

**Birla Institute of Technology & Science – Pilani, K.K. Birla Goa Campus**  
**First Semester 2020-21**

**PHY F313**

**Lab test-1 (Open Book)**  
**Computational Physics    19<sup>th</sup> September 2020**

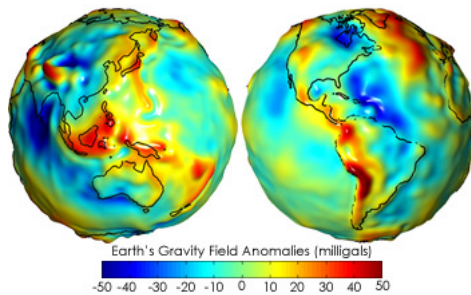
**Time: 120 mins**

1. An object falling vertically through air is subjected to viscous forces as well as gravity. Assume that an object of mass  $m = 0.1\text{Kg}$  is dropped from a height  $h_0 = 10\text{m}$ . The height of the object  $h(t)$  after  $t$  seconds is (assuming damping force to be proportional to velocity) :

$$h(t) = h_0 - \frac{mg}{b}t + \frac{m^2g}{b^2}(1 - e^{-bt/m}) \quad (1)$$

$b = 1.9 \times 10^{-4}\text{Kgs}^{-1}$  is the damping constant<sup>1</sup>. Acceleration due to gravity varies over the surface of the earth due to many factors - non-spherical shape, rotation, height above sea-level. Its variation from the earth's uniformly standard value is depicted below (see figure) from results obtained by NASA's Grace mission<sup>2</sup>.

In today's exercise you have to determine the time of fall for the above mass to reach the ground at different cities around the world.



- Write down the equation whose roots will give you the time taken  $t_{fall}$  for mass to reach the ground.
- Write a code to implement **Secant method** for finding roots.
- Test your code for a  $f(x)$  whose roots are known to you. In the answer sheet you will be required to describe the test that you carried out.
- Find the time of fall  $t_{fall}$  at the following cities around the world. The values of  $g$  are given in table below

City	Value of $g$ ( $\text{m/sec}^2$ )
Helsinki	9.825
Toronto	9.807
Kuala-Lampur	9.776

Accuracy of  $t_{fall}$  value you compute is important here. It should be good enough to distinguish between time of falls at the above cities. Calculate your  $t_{fall}$  to an accuracy such  $t_{fall}$  differs

<sup>1</sup>Ref: Determining the damping coefficient of a simple pendulum oscillating in air, Luis A Ladino & Hermilda S Rondón, Physics Education, Vol. 52, 2017

<sup>2</sup>Ref: Wikipedia

at these 3 cities by atleast 2 significant figures. While terminating Secant method you should bear this in mind.

Note: In the final answer sheet (templated uploaded on Quanta) along with value of  $t_{\text{fall}}$  you also have to write down your initial two guesses in Secant method & the termination value for  $|x_{n+1} - x_n|$ . Additionally you also have to describe the test results.

UPLOAD THE FINAL ANSWER SHEET & YOUR CODE