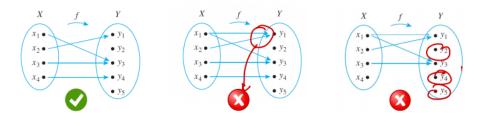
Functions

A function is built from two sets, X and Y. What the function does is build a relation between these two sets following these two rules:

- Every element of X is related to some elements in Y
- No element of X is related to more than one element in Y

Following cases are also allowed:

- There can be elements of the co-domain Y that are not function of any input element.
- Different inputs can mapped to the same element of Y.



Notable functions

- The identity function: $I: X \to X$, where each element is mapped to itself.
- The exponential function
- The log-function
- The Hamming-Distance Function
- The image function

Laws of Exponents

If b and c are any positive real numbers and u and v are any real numbers, the following laws of exponents hold true:

$$b^{u}b^{v} = b^{u+v}$$

$$(b^{u})^{v} = b^{u}$$

$$\frac{b^{u}}{b^{v}} = b^{u-v}$$

$$(bc)^{u} = b^{u}c^{u}$$

$$7.2.1$$

$$7.2.2$$

$$7.2.3$$

Exponential rules

Theorem 7.2.1 Properties of Logarithms

For any positive real numbers b, c and x with $b \neq 1$ and $c \neq 1$:

a.
$$\log_b(xy) = \log_b x + \log_b y$$

b.
$$\log_b \left(\frac{x}{y}\right) = \log_b x - \log_b y$$

c.
$$\log_b(x^a) = a \log_b x$$

Logarithmic rules

Convolution

- Check slides for explaination
- See this link for a demo