

Quick Intro to Sensitivity, Specificity, PPV, and NPV

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Screening Tests: Validity – Result Combinations

- 4 possible combinations of **truth (gold standard)** (diseased/nondiseased) and **test results** (positive/negative)
 - **True positives (a)**: screen positive + have disease (**GOOD!**)
 - **False positives (b)**: screen positive + don't have disease (**BAD!**)
 - **False negatives (c)**: screen negative + have disease (**BAD!**)
 - **True negatives (d)**: screen negative + don't have disease (**GOOD!**)

Condition According to Gold Standard					
		Present	Absent	Total	
Test result	Positive	a = True positives	b = False positives	a + b	Predictive value (+) $\frac{a}{a + b}$
	Negative	c = False negatives	d = True negatives	c + d	Predictive value (-) $\frac{d}{c + d}$
	Total	a + c	b + d	Grand total a + b + c + d	
		Sensitivity $\frac{a}{a + c}$	Specificity $\frac{d}{b + d}$		

Screening Tests: Validity – Metrics

- 4 numbers important to a test's validity:

- Sensitivity (Se)

- Specificity (Sp)

- Positive Predictive Value (PPV) or Predictive Value (+)

- Negative Predictive Value (NPV) or Predictive Value (-)

- Higher is better for all numbers!

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Screening Tests: Validity – Sensitivity and Specificity

- **Sensitivity (Se):** the **ability** of the test to **correctly identify** individuals who actually **have the disease**

– Math: $\frac{a}{a+c} = \frac{\text{True Positives}}{\text{Total Who Have the Disease}}$

- Ranges 0-100%

- English: “What percent of sick people did the test catch?”

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Screening Tests: Validity – Sensitivity and Specificity

- **Specificity (Sp):** The ability of the test to identify **non-diseased** individuals who actually do not have the disease

– Math: $\frac{d}{b+d} = \frac{\text{True Negatives}}{\text{Total Who Don't Have the Disease}}$

- Ranges 0-100%

- English: “What percent of non-sick people did the test correctly screen out?”

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		Present	Absent	Total	
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Screening Tests: Validity – Sensitivity and Specificity

- Both Se & Sp important, but which is more important varies from test to test
 - Bad **Sensitivity**: lots of **false negatives**
 - Especially bad when the costs of missing a case are high (e.g. you're fine, go home)
 - Bad **Specificity**: lots of **false positives**
 - Especially bad when the costs of misidentifying someone as + are high (e.g. you're immune when you're not)
- **Se & Sp often a tradeoff** – improving one may require worsening the other. Do you need to be able to ID every case vs. are false positives extremely bad?

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Screening Tests: Validity – Sensitivity and Specificity

- Example:
 - 1,000 people
 - 100 (10%) have disease

<u>Test Results</u>	<u>Gold Standard Result / “True” Disease Status</u>		<u>Total</u>
	Diseased	Not Diseased	
Positive	a = 80	b = 100	180
Negative	c = 20	d = 800	820
<u>Total</u>	a + c = 100	b + d = 900	1,000

Screening Tests: Validity – Sensitivity and Specificity

- **Sensitivity:** percent of people with disease who test positive
 - 100 have disease, 80 of them test positive
 - **Sensitivity** = $80/100 = 80\%$

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Screening Tests: Validity – Sensitivity and Specificity

- **Specificity:** percent of people *without* disease who test negative
 - 900 don't have disease, 800 of them test negative
 - **Specificity** = $800/900 = 89\%$

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Screening Tests: Validity – Metrics

- Imagine you go into a doctor's office and get a blood test for HIV
 - **Sensitivity**: If you have HIV, how likely is the test to be positive?
 - **Specificity**: If you don't have HIV, how likely is the test to be negative?
 - How useful are these questions?
 - Why would we do the test if we already knew you were or weren't sick?
- Flip it around to get more relevant questions:
 - If you test positive, how likely is it you have HIV? – This is **PPV**
 - If you test negative, how likely is it you *don't* have HIV? – This is **NPV**

Screening Tests: Validity – Metrics

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- Higher is better for all numbers!

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Screening Tests: Validity – PPV and NPV

- **PPV or PV+:** proportion of patients who test positive who actually have the disease

– Math: $\frac{a}{a+b} = \frac{\text{True Positives}}{\text{Total Who Test Positive}}$

- Ranges 0-100%

– English: “If you test positive, how likely is it that you’re really sick (or immune in the case of an antibody test)?”

Condition According to Gold Standard					
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Screening Tests: Validity – PPV and NPV

- **NPV or PV-:** proportion of patients who test negative who do not have the disease
 - Math: $\frac{d}{c+d} = \frac{\text{True Negatives}}{\text{Total Who Test Negative}}$
 - Ranges 0-100%
 - English: “If you test negative, how likely is it that you’re really not sick (or not immune in the case of an antibody test)?”

Condition According to Gold Standard					
		Present	Absent	Total	
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Screening Tests: Validity – PPV and NPV

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<u>Total</u>	100	900	1,000

Screening Tests: Validity – PPV and NPV

- **PPV**: probability of a positive test having disease
 - 180 test positive, 80 of them have disease
 - **PPV** = $80/180 = 44\%$ (remember **sensitivity** was much higher at 80%)

<u>Test Results</u>	<u>Gold Standard Result / “True” Disease Status</u>		<u>Total</u>
	Diseased	Not Diseased	
Positive	a = 80	b = 100	a + b = 180
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<u>Total</u>	100	900	1,000

Screening Tests: Validity – PPV and NPV

- **NPV**: probability of a negative test *not* having disease
 - 820 test negative, 800 of them don't have disease
 - **NPV** = $800/820 = 98\%$ (remember **specificity** was also high at 89%)

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	Diseased	Not Diseased	
Positive	a = 80	b = 100	a + b = 180
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<u>Total</u>	100	900	1,000

Screening Tests: Validity – PPV and NPV

- Example: let's summarize...

– **Se** = 80% **Sp** = 89%
– **PPV** = 44% **NPV** = 98%

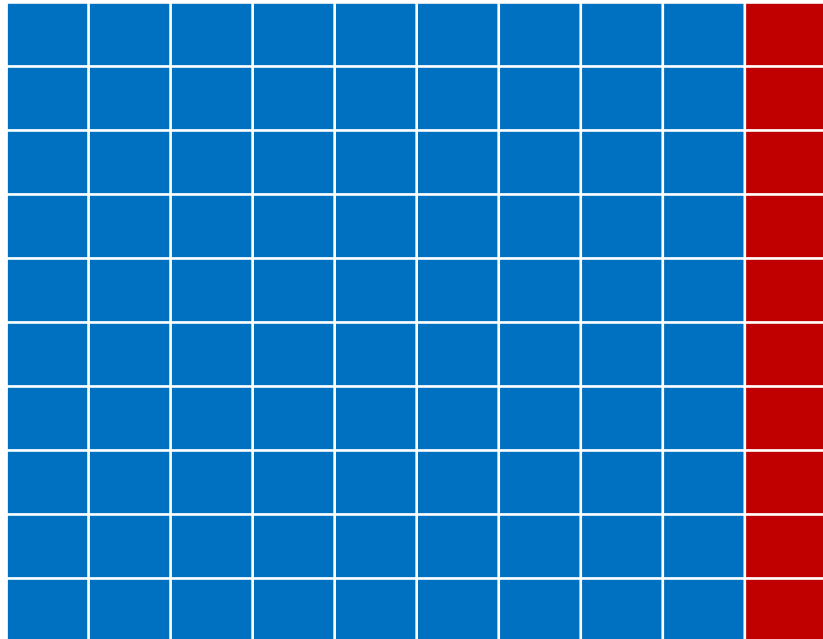
Common pattern for rare diseases: **test is right most of the time** (high Se & Sp), but a **single positive test doesn't mean that much** (low PPV)

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Screening Tests: PPV/NPV and Prevalence

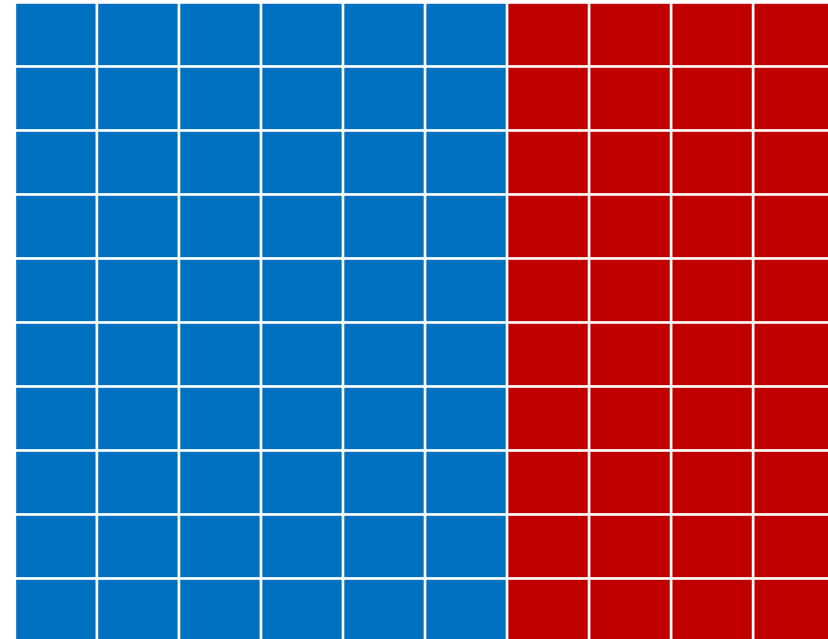
- **Sensitivity and Specificity**: **fixed characteristic of test**; the same for every population tested
- **PPV and NPV**: different for every population tested
 - Depends on **disease prevalence!**
- Consider **two groups** of 100 people with **different prevalence of diabetes**

Prevalence = 10%



**Red =
diabetes**

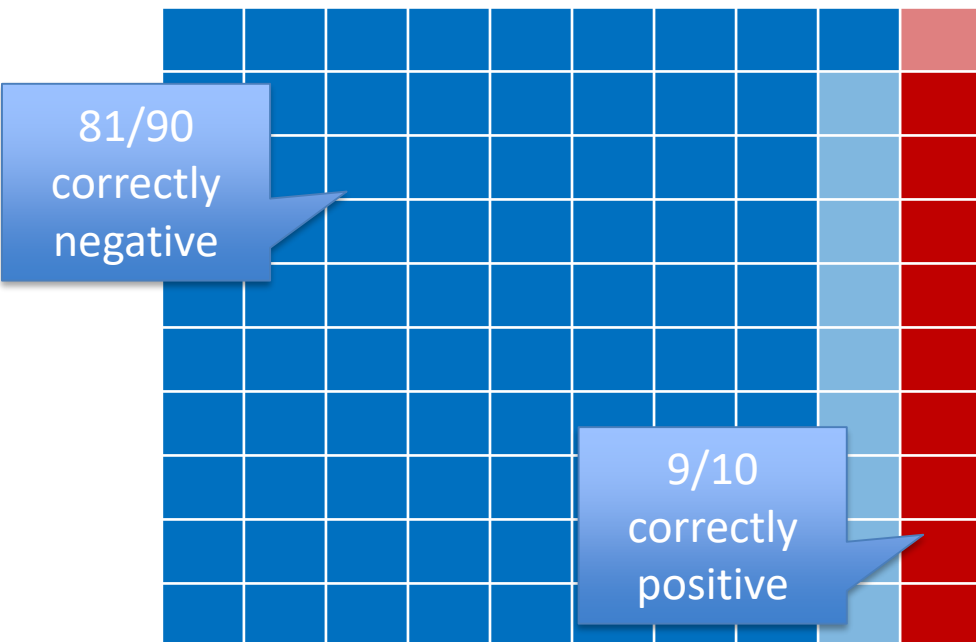
Prevalence = 40%



Screening Tests: PPV/NPV and Prevalence

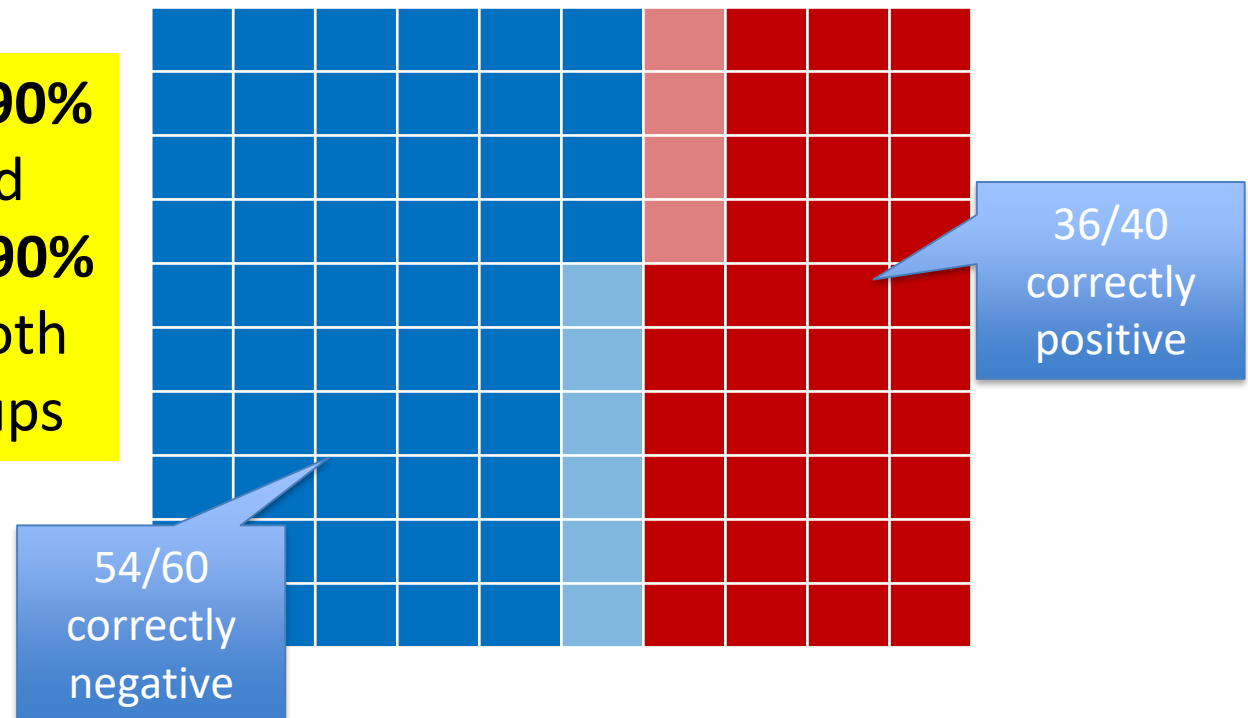
- Say we have a test that correctly identifies diabetics 90% of the time ($Se = 90\%$) and non-diabetics also 90% of the time ($Sp = 90\%$)
 - Correct identifications are brightly-colored

Prevalence = 10%



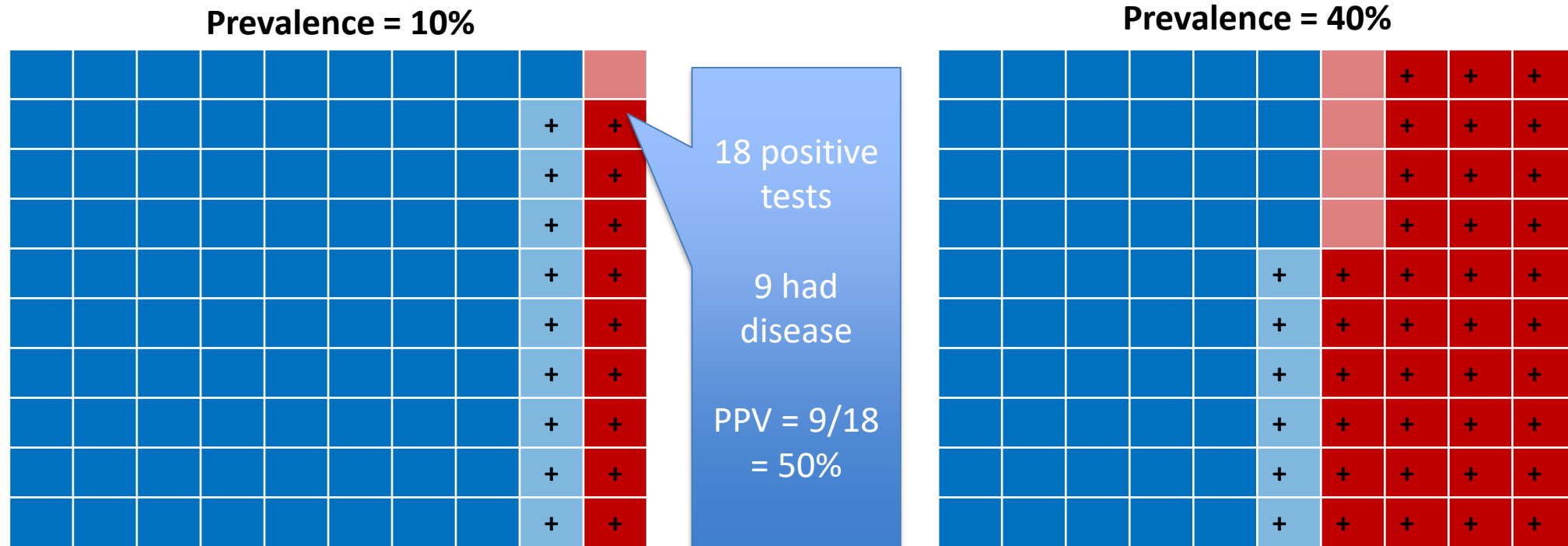
Se = 90%
and
Sp = 90%
in both
groups

Prevalence = 40%



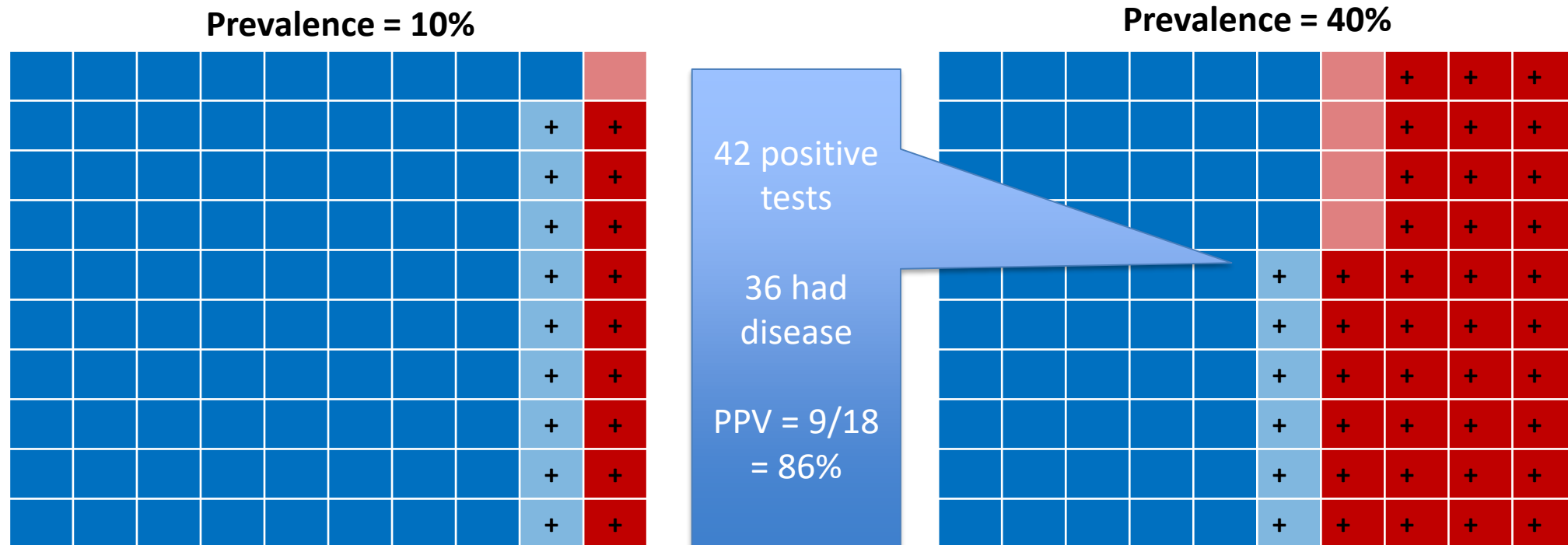
Screening Tests: PPV/NPV and Prevalence

- What is the PPV in both groups?
 - “+” = tested positive, regardless of true status



Screening Tests: PPV/NPV and Prevalence

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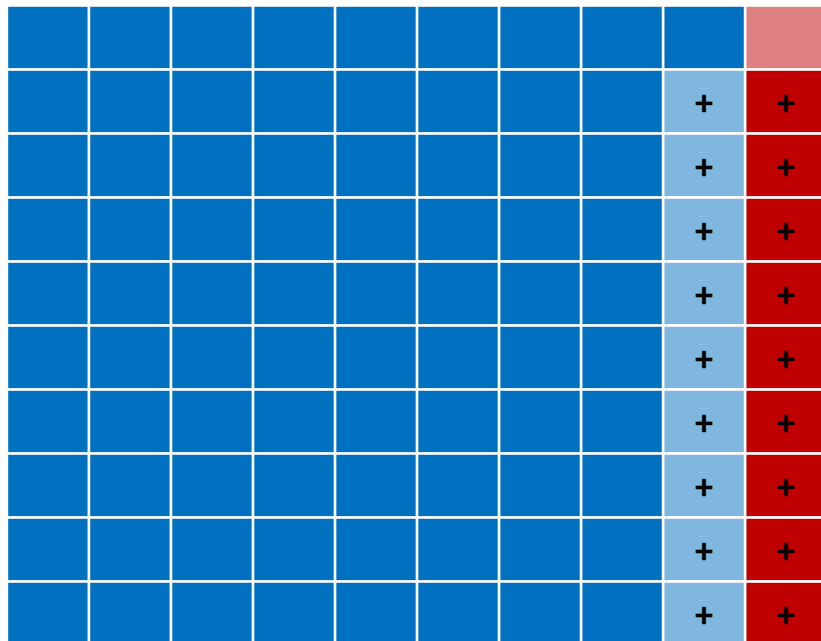


Screening Tests: PPV/NPV and Prevalence

- What is the PPV in both groups?
 - Same test: Se = 90%, Sp = 90%

PPV = 50%

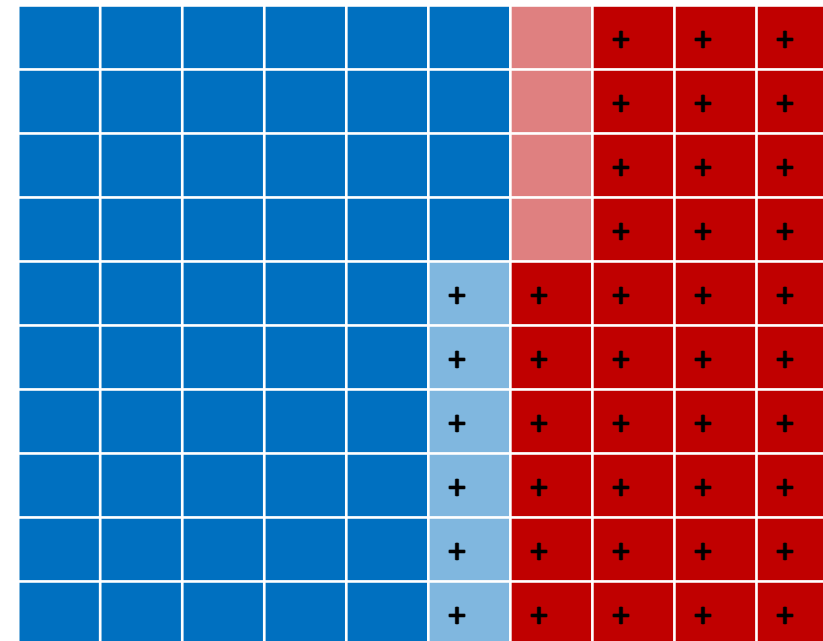
Prevalence = 10%



Regardless of your test result you're just more likely to have diabetes in the higher-risk group...period!

PPV = 86%

Prevalence = 40%



Screening Tests: PPV/NPV and Prevalence

- Here's a more mathematical example

EXAMPLE: SENSITIVITY = 99%, SPECIFICITY = 95%					
Disease Prevalence	Test Results	Sick	Not Sick	Totals	Positive Predictive Value
1%	+	99	495	594	$\frac{99}{594} = 17\%$
	-	1	9,405	9,406	
	Totals	100	9,900	10,000	

Screening Tests: PPV/NPV and Prevalence

- Here's a more mathematical example

EXAMPLE: SENSITIVITY = 99%, SPECIFICITY = 95%					
Disease Prevalence	Test Results	Sick	Not Sick	Totals	Positive Predictive Value
1%	+	99	495	594	$\frac{99}{594} = 17\%$
	-	1	9,405	9,406	
	Totals	100	9,900	10,000	
5%	+	495	475	970	$\frac{495}{970} = 51\%$
	-	5	9,025	9,030	
	Totals	500	9,500	10,000	

Screening Tests: PPV/NPV and Prevalence

- Similar but opposite relationship for prevalence and NPV
- **Higher prevalence → higher PPV, lower NPV**
 - Screening programs are “**more efficient**” (higher % of positive tests are diseased) when directed to **high-risk target population**
 - Does **NOT** mean screening programs should *only* ever be targeted to high-risk groups
 - Is “ruling out” or “ruling in” a disease more important?