

7.  $(A \uparrow B)$  is equivalent to  $(\overline{A \cdot B})$  (NAND)  
 $(A \downarrow B)$  is equivalent to  $(\overline{A + B})$  (NOR)

Given the expression:

$$(A \uparrow A) \downarrow (B \uparrow B)$$

$$(A \uparrow A) = \overline{A \cdot A} = \bar{A}$$

$$(B \uparrow B) = \overline{B \cdot B} = \bar{B}$$

$$((A \uparrow A) \downarrow (B \uparrow B)) :$$

$$\overline{\bar{A} \cdot \bar{B}} = A + B \quad \rightarrow \text{De Morgan's law}$$

$$(A \uparrow A) \downarrow (B \uparrow B) = A + B$$

$$(A \downarrow A) \uparrow (B \downarrow B) :$$

$$(\bar{A} \downarrow \bar{A}) = \overline{\bar{A} + \bar{A}} = A$$

$$(\bar{B} \downarrow \bar{B}) = \overline{\bar{B} + \bar{B}} = B$$

$$(\bar{A} \downarrow \bar{A}) \uparrow (\bar{B} \downarrow \bar{B}) =$$

$$\overline{\bar{A} + \bar{B}} = A \cdot B$$

De Morgan's law

Therefore,

$$(A \uparrow A) \downarrow (B \uparrow B) = (\bar{A} \downarrow \bar{A}) \uparrow (\bar{B} \downarrow \bar{B})$$