

A Zoo of Computational Models

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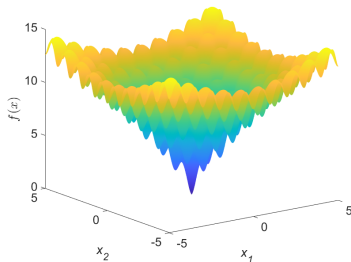
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The codes for the tutorials are available on GitHub

<https://github.com/americocunhajr/UQ-CSE>



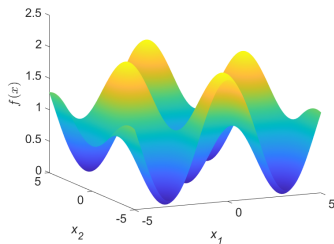
Ackley function



$$f(x) = -a \exp \left(-b \sqrt{\frac{1}{2} \sum_{i=1}^2 x_i^2} \right) - \exp \left(\frac{1}{2} \sum_{i=1}^2 \cos(2\pi x_i) \right) + a + \exp(1)$$

* Tutorial elaborated by Marcos Vinícius Issa.

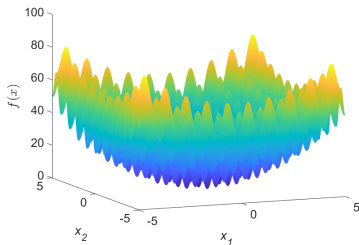
Griewank function



$$f(x) = \sum_{i=1}^2 \frac{x_i^2}{4000} - \prod_{i=1}^2 \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$$

* Tutorial elaborated by Marcos Vinícius Issa.

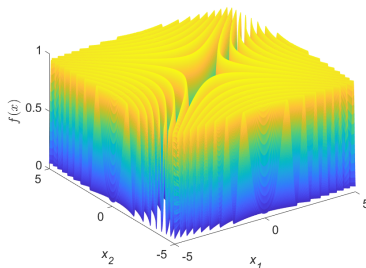
Rastrigin function



$$f(x) = 20 + \sum_{i=1}^2 \left(x_i^2 - 10 \cos(2\pi x_i) \right)$$

* Tutorial elaborated by Marcos Vinícius Issa.

Schaffer function

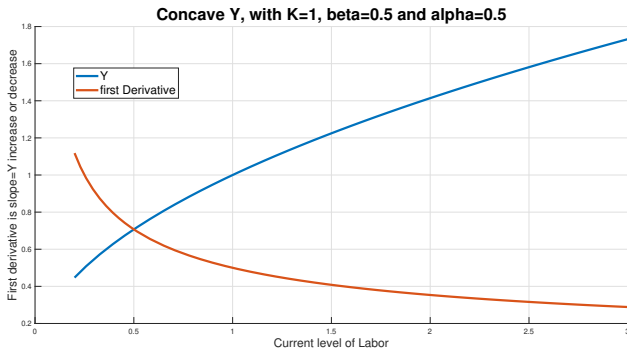


$$f(x) = 0.5 + \frac{\sin^2(x_1^2 - x_2^2) - 0.5}{(1 + 0.001(x_1^2 - x_2^2))^2}$$

* Tutorial elaborated by Marcos Vinícius Issa.

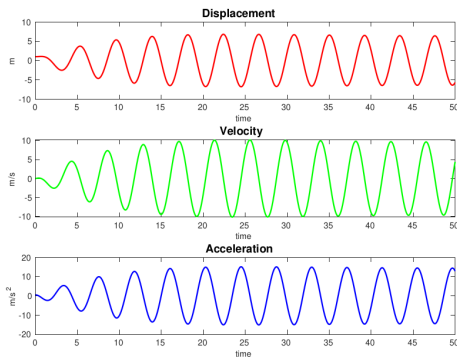
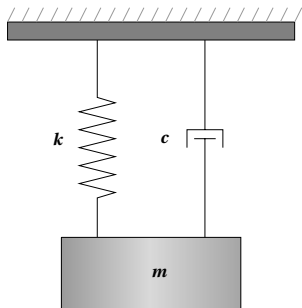
Cobb–Douglas production function

$$Y = L^{\beta} K^{\alpha}$$



* Tutorial elaborated by Bruna Pavlack.

Harmonic oscillator

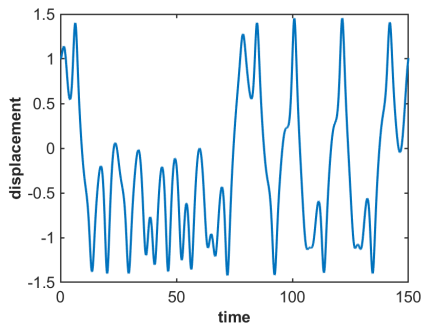
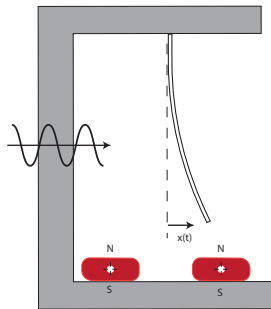


$$m\ddot{x} + c\dot{x} + kx = f \cos(\omega t)$$

+ initial conditions

* Tutorial elaborated by Diego Matos.

Duffing Oscillator

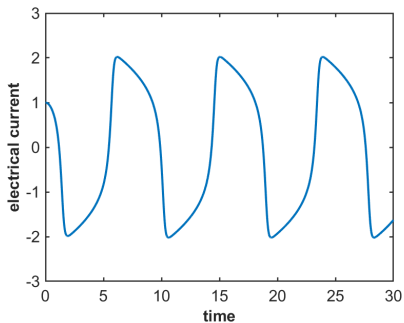
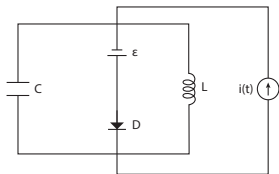


$$\ddot{x} + \delta \dot{x} + \alpha x + \beta x^3 = \gamma \cos(\Omega t)$$

+ initial conditions

* Tutorial elaborated by Joao Pedro Norenberg.

Van der Pol Oscillator



$$\ddot{x} - \mu(1 - x^2)\dot{x} + x = 0$$

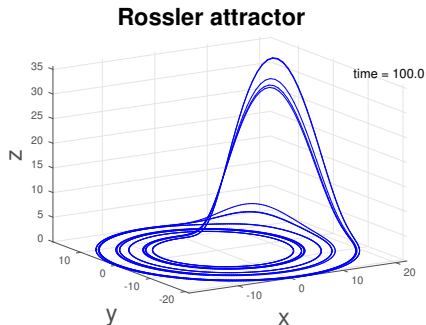
+ initial conditions

* Tutorial elaborated by Joao Pedro Norenberg.

Rössler system

$$\begin{aligned}\dot{x} &= -y - z \\ \dot{y} &= x + \alpha y \\ \dot{z} &= \beta + z(x - \gamma)\end{aligned}$$

+ initial conditions



* Tutorial elaborated by Diego Matos.

Shear Building

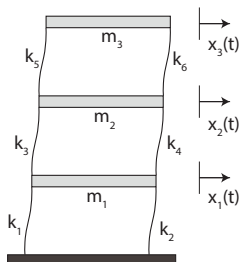
Generalized eigenvalue problem:

$$[K] \mathbf{u}_n = \omega_n^2 [M] \mathbf{u}_n$$

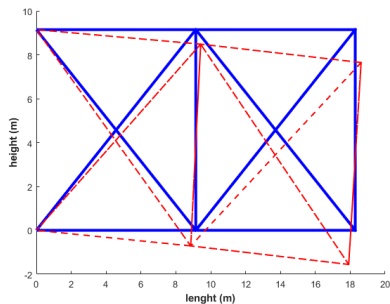
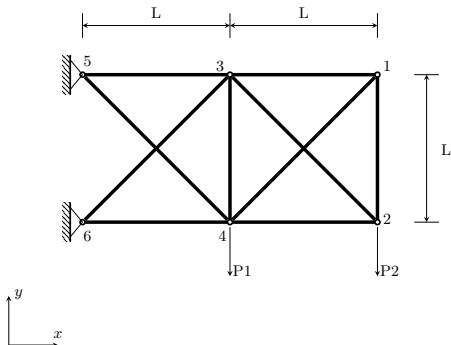
$$\omega_n = 2 \pi f_n \quad n \in \{1, 2, 3\}$$

Natural frequencies:

- $f_1 = 7.01 \text{ Hz}$
- $f_2 = 55.00 \text{ Hz}$
- $f_3 = 114.84 \text{ Hz}$



2D Truss



$$[K] \mathbf{u} = \mathbf{f}$$

* Tutorial elaborated by Marcos Vinícius Issa.

SIR-type temporal model

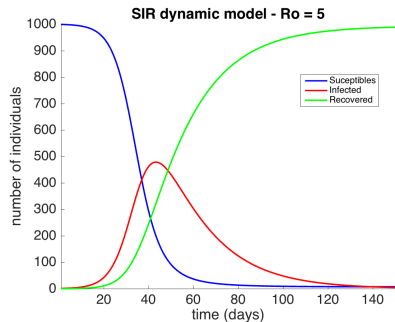


$$\frac{dS}{dt} = -\beta \frac{I}{N} S$$

$$\frac{dI}{dt} = \beta \frac{I}{N} S - \gamma I$$

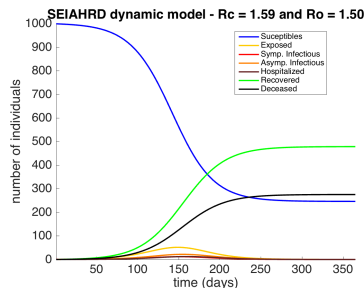
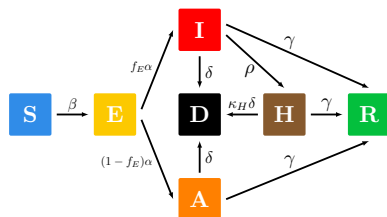
$$\frac{dR}{dt} = \gamma I$$

+ initial conditions



* Tutorial elaborated by Rachel Lucena.

SEIAHRD-type temporal model



* Tutorial elaborated by Rachel Lucena.

$$\frac{dS}{dt} = -\beta S \frac{(I + A + H)}{N}$$

$$\frac{dE}{dt} = \beta S \frac{(I + A + H)}{N} - \alpha E$$

$$\frac{dI}{dt} = f_E \alpha E - (\gamma + \rho + \delta) I$$

$$\frac{dA}{dt} = (1 - f_E) \alpha E - (\gamma + \delta) A$$

$$\frac{dH}{dt} = \rho I - (\gamma + \kappa_H \delta) H$$

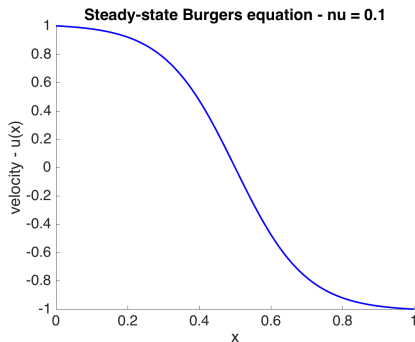
$$\frac{dR}{dt} = \gamma (I + A + H)$$

$$\frac{dD}{dt} = \delta (I + A + \kappa_H H)$$

+ initial conditions

Steady-state Burgers equation

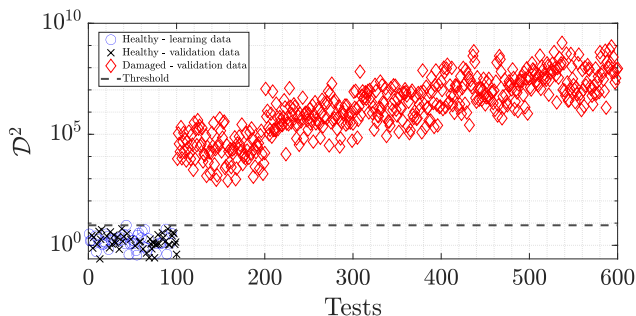
$$\begin{aligned}\nu \frac{d^2 u}{dx^2} - u \frac{du}{dx} &= 0, & 0 < x < 1 \\ u &= 1, & x = 0 \\ u &= -1, & x = 1\end{aligned}$$



* Tutorial elaborated by Rachel Lucena.

Data-driven damage detection

$$\mathcal{D} = \sqrt{(\mathbf{T}^i - \boldsymbol{\mu}_B)^t \boldsymbol{\Sigma}^{-1} (\mathbf{T}^i - \boldsymbol{\mu}_B)}$$



* Tutorial elaborated by Bruna Pavlack.

How to cite this material?

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