

## ## Graph isomorphism ##

Two graphs are isomorphic if they are identical in every way except for vertex labels

Definition: Isomorphic graphs

Let  $G = (V, E)$  and  $G' = (V', E')$ .  $G$  and  $G'$  are isomorphic if there is a bijection  $f: V \rightarrow V'$  such that for every pair of vertices  $x, y \in V$ ,  $\{x, y\} \in E$  if and only if  $\{f(x), f(y)\} \in E'$ .

The function  $f$  is called an isomorphism from  $G$  to  $G'$

Graph properties preserved under isomorphism:

- vertex degree -  $\deg(v)$  in  $G = \deg(f(v))$  in  $G'$
- degree sequence - list of all vertex degrees in non-increasing order
- total degree
- graph order (i.e. total # of vertices)  $|V|$  in  $G = |V'|$  in  $G'$
- graph size (i.e. total # of edges)  $|E|$  in  $G = |E'|$  in  $G'$
- connectivity