

Table 1. Comparison of stochastic Lanczos quadrature (SLQ, with degree l , s Monte Carlo samples, and full re-orthogonalization), MEMDET, and FLODANCE on a dense $500,000 \times 500,000$ NTK matrix for a ResNet50 model trained on CIFAR-10 with 50,000 datapoints. MEMDET computes the exact log-determinant and serves as the benchmark, with relative errors of other methods measured against it. Costs and wall time are based on an NVIDIA H100 GPU (\$2/hour) and an 8-core 3.6GHz CPU (\$0.2/hour) using Amazon pricing and include NTK formation from a pre-trained network.

| Method | | TFLOPs | Rel. Error | Est. Cost | Wall Time |
|----------|---------------------|-------------|---------------|--------------|--------------|
| Name | Settings | | | | |
| SLQ | $l = 100, s = 104$ | 5203 | 55% | \$83 | 1.8 days |
| MEMDET | LDL, $n_b = 32$ | 41,667 | 0% | \$364 | 8.8 days |
| FLODANCE | $n_s = 500, q = 0$ | 0.04 | 4% | \$0.04 | 1 min |
| FLODANCE | $n_s = 5000, q = 4$ | 41.7 | 0.02% | \$4 | 1.5 hr |