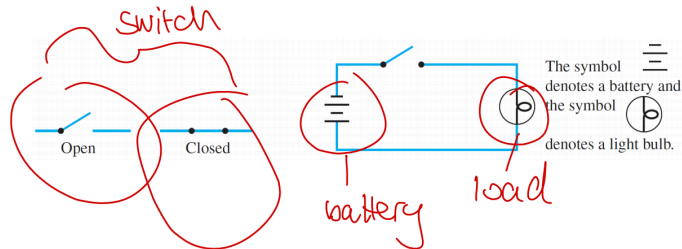
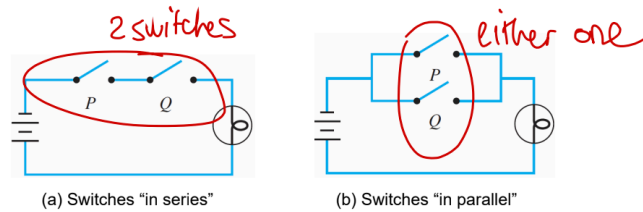


Digital logic circuits

Simple circuit



A simple circuit has three elements: switch, battery and load



Switches can either be used "in series" (the circuit will only work when both switches are closed) or "in parallel" (the circuit will work when one of the both switches are closed).

The in series circuit is equivalent to the AND truth table, where closed is equivalent to true and the truth table is only true when both values are true (closed).

The in parallel circuit is equivalent to the OR truth table, where closed is equivalent to true and the truth table is only false when both values are false (open).

Combinatorial circuit

- combinational: type of digital circuit whose output only depends on the current input.
- sequential: output depends on both the current input and previous outputs. This means a sequential circuit preserves a memory of the input while a combinational circuit does not (out of scope for this course)

3 possible inputs




Input			Output
P	Q	R	S
1	1	1	1
1	1	0	0
1	0	1	0
1	0	0	1
0	1	1	0
0	1	0	1
0	0	1	1
0	0	0	0

1 possible output

Rules for combinational circuits

1. Never combine the input wires.
 2. Never feed back the output of a gate into the same gate
- combinational equivalence: two circuits can have the same output but built completely differently
 - circuit minimization: for production of electrical circuit it makes sense minimizing more complicated circuits to simplified ones so that they cost lesser in production.

Logic gates

Type of Gate	Symbolic Representation	Action																	
NOT		<table><tr><th>Input</th><th>Output</th></tr><tr><th>P</th><th>R</th></tr><tr><td>1</td><td>0</td></tr><tr><td>0</td><td>1</td></tr></table>	Input	Output	P	R	1	0	0	1									
Input	Output																		
P	R																		
1	0																		
0	1																		
AND		<table><tr><th>Input</th><th>Output</th></tr><tr><th>P</th><th>Q</th><th>R</th></tr><tr><td>1</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>0</td><td>0</td><td>0</td></tr></table>	Input	Output	P	Q	R	1	1	1	1	0	0	0	1	0	0	0	0
Input	Output																		
P	Q	R																	
1	1	1																	
1	0	0																	
0	1	0																	
0	0	0																	
OR		<table><tr><th>Input</th><th>Output</th></tr><tr><th>P</th><th>Q</th><th>R</th></tr><tr><td>1</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>0</td><td>0</td><td>0</td></tr></table>	Input	Output	P	Q	R	1	1	1	1	0	1	0	1	1	0	0	0
Input	Output																		
P	Q	R																	
1	1	1																	
1	0	1																	
0	1	1																	
0	0	0																	

Disjunctive Normal Form (DNF)

Also called “Or of And’s”

$$G(p, q) \equiv (p \wedge q) \vee (\neg p \wedge q)$$

- Best when output is 0
- AND together all variables where output is 1
- OR together all the 1 rows
- Simplify

Conjunctive Normal Form (CNF)

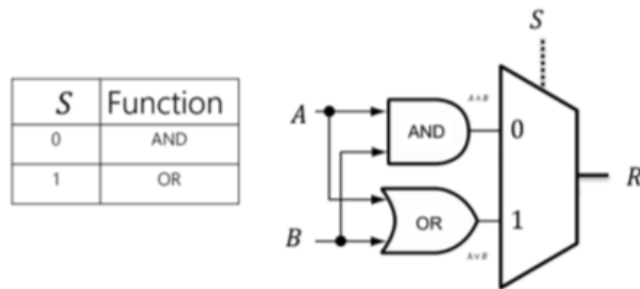
Also called “And of Or’s”

$$G(p, q) \equiv (p \vee q) \wedge (\neg p \vee q)$$

- Best when output is mostly 1
- Identify rows with output 0
- OR together all variables in some row (negate when 1)
- AND together the 0 rows

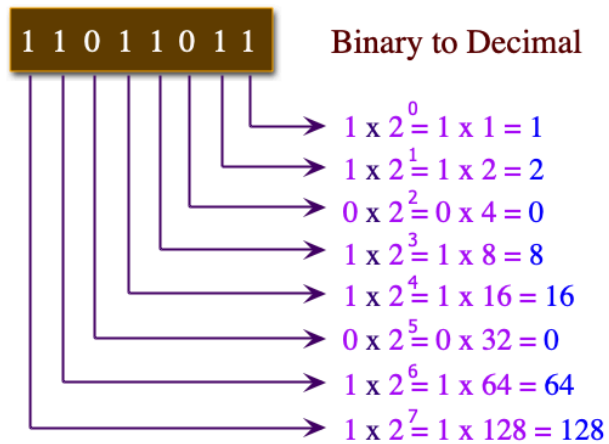
Multiplexer

This Multiplexer selects the output of the AND operation if the selector $S=0$, otherwise it selects the output of the OR operation.



Binary to decimal

For the binary number, read the numbers from bottom to top.



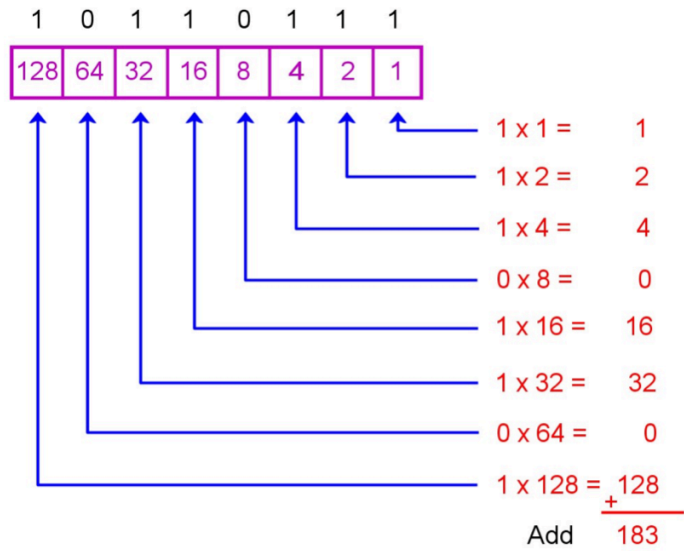
$$1 + 2 + 8 + 16 + 64 + 128 = 219$$

$$(11011011)_2 = (219)_{10}$$

Decimal to binary

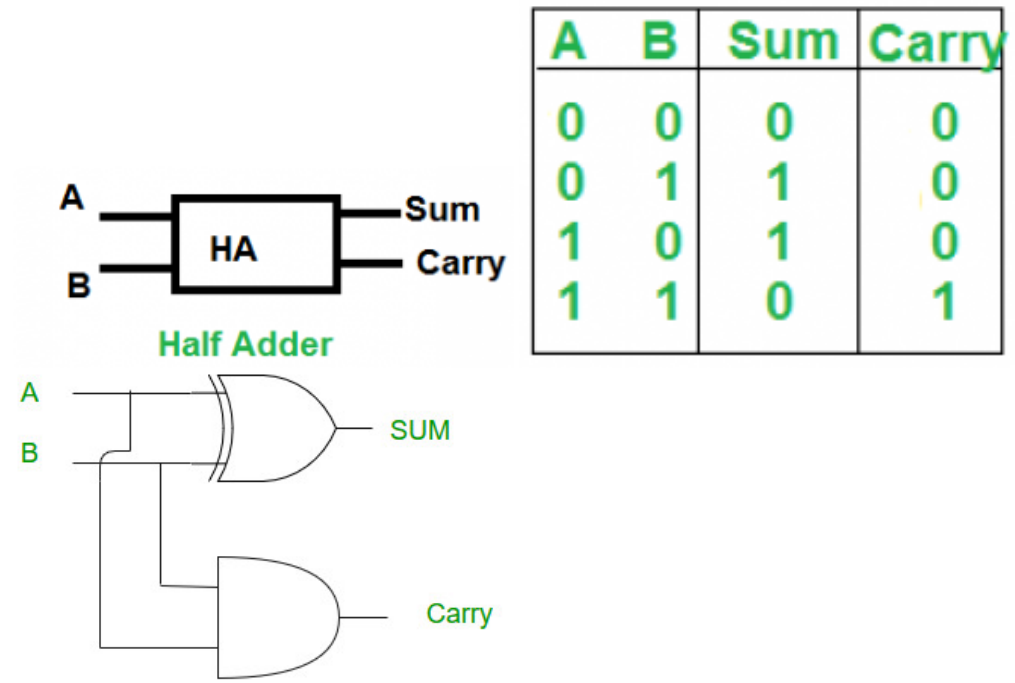
Multiply each digit with it's binary equivalent.

Convert 10110111 to Decimal

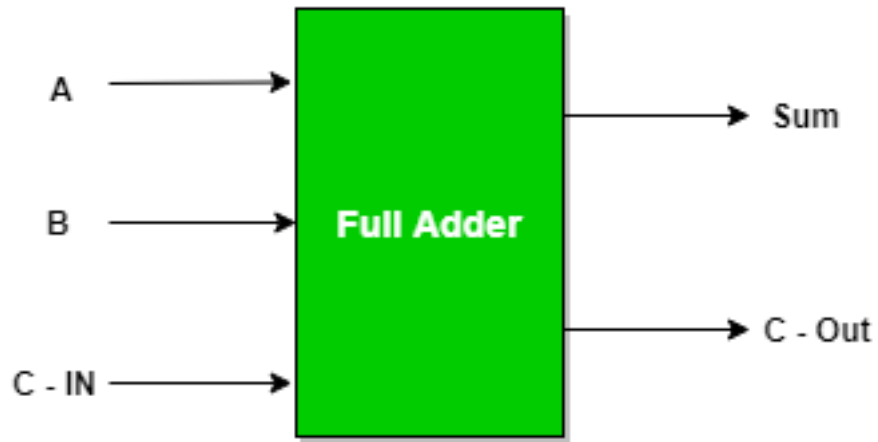


10110111 = 183 decimal

Half-Adder



Full-Adder



Inputs			Outputs	
A	B	C - IN	Sum	C - Out
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

