

Research Article

Source-detector trajectory optimization for FOV extension in dental CBCT imaging

S M Ragib Shahriar Islam^{a,b,c,*}, Ander Biguri^d, Claudio Landi^e, Giovanni Di Domenico^f, Benedikt Schneider^g, Pascal Grün^g, Cristina Sarti^e, Ramona Woitek^h, Andrea Delmiglio^e, Carola-Bibiane Schönlieb^d, Dritan Turhani^g, Gernot Kronreif^a, Wolfgang Birkfellner^c, Sepideh Hatamikia^{b,a}

^a Austrian Center for Medical Innovation and Technology, Wiener Neustadt, Austria

^b Research Center for Clinical AI-Research in Omics and Medical Data Science (CAROM), Department of Medicine, Danube Private University (DPU), Krems, Austria

^c Center for Medical Physics and Biomedical Engineering, Medical University Vienna, Vienna, Austria

^d Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge, United Kingdom

^e SeeThrough Srl, Via Bolgara 2, Brusaporto (BG), Italy

^f Department of Physics and Earth Science, University of Ferrara, Ferrara, Italy

^g Center for Oral and Maxillofacial Surgery, Department of Dentistry, Faculty of Medicine and Dentistry, Danube Private University (DPU), Krems, Austria

^h Research Center for Medical Image Analysis and Artificial Intelligence (MIAAI), Department of Medicine, Danube Private University (DPU), Krems, Austria

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ABSTRACT

In dental imaging, Cone Beam Computed Tomography (CBCT) is a widely used imaging modality for diagnosis and treatment planning. Small dental scanning units are the most popular due to their cost-effectiveness. However, these small systems have the limitation of a small field of view (FOV) as the source and detector move at a limited angle in a circular path. This often limits the FOV size. In this study, we addressed this issue by modifying the source-detector trajectory of the small dental device. The main goal of this study was to extend the FOV algorithmically by acquiring projection data with optimal projection angulation and isocenter location rather than upgrading any physical parts of the device. A novel algorithm to implement a Volume of Interest (VOI) guided trajectory is developed in this study based on the small dental imaging device's geometry. In addition, this algorithm is fused with a previously developed off-axis scanning method which uses an elliptical trajectory, to compensate for the existing constraints and to further extend the FOV. A comparison with standard circular trajectory is performed. The FOV of such a standard trajectory is a circle of 11 cm diameter in the axial plane. The proposed novel trajectory extends the FOV significantly and a maximum FOV of 19.5 cm is achieved with the Structural Similarity Index Measure (SSIM) score ranging between (≈ 98 –99%) in different VOIs. The study results indicate that the proposed source-detector trajectory can extend dental imaging FOV and increase imaging performance, which ultimately results in more precise diagnosis and enhanced patient outcomes.

1. Introduction

Cone Beam Computed Tomography (CBCT) is one of the most rapidly growing imaging modalities in medicine, especially for image-guided therapy and surgical planning. The early stage of CBCT imaging application has been recorded in the late '70s as the projections from cross-plane rays [1]. It was demonstrated that a CBCT scan can provide extensive 2D projection data, as infinite X-ray beams radiate from various angles and intersect each point of the imaging object. Follow-

ing, the circular source-detector trajectory is the simplest and easy-to-implement trajectory to image a point or spherical object [2]. Given its ease of use, this approach is utilized extensively in medical CBCT scanning and reconstruction applications. Almost two decades later, CBCT was used for the first time in dentistry with the same trajectory principle [3,4]. However, in clinical practice, the circular trajectory is not necessarily the best way to achieve optimum 3D reconstruction. Hence, the optimum trajectory varies depending on the application circumstance.

* Corresponding author.

E-mail addresses: ragib.shahriar@acmit.at, tusharragib@gmail.com (S.M.R.S. Islam).

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Despite its limitation of imaging soft tissues, CBCT is incredibly useful for evaluating anatomical dental treatments. Small-volume CBCT is useful in endodontics procedures for mapping the bone around the tooth root and assessing the anatomy of the root canal, aiding the pre-surgical inspection [5]. This leads to the development of dental implant-based therapies since the key anatomical characteristics, surgical guide design, and implant planning can also be reviewed [6–8]. Furthermore, CBCT scanning is beneficial to generate 3D data to analyze the dilacerated, unerupted, supernumerary teeth, and clefts in the cases of inadequate information for orthodontic treatments. CBCT also can help treat dental trauma when 2D scans cannot provide sufficient information for surgical planning [9–11]. Moreover, CBCT is a decent alternative to multi-detector computed tomography (MDCT) imaging for chronic rhinosinusitis surgery planning as it has comparable accuracy to sinus endoscopy [12,13]. CBCT scan is also applicable to the primary diagnosis and supervision of temporomandibular joint (TMJ) bone disorder [14].

Typically, based on the size of Field of View (FOV), the CBCT can be grouped into four types including dentoalveolar CBCT (with FOV < 8 cm), maxillo-mandibular CBCT (with FOV 8–15 cm), skeletal CBCT (with FOV 15–21 cm), and head and neck CBCT (with FOV > 21 cm) [15,16]. The FOV size requirement of dental CBCT scan can be diversified based on the region of interest and treatment type [17]. This makes the treatment more complex in medical practice as considering the different imaging organs and tasks, a different CBCT scanning device is required. Moreover, it is challenging to image different ROIs with a small CBCT unit, where the FOV is restricted. The simplest fix to this small FOV problem is to use larger detectors to capture more projection information. However, the drawback of this approach is the high cost associated with such large detectors. Another solution to this FOV expansion issue is to fuse more sets of scan data or to stitch separately reconstructed volumes. However, this approach induces increased exposure to radiation and complexity in maintaining stitching accuracy [18,19]. The shifted detector and collimation of the X-ray beams can also be a solution. However, it requires hardware modifications during the scan [20].

Alternatively, source-detector trajectory manipulation can address the limited FOV problem which could maximize the VOI imaging volume by acquiring heterogeneous projection data for reconstruction. Source-detector trajectory optimization of CBCT is an extensive research field which has gained a lot of attention in recent years. Numerous trajectories were developed over the years for different purposes such as image quality improvement, collision avoidance, dose reduction and metal, CBCT artifact reduction, and FOV extension [21]. However, the trajectories introduced for FOV extension in medical imaging have focused on expanding the FOV either in the longitudinal direction (in the perpendicular direction of the source-detector plane) or the lateral direction (in the source-detector plane) expansion. In the earlier research studies on longitudinal FOV expansion, numerous combinations of different shapes and sizes of arcs, circles, and linear paths have been tested. Two same distant linear paths reinforced with a circle, a linear path with two arcs, parallel circular trajectory, double overlapping cone beam circular orbit, an ellipse-line-ellipse path, an extended version of ellipse-line-ellipse, and multiple scans with table translation were proposed [22–28]. Following, helical trajectory, reverse helical, and multi-turn reverse helical trajectory were also examined [29–32]. All these approaches exhibit good results, while the trajectory involved with the movement in the perpendicular z-axis, makes the trajectory a non-planner 3D path. Whereas, in the small dental CBCT scanning units the 2D planner trajectories are widely used. In addition, for longitudinal FOV extension multiple X-ray source approach was used [33], however, the multiple X-ray method has hardware and software complexity as well as has increased radiation dose due to the multiple X-ray sources. For circular trajectory, the FOV is always a circle in the source-detector plane. As the endeavors of lateral FOV extension, non-stationary iso-centric elliptical trajectory, complimentary circular scan,

rotated detector, and dynamic detector offset approaches are used which are the different forms of offset detector or displaced detector approach [20,34–36]. The displaced detector approach has the additional burden of collimation adjustment and may not fulfill the data incompleteness according to Tuy's conditions [2] which makes it challenging for the generally used reconstruction algorithms as FDK [37] to reconstruct the correct 3D volume.

Despite all these approaches, according to our best knowledge there is still no study that has developed optimal source-detector trajectories for FOV expansion specifically for dental imaging. Moreover, all the aforementioned studies were developed based on experimental trials with a trial and error approach, none of these studies were developed based on a trajectory optimization pipeline according to specific volumes/regions of interest (VOI/ROI) based on imaging requirements. The goal of this study is to develop a VOI-guided trajectory aiming to extend the FOV and to maximize the image quality at the interested VOIs. In doing so, an algorithm was developed to establish such a trajectory and later on it was fused with a previously developed off-axis scanning method which uses an elliptical trajectory under certain movement restrictions [34]. The proposed algorithm lifts the restriction and extends the FOV of the small dental CBCT device with excellent image quality.

2. Methodology

The prime task of this study is to develop a source-detector trajectory and to apply the most suitable reconstruction algorithm to expand the lateral FOV of the small dental unit while maintaining the diagnostic quality. In section 2.1, the geometry of the experimental device is explained. Then, in section 2.2, the experimental phantoms and the Volume of Interests (VOIs) of the imaging was briefly explained. Section 2.3 depicts the possible region of the trajectory area, and then in section 2.4 the process of the trajectory development is explained. Section 2.5 describes the image reconstruction algorithms that has been used in this study and in section 2.6 all the different experiments of this study have been explained. Finally, in section 2.7, all the image quality measurement metrics used in this study are described with their ideal characteristics. TIGRE: MATLAB/Python-GPU-based toolbox was used for all the simulation, reconstruction, and validation in this study [38].

2.1. Geometry of the experimental CBCT unit

In this study, we simulated the geometry of the small dental CBCT unit which has the freedom to translate the gantry within a certain area during the scanning (resulting a shifted isocenter for each projection in a rectangular region of 11 cm × 6 cm, starting from 1 cm behind the bite point of the machine geometry) as shown in Fig. 1. It has a center of rotation to detector distance of 17 cm, and to X-ray source distance of 38 cm, with a total source to detector distance of 55 cm. Due to non-equal source-to-origin and detector-to-origin distances, the source and detector have different trajectory paths. For stationary iso-centric scan, the detector only performs a movement of about 195° angular area, whether the maximum allowable range is 240°. The device has a detector of 664 × 654 pixel with 0.24 mm resolution pitch.

2.2. Anthropomorphic phantoms, the digital phantoms, and volume of interests (VOI)

Two anthropomorphic head phantoms were used for this study. The phantom named Jerry is the smaller phantom which has a naso-occipital length of 17 cm and a cranial breadth of 15 cm. The standard head-sized phantom named Tom was used which has a naso-occipital length of 23 cm and a cranial breadth of 16 cm. Both phantoms were used for the development and testing of the proposed trajectory development algorithm (described in the section: 2.4 and 2.6).

Jerry digital phantom: A large-size CBCT reconstructed volume of 713 × 713 × 712 pixels with 0.24 mm × 0.24 mm × 0.24 mm of resolution

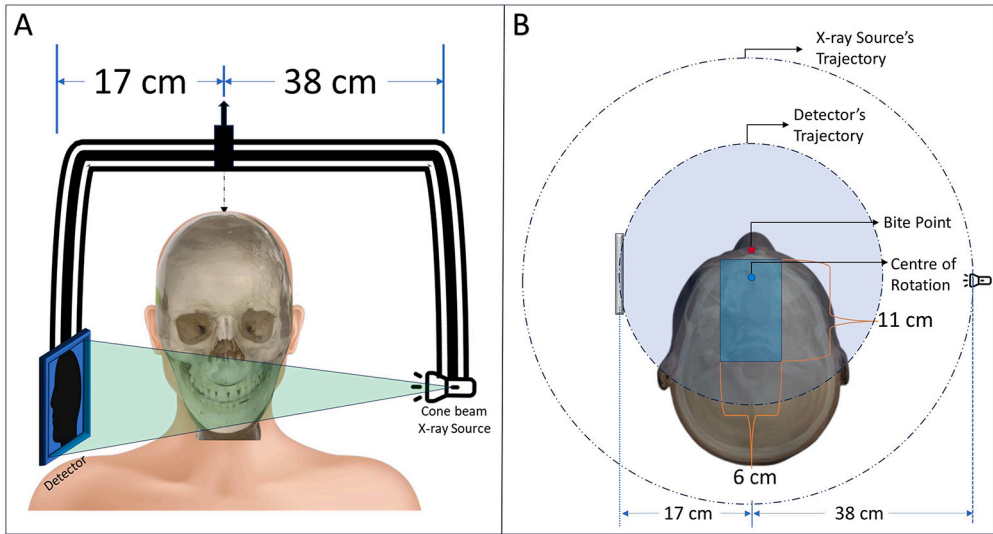


Fig. 1. The geometry of the dental CBCT system used in this study. A: The X-ray source, detector, and the patient position. B: The top view of the geometrical setup.

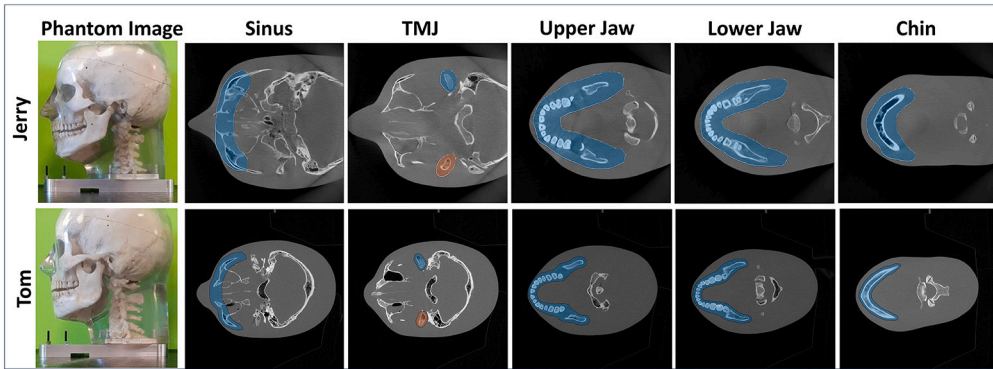


Fig. 2. The anthropomorphic phantoms and the respective target VOIs to the image.

was used as the digital phantom for Jerry to perform the trajectory computer simulations to produce the Digitally Rendered Radiographs (DRR) or synthetic projections, and to reconstructed image's quality testing. These DRRs are computed in TIGRE using the mathematical model described in Section-2.4.3 and 2.5 for all the experiments-2.6.1, 2.6.2, and 2.6.3

Tom digital phantom: For Tom, a digital phantom of $512 \times 512 \times 304$ pixels with a resolution of $0.48 \text{ mm} \times 0.48 \text{ mm} \times 0.75 \text{ mm}$, was used same as Jerry.

For both the phantoms five volumes of interest (VOI) were selected to reconstruct; the maxillary sinus, the temporomandibular joint (TMJ) bones, the upper jaw, the lower jaw, and the chin as shown in Fig. 2. The primary target of the study was to achieve lateral FOV extension for the upper and lower jaw and then, apply more progressive approaches to reconstruct in both longitudinal directions for the maxillary sinus, TMJ, and the chin.

2.3. Possible movement space for trajectory: identifying the collision area

For the anthropomorphic phantoms described in section 2.2, the ideal patient positioning headspace is an elliptical region with 25 cm and 16 cm of major and minor axes respectively as shown in Fig. 3(A). An extra 3 cm space has been taken around the existing elliptical region into the headspace considering the safety of the patient. Therefore, the experimental extended headspace is an elliptical region with major and minor axes of 31 cm and 22 cm respectively. There is a "Bite point" where the patient is supposed to bite during the scanning and there is an estimated rectangular region for the positioning of the iso-center during

the scanning. Considering the center of rotation to the source and detector distance in the whole iso-center placement region, it is obvious that there is no possible collision between the patient and the source, however, the detector is closer to the head. Hence, it has some valid and invalid regions to move during the scan to avoid collision with the patient. In the existing setup, the device only can perform a limited angle circular scan due to the collision as shown in Fig. 3(B).

At the initial step, the possible detector's movable space was calculated. Section Appendix A in the supplementary materials explains the estimated valid and non-valid region for the detector movement which is also the search space for the trajectory of this study.

2.4. Development of the proposed trajectory

The proposed trajectory was developed based on the maximum scan data acquisition principle of Tuy's condition and by augmenting it to a modified iso-center shifted elliptical scan trajectory. In section 2.4.1, the principle of Tuy's condition is briefly explained. Section 2.4.2 illustrates how the initial VOI-guided trajectory estimation algorithm was developed and used to develop VOI-guided trajectory. Then, in section 2.4.3, the fusion of Tuy's condition-based VOI-guided algorithm with the modified iso-center shifted elliptical scan to develop the proposed trajectory was explained.

2.4.1. Tuy's condition

According to Tuy's condition [2], for obtaining maximum useful scan data, there should be infinite numbers of X-rays intersecting every 3D

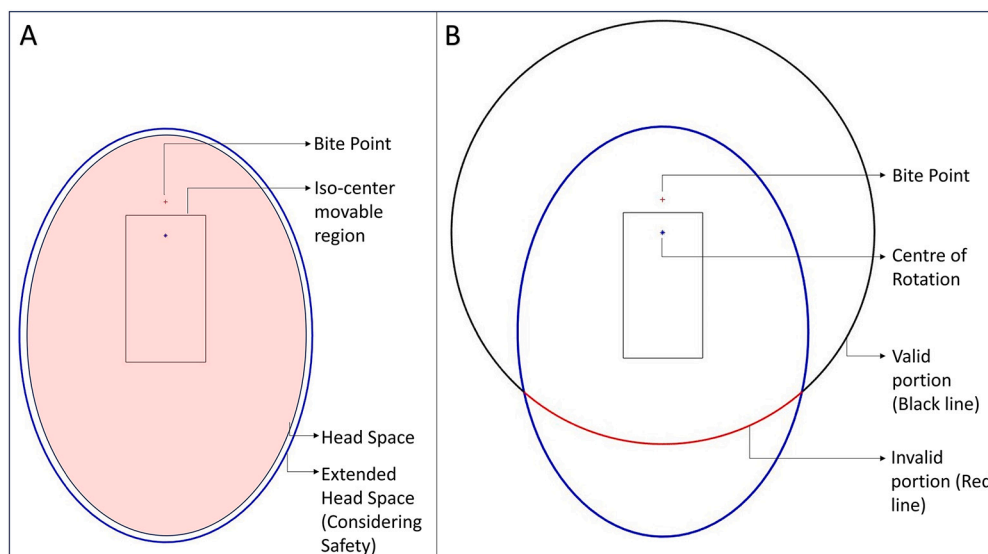


Fig. 3. A: The pink shade is the original headspace, and the larger blue ellipse is the extended headspace. B: The semi-circular trajectory, black portion is the possible standard detector's trajectory, red portion is under collision region.

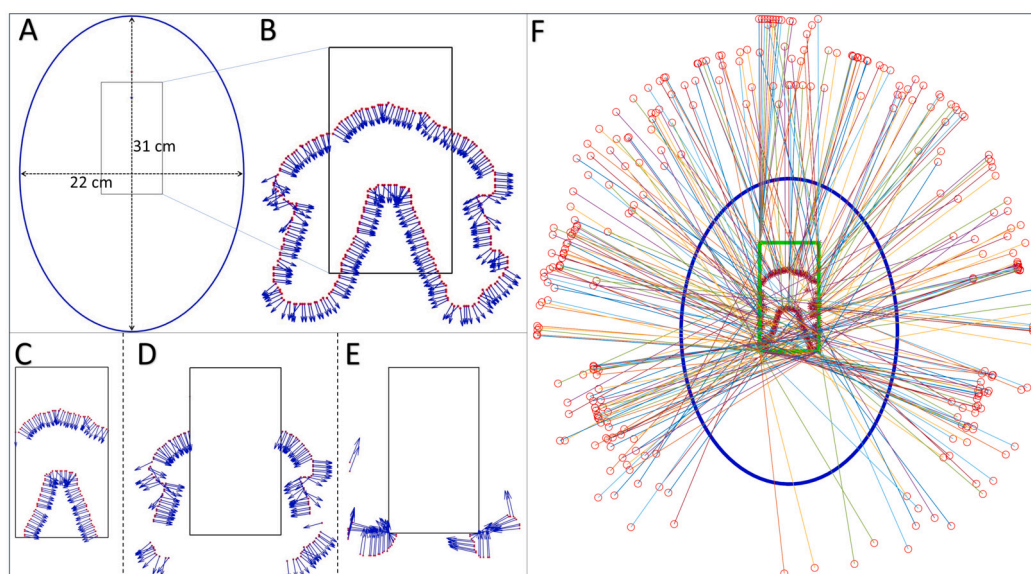


Fig. 4. The VOI-guided trajectory, A: The headspace and iso-center movable region, B: The calculated points for iso-center placement, C: Category-I points, D: Category-II points, E: Category-III points, F: The Predicted VOI-guided trajectory.

voxel in the imaging volume from infinite numbers of different directions. Therefore, for the simplest real-life implementation, the circular trajectory is widely used, however, as mentioned before it is not necessarily the best trajectory due to Tuy's second condition, which claims that the X-rays should intersect the 3D-voxels at the perpendicular angle of the tangent line drawn at the VOI boundary. In consequence, the VOI is supposed to be a cylinder-shaped region which is not desired or useful for all clinical applications.

2.4.2. VOI-guided trajectory construction

The symmetrical shape of the human head allows us to predict a common ROI polyline as shown in Fig. 4(A), (B), taken in the Z-axis in an intermediate axial plane ideally at the middle of the full 3D VOI. This plane was chosen to set the detector and source position vertically such that the central X-ray beam passes through it. The VOI-polyline was predicted by taking the union of all the five VOIs shown in Fig. 2. It was considered as the VOI's boundary to predict the tangent lines at

the projection points. Then the perpendicular angles to the tangent lines were calculated which were used as the projection angles to meet Tuy's condition. However, to avoid collisions between the detector and the patient, it is not possible to move the isocenters at all calculated projection points. Therefore, the computed points were categorized into three different classes. **category-I:** the directly reachable points lie inside the iso-center moving region; **category-II:** the points that are outside of this region and calculated projection angles permit the creation of pseudo-points inside the region; and **category-III:** the points that are outside of the region and the projection angles do not allow the x-rays to pass through the VOI. The category-I points and the category-II pseudo-points were directly considered for the iso-center placement during the scanning. Category-III pseudo-points were computed as per the closest possible projection angles that pass through the iso-center moving region. Fig. 4(F) shows the predicted VOI-based trajectory heat map for iso-center and detector placement.

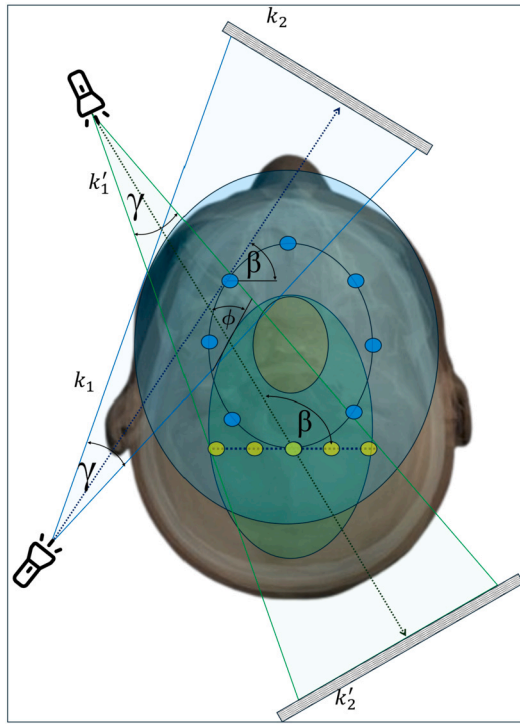


Fig. 5. The projection geometry of the proposed trajectory.

2.4.3. Proposed extended FOV trajectory

The predicted VOI-guided trajectory consists of scattered calculated iso-center points with non-sequential projection angles which makes it challenging to implement the trajectory directly in a scanner. Thus, the idea of the shifted iso-center rotation trajectory in an elliptical path described in [34] was implemented as Fig. 6(A) and then enhanced with the algorithm developed for the VOI-guided method described in Section-2.4.2 to replicate an elliptical path outside of the iso-center positioning area (Fig. 6(A, B)). The shifted iso-center trajectory has the limitation of detector movement such that the outmost X-ray beam and the detector should be tangential to the elliptical path to avoid non-sampling in the middle of the VOI. However, in this study, this movement constraint was lifted, and as a result for the larger acquisition, a void space appeared as no central X-ray beam of CBCT scan passes through the yellow-shaded region in Fig. 5. This limitation and FOV extension both were addressed by fusing the VOI-guided method to the shifted iso-center rotation trajectory. An imaginary elliptical VOI shown in Fig. 6(A) (the dotted ellipse) was taken in the calculation for the expansion of the FOV, additionally, it was designed such that it allows enough X-ray beams to pass through the missing region for data augmentation and to form the estimated proposed trajectory (Fig. 6(B)). As the scan geometry shown in Fig. 5, considering ϕ be the incident angle to the VOI, varying from 0 to $\pi/2$, γ be the half-fan span angle, and β be the projection angle and let a and b be the major and minor axis of the elliptical detector moving path respectively, the trajectory equation described in [34] gets extended as follows,

$$k'_1 = k_1 = tg(\phi + \gamma + \beta); \quad k'_2 = k_2 = tg(\beta) \quad (1)$$

$$M = \sqrt{(k_1^2 a^2 + b^2)}; \quad N = \sqrt{(k_2^2 a^2 + b^2)} \quad (2)$$

Thus, the coordinate of any point in the VOI is,

$$x = \pm \frac{M + N}{k_2 + k_1}, \quad y = \pm \frac{k_2 M + k_1 N}{k_2 - k_1} \quad (3)$$

and, the X-ray source shift is defined by,

$$S_x = x + L \cdot \cos(\phi + \gamma + \beta), \quad S_y = y + L \cdot \sin(\phi + \gamma + \beta) \quad (4)$$

The VOI-guided portion was smoothed on the post-processing as Fig. 6(C) to make it mechanically feasible. The final proposed trajectory looks like Fig. 6(D)

2.5. Image reconstruction

The imaging object X-ray attenuation $f(x)$ is estimated from the projection value $p(u, v, \alpha)$ for the given X-ray source angle from Eq. (1) of $\alpha = \phi + \gamma + \beta$. Hence, the projection on a point (u, v) on the detector can be estimated as

$$p(u, v, \alpha) = \int_0^\infty f(s(\alpha) + \lambda \theta(\alpha, u, v)) d\lambda \quad (5)$$

Here, the source location s is estimated from Eq. (4) as $s(\alpha) = (x + L \cdot \cos \alpha, y + L \cdot \sin \alpha)$ and $\lambda \in [0, \sqrt{u^2 + v^2 + D^2}]$, where as L and D are the source-iso-center and source-detector distances respectively. $\theta(\alpha, u, v)$ is the estimated unit vector from $s(\alpha)$ to the point (u, v) on the detector. The reconstruction system for the voxels calculated from the projections recorded in Eq. (5) can be described as

$$A \cdot x = b + e \quad (6)$$

Whereas x is the voxel to be reconstructed, b is the projection data, and e is the error term which represents the reconstruction noise. A is the system matrix that relates the voxel values x to projections data b . The system matrix A is a sparse matrix which makes the system an ill-posed system to solve by direct mathematical calculations. Therefore, the iterative reconstruction form of Eq. (6) can be described as

$$x^* = \operatorname{argmin}_x \|A \cdot x - b\|^2 + G(x) \quad (7)$$

Here, $G(x)$ is the regularization function that is tuned over each iteration to obtain better image volume x . In this study, we have used two Gradient-based algorithms to regularize $G(x)$. The regularization process for these algorithms is described in the following paragraph OS-SART and ASD-POCS.

Ordered-Subset Simultaneous Algebraic Reconstruction Technique (OS-SART):

SART algorithm [39] is described by the following equation.

$$x^{(iter+1)} = x^{(iter)} + \lambda_{OSSART} \cdot A_{nProj} \cdot (b_{nProj} - A_{nProj} \cdot x^{(iter)}) \quad (8)$$

where $iter$ is the iteration number, $nProj$ is the projection number, and λ_{OSSART} is the relaxation parameter that tunes the effect of the gradient in each iteration to calculate the image in the next iteration $x^{(iter+1)}$. The OS-SART algorithm is the extension of SART where instead of considering only one projection per iteration a group of projections are taken for the calculation [40].

Eq. (8) represents an iterative method to solve the optimization problem in Eq. (7), where it specifically targets minimizing the data fidelity term $\|A \cdot x - b\|^2$. The update rule in Eq. (8) can be viewed as a gradient descent step aimed at reducing the residual, thereby working towards the overall minimization objective defined in Eq. (7).

Adaptive steepest descent projection onto convex sets (ASD-POCS):

ASD-POCS is the extended gradient-based algorithm which also considers the Total Variation (TV) in the smoothing process per iteration [41]. The ASD-POCS algorithm expresses the $G(x)$ of Eq. (7) as.

$$G(x) = \|x\|_{TV} = \sum_{ijk} \sqrt{(x_{ijk} - x_{ij-1k})^2 + (x_{ijk} - x_{i-1jk})^2 + (x_{ijk} - x_{ijk-1})^2} \quad (9)$$

Here i, j, k are the voxel indices in 3D space. ASD-POCS takes the images created by the SART algorithm and then perform further TV optimiza-

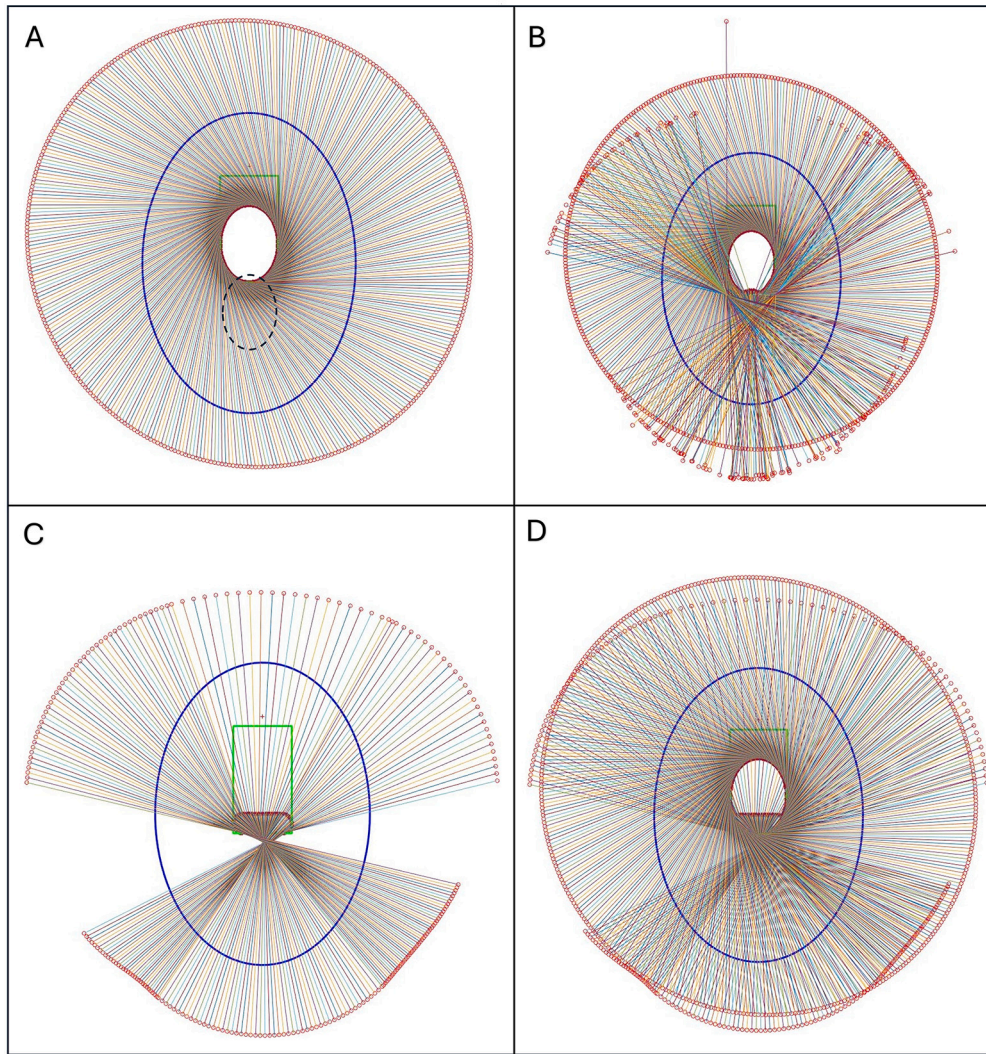


Fig. 6. **A:** The shifted iso-centric scan and intended augmentation region (dotted ellipse) by VOI-guided method. **B:** The estimated proposed fusion trajectory. **C:** Smoothed fusion projections. **D:** The final proposed fusion trajectory.

tion by the steepest gradient algorithm. Therefore, the final equation for ASD-POCS can be described as,

$$x^* = \operatorname{argmin} \|x\|_{TV} \quad (10)$$

ASD-POCS optimizes the image such that $|A \cdot x - b| < \varepsilon$ where ε is the acceptable error between the observed and predicted projections.

Eq. (10) is a specific instance of the optimization problem in Eq. (7), where it focuses solely on minimizing the total variation (TV) norm, $\|x\|_{TV}$ to deal with the data fidelity.

For both the OS-SART and ASD-POCS algorithms there are initial hyperparameters described in [40,41] which must need to be optimized for a specific device geometry and trajectory for the convergence to the solution. For this study, a semi-automated trial and error-based brute-force approach was applied for the parameter optimization. All the parameters were taken as a variable one by one in a feasible range and were fixed at the best reconstruction performance. Initially, the parameters were optimized for the proposed trajectory which was developed with 600 projections. Furthermore, the trajectory and reconstruction algorithm parameters were optimized again for a reduced 380 projection setup to make it comparable with the conventional limited-angle circular trajectory setup.

A typical algorithm for the parameter optimization is shown in Algorithm 1. The optimization time is dependent on the empirical values chosen and the computing device.

2.6. Experiments

This study has three sets of experiments considering the trajectories and the two iterative reconstruction algorithms for both the imaging phantoms, Jerry and Tom. Poisson noise and Gaussian noise have been added to the simulated projection data in every experiment to mimic the CT noise.

2.6.1. Experiment-1: reconstruction with standard trajectory using OS-SART

The first experiment is the reconstruction of the volume using the Digitally Rendered Radiograph (DRR) data computed in computer simulation from the standard limited angle circular scan of the device using the OS-SART reconstruction algorithm which is similar to the real-life scan setup of 390 projections.

2.6.2. Experiment-2: reconstruction with proposed fusion trajectory using OS-SART and ASD-POCS

The second experiment consists of simulating the DRRs with the proposed fusion trajectory, and then to reconstruct the volume with OS-SART and ASD-POCS algorithms for both Jerry and Tom Phantoms. The experimental device can take a maximum of 720 projections for a full circular scan. Therefore, for this experiment, a total of 600 numbers of projections were taken from the proposed trajectory containing 375

Algorithm 1 The brute-force approach to optimize the initial parameter set for iterative reconstruction algorithms.

Data: $Parameters = \{Param_1, Param_2, \dots, Param_n\}, Projections,$
 $System\ matrix;$

Result: *Best fit value of initial parameter set;*

$Param_1 \leftarrow [A\ set\ of\ values\ of\ Param_1\ from\ an\ empirical\ range];$
 $Param_2 \leftarrow [A\ set\ of\ values\ of\ Param_2\ from\ an\ empirical\ range];$
 \vdots
 \vdots
 $Param_n \leftarrow [A\ set\ of\ values\ of\ Param_n\ from\ an\ empirical\ range];$
 $best\ score \leftarrow 0;$
for $i \leftarrow 1$ **to** n **do**
 freeze all the Param except Param_i;
 for $j \leftarrow$ **first element to last element of** $Param_i$ **do**
 $recon_image \leftarrow recon_algorithm(Data);$
 $current\ score \leftarrow SSIM \& \text{visual comparison between}$
 $recon_image\ and\ Groundtruth;$
 if $current\ score \geq best\ score$ **then**
 $best\ score \leftarrow current\ score;$
 else
 continue;
 end if
 end for
 Store the Param_i value for best score;
end for

projections from the shifted iso-center elliptical trajectory part and 225 projections from the VOI-guided part (as data augmentation) for maximum FOV volume reconstruction with the best possible image quality.

2.6.3. Experiment-3: reconstruction with proposed fusion trajectory using OS-SART and ASD-POCS in less projections set up

For the third part of the experiment, the second part was repeated with the same proposed fusion trajectory, however, with less number of projections. For this experiment, a total of 387 projections were taken containing 272 numbers of elliptical trajectory projections and 115 numbers of VOI-guided projections (as data augmentation) from the proposed fusion trajectory. This experiment is the refined version of experiment-2.6.2 with fewer projections to compare the result with the current limited circular trajectory scanning which uses 390 numbers of projections to reconstruct the volume.

2.7. Image quality assessment metrics

To perform the quantitative analysis of this study, The Peak Signal to Noise Ratio (PSNR) and Structural Similarity Index Measurements (SSIM) metrics were used for a heterogeneous image reconstruction quality analysis. Moreover, to cross-check the performance of PSNR and SSIM metrics, Root Mean Squared Error (RMSE) and the Universal Quality Index (UQI) scores were also calculated. The detailed mathematical explanation of these metrics has been explained in Section Appendix B, Appendix C, Appendix D, and Appendix E in the supplementary materials.

In all the experiments (2.6.1, 2.6.2, 2.6.3), these image quality measurement metrics have been applied in the prominent slices (mostly the middle slices where the organ is maximally visible) containing the VOIs and specifically at the VOIs to evaluate the quantitative accuracy of the reconstructed images. Furthermore, these metrics were applied to the 3D volume of the VOIs, and the whole reconstructed volume containing the VOIs.

3. Results

The optimized parameter set for both the OS-SART and ASD-POCS algorithm is listed in Table 1. The parameter labels are taken from TIGRE toolbox [38]. The toolbox is open source and available on GitHub.

Table 1

The optimized set of parameters of OS-SART and ASD-POCS algorithm for the proposed fusion trajectory.

OS-SART		ASD-POCS	
Parameter	Optimized Value	Parameter	Optimized Value
niter	20	niter	20
lambda	1	lambda	1
lambda_red	0.999	lambda_red	0.9999
BlockSize	17	TViter	15
OrderStrategy	'angular distance'	maxL2err	90%
		alpha	0.003
		Ratio	0.94

Table 2

Jerry: Quality measurement scores in different VOIs for different trajectories and corresponding reconstruction algorithms. Measurement is taken at the most prominent slices of the respected VOI along the z-axis. **In VOI:** measurement only inside each VOI region; **Whole Slice:** measurement in the whole slice related to each VOI.

Trajectory	VOI	PSNR		SSIM	
		In VOI	Whole slice	in VOI	Whole slice
Circular; OSSART	Sinus	28.5935	21.1281	0.9792	0.7520
	TMJ	37.4164	22.1337	0.9935	0.7789
	Upper Jaw	25.7520	22.7246	0.9542	0.8170
	Lower Jaw	27.4749	25.0951	0.9672	0.8597
	Chin	31.1546	27.0987	0.9834	0.9080
Fusion; OSSART	Sinus	36.1103	30.7057	0.9837	0.8686
	TMJ	43.2929	31.1151	0.9948	0.8672
	Upper Jaw	32.6921	30.8363	0.9598	0.8996
	Lower Jaw	33.4874	31.3960	0.9691	0.9084
	Chin	35.1400	32.1087	0.9816	0.9148
Fusion; ASDPOCS	Sinus	46.6413	40.1683	0.9962	0.9665
	TMJ	53.8594	41.5986	0.9991	0.9688
	Upper Jaw	45.0462	42.8082	0.9946	0.9832
	Lower Jaw	45.7294	43.3618	0.9962	0.9860
	Chin	49.0815	45.7565	0.9986	0.9912
Fusion; OSSART; Reduced projections	Sinus	35.1702	30.3879	0.9829	0.8696
	TMJ	43.2229	30.9937	0.9950	0.8743
	Upper Jaw	32.1469	30.4541	0.9609	0.9027
	Lower Jaw	33.0697	31.1404	0.9704	0.9140
	Chin	34.3213	31.6757	0.9831	0.9245
Fusion; ASDPOCS; Reduced projections	Sinus	41.1827	35.3547	0.9941	0.9499
	TMJ	49.0731	36.6566	0.9987	0.9573
	Upper Jaw	38.9620	36.9718	0.9923	0.9716
	Lower Jaw	39.5378	37.5330	0.9945	0.9765
	Chin	41.5771	38.5493	0.9977	0.9856

Fig. 7 and 8 exhibit the results for all three experiments performed in this study for the phantom Jerry and Tom respectively in different VOIs: sinus, TMJ, upper jaw, lower jaw, and chin. For the conventional limited angle circular scan, the FOV size is a circle of 11 cm diameter. However, the FOVs obtained from our proposed trajectory do not have any uniform or regular shape, although it was undoubtedly extended compared to the FOV obtained from the regular trajectory which is cylindrical in 3D space. Therefore, the FOV for the proposed trajectory was measured in the previously mentioned five VOI slices in both cranial breadth and naso-occipital length direction, and with our proposed trajectory the maximum FOV achieved in the cranial breadth and naso-occipital length is 15 cm and 19.5 cm respectively. Highlighting the significant FOV extension in both directions using our proposed novel trajectory.

Table 2 and 4 report the detailed quantitative quality measurement score for all the metrics mentioned in Section-2.7 for each of the five VOIs for both Jerry and Tom respectively. The middle or most prominent slices of the particular VOIs have been chosen to evaluate the extended FOV size for the lateral extended FOV. Section Appendix G in the sup-

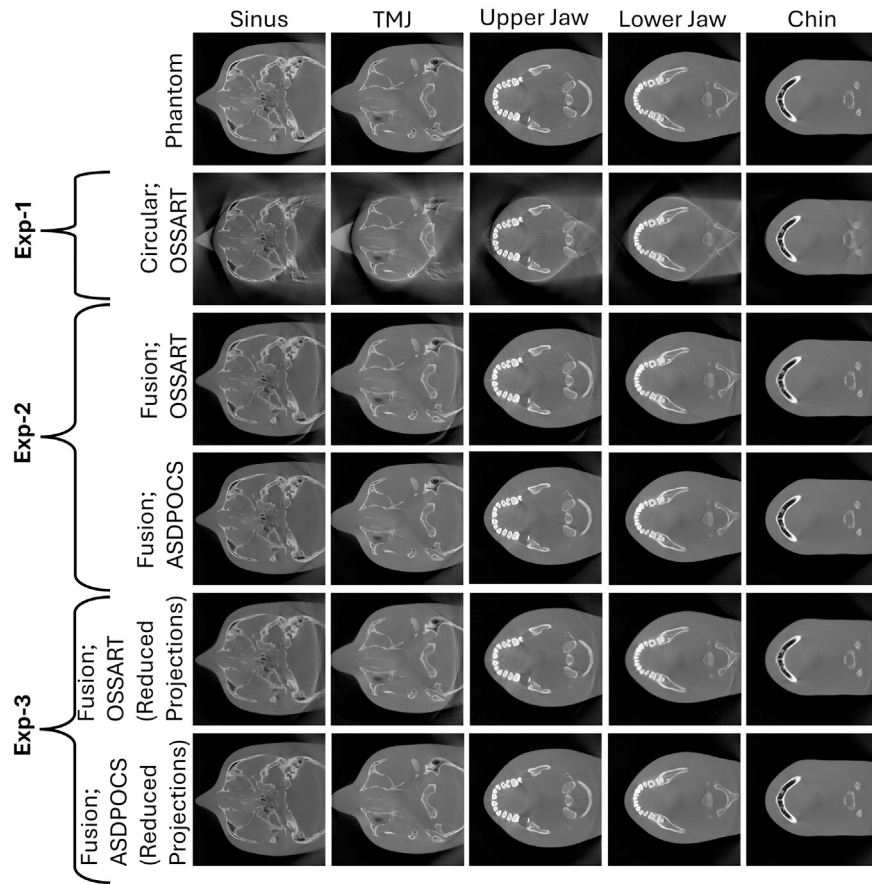


Fig. 7. All the reconstructed images for the **Jerry phantom** from experiment 1, 2, 3. Five different columns exhibit five different VOIs. **First row:** The digital phantom; **Second row:** The results from experiment 1; **Third and Fourth row:** The results from experiment 2; And, the **Fifth and Sixth row:** The results from experiment 3.

Table 3

Jerry: Quality measurement scores measured in the whole reconstructed volume for different trajectories and corresponding reconstruction algorithms. **In VOI:** measurement in the total VOI region (related to all five VOIs); **Whole Volume:** measurement in the whole reconstructed volume containing the VOI.

Trajectory	PSNR		SSIM	
	(in VOI)	(Whole Volume)	(in VOI)	(Whole Volume)
Circular;OSSART	31.8048	25.9080	0.9880	0.9373
Fusion;OSSART	38.2879	33.3871	0.9896	0.9444
Fusion;ASDPOCS	50.3861	45.0632	0.9986	0.9917
Fusion;OSSART; Reduced projections	37.7906	33.1499	0.9899	0.9491
Fusion;ASDPOCS; Reduced projections	44.2543	38.6958	0.9979	0.9885

plementary material exhibits the detailed FOV measurement for all the VOIs.

Table 3 and 5 show the quantitative measurement scores of the reconstructed volume (3D). The measurement was taken both in only combined indicated VOI region i.e., all combined five VOIs (In VOI) and in the whole reconstructed region (Whole Volume).

Image quality metrics were always calculated in both inside the VOI region (In VOI) and the entire region (Whole Slice). In all experiments, higher performance was observed in the quantitative image quality metrics for the fusion trajectory compared to the circular trajectory, emphasizing the improved image quality by our proposed trajectory.

For the reduced projection version of the proposed trajectory, the quality measurement metric scores decrease slightly, however, still out-

performs the limited angle circular trajectory in both metric scores and FOV size.

4. Discussion and conclusion

In this study, a novel source-detector trajectory was developed targeting the FOV extension preserving the acceptable image quality in certain VOIs. The proposed trajectory uses the concept of maximum projection data acquisition from Tuy's condition and an off-axis scanning method. The proposed trajectory exhibited excellent results in FOV expansion with adequate image reconstruction quality.

The proposed fusion trajectory was designed based on the device geometry and the extended headspace discussed in Sections 2.1 and 2.3. Consequently, this trajectory can be applied to any head phantom that fits within the extended headspace. Fig. 7 shows that, for the small phantom-Jerry, the upper jaw, lower jaw, and chin are well-reconstructed, however, sinus and TMJ bones were partially reconstructed at the FOV boundary for the limited angle circular trajectory. With the proposed trajectory, All the VOIs; sinus, TMJ, upper jaw, lower jaw, and chin are well-reconstructed. Moreover, the whole Jerry phantom volume is nearly well-reconstructed in the VOI-containing regions. On the other hand, for the ideal-sized phantom-Tom, Fig. 8 shows that only the upper jaw, lower jaw, and chin are well-reconstructed, the sinus is partially reconstructed at the FOV boundary, and TMJ bones are completely out of the reconstructed FOV boundary for the limited angle circular scan. However, with the proposed trajectory all the VOIs (sinus, TMJ, upper jaw, lower jaw, and chin) are well-reconstructed, and the FOV almost has reconstructed nearly 90% of the target volume of the VOI-containing region. Moreover, the refined fewer projection setup of the proposed trajectory also can reconstruct the extended volume. The

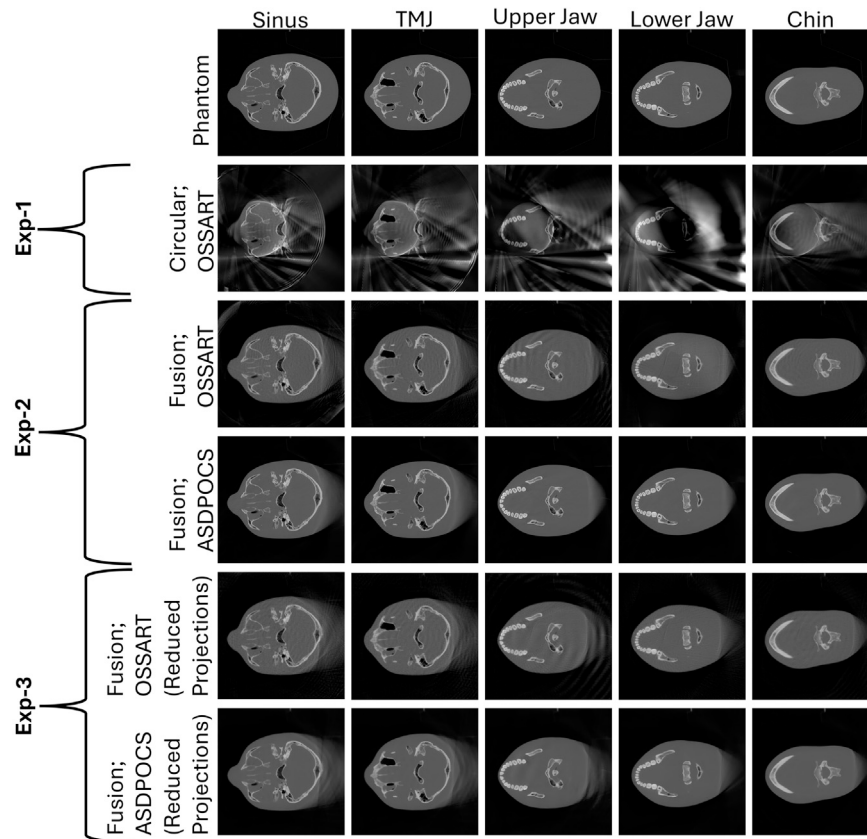


Fig. 8. All the reconstructed images for the **Tom phantom** from experiment 1, 2, 3. Five different columns exhibit five different VOIs. **First row:** The digital phantom; **Second row:** The results from experiment 1; **Third and Fourth row:** The results from experiment 2; And, the **Fifth and Sixth row:** The results from experiment 3.

Table 4

Tom: Quality measurement scores in different VOIs for different trajectories and corresponding reconstruction algorithms. Measurement is taken at the most prominent slices of the respected VOI along the z-axis. **In VOI:** measurement only inside each VOI region; **Whole Slice:** measurement in the whole slice related to each VOI.

Trajectory	VOI	PSNR		SSIM	
		(in VOI)	(Whole slice)	(in VOI)	(Whole slice)
Circular; OSSART	Sinus	24.8817	15.5644	0.9567	0.6810
	TMJ	31.8350	15.7035	0.9892	0.6824
	Upper Jaw	20.8897	15.8851	0.9354	0.7131
	Lower Jaw	21.4372	16.3203	0.9432	0.7202
	Chin	23.4239	17.2051	0.9630	0.7802
Fusion; OSSART	Sinus	38.7543	29.7584	0.9912	0.9164
	TMJ	45.7258	30.3802	0.9985	0.9158
	Upper Jaw	34.9699	31.0197	0.9876	0.9233
	Lower Jaw	35.5231	31.7132	0.9908	0.9303
	Chin	39.3963	33.9972	0.9960	0.9568
Fusion; ASDPOCS	Sinus	47.8494	35.2701	0.9976	0.9599
	TMJ	53.1047	34.8657	0.9997	0.9592
	Upper Jaw	45.2907	37.6667	0.9977	0.9641
	Lower Jaw	45.8654	39.1038	0.9989	0.9703
	Chin	48.4115	40.2593	0.9993	0.9770
Fusion; OSSART; Reduced projections	Sinus	40.3104	31.2519	0.9909	0.9085
	TMJ	47.1235	30.7181	0.9984	0.9047
	Upper Jaw	36.5774	31.3960	0.9885	0.9083
	Lower Jaw	37.1682	33.0961	0.9909	0.9284
	Chin	42.7239	36.6161	0.9963	0.9524
Fusion; ASDPOCS; Reduced projections	Sinus	40.2724	31.3741	0.9919	0.9195
	TMJ	46.5171	31.1403	0.9980	0.9240
	Upper Jaw	37.3895	31.7105	0.9908	0.9313
	Lower Jaw	38.1525	33.8002	0.9924	0.9488
	Chin	42.7103	36.5687	0.9966	0.9621

Table 5

Tom: Quality measurement scores measured in the whole reconstructed volume for different trajectories and corresponding reconstruction algorithms. **In VOI:** measurement in the total VOI region (related to all five VOIs); **Whole Volume:** measurement in the whole reconstructed volume containing the VOI.

Trajectory	PSNR		SSIM	
	(in VOI)	(Whole Volume)	(in VOI)	(Whole Volume)
Circular;OSSART	27.8173	21.3781	0.9826	0.9075
Fusion;OSSART	42.4092	36.7414	0.9978	0.9805
Fusion;ASDPOCS	51.9708	42.8008	0.9996	0.9910
Fusion;OSSART; Reduced projections	44.2972	37.5982	0.9980	0.9777
Fusion;ASDPOCS; Reduced projections	44.6559	37.6372	0.9981	0.9819

detailed FOV measurement is provided in Section Appendix G in the supplementary materials.

The quality measurement scores from Table 2, 3, 4 and 5 show that all the quality measurement scores are higher for the proposed trajectory. Although for the refined less projection setup of the trajectory, the scores drop a little bit, however, still it outperforms the limited circular scan reconstruction result. In addition, the quantitative results prove that the ASD-POCS algorithm outperforms OS-SART in all experiments. The detailed score and their inter-trajectory relations are explained in Figure H.2 and Figure H.3 provided in the supplementary materials.

The primary goals of this study were fulfilled, as the proposed trajectory can reconstruct an extended FOV than the standard limited angle circular scan trajectory. Although for the proposed trajectory, the gantry needs to rotate twice, no complex hardware modification is needed. Moreover, excellent image quality performance was observed with the trajectory for a reduced projection number compared to the standard circular trajectory which reduces the necessity of a high projection number,

thus reducing the radiation dose. Our study is the first demonstration of the lateral FOV extension in dental CBCT imaging. In the aforementioned non-stationary off-axis iso-centric elliptical trajectory [34], the FOV was extended with certain source-detector movement constraints. Our proposed trajectory compensates for the existing movement constraints and achieves a larger FOV than the standard circular scan. Considering that our device is the small dental CBCT unit and comparing the device size used in this study [34], the achieved FOV based on our method is more significant. Moreover, a complimentary circular scan approach [35] requires two different circular scans which increase the radiation dosage. Although our trajectory requires two rotations, it needs the same number of projections as the standard circular scan which achieves a larger FOV without increasing the radiation dosage. In the rotating detector [36] and dynamic detector offset approach [20], complex mechanical modification and tuning are required during the scanning. However, our proposed trajectory exhibits better projection acquisition without any complex mechanical modification during the scan and using the same radiation dose as the standard circular trajectory. In addition, our proposed trajectory exhibits a better image quality measurement score than the standard circular trajectory. A comprehensive comparison of image quality metrics for the reconstructed images, derived from all the used trajectories and reconstruction algorithms, is provided in Section Appendix H of the supplementary materials.

We acknowledge that the scanning time for the proposed trajectory may be higher than the regular trajectory scanning time. This scanning time is device-dependent and varies considering the build-equipment of the device. This extended scanning may also lead to motion artifacts in case the patient moves during the scanning process. To minimize the patient's movement the device has a biting mechanism where the patient will bite during the scanning. Therefore, it should reduce the artifact mechanically. Moreover, post-scanning algorithmic processes such as motion compensation and image registration-based approaches may be required for further motion artifact reduction. We also acknowledge some limitations of this study. The experiments were done based on simulations and a verification of all experiments using real-world data is required which is a future perspective of this study. In addition, for the mechanical implementation, minor upgradation may need based on the machine's geometry and its specific mechanical movement possibilities.

In summary, the trajectory proposed in our technical study shows strong potential for significantly expanding the field of view (FOV) and enhancing image quality, as indicated by improved metric scores. Additionally, both the FOV and image quality metrics suggest that this approach could reduce radiation exposure compared to the standard circular trajectory of smaller dental CBCT devices. Although not yet tested in clinical cases, the strong mathematical background of the study supports that the proposed fusion trajectory may ultimately reduce the need for larger CBCT devices for numerous clinical applications, offering a more cost-effective solution that supports precise diagnosis and tailored treatment plans for patients in future.

CRediT authorship contribution statement

S M Ragib Shahriar Islam: Writing – review & editing, Writing – original draft, Visualization, Validation, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. **Andri Biguri:** Writing – review & editing, Validation, Supervision, Software, Methodology, Investigation, Formal analysis, Conceptualization. **Claudio Landi:** Resources, Project administration, Funding acquisition, Conceptualization. **Giovanni Di Domenico:** Writing – review & editing, Validation, Supervision, Methodology, Investigation, Formal analysis, Conceptualization. **Benedikt Schneider:** Validation, Supervision, Investigation. **Pascal Grün:** Validation, Supervision. **Cristina Sarti:** Resources, Investigation, Conceptualization. **Ramona Woitek:** Supervision, Conceptualization. **Andrea Delmiglio:** Validation, Conceptualization. **Carola Bibiane Schönlieb:** Writing – review & editing, Validation. **Dritan Turhani:** Validation. **Gernot Kronreif:** Supervision, Resources, Project

administration, Funding acquisition. **Wolfgang Birkfellner:** Writing – review & editing, Supervision, Conceptualization. **Sepideh Hatamikia:** Writing – review & editing, Writing – original draft, Supervision, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis, Conceptualization.

Declaration of competing interest

The authors have declared no conflict of interest.

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Appendix. Supplementary material

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.csbj.2024.11.010>.

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