

9. Analyze $(B \Rightarrow \bar{A})$

$B \Rightarrow \bar{A}$ is equivalent to $\bar{B} + \bar{A}$ being true.

$$\text{So, } \bar{B} + \bar{A} = T$$

Now, Simplify the expression:

$$\underbrace{(A + \bar{B})(\bar{A} + \bar{A}B)}_{\text{Term 1}} + \underbrace{\bar{A}B(A + B)}_{\text{Term 2}}$$

Term 1:

$$(A + \bar{B})(\bar{A} + \bar{A}B) = A \cdot \bar{A} + A \cdot \bar{A}B + \bar{B} \cdot \bar{A} + \bar{B} \cdot A\bar{B}$$

$$A \cdot \bar{A} = F \quad (\because A \text{ and } \bar{A} \text{ cannot be true})$$

$$A \cdot \bar{A}B = \bar{A}B$$

$$\bar{B} \cdot \bar{A} = \bar{A}\bar{B}$$

$$\bar{B} \cdot A\bar{B} = F \quad (\because \bar{B} \cdot B \text{ is false})$$

So,

$$\bar{A}B + \bar{A}\bar{B} = \bar{A}(A + \bar{A}) = \bar{A} \cdot 1 = \bar{A}$$

Term 2:

$$\bar{A}B(A + B)$$

$$\bar{A}B(A + B) = \bar{A}BA + \bar{A}BB$$

$$\bar{A}BA = \text{false}$$

$$\bar{A}B \cdot B = \bar{A}B$$

$$\text{So, } \bar{A}B \Rightarrow B \Rightarrow \bar{A}$$

$\therefore \bar{B} + \bar{A} = \text{True}$ shows that the expression $\bar{B} + \bar{A}B$ is always true.

Thus, $B \Rightarrow \bar{A}$ is true, therefore

$(A + \bar{B})(\bar{A} + \bar{A}B) + \bar{A}B(A + B)$ is also true & both are equivalent.