Social network Graph Link Prediction - Facebook Challenge

Problem statement: ¶

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

Data Overview

Taken data from facebook's recruting challenge on kaggle https://www.kaggle.com/c/FacebookRecruiting (https://www.kaggle.com/c/FacebookRecruiting) data contains two columns source and destination eac edge in graph

Data columns (total 2 columns):source node int64

- destination node int64

Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos :
 - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
 (https://www.cs.cornell.edu/home/kleinber/link-pred.pdf)
 - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf
 (https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf)
 - https://kaggle2.blob.core.windows.net/forum-messageattachments/2594/supervised_link_prediction.pdf
 (https://kaggle2.blob.core.windows.net/forum-messageattachments/2594/supervised_link_prediction.pdf)
 - https://www.youtube.com/watch?v=2M77Hgy17cg (https://www.youtube.com/watch?v=2M77Hgy17cg)

Business objectives and constraints:

- No low-latency requirement.
- · Probability of prediction is useful to recommend ighest probability links

Performance metric for supervised learning:

- Both precision and recall is important so F1 score is good choice
- Confusion matrix

```
In [0]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xqboost: pip3 install xqboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
```

```
In [0]: #reading graph
   if not os.path.isfile('data/after_eda/train_woheader.csv'):
        traincsv = pd.read_csv('data/train.csv')
        print(traincsv[traincsv.isna().any(1)])
        print("Number of diplicate entries: ",sum(traincsv.duplicated()))
        traincsv.to_csv('data/after_eda/train_woheader.csv',header=False,index=False)
        print("saved the graph into file")
   else:
        g=nx.read_edgelist('data/after_eda/train_woheader.csv',delimiter=',',create_u
        print(nx.info(g))
```

Name:

Type: DiGraph

Number of nodes: 1862220 Number of edges: 9437519 Average in degree: 5.0679 Average out degree: 5.0679

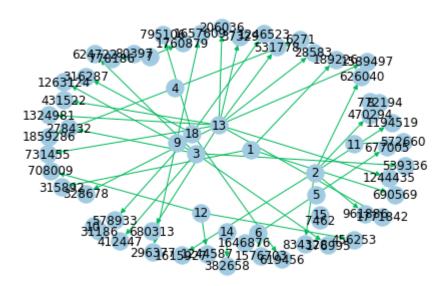
Displaying a sub graph

Name:

Type: DiGraph

Number of nodes: 66 Number of edges: 50

Average in degree: 0.7576 Average out degree: 0.7576



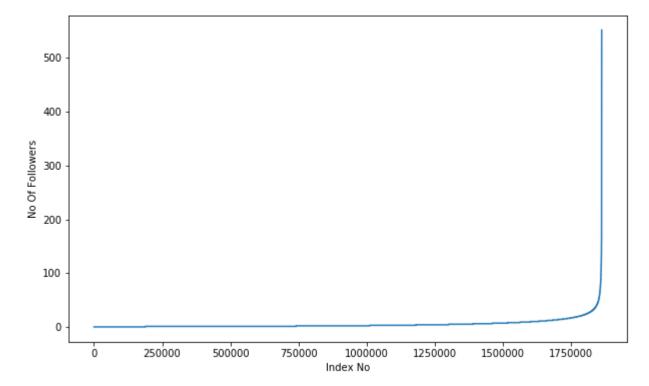
1. Exploratory Data Analysis

In [0]: # No of Unique persons
print("The number of unique persons",len(g.nodes()))

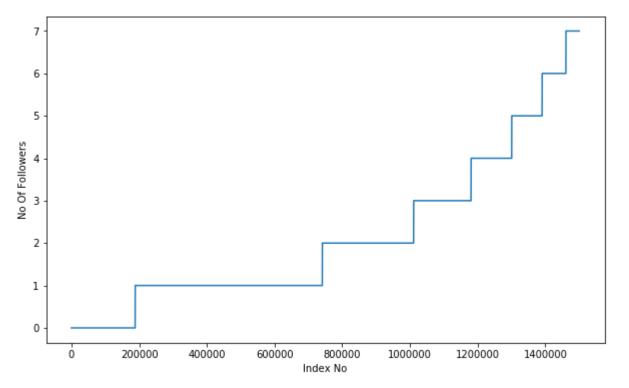
The number of unique persons 1862220

1.1 No of followers for each person

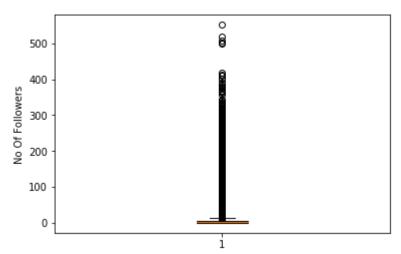
```
In [0]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
```



```
In [0]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
```





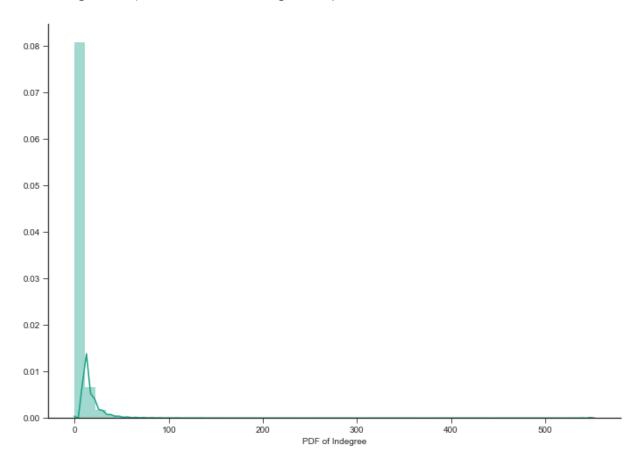


```
In [0]: ### 90-100 percentile
        for i in range(0,11):
            print(90+i,'percentile value is',np.percentile(indegree_dist,90+i))
        90 percentile value is 12.0
        91 percentile value is 13.0
        92 percentile value is 14.0
        93 percentile value is 15.0
        94 percentile value is 17.0
        95 percentile value is 19.0
        96 percentile value is 21.0
        97 percentile value is 24.0
        98 percentile value is 29.0
        99 percentile value is 40.0
        100 percentile value is 552.0
        99% of data having followers of 40 only.
In [0]: | ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is',np.percentile(indegree_dist,99+(i/100)
        99.1 percentile value is 42.0
        99.2 percentile value is 44.0
        99.3 percentile value is 47.0
        99.4 percentile value is 50.0
        99.5 percentile value is 55.0
        99.6 percentile value is 61.0
        99.7 percentile value is 70.0
        99.8 percentile value is 84.0
        99.9 percentile value is 112.0
        100.0 percentile value is 552.0
```

```
In [0]: %matplotlib inline
    sns.set_style('ticks')
    fig, ax = plt.subplots()
    fig.set_size_inches(11.7, 8.27)
    sns.distplot(indegree_dist, color='#16A085')
    plt.xlabel('PDF of Indegree')
    sns.despine()
    #plt.show()
```

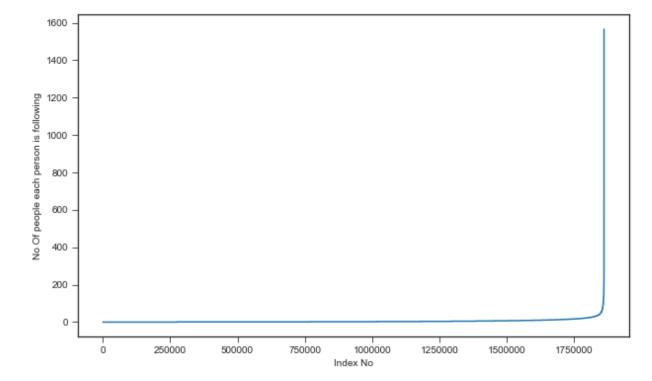
D:\installed\Anaconda3\lib\site-packages\matplotlib\axes_axes.py:6571: UserWar ning: The 'normed' kwarg is deprecated, and has been replaced by the 'density' kwarg.

warnings.warn("The 'normed' kwarg is deprecated, and has been "

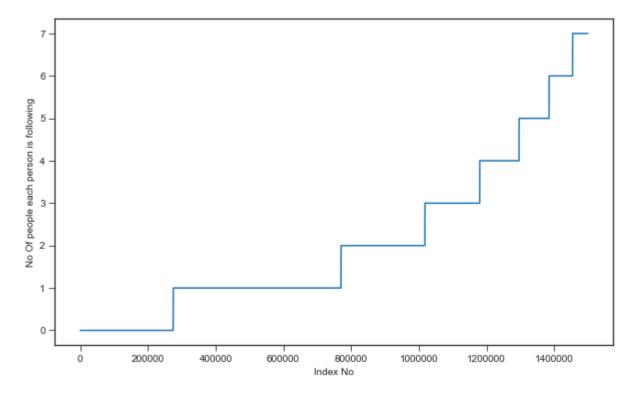


1.2 No of people each person is following

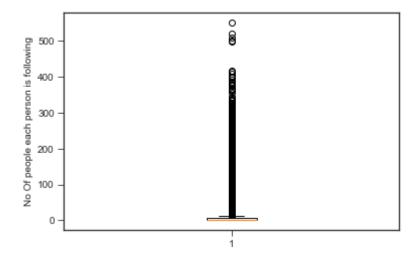
```
In [0]: outdegree_dist = list(dict(g.out_degree()).values())
    outdegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(outdegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following')
    plt.show()
```



```
In [0]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(outdegree_dist[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following')
    plt.show()
```



In [0]: plt.boxplot(indegree_dist)
 plt.ylabel('No Of people each person is following')
 plt.show()

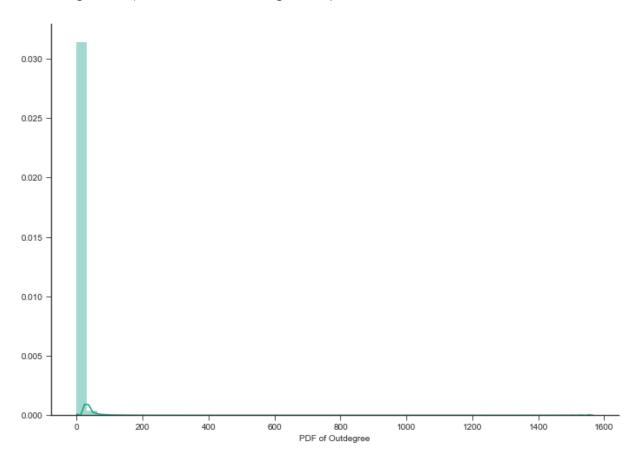


```
In [0]: | ### 90-100 percentile
        for i in range(0,11):
            print(90+i, 'percentile value is',np.percentile(outdegree_dist,90+i))
        90 percentile value is 12.0
        91 percentile value is 13.0
        92 percentile value is 14.0
        93 percentile value is 15.0
        94 percentile value is 17.0
        95 percentile value is 19.0
        96 percentile value is 21.0
        97 percentile value is 24.0
        98 percentile value is 29.0
        99 percentile value is 40.0
        100 percentile value is 1566.0
In [0]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is', np.percentile(outdegree dist, 99+(i/100
        99.1 percentile value is 42.0
        99.2 percentile value is 45.0
        99.3 percentile value is 48.0
        99.4 percentile value is 52.0
        99.5 percentile value is 56.0
        99.6 percentile value is 63.0
        99.7 percentile value is 73.0
        99.8 percentile value is 90.0
        99.9 percentile value is 123.0
        100.0 percentile value is 1566.0
```

```
In [0]: sns.set_style('ticks')
    fig, ax = plt.subplots()
    fig.set_size_inches(11.7, 8.27)
    sns.distplot(outdegree_dist, color='#16A085')
    plt.xlabel('PDF of Outdegree')
    sns.despine()
```

D:\installed\Anaconda3\lib\site-packages\matplotlib\axes_axes.py:6571: UserWar ning: The 'normed' kwarg is deprecated, and has been replaced by the 'density' kwarg.

warnings.warn("The 'normed' kwarg is deprecated, and has been "



No of persons those are not following anyone are 274512 and % is 14.74111544285 8524

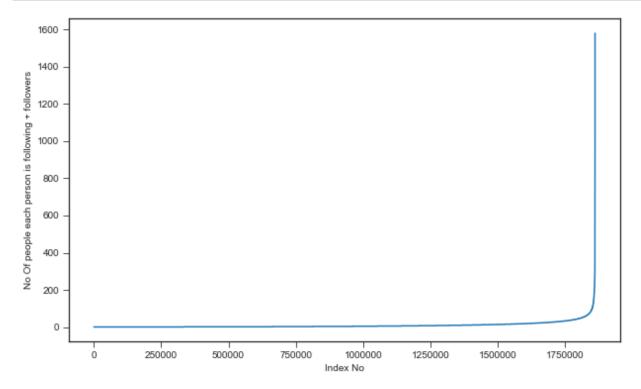
No of persons having zero followers are 188043 and % is 10.097786512871734

No of persons those are not not following anyone and also not having any follow ers are θ

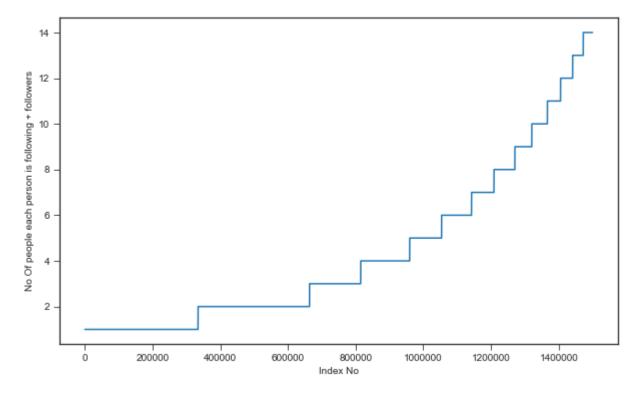
1.3 both followers + following

```
In [0]: from collections import Counter
    dict_in = dict(g.in_degree())
    dict_out = dict(g.out_degree())
    d = Counter(dict_in) + Counter(dict_out)
    in_out_degree = np.array(list(d.values()))
```

```
In [0]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [0]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [0]: ### 90-100 percentile
for i in range(0,11):
    print(90+i,'percentile value is',np.percentile(in_out_degree_sort,90+i))
```

```
90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
```

```
In [0]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is',np.percentile(in_out_degree_sort,99+(i/
        99.1 percentile value is 83.0
        99.2 percentile value is 87.0
        99.3 percentile value is 93.0
        99.4 percentile value is 99.0
        99.5 percentile value is 108.0
        99.6 percentile value is 120.0
        99.7 percentile value is 138.0
        99.8 percentile value is 168.0
        99.9 percentile value is 221.0
        100.0 percentile value is 1579.0
In [0]: print('Min of no of followers + following is',in out degree.min())
        print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of f
        Min of no of followers + following is 1
        334291 persons having minimum no of followers + following
        print('Max of no of followers + following is',in out degree.max())
In [0]:
        print(np.sum(in_out_degree==in_out_degree.max()),' persons having maximum no of fe
        Max of no of followers + following is 1579
        1 persons having maximum no of followers + following
In [0]: print('No of persons having followers + following less than 10 are',np.sum(in_out)
        No of persons having followers + following less than 10 are 1320326
In [0]: print('No of weakly connected components',len(list(nx.weakly connected components
        for i in list(nx.weakly_connected_components(g)):
            if len(i)==2:
                count+=1
        print('weakly connected components wit 2 nodes',count)
        No of weakly connected components 45558
```

2. Posing a problem as classification problem

weakly connected components wit 2 nodes 32195

2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
In [0]:
        %%time
        ###generating bad edges from given graph
        import random
        if not os.path.isfile('data/after eda/missing edges final.p'):
             #getting all set of edges
             r = csv.reader(open('data/after_eda/train_woheader.csv','r'))
             edges = dict()
             for edge in r:
                 edges[(edge[0], edge[1])] = 1
             missing_edges = set([])
             while (len(missing_edges)<9437519):</pre>
                 a=random.randint(1, 1862220)
                 b=random.randint(1, 1862220)
                 tmp = edges.get((a,b),-1)
                 if tmp == -1 and a!=b:
                     try:
                         if nx.shortest_path_length(g,source=a,target=b) > 2:
                             missing edges.add((a,b))
                         else:
                             continue
                     except:
                             missing_edges.add((a,b))
                 else:
                     continue
             pickle.dump(missing_edges,open('data/after_eda/missing_edges_final.p','wb'))
        else:
             missing_edges = pickle.load(open('data/after_eda/missing_edges_final.p','rb')
        Wall time: 5.08 s
In [0]: len(missing_edges)
```

Out[47]: 9437519

2.2 Training and Test data split:

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

```
In [0]:
        from sklearn.model selection import train test split
        if (not os.path.isfile('data/after eda/train pos after eda.csv')) and (not os.pat
            #reading total data df
            df pos = pd.read csv('data/train.csv')
            df neg = pd.DataFrame(list(missing edges), columns=['source node', 'destination

            print("Number of nodes in the graph with edges", df pos.shape[0])
            print("Number of nodes in the graph without edges", df neg.shape[0])
            #Trian test split
            #Spiltted data into 80-20
            #positive links and negative links seperatly because we need positive training
            #and for feature generation
            X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,n
            X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,n
            print('='*60)
            print("Number of nodes in the train data graph with edges", X train pos.shape
            print("Number of nodes in the train data graph without edges", X_train_neg.sh
            print('='*60)
            print("Number of nodes in the test data graph with edges", X test pos.shape[0]
            print("Number of nodes in the test data graph without edges", X_test_neg.shap
            #removing header and saving
            X_train_pos.to_csv('data/after_eda/train_pos_after_eda.csv',header=False, ind
            X test pos.to csv('data/after eda/test pos after eda.csv',header=False, index
            X train neg.to csv('data/after eda/train neg after eda.csv',header=False, ind
            X_test_neg.to_csv('data/after_eda/test_neg_after_eda.csv',header=False, index
        else:
            #Graph from Traing data only
            del missing edges
```

```
Number of nodes in the graph with edges 9437519
Number of nodes in the graph without edges 9437519
```

Number of nodes in the train data graph with edges 7550015 = 7550015 Number of nodes in the train data graph without edges 7550015 = 7550015

Number of nodes in the test data graph with edges 1887504 = 1887504 Number of nodes in the test data graph without edges 1887504 = 1887504

```
In [0]: if (os.path.isfile('data/after eda/train pos after eda.csv')) and (os.path.isfile
            train graph=nx.read edgelist('data/after eda/train pos after eda.csv',delimit
            test_graph=nx.read_edgelist('data/after_eda/test_pos_after_eda.csv',delimiter
            print(nx.info(train graph))
            print(nx.info(test graph))
            # finding the unique nodes in the both train and test graphs
            train nodes pos = set(train graph.nodes())
            test nodes pos = set(test graph.nodes())
            trY teY = len(train nodes pos.intersection(test nodes pos))
            trY_teN = len(train_nodes_pos - test_nodes_pos)
            teY_trN = len(test_nodes_pos - train_nodes_pos)
            print('no of people common in train and test -- ',trY teY)
            print('no of people present in train but not present in test -- ',trY_teN)
            print('no of people present in test but not present in train -- ',teY trN)
            print(' % of people not there in Train but exist in Test in total Test data a
        4
```

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

Name:

Type: DiGraph

Number of nodes: 1144623 Number of edges: 1887504 Average in degree: 1.6490 Average out degree: 1.6490 no of people common in train and test -- 1063125

no of people present in train but not present in test -- 717597

no of people present in test but not present in train -- 81498

% of people not there in Train but exist in Test in total Test data are 7.1200 735962845405 %

we have a cold start problem here

```
In [0]: #final train and test data sets
        if (not os.path.isfile('data/after eda/train after eda.csv')) and \
        (not os.path.isfile('data/after eda/test after eda.csv')) and \
        (not os.path.isfile('data/train y.csv')) and \
        (not os.path.isfile('data/test y.csv')) and \
        (os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and \
        (os.path.isfile('data/after eda/test pos after eda.csv')) and \
        (os.path.isfile('data/after eda/train neg after eda.csv')) and \
        (os.path.isfile('data/after eda/test neg after eda.csv')):
            X train pos = pd.read csv('data/after eda/train pos after eda.csv', names=['s
            X_test_pos = pd.read_csv('data/after_eda/test_pos_after_eda.csv', names=['sou
            X_train_neg = pd.read_csv('data/after_eda/train_neg_after_eda.csv', names=['s
            X test neg = pd.read csv('data/after eda/test neg after eda.csv', names=['sou
            print('='*60)
            print("Number of nodes in the train data graph with edges", X train pos.shape
            print("Number of nodes in the train data graph without edges", X train neg.sh
            print('='*60)
            print("Number of nodes in the test data graph with edges", X_test_pos.shape[0]
            print("Number of nodes in the test data graph without edges", X test neg.shap
            X train = X train pos.append(X train neg,ignore index=True)
            y_train = np.concatenate((y_train_pos,y_train_neg))
            X_test = X_test_pos.append(X_test_neg,ignore_index=True)
            y test = np.concatenate((y test pos,y test neg))
            X_train.to_csv('data/after_eda/train_after_eda.csv',header=False,index=False)
            X test.to csv('data/after eda/test after eda.csv',header=False,index=False)
            pd.DataFrame(y_train.astype(int)).to_csv('data/train_y.csv',header=False,inde
            pd.DataFrame(y_test.astype(int)).to_csv('data/test_y.csv',header=False,index=
```

```
Number of nodes in the train data graph with edges 7550015

Number of nodes in the train data graph without edges 7550015

-----

Number of nodes in the test data graph with edges 1887504

Number of nodes in the test data graph without edges 1887504
```

```
In [0]: print("Data points in train data",X_train.shape)
    print("Data points in test data",X_test.shape)
    print("Shape of traget variable in train",y_train.shape)
    print("Shape of traget variable in test", y_test.shape)
```

```
Data points in train data (15100030, 2)
Data points in test data (3775008, 2)
Shape of traget variable in train (15100030,)
Shape of traget variable in test (3775008,)
```

```
In [0]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xqboost: pip3 install xqboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import HDFStore,DataFrame
        from pandas import read hdf
        from scipy.sparse.linalg import svds, eigs
        import gc
        from tqdm import tqdm
```

1. Reading Data

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

2. Similarity measures

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

```
In [0]: #for followees
        def jaccard_for_followees(a,b):
            try:
                 if len(set(train graph.successors(a))) == 0 | len(set(train graph.succes
                     return 0
                 sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.su
                                             (len(set(train graph.successors(a)).union(set
            except:
                 return 0
            return sim
In [0]: #one test case
        print(jaccard for followees(273084,1505602))
        0.0
In [0]: #node 1635354 not in graph
        print(jaccard_for_followees(273084,1505602))
        0.0
In [0]: #for followers
        def jaccard_for_followers(a,b):
            try:
                 if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecessors(b)
                     return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.
                                          (len(set(train_graph.predecessors(a)).union(set())
                 return sim
            except:
                 return 0
In [0]: print(jaccard for followers(273084,470294))
        #node 1635354 not in graph
In [0]:
        print(jaccard for followees(669354,1635354))
```

2.2 Cosine distance

$$CosineDistance = \frac{|X \cap Y|}{|X| \cdot |Y|}$$

Loading [MathJax]/jax/output/HTML-CSS/fonts/STIX-Web/Size1/Regular/Main.js

0

```
In [0]: #for followees
        def cosine for followees(a,b):
            try:
                 if len(set(train graph.successors(a))) == 0 | len(set(train graph.succes
                     return 0
                 sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.su
                                             (math.sqrt(len(set(train graph.successors(a)))
                 return sim
            except:
                 return 0
In [0]: print(cosine_for_followees(273084,1505602))
        0.0
In [0]: print(cosine for followees(273084,1635354))
In [0]:
        def cosine_for_followers(a,b):
            try:
                 if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.pred
                     return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.
                                              (math.sqrt(len(set(train_graph.predecessors()))
                 return sim
            except:
                 return 0
In [0]: print(cosine_for_followers(2,470294))
        0.02886751345948129
In [0]:
        print(cosine for followers(669354,1635354))
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-

- <u>1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html</u> (https://networkx.github.io/documentation/networkx-
- 1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

```
In [0]: if not os.path.isfile('data/fea sample/page rank.p'):
            pr = nx.pagerank(train graph, alpha=0.85)
            pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
            pr = pickle.load(open('data/fea sample/page rank.p','rb'))
In [0]:
        print('min',pr[min(pr, key=pr.get)])
        print('max',pr[max(pr, key=pr.get)])
        print('mean',float(sum(pr.values())) / len(pr))
        min 1.6556497245737814e-07
        max 2.7098251341935827e-05
        mean 5.615699699389075e-07
In [0]:
        #for imputing to nodes which are not there in Train data
        mean pr = float(sum(pr.values())) / len(pr)
        print(mean pr)
        5.615699699389075e-07
```

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

Out[22]: -1

```
p=-1
             try:
                  if train_graph.has_edge(a,b):
                      train_graph.remove_edge(a,b)
                      p= nx.shortest_path_length(train_graph,source=a,target=b)
                      train_graph.add_edge(a,b)
                  else:
                      p= nx.shortest_path_length(train_graph,source=a,target=b)
                  return p
             except:
                  return -1
In [0]: #testing
         compute shortest path length(77697, 826021)
Out[21]: 10
In [0]:
         #testing
         compute_shortest_path_length(669354,1635354)
```

In [0]: #if has direct edge then deleting that edge and calculating shortest path

def compute_shortest_path_length(a,b):

4.2 Checking for same community

```
In [0]: #getting weekly connected edges from graph
         wcc=list(nx.weakly_connected_components(train_graph))
         def belongs_to_same_wcc(a,b):
             index = []
             if train_graph.has_edge(b,a):
                 return 1
             if train_graph.has_edge(a,b):
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if (b in index):
                         train_graph.remove_edge(a,b)
                         if compute_shortest_path_length(a,b)==-1:
                             train_graph.add_edge(a,b)
                             return 0
                         else:
                             train_graph.add_edge(a,b)
                             return 1
                     else:
                         return 0
             else:
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if(b in index):
                         return 1
                     else:
                         return 0
```

```
In [0]: belongs_to_same_wcc(861, 1659750)
Out[24]: 0
In [0]: belongs_to_same_wcc(669354,1635354)
Out[25]: 0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x,y) = \sum_{u \in N(x) \cap N(y)} \frac{1}{log(|N(u)|)}$$

```
In [0]: #adar index
def calc_adar_in(a,b):
    sum=0
    try:
        n=list(set(train_graph.successors(a)).intersection(set(train_graph.succes
        if len(n)!=0:
            for i in n:
                 sum=sum+(1/np.log10(len(list(train_graph.predecessors(i)))))
            return sum
        else:
            return 0
    except:
        return 0
```

```
In [0]: calc_adar_in(1,189226)
Out[27]: 0
In [0]: calc_adar_in(669354,1635354)
Out[28]: 0
```

4.4 Is persion was following back:

```
In [0]: def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0

In [0]: follows_back(1,189226)

Out[30]: 1

In [0]: follows_back(669354,1635354)

Out[31]: 0
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality (https://en.wikipedia.org/wiki/Katz_centrality)

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/

(https://www.geeksforgeeks.org/katz-centrality-centrality-measure/) Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

 $x_i = \alpha \sum_{j} A_{ij} x_j + \beta x_j + \beta$

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 $\$ \square \frac{1}{\lambda_{max}}.\$\$

```
In [0]: if not os.path.isfile('data/fea_sample/katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('data/fea_sample/katz.p','wb'))
else:
    katz = pickle.load(open('data/fea_sample/katz.p','rb'))

In [0]: print('min',katz[min(katz, key=katz.get)])
    print('max',katz[max(katz, key=katz.get)])
    print('mean',float(sum(katz.values())) / len(katz))

min 0.0007313532484065916
    max 0.003394554981699122
    mean 0.0007483800935562018

In [0]: mean_katz = float(sum(katz.values())) / len(katz)
    print(mean_katz)
    0.0007483800935562018
```

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm (https://en.wikipedia.org/wiki/HITS_algorithm)

```
In [0]: if not os.path.isfile('data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=
    pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
    else:
        hits = pickle.load(open('data/fea_sample/hits.p','rb'))

In [0]: print('min',hits[0][min(hits[0], key=hits[0].get)])
    print('max',hits[0][max(hits[0], key=hits[0].get)])
    print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
```

5. Featurization

max 0.004868653378780953 mean 5.615699699344123e-07

5. 1 Reading a sample of Data from both train and test

```
In [0]: import random
if os.path.isfile('data/after_eda/train_after_eda.csv'):
    filename = "data/after_eda/train_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 15100030
    # n_train = sum(1 for line in open(filename)) #number of records in file (exc
    n_train = 15100028
    s = 100000 #desired sample size
    skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
    #https://stackoverflow.com/a/22259008/4084039
```

```
In [0]: if os.path.isfile('data/after_eda/train_after_eda.csv'):
    filename = "data/after_eda/test_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 3775008
    # n_test = sum(1 for line in open(filename)) #number of records in file (exclun_test = 3775006
    s = 50000 #desired sample size
    skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
    #https://stackoverflow.com/a/22259008/4084039
```

```
In [0]: print("Number of rows in the train data file:", n_train)
    print("Number of rows we are going to elimiate in train data are",len(skip_train)
    print("Number of rows in the test data file:", n_test)
    print("Number of rows we are going to elimiate in test data are",len(skip_test))
```

```
Number of rows in the train data file: 15100028
Number of rows we are going to elimiate in train data are 15000028
Number of rows in the test data file: 3775006
Number of rows we are going to elimiate in test data are 3725006
```

Our train matrix size (100002, 3)

Out[49]:

		source_node	destination_node	indicator_link
	0	273084	1505602	1
	1	832016	1543415	1

Our test matrix size (50002, 3)

Out[50]:

	source_node	destination_node	indicator_link
0	848424	784690	1
1	483294	1255532	1

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard followees
- 3. cosine followers
- 4. cosine followees
- 5. num followers s
- num_followees_s
- 7. num followers d
- 8. num followees d
- 9. inter followers
- 10. inter followees

```
In [0]:
           if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
                #mapping jaccrd followers to train and test data
                df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
                                                         jaccard for followers(row['source nod
                df final test['jaccard followers'] = df final test.apply(lambda row:
                                                         jaccard_for_followers(row['source_nod
                #mapping jaccrd followees to train and test data
                df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                                         jaccard for followees(row['source nod
                df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                                         jaccard_for_followees(row['source_nod
                    #mapping jaccrd followers to train and test data
                df final train['cosine followers'] = df final train.apply(lambda row:
                                                         cosine for followers(row['source node
                df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                         cosine_for_followers(row['source_node
                #mapping jaccrd followees to train and test data
                df final train['cosine followees'] = df final train.apply(lambda row:
                                                         cosine for followees(row['source node
                df_final_test['cosine_followees'] = df_final_test.apply(lambda row:
Loading [MathJax]/jax/output/HTML-CSS/fonts/STIX-Web/Size1/Regular/Main.js
                                                         cosine_for_followees(row['source_node
```

```
In [0]: def compute features stage1(df final):
            #calculating no of followers followees for source and destination
            #calculating intersection of followers and followees for source and destination
            num followers s=[]
            num followees s=[]
            num_followers_d=[]
            num followees d=[]
            inter followers=[]
            inter followees=[]
            for i,row in df_final.iterrows():
                try:
                     s1=set(train_graph.predecessors(row['source_node']))
                     s2=set(train_graph.successors(row['source_node']))
                 except:
                     s1 = set()
                     s2 = set()
                try:
                     d1=set(train_graph.predecessors(row['destination_node']))
                     d2=set(train_graph.successors(row['destination_node']))
                     d1 = set()
                     d2 = set()
                 num followers s.append(len(s1))
                 num_followees_s.append(len(s2))
                 num followers d.append(len(d1))
                 num followees d.append(len(d2))
                 inter followers.append(len(s1.intersection(d1)))
                 inter followees.append(len(s2.intersection(d2)))
            return num_followers_s, num_followers_d, num_followees_s, num_followees_d, in
In [0]: if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
            df final train['num followers s'], df final train['num followers d'], \
            df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
            df_final_train['inter_followers'], df_final_train['inter_followees']= compute
            df final test['num followers s'], df final test['num followers d'], \
            df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
            df_final_test['inter_followers'], df_final_test['inter_followees']= compute_f
            hdf = HDFStore('data/fea_sample/storage_sample_stage1.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test df',df final test, format='table', data columns=True)
            hdf.close()
        else:
            df_final_train = read_hdf('data/fea_sample/storage_sample_stage1.h5', 'train_
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

df_final_test = read_hdf('data/fea_sample/storage_sample_stage1.h5', 'test_df

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [0]: if not os.path.isfile('data/fea_sample/storage_sample_stage2.h5'):
            #mapping adar index on train
            df final train['adar index'] = df final train.apply(lambda row: calc adar in(
            #mapping adar index on test
            df final test['adar index'] = df final test.apply(lambda row: calc adar in(row)
            #mapping followback or not on train
            df final train['follows back'] = df final train.apply(lambda row: follows bac
            #mapping followback or not on test
            df final test['follows back'] = df final test.apply(lambda row: follows back(
            #mapping same component of wcc or not on train
            df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_to_same
            ##mapping same component of wcc or not on train
            df_final_test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_
            #mapping shortest path on train
            df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path')
            #mapping shortest path on test
            df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_shor
            hdf = HDFStore('data/fea sample/storage sample stage2.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test df',df final test, format='table', data columns=True)
            hdf.close()
        else:
            df_final_train = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'train_
            df_final_test = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'test_df
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - weight of incoming edges + weight of outgoing edges
 - weight of incoming edges weight of outgoing edges
 - 2weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges

```
2. Page Ranking of source
Loading [MathJax]/jax/output/HTML-CSS/fonts/STIX-Web/Size1/Regular/Main.js
3. Page Ranking of dest
```

- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

\begin{equation} W = \frac{1}{\sqrt{1+|X|}} \end{equation}

it is directed graph so calculated Weighted in and Weighted out differently

```
In [0]: #weight for source and destination of each link
Weight_in = {}
Weight_out = {}
for i in tqdm(train_graph.nodes()):
    s1=set(train_graph.predecessors(i))
    w_in = 1.0/(np.sqrt(1+len(s1)))
    Weight_in[i]=w_in

    s2=set(train_graph.successors(i))
    w_out = 1.0/(np.sqrt(1+len(s2)))
    Weight_out[i]=w_out

#for imputing with mean
mean_weight_in = np.mean(list(Weight_in.values()))
mean_weight_out = np.mean(list(Weight_out.values()))
```

722/1780722 [00:11<00:00, 152682.24it/s]

1780

```
In [0]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
            #mapping to pandas train
            df final train['weight in'] = df final train.destination node.apply(lambda x:
            df final train['weight out'] = df final train.source node.apply(lambda x: Weight
            #mapping to pandas test
            df final test['weight in'] = df final test.destination node.apply(lambda x: W
            df final test['weight out'] = df final test.source node.apply(lambda x: Weight
            #some features engineerings on the in and out weights
            df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight
            df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight
            df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.
            df final train['weight f4'] = (1*df final train.weight in + 2*df final train.
            #some features engineerings on the in and out weights
            df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_o
            df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_o
            df final test['weight f3'] = (2*df final test.weight in + 1*df final test.weight
            df final test['weight f4'] = (1*df final test.weight in + 2*df final test.weight
```

```
In [0]: if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
            #page rank for source and destination in Train and Test
            #if anything not there in train graph then adding mean page rank
            df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda x:pr.
            df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda
            df final test['page rank s'] = df final test.source node.apply(lambda x:pr.ge
            df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x:
            #Katz centrality score for source and destination in Train and test
            #if anything not there in train graph then adding mean katz score
            df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.ge
            df final train['katz d'] = df final train.destination node.apply(lambda x: ka
            df final test['katz s'] = df final test.source node.apply(lambda x: katz.get()
            df final test['katz d'] = df final test.destination node.apply(lambda x: katz
            #Hits algorithm score for source and destination in Train and test
            #if anything not there in train graph then adding 0
            df final train['hubs s'] = df final train.source node.apply(lambda x: hits[0]
            df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x: hi
            df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].g
            df final test['hubs d'] = df final test.destination node.apply(lambda x: hits
            #Hits algorithm score for source and destination in Train and Test
            #if anything not there in train graph then adding 0
            df final train['authorities s'] = df final train.source node.apply(lambda x:
            df final train['authorities d'] = df final train.destination node.apply(lambd)
            df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hi
            df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda
            hdf = HDFStore('data/fea sample/storage sample stage3.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test_df',df_final_test, format='table', data_columns=True)
            hdf.close()
        else:
            df final train = read hdf('data/fea sample/storage sample stage3.h5', 'train
            df final test = read hdf('data/fea sample/storage sample stage3.h5', 'test df
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [0]: def svd(x, S):
            try:
                 z = sadj_dict[x]
                 return S[z]
            except:
                 return [0,0,0,0,0,0]
In [0]: #for svd features to get feature vector creating a dict node val and inedx in svd
         sadj_col = sorted(train_graph.nodes())
         sadj dict = { val:idx for idx,val in enumerate(sadj col)}
In [0]: Adj = nx.adjacency_matrix(train_graph, nodelist=sorted(train_graph.nodes())).asfpt
In [0]: U, s, V = svds(Adj, k = 6)
         print('Adjacency matrix Shape',Adj.shape)
         print('U Shape',U.shape)
         print('V Shape', V.shape)
         print('s Shape',s.shape)
        Adjacency matrix Shape (1780722, 1780722)
        U Shape (1780722, 6)
        V Shape (6, 1780722)
        s Shape (6,)
```

```
In [0]: if not os.path.isfile('data/fea_sample/storage_sample_stage4.h5'):
           df final train[['svd u s 1', 'svd u s 2','svd u s 3', 'svd u s 4', 'svd u s 5
           df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_
           df final train.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5
           df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_
           df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df_final_test[['svd_u_s_1', 'svd_u_s_2','svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5'
           df_final_test.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5
           df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5'
           df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5
           df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           hdf = HDFStore('data/fea sample/storage sample stage4.h5')
           hdf.put('train_df',df_final_train, format='table', data_columns=True)
           hdf.put('test_df',df_final_test, format='table', data_columns=True)
           hdf.close()
```

In [0]: # prepared and stored the data from machine learning models
 # pelase check the FB_Models.ipynb

Preparing Data for Models

In [0]: #Importing Libraries

```
# please do go through this python notebook:
            import warnings
            warnings.filterwarnings("ignore")
            import csv
            import pandas as pd#pandas to create small dataframes
            import datetime #Convert to unix time
            import time #Convert to unix time
            # if numpy is not installed already : pip3 install numpy
            import numpy as np#Do aritmetic operations on arrays
            # matplotlib: used to plot graphs
            import matplotlib
            import matplotlib.pylab as plt
            import seaborn as sns#Plots
            from matplotlib import rcParams#Size of plots
            from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
            import math
            import pickle
            import os
            # to install xqboost: pip3 install xqboost
            import xgboost as xgb
            import warnings
            import networkx as nx
            import pdb
            import pickle
            from pandas import HDFStore,DataFrame
            from pandas import read hdf
            from scipy.sparse.linalg import svds, eigs
            import gc
            from tqdm import tqdm
            from sklearn.ensemble import RandomForestClassifier
            from sklearn.metrics import f1 score
   In [0]: #reading
            from pandas import read hdf
            df_final_train = read_hdf('storage_sample_stage4.h5', 'train_df',mode='r')
            df_final_test = read_hdf('storage_sample_stage4.h5', 'test_df',mode='r')
   In [0]: | df final train.columns
  Out[31]: Index(['source_node', 'destination_node', 'indicator_link',
                    jaccard_followers', 'jaccard_followees', 'cosine_followers',
                   'cosine_followees', 'num_followers_s', 'num_followees_s',
                   'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                   'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                   'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                   'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                   'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                   'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                   'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                   'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                   'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
Loading [MathJax]/jax/output/#TMP&SSPAnjeSTAX-Web/Size1/Regular/Main.js
```

```
In [0]: | df_final_test.columns
Out[32]: Index(['source node', 'destination node', 'indicator link',
                 'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                'cosine_followees', 'num_followers_s', 'num_followees_s',
                'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                 'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                 'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                 'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
               dtype='object')
In [0]: df final train['num followers s'].shape
Out[33]: (100002,)
In [0]: | y_train = df_final_train.indicator_link
         y test = df final test.indicator link
In [0]: df_final_train.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,i
```

df final test.drop(['source node', 'destination node', 'indicator link'],axis=1,in

```
In [0]: estimators = [10,50,100,250,450]
        train scores = []
        test scores = []
        for i in estimators:
            clf = RandomForestClassifier(bootstrap=True, class weight=None, criterion='gi
                     max_depth=5, max_features='auto', max_leaf_nodes=None,
                     min impurity decrease=0.0, min impurity split=None,
                     min samples leaf=52, min samples split=120,
                     min weight fraction leaf=0.0, n estimators=i, n jobs=-1, random state=
            clf.fit(df_final_train,y_train)
            train sc = f1 score(y train,clf.predict(df final train))
            test_sc = f1_score(y_test,clf.predict(df_final_test))
            test_scores.append(test_sc)
            train scores.append(train sc)
            print('Estimators = ',i,'Train Score',train sc,'test Score',test sc)
        plt.plot(estimators,train_scores,label='Train Score')
        plt.plot(estimators,test scores,label='Test Score')
        plt.xlabel('Estimators')
        plt.ylabel('Score')
        plt.title('Estimators vs score at depth of 5')
```

Estimators = 10 Train Score 0.9063252121775113 test Score 0.8745605278006858

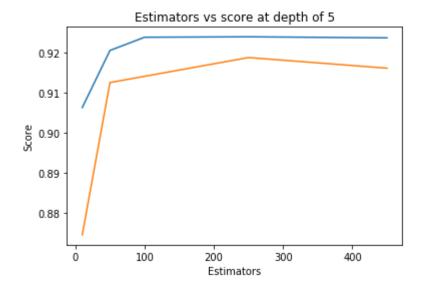
Estimators = 50 Train Score 0.9205725512208812 test Score 0.9125653355634538

Estimators = 100 Train Score 0.9238690848446947 test Score 0.9141199714153599

Estimators = 250 Train Score 0.9239789348046863 test Score 0.9188007232664732

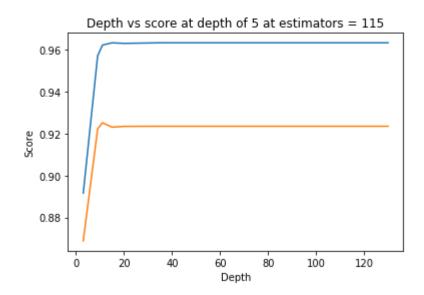
Estimators = 450 Train Score 0.9237190618658074 test Score 0.9161507685828595

Out[6]: Text(0.5,1, 'Estimators vs score at depth of 5')



```
In [0]: depths = [3,9,11,15,20,35,50,70,130]
        train scores = []
        test scores = []
        for i in depths:
            clf = RandomForestClassifier(bootstrap=True, class weight=None, criterion='gi
                     max_depth=i, max_features='auto', max_leaf_nodes=None,
                     min impurity decrease=0.0, min impurity split=None,
                     min samples leaf=52, min samples split=120,
                     min weight fraction leaf=0.0, n estimators=115, n jobs=-1, random state
            clf.fit(df_final_train,y_train)
            train sc = f1 score(y train,clf.predict(df final train))
            test_sc = f1_score(y_test,clf.predict(df_final_test))
            test scores.append(test sc)
            train scores.append(train sc)
            print('depth = ',i,'Train Score',train sc,'test Score',test sc)
        plt.plot(depths,train_scores,label='Train Score')
        plt.plot(depths,test scores,label='Test Score')
        plt.xlabel('Depth')
        plt.ylabel('Score')
        plt.title('Depth vs score at depth of 5 at estimators = 115')
        plt.show()
```

depth = 3 Train Score 0.8916120853581238 test Score 0.8687934859875491
depth = 9 Train Score 0.9572226298198419 test Score 0.9222953031452904
depth = 11 Train Score 0.9623451340902863 test Score 0.9252318758281279
depth = 15 Train Score 0.9634267621927706 test Score 0.9231288356496615
depth = 20 Train Score 0.9631629153051491 test Score 0.9235051024711141
depth = 35 Train Score 0.9634333127085721 test Score 0.9235601652753184
depth = 50 Train Score 0.9634333127085721 test Score 0.9235601652753184
depth = 70 Train Score 0.9634333127085721 test Score 0.9235601652753184
depth = 130 Train Score 0.9634333127085721 test Score 0.9235601652753184



```
In [0]: from sklearn.metrics import f1 score
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1 score
        from sklearn.model selection import RandomizedSearchCV
        from scipy.stats import randint as sp randint
        from scipy.stats import uniform
        param_dist = {"n_estimators":sp_randint(105,125),
                       "max depth": sp randint(10,15),
                       "min_samples_split": sp_randint(110,190),
                       "min_samples_leaf": sp_randint(25,65)}
        clf = RandomForestClassifier(random state=25,n jobs=-1)
        rf_random = RandomizedSearchCV(clf, param_distributions=param_dist,
                                            n_iter=5,cv=10,scoring='f1',random_state=25)
        rf_random.fit(df_final_train,y_train)
        print('mean test scores',rf_random.cv_results_['mean_test_score'])
        print('mean train scores',rf random.cv results ['mean train score'])
```

In [0]: print(rf_random.best_estimator_)

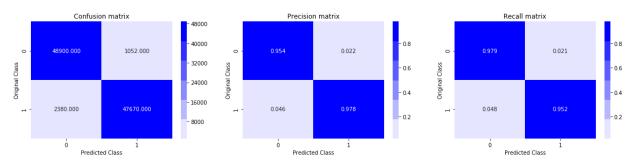
- In [0]: clf.fit(df_final_train,y_train)
 y_train_pred = clf.predict(df_final_train)
 y_test_pred = clf.predict(df_final_test)
- In [0]: from sklearn.metrics import f1_score
 print('Train f1 score',f1_score(y_train,y_train_pred))
 print('Test f1 score',f1_score(y_test,y_test_pred))

Train f1 score 0.9652533106548414 Test f1 score 0.9241678239279553

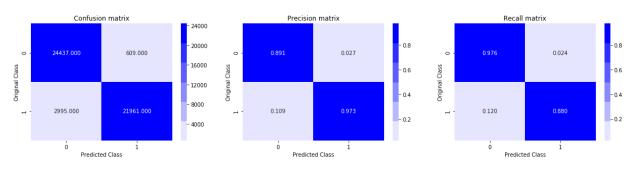
```
In [0]:
        from sklearn.metrics import confusion matrix
        def plot confusion matrix(test y, predict y):
            C = confusion_matrix(test_y, predict_y)
            A = (((C.T)/(C.sum(axis=1))).T)
            B = (C/C.sum(axis=0))
            plt.figure(figsize=(20,4))
            labels = [0,1]
            # representing A in heatmap format
            cmap=sns.light_palette("blue")
            plt.subplot(1, 3, 1)
            sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklab
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Confusion matrix")
            plt.subplot(1, 3, 2)
            sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklab
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Precision matrix")
            plt.subplot(1, 3, 3)
            # representing B in heatmap format
            sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklab
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Recall matrix")
            plt.show()
```

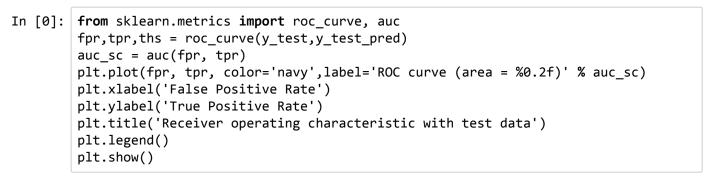
In [0]: print('Train confusion_matrix') plot_confusion_matrix(y_train,y_train_pred) print('Test confusion_matrix') plot_confusion_matrix(y_test,y_test_pred)

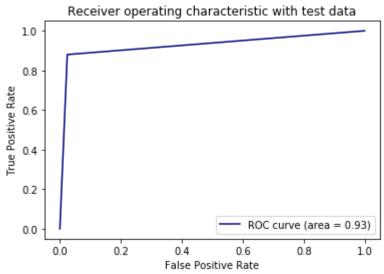
Train confusion_matrix



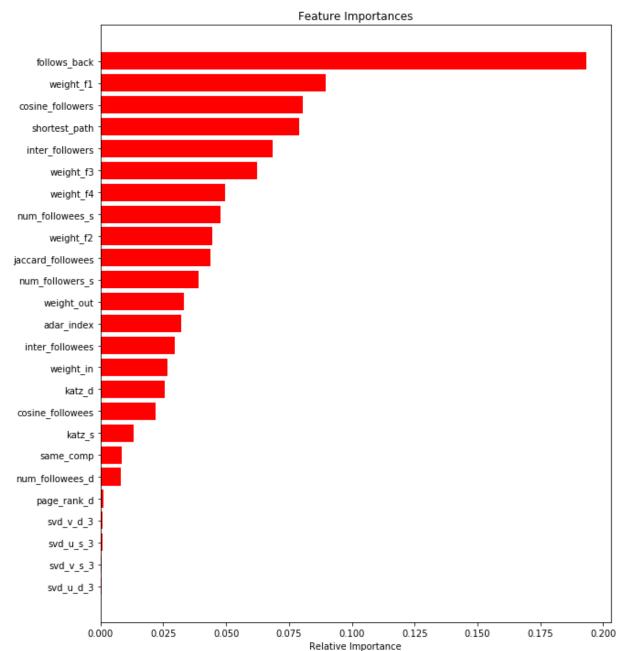
Test confusion_matrix







```
In [0]: features = df_final_train.columns
    importances = clf.feature_importances_
    indices = (np.argsort(importances))[-25:]
    plt.figure(figsize=(10,12))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='r', align='center')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```



Adding another feature called Preferential Attachment with followers and followees data of vertex. you can check about Preferential Attachment in below link

http://be.amazd.com/link-prediction/ (http://be.amazd.com/link-prediction/)
Loading [MathJax]/jax/butput/111ML-CSS/joints/STIX-Web/Size1/Regular/Main.js

```
In [0]: train graph=nx.read edgelist('train pos after eda.csv',delimiter=',',create using
         test graph=nx.read edgelist('test pos after eda.csv',delimiter=',',create using=n
In [0]: def train preferential attachment(final train data):
             try:
                  final_train_data = final_train_data.values.tolist()
                  src = nx.neighbors(train graph, final train data[0])
                  dest = nx.neighbors(train graph, final train data[1])
                  len src = len(set([i for i in src]))
                  len dest = len(set([j for j in dest]))
                  return len src * len dest
             except:
                  return 0
         def test preferential attachment(final test data):
             try:
                  final test data = final test data.values.tolist()
                  src = nx.neighbors(test_graph, final_test_data[0])
                  dest = nx.neighbors(test_graph, final_test_data[1])
                  len src = len(set([i for i in src]))
                  len_dest = len(set([j for j in dest]))
                  return len src * len dest
             except:
                  return 0
In [0]: df final train['preferential attachment'] = df final train[['source node', 'desti
         df_final_test['preferential_attachment'] = df_final_train[['source_node', 'destin']
In [0]: | df_final_train.columns
Out[6]: Index(['source node', 'destination node', 'indicator link',
                  jaccard_followers', 'jaccard_followees', 'cosine_followers',
                 'cosine_followees', 'num_followers_s', 'num_followees_s',
                 'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                 'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                 'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                 'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                 'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                 'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                 'preferential attachment'],
                dtype='object')
```

Adding feature called svd_dot. you can calculate svd_dot as Dot product between sourse node svd and destination node svd features. you can read about this in below pdf

https://storage.googleapis.com/kaggle-forum-message-attachments/2594/supervised_link_prediction.pdf (https://storage.googleapis.com/kaggle-forum-message-attachments/2594/supervised_link_prediction.pdf)

```
In [0]: df_final_train['svd_dot_u'] = df_final_train.apply(svd_dot_u, axis=1)
    df_final_train['svd_dot_v'] = df_final_train.apply(svd_dot_v, axis=1)
    df_final_test['svd_dot_u'] = df_final_test.apply(svd_dot_u, axis=1)
    df_final_test['svd_dot_v'] = df_final_test.apply(svd_dot_v, axis=1)
```

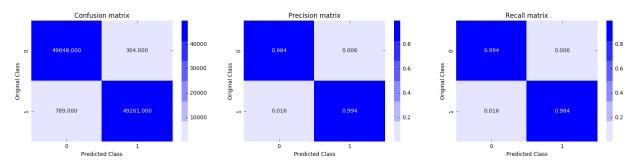
```
In [0]: | df final train.columns
Out[10]: Index(['source node', 'destination node', 'indicator link',
                  'jaccard_followers', 'jaccard_followees', 'cosine_followers', 'cosine_followees', 'num_followers_s', 'num_followees_s',
                  'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                  'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                  'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                  'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                  'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                  'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                  'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                  'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                  'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                  'preferential_attachment', 'svd_dot_u', 'svd_dot_v'],
                 dtype='object')
In [0]: df_final_test.columns
Out[11]: Index(['source_node', 'destination_node', 'indicator_link',
                  'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                  'cosine_followees', 'num_followers_s', 'num_followees_s',
                  'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                  'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                  'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                  'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                  'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                  'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                  'preferential_attachment', 'svd_dot_u', 'svd_dot_v'],
                 dtype='object')
 In [0]: y train = df final train.indicator link
          y_test = df_final_test.indicator_link
 In [0]: | df_final_train.drop(['source_node', 'destination_node', 'indicator_link'], axis=1,i
          df_final_test.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,in
 In [0]: hdf = HDFStore('storage_sample_stage5.h5')
          hdf.put('train_df',df_final_train, format='table', data_columns=True)
          hdf.put('test df',df final test, format='table', data columns=True)
          hdf.close()
 In [0]: #reading
          from pandas import read hdf
          df final train = read hdf('storage sample stage5.h5', 'train df',mode='r')
          df final test = read hdf('storage sample stage5.h5', 'test df',mode='r')
```

Tuning hyperparameters for XG boost with all the above features and Loading [MathJax]/iz/het/killing the characteristic legular/Main.js

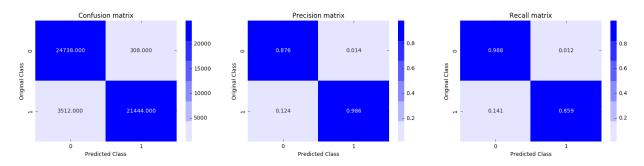
```
In [0]: | from xgboost import XGBClassifier
           from sklearn.model selection import RandomizedSearchCV
   In [0]: param grid = {'max depth': [2, 3, 4, 5, 6, 7, 8, 9, 10], 'n estimators': [5, 10,
   In [0]: random search xgb = RandomizedSearchCV(XGBClassifier(), param grid,
                                                   return train score = True, verbose = 2, n
           random_search_xgb.fit(df_final_train, y_train)
           Fitting 3 folds for each of 10 candidates, totalling 30 fits
           [Parallel(n jobs=-1)]: Using backend LokyBackend with 8 concurrent workers.
           [Parallel(n jobs=-1)]: Done 30 out of 30 | elapsed: 4.9min finished
  Out[16]: RandomizedSearchCV(cv='warn', error score='raise-deprecating',
                      estimator=XGBClassifier(base_score=0.5, booster='gbtree', colsample_b
           ylevel=1,
                  colsample bynode=1, colsample bytree=1, gamma=0, learning rate=0.1,
                  max delta step=0, max depth=3, min child weight=1, missing=None,
                  n_estimators=100, n_jobs=1, nthread=None,
                  objective='binary:logistic', random state=0, reg alpha=0,
                  reg lambda=1, scale pos weight=1, seed=None, silent=None,
                  subsample=1, verbosity=1),
                      fit params=None, iid='warn', n iter=10, n jobs=-1,
                     param distributions={'max depth': [2, 3, 4, 5, 6, 7, 8, 9, 10], 'n es
           timators': [5, 10, 50, 100, 200, 500, 1000]},
                      pre_dispatch='2*n_jobs', random_state=None, refit=True,
                      return train score=True, scoring=None, verbose=2)
   In [0]: print("Best Parameters: ", random_search_xgb.best_params_)
           print("Best Estimator: ", random_search_xgb.best_estimator_)
           bst = random_search_xgb.best_estimator_
           Best Parameters: {'max depth': 4, 'n estimators': 500}
           Best Estimator: XGBClassifier(base_score=0.5, booster='gbtree', colsample_byle
           vel=1,
                  colsample_bynode=1, colsample_bytree=1, gamma=0, learning_rate=0.1,
                  max_delta_step=0, max_depth=4, min_child_weight=1, missing=None,
                  n estimators=500, n jobs=1, nthread=None,
                  objective='binary:logistic', random_state=0, reg_alpha=0,
                  reg_lambda=1, scale_pos_weight=1, seed=None, silent=None,
                  subsample=1, verbosity=1)
   In [0]: y_train_pred = bst.predict(df_final_train)
           y test pred = bst.predict(df final test)
   In [0]: from sklearn.metrics import f1 score
           print('Train f1 score',f1 score(y train,y train pred))
           print('Test f1 score',f1_score(y_test,y_test_pred))
           Train f1 score 0.9890277568639261
           Test f1 score 0.918215295024407
Loading [MathJax]/jax/output/HTML-CSS/fonts/STIX-Web/Size1/Regular/Main.js
```

In [0]: print('Train confusion_matrix')
 plot_confusion_matrix(y_train,y_train_pred)
 print('Test confusion_matrix')
 plot_confusion_matrix(y_test,y_test_pred)

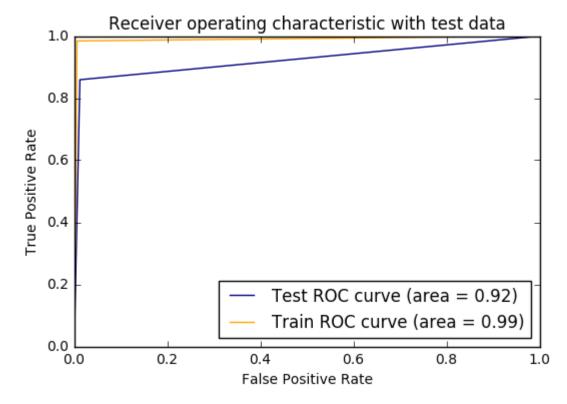
Train confusion_matrix



Test confusion_matrix



```
In [0]: from sklearn.metrics import roc_curve, auc
    fpr_test, tpr_test, ths_test = roc_curve(y_test,y_test_pred)
    auc_sc_test = auc(fpr_test, tpr_test)
    fpr_train, tpr_train, ths_train = roc_curve(y_train,y_train_pred)
    auc_sc_train = auc(fpr_train, tpr_train)
    plt.plot(fpr_test, tpr_test, color='navy',label='Test ROC curve (area = %0.2f)' %
    plt.plot(fpr_train, tpr_train, color='orange',label='Train ROC curve (area = %0.2f)' %
    plt.xlabel('False Positive Rate')
    plt.ylabel('True Positive Rate')
    plt.title('Receiver operating characteristic with test data')
    plt.legend(loc = 4)
    plt.show()
```



```
In [0]: print()
    from prettytable import PrettyTable
    ptable = PrettyTable()
    ptable.field_names=["Model Name","n_estimators","max_depth","Train F1-Score","Test
    ptable.add_row(["Random Forest","121","14","0.9652","0.9241"])
    ptable.add_row(["XGBoost","500","4","0.9890","0.9182"])
    print(ptable)
    print()
```

Model Name	n_estimators	max_depth	+ Train F1-Score +	Test F1-Score
Random Forest XGBoost		14 4	0.9652 0.9890	0.9241 0.9182

Procedure Followed:

- Loaded the data and did preprocessing and transformations.
- · Added features using techniques in Grapth Theory.
- Did Exploratory Data Analysis of features.
- Splitted the data into Train and Test.
- Trained a Random Forest Classifier by tuning hyperparameters using RandomSearchCV.
- Added two more features Preferential Attachment and SVD Dot product.
- Trained XGBoost Model by tuning hyperparameters using RandomSearchCV.
- Calculated the F1 Scores for both Train and Test data.