

### Homework 5:Dynamic Programming

Due at the start of class Thu, April 12. You are allowed to do this homework individually, or in groups of two. Each group will return a single homework and will get the same grade. But a group is NOT allowed to share anything written with another group. Remember that each group member has to fully participate in the solution.

**Problem 1.** Use the matrix multiplication algorithm to find the optimal way to compute  $A_1 A_2 A_3 A_4$  where  $p=[10,10,20,30,40]$ .

**Problem 2.** Consider the following variation of the interval scheduling problem (we discussed in class). The input is a set of  $n$  activity requests  $R = \{1, 2, \dots, n\}$ , where the  $i$ -th request starts at time  $s_i$  and ends at time  $f_i$ . Each request is associated with a numeric value  $v_i$ . Give a DP solution to find a set of non-interfering requests such that the sum of their values is maximum.

**Problem 3.** Consider a test with  $n$  questions, numbered from 1 to  $n$ . Question number  $i$  has an integer point value,  $v_i > 0$ , and requires  $m_i$  minutes to solve. Suppose further that no partial credit is awarded. Given  $v_i, 1 \leq i \leq n$  and  $m_i, 1 \leq i \leq n$ , and an integer  $V$ , provide a dynamic programming formulation that computes the minimum number of minutes required to earn  $V$  points on the test. Clearly state the dynamic programming formulation, provide a brief explanation of it and explain how you compute the table by giving a small example.