

**Table J.2.** Computational complexity of log-determinant estimation methods. We count one FLOP as one fused multiply-add (FMA) operation.

Method	Complexity	Description
MEMDET	$\frac{1}{6}m^3 - \frac{1}{4}m^2 + \frac{1}{12}m$	$m$ : Full matrix size, $m = nd$
FLODANCE	$\frac{1}{6}m_s^3 - \frac{1}{4}m_s^2 + \frac{1}{12}m_s + (q + 3)^2n_s$	$n_s$ : Number of sampled data points from $n$ $m_s$ : Sampled matrix size, $m_s = n_s d$ $q$ : Truncation order of Laurent series
SLQ	$(m^2l + ml^2)s$	$l$ : Lanczos iterations (Krylov subspace size) $s$ : Number of Monte Carlo samples
Pseudo NTK	$\frac{1}{6} \left(\frac{m}{d}\right)^3 - \frac{1}{4} \left(\frac{m}{d}\right)^2 + \frac{1}{12} \left(\frac{m}{d}\right) + m^2$	$m$ : Full matrix size $d$ : Number of model outputs
Block Diagonal	$\frac{1}{6}md^2 - \frac{1}{4}md + \frac{1}{12}m$	$m$ : Full matrix size $d$ : Number of model outputs