### Introduction - Insertion and Search

In this lesson, you will learn how to implement Binary Search Trees in Python and how to insert and search elements within them.

#### WE'LL COVER THE FOLLOWING

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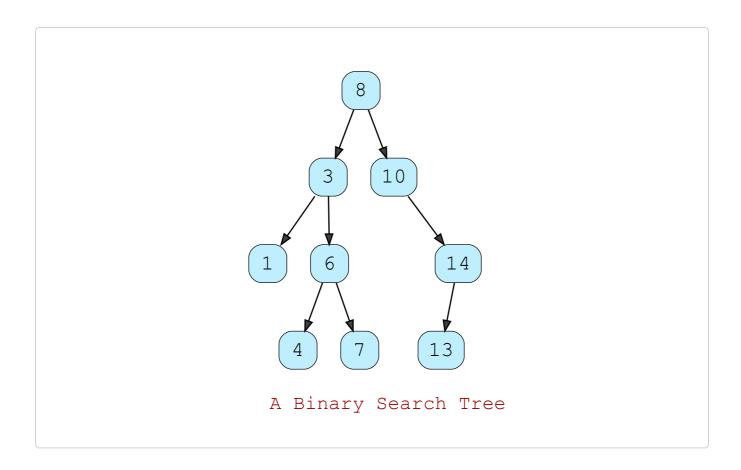
- Insertion
  - Insertion of a Reverse Sorted List
- Search
- Implementation
  - insert
  - search

In this lesson, we will go over the binary search tree data structure. We will first cover the general idea of what a binary search tree is and how one may go about inserting data into this structure as well as how one searches for data. Once we cover the general idea, we will move over to the implementation of the binary search tree data structure in Python. We will construct two class methods that will implement the search and insertion algorithms.

A **binary search tree** is a tree data structure in which nodes are arranged according to the BST property which is as follows:

The value of the left child of any node in a binary search tree will be less than whatever value we have in that node, and the value of the right child of a node will be greater than the value in that node.

This type of pattern persists throughout the tree. Let's look at an example illustrated below:



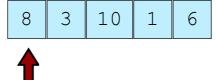
# Insertion #

Let's see how we can insert elements in a binary search tree. In the illustration below, we have an array of elements where we want to insert all the elements one by one into the binary search tree. The way we go about insertion is to start from the root node and compare the new value to be inserted with the current node's value. If the new value is less than the value of the current node, then the new value must be inserted in the left subtree of the current node. On the other hand, if it's greater, it must be inserted in the right subtree to satisfy the BST property. We keep comparing the values as we traverse the tree and insert wherever we find a null position.

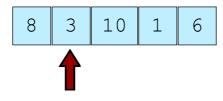


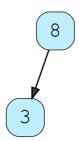
Let's make a BST using the values from the array.

of 6



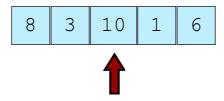


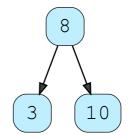




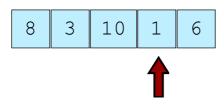
As 3 < 8, it is inserted in the left subtree of 8.

**3** of 6

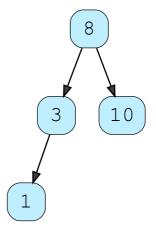




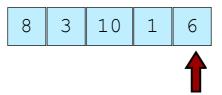
As 10 > 8, it is inserted in the right subtree of 8.



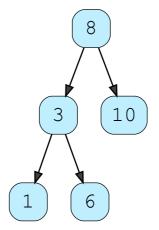
As 1 < 8, we traverse to the left subtree of 8. As 1 < 3, it is inserted in the left subtree of 3.



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As 6 < 8, we traverse to the left subtree of 8. As 6 > 3, it is inserted in the right subtree of 3.



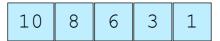
**6** of 6



## Insertion of a Reverse Sorted List #

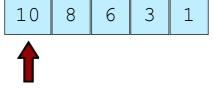
I at's see what happens if we insert elements from a reverse serted list one by

one in a binary search tree.

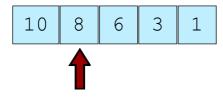


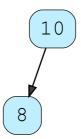
Let's make a BST using the values from the array.

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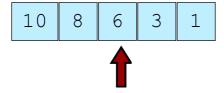
(10)



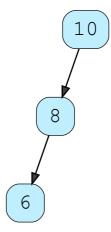


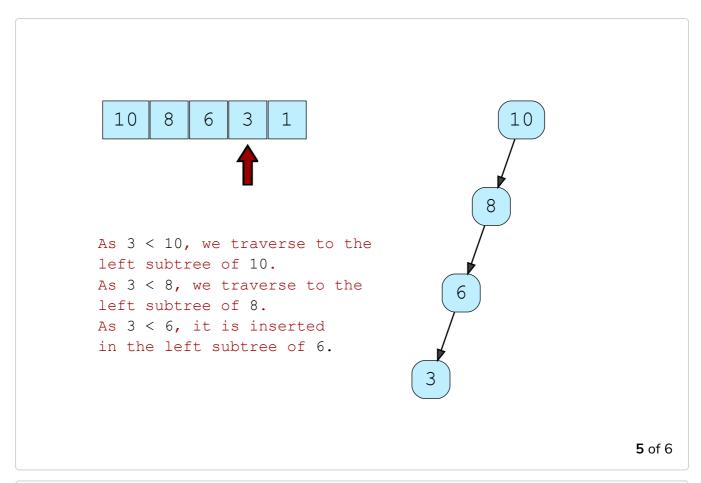
As 8 < 10, it is inserted in the left subtree of 10.

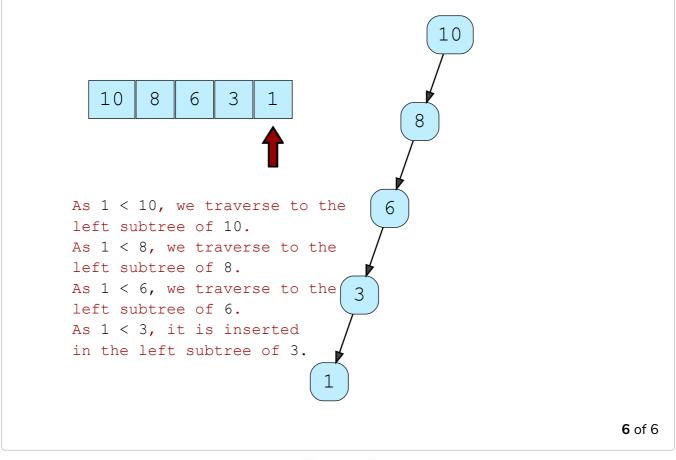
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As 6 < 10, we traverse to the left subtree of 10. As 6 < 8, it is inserted in the left subtree of 8.







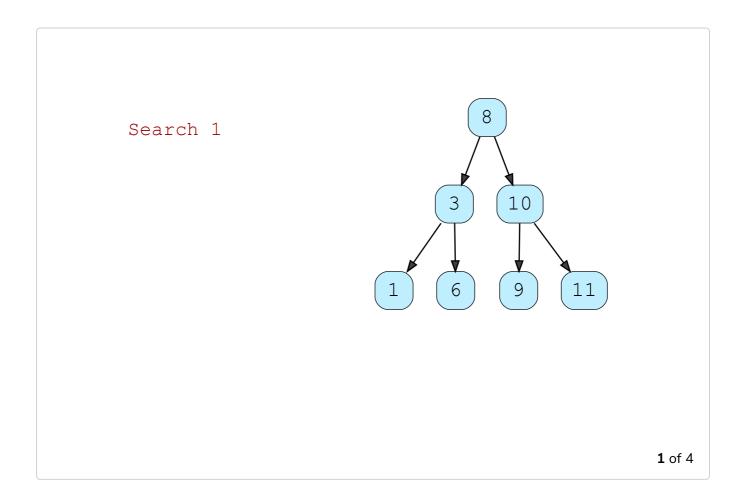
As you can see, we end up with a linear sort of a binary search tree. In such a case, if you want to find **node 1** in the above binary search tree, you might

have to traverse down. However, if you have a structure other than the linear one, then you can substantially cut down the number of operations that you would have to do to find **node 1**. We will look at that sort of a structure when we cover searching. The linear binary search tree is a structure we want to avoid when we perform operations on binary search trees because it kills the purpose of having a binary search tree. If you're curious about how you can prevent getting the structure from reading data and forming a binary search tree out of it, then you can look into something called an AVL tree. An AVL tree rebalances the nodes so that you get a hierarchically spread-out structure instead of a linear one. However, that is beyond the scope of this lesson.

# Search #

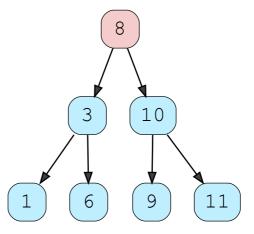
We search using a similar approach as we used in the insertion in a binary search tree. Starting from the root node, we decide which subtree to traverse by comparing the value to be searched with the current node. Then we traverse to the appropriate subtree and discard the other subtree that does not contain the element we are searching for due to the BST property.

Have a look at the illustrations to get a fair idea:



### Search 1

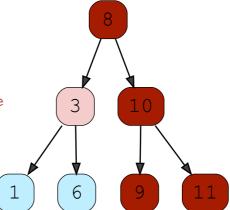
Start from the root node

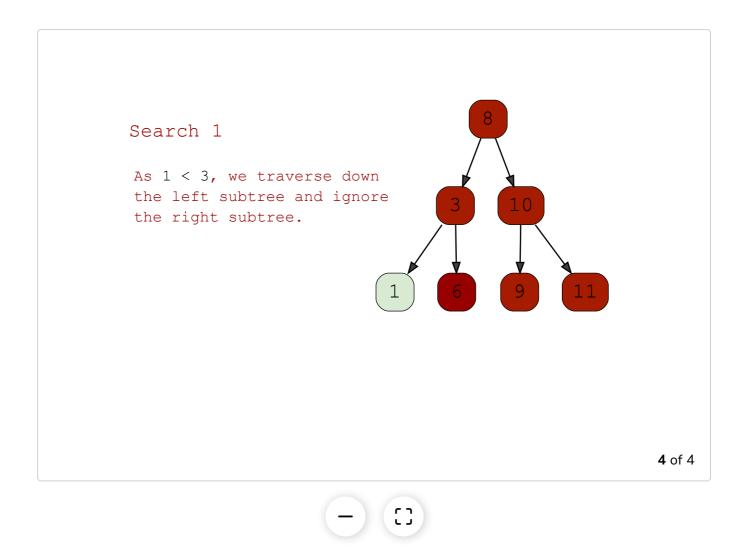


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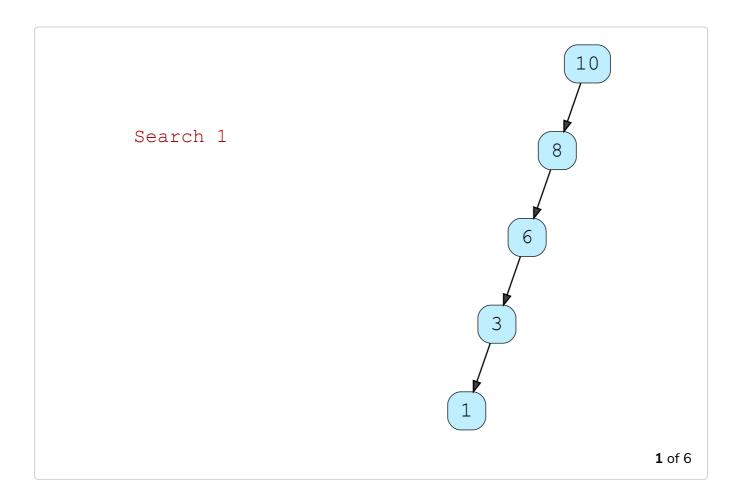
#### Search 1

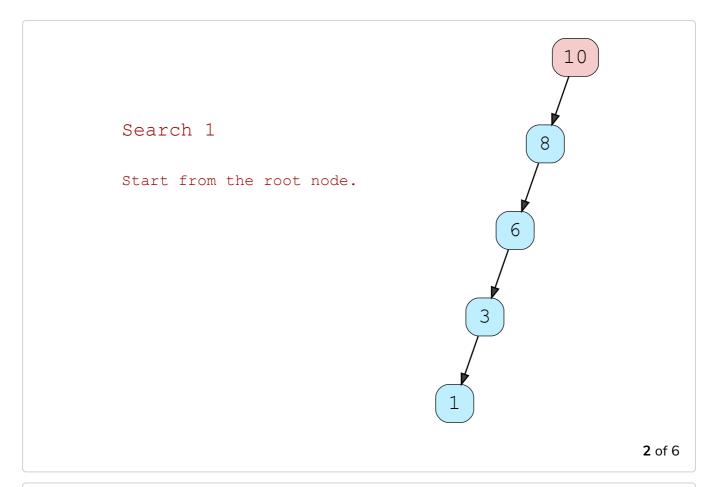
As 1 < 8, we traverse down the left subtree and ignore the right subtree.





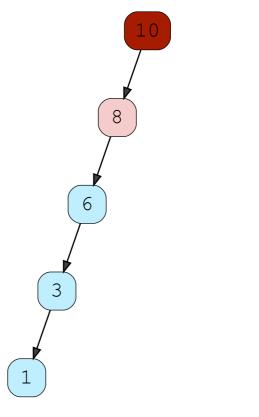
Now let's also illustrate an example to search on a linear binary tree.

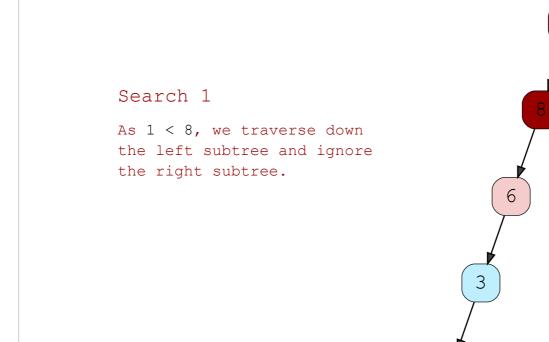




#### Search 1

As 1 < 10, we traverse down the left subtree and ignore the right subtree.

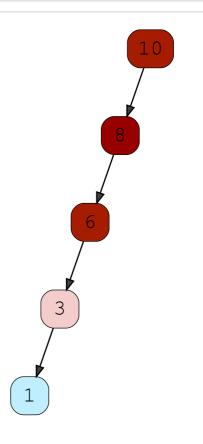


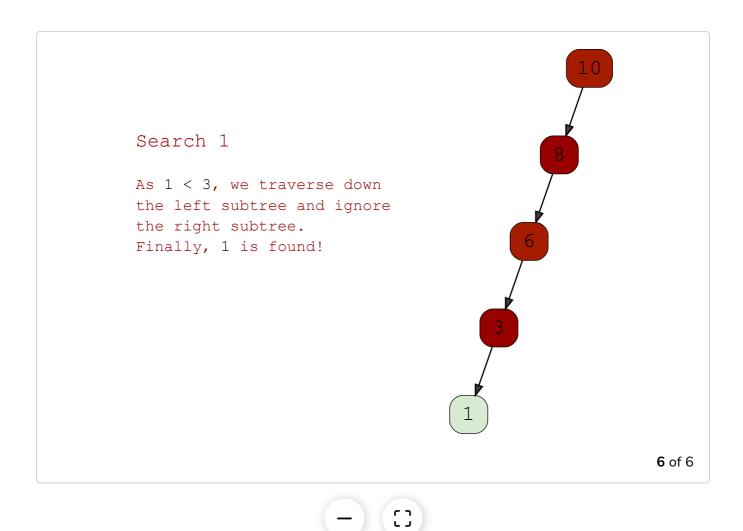


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#### Search 1

As 1 < 6, we traverse down the left subtree and ignore the right subtree.





As you can see from the illustration above, we don't discard anything in a linear structure, so we have to traverse *all the nodes* to find the node we are looking for. This makes it an operation of O(n) in the worst case. If we have a non-linear structure for a BST, the time complexity significantly improves to  $O(\log n)$ .

This table summarizes the time complexities for a BST:

Algorithm	Average Case	Worst Case
Search	O(logn)	O(n)
Insert	O(logn)	O(n)
Delete	O(logn)	O(n)

Now let's jump to the implementations in Python!

# Implementation #

The implementation of the BST class is similar to the implementation of the BinaryTree class. The Node class is exactly the same as the Node class in the Binary Trees chapter.

Have a look at the implementation below:

```
class Node(object):
    def __init__(self, data):
        self.data = data
        self.left = None
        self.right = None

class BST(object):
    def __init__(self, root):
        self.root = Node(root)
```

class Node and class BST

### insert

Now we'll look into the implementation of insert operation in Python.

```
def insert(self, new_val):
    self.insert_helper(self.root, new_val)

def insert_helper(self, current, new_val):
    if current.data < new_val:
        if current.right:
        self.insert_helper(current.right, new_val)
        else:
            current.right = Node(new_val)

else:
        if current.left:
        self.insert_helper(current.left, new_val)
        else:
        current.left = Node(new_val)</pre>
```

insert(self, new\_val) and insert\_helper(self, current, new\_val)

The insert method on line 1 invokes the helper function (insert\_helper) on line 2, while also passing self.root and new\_val into that method. In the insert\_helper method, we have current and new\_val which refer to the current node and the new value to be inserted. In order to find the

appropriate location to insert <code>new\_value</code>, we compare <code>current.data</code> to <code>new\_value</code>. If <code>current.data</code> is less than <code>new\_val</code>, then <code>new\_val</code> must be placed somewhere in the right subtree. Therefore, we check on <code>line 6</code> if <code>current.right</code> is <code>None</code>. If it's not, this implies that we have to traverse the tree further and we recursively call <code>insert\_helper</code> on <code>line 7</code> and pass <code>current.right</code> and <code>new\_value</code> to it. On the other hand, if <code>current.right</code> is <code>None</code>, then <code>current</code> must be a leaf node, and we have found an appropriate position to insert the <code>new\_val</code>. Then we initialize <code>current.right</code> to a new <code>Node</code> by <code>passing new\_val</code> to the <code>constructor</code> on <code>line 9</code>.

Let's talk about when current.data is greater than or equal to new\_val. If that's the case, we repeat what we discussed above about the code in lines 6-9, but replace current.right with current.left as new\_val must be placed in the left subtree of the current node.

#### search

Let's discuss the search method:

```
def search(self, find_val):
    return self.search_helper(self.root, find_val)

def search_helper(self, current, find_val):
    if current:
    if current.data == find_val:
        return True
    elif current.data < find_val:
        return self.search_helper(current.right, find_val)
    else:
        return self.search_helper(current.left, find_val)</pre>
```

search(self, find\_val) and search\_helper(self, current, find\_val)

If you get the hang of the insert operation, then the search method is relatively simple to understand. Like the insert method, the search method invokes a helper function (search\_helper) and passes the root node and the value to search (find\_val) to the helper method. It also returns whatever is returned from the helper method.

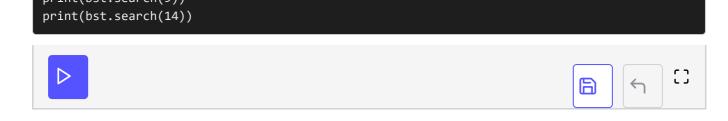
In search\_helper, we check on line 5 if current is None. If it's not, then the execution jumps to line 6 where the condition acts as a sort of base case to the recursive method. If the value of the current node (current.data) is equal to find\_val, then we have found the node that we are supposed to search. True

However, if the condition on **line 6** does not evaluate to **True**, we check on

**line 8** to see if current.data is less than find\_val. If this evaluates to True, find\_val must be in the right subtree of the current node to which we make a recursive call on line 9. Otherwise, if current.data is greater than find\_val, we make a recursive call to the left subtree on line 11.

The entire code that we have implemented can be found below. Make a BST and insert elements to it to verify the insert and the search methods.

```
class Node(object):
                                                                                          6
  def __init__(self, data):
   self.data = data
    self.left = None
    self.right = None
class BST(object):
  def __init__(self, root):
    self.root = Node(root)
  def insert(self, new val):
    self.insert_helper(self.root, new_val)
  def insert_helper(self, current, new_val):
    if current.data < new_val:</pre>
      if current.right:
        self.insert_helper(current.right, new_val)
        current.right = Node(new_val)
    else:
        if current.left:
          self.insert_helper(current.left, new_val)
        else:
          current.left = Node(new_val)
  def search(self, find_val):
    return self.search_helper(self.root, find_val)
  def search_helper(self, current, find_val):
    if current:
      if current.data == find_val:
          return True
      elif current.data < find_val:</pre>
          return self.search_helper(current.right, find_val)
      else:
          return self.search_helper(current.left, find_val)
bst = BST(10)
bst.insert(3)
bst.insert(1)
bst.insert(25)
bst.insert(9)
bst.insert(13)
nrint(hst spanch(9))
```



Brace yourself for a challenge in the next lesson!