



CS-202

Dynamic Data Structures (Pt.4)

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Course Week

Course , Projects , Labs:

Monday	Tuesday	Wednesday	Thursday	Friday	Sunday
			Lab (8 Sections)		
	CLASS		CLASS		
PASS Session	PASS Session	Project DEADLINE	NEW Project	PASS Session	PASS Session



Your 8th Project Deadline is this Wednesday 4/17.

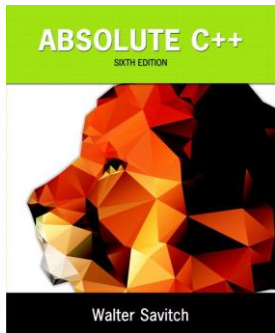
- PASS Sessions held Friday-Sunday-&-Monday-Tuesday, get all the help you need!
- 24-hrs delay after Project Deadline incurs 20% grade penalty.
- Past that, NO Project accepted. Better send what you have in time!

Today's Topics

Dynamic Data Structures

Stack(s)

- Array-based
- List-based
- Traversal
- Insertion
- Deletion
- Search



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What is a Stack?

- Data structure
 - that has homogeneous items or elements.
 - Elements are added and removed from the top of the stack
 - The last element to be added is the first to be removed
- LIFO:** Last In, First Out

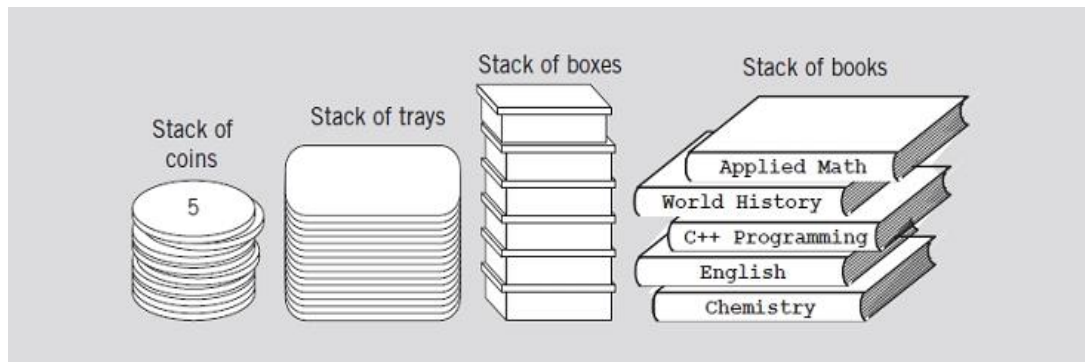
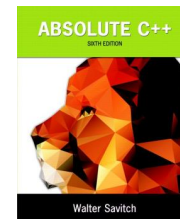
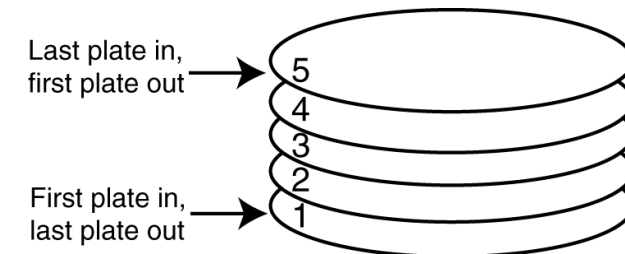
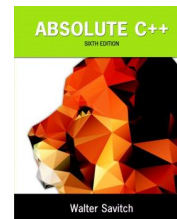
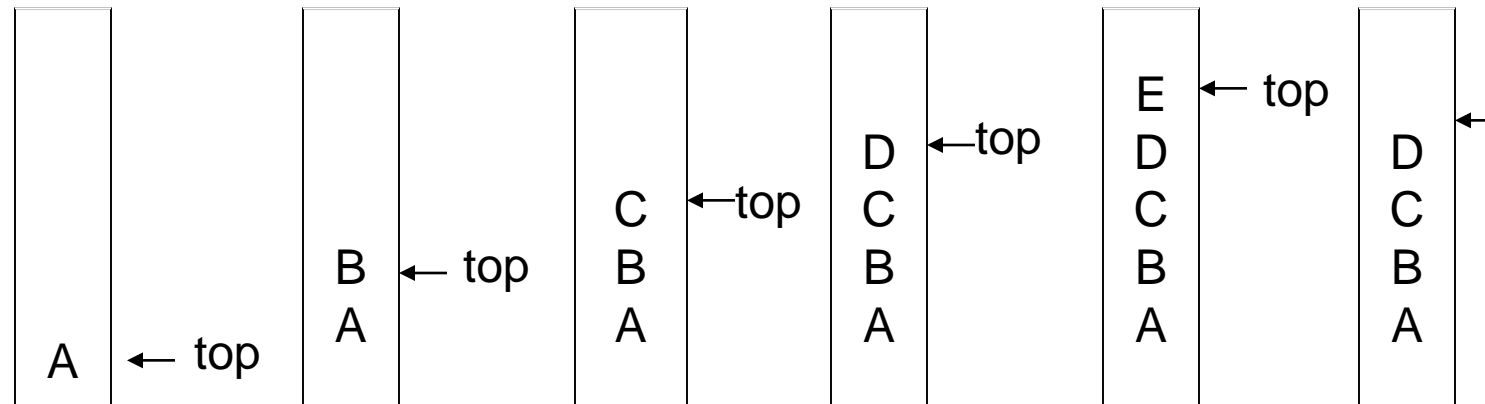


FIGURE 7-1 Various examples of stacks



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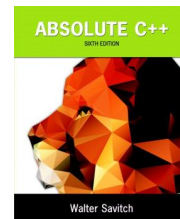
Last In First Out



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Stacks

- Some operations on a stack
 - `push` operation
 - Add element onto the stack
 - `top` operation
 - Retrieve top element of the stack
 - `pop` operation
 - Remove top element from the stack



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Stacks (cont'd.)

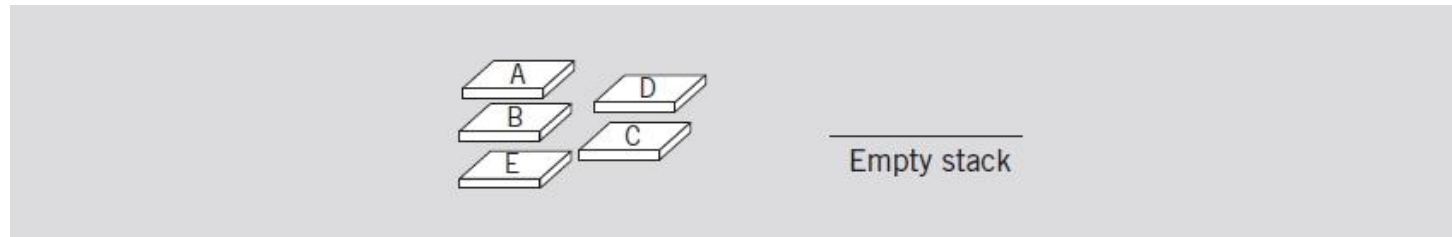


FIGURE 7-2 Empty stack

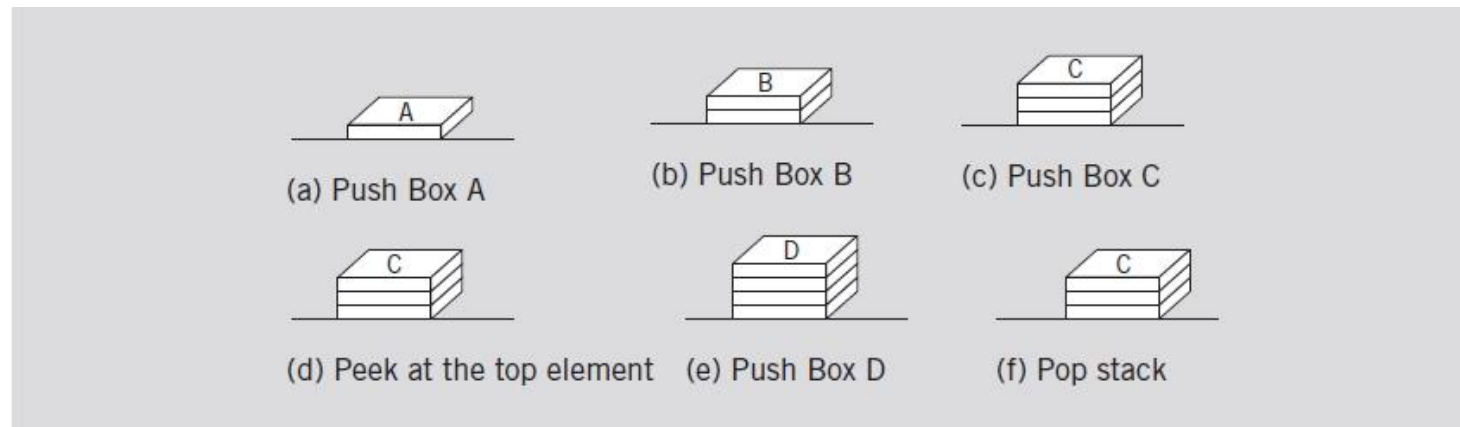
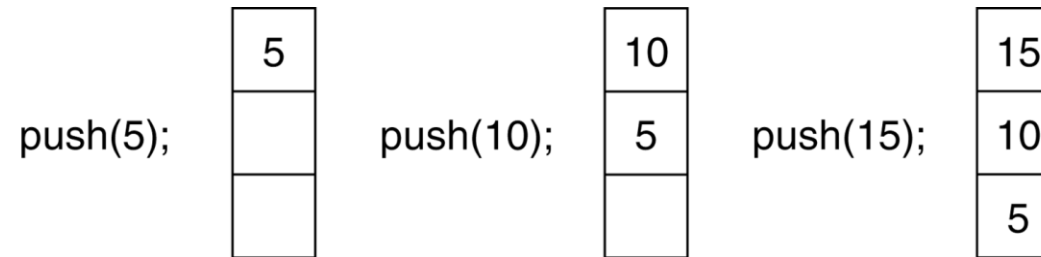


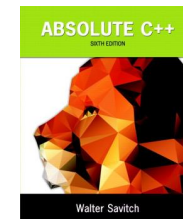
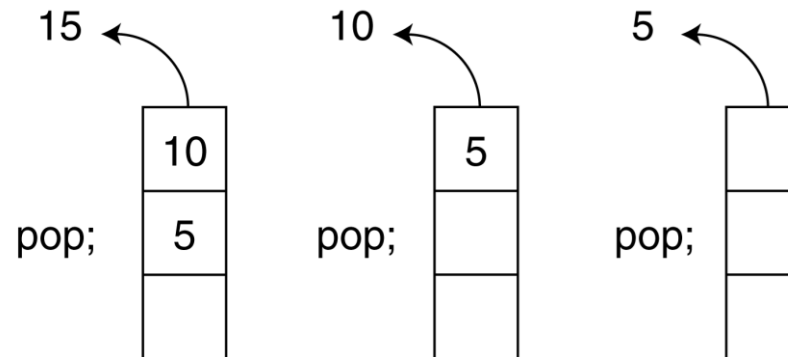
FIGURE 7-3 Stack operations

Push and Pop Example

The state of the stack after each of the `push` operations:



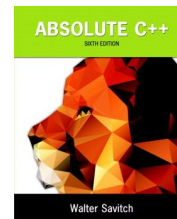
Now, suppose we execute three consecutive `pop` operations on the same stack:



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Stacks (cont'd.)

- Stack element removal
 - Occurs only if something is in the stack
- Stack element added only if room available
- `isFullStack` operation
 - Checks for full stack
- `isEmptyStack` operation
 - Checks for empty stack
- `initializeStack` operation
 - Initializes stack to an empty state



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Stacks (cont'd.)

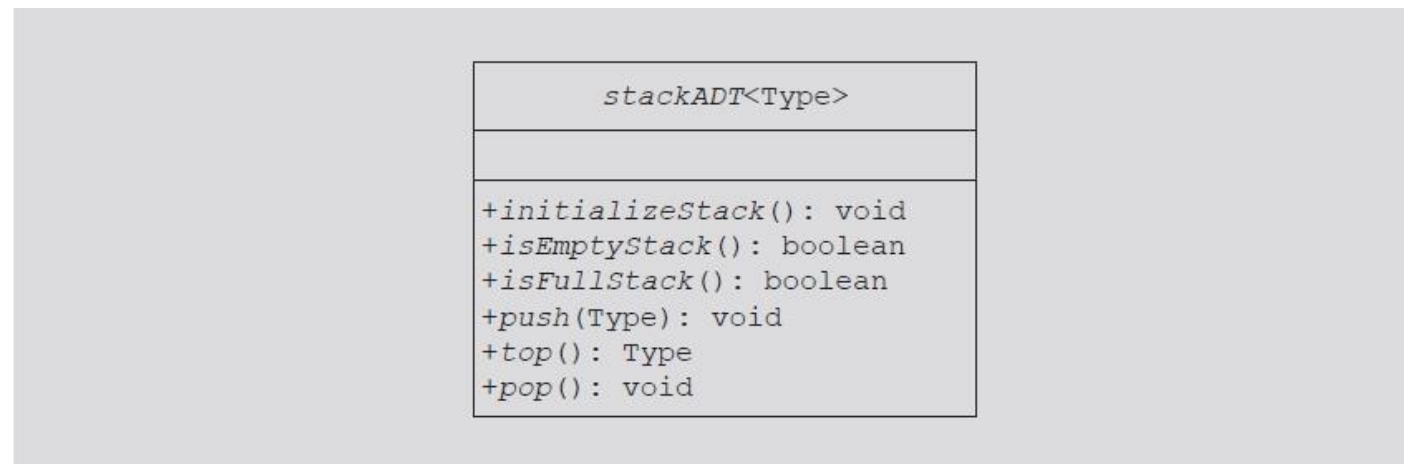


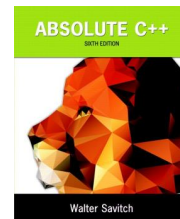
FIGURE 7-4 UML class diagram of the class `stackADT`



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Static and Dynamic Stacks

- Static Stacks
 - Fixed size
 - Can be implemented with an array
- Dynamic Stacks
 - Grow in size as needed
 - Can be implemented with a linked list



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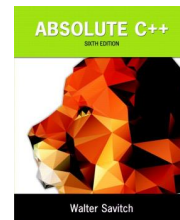
Implementation of Stacks as Arrays



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Implementation of Stacks as Arrays

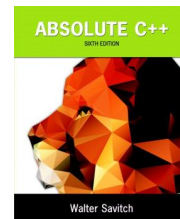
- Advantages
 - best performance
- Disadvantage
 - fixed size
- Basic implementation
 - initially empty array
 - field to record where the next data gets placed into
 - if array is full, push() returns false
 - otherwise adds it into the correct spot
 - if array is empty, pop() returns null
 - otherwise removes the next item in the stack



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Implementation of Stacks as Arrays

- First stack element
 - Put in first array slot
- Second stack element
 - Put in second array slot, and so on
- Top of stack
 - Index of last element added to stack
- Stack element accessed only through the top
 - Problem: array is a random access data structure
 - Solution: use another variable (`stackTop`)
 - Keeps track of the top position of the array



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Implementation of Stacks as Arrays (cont'd.)

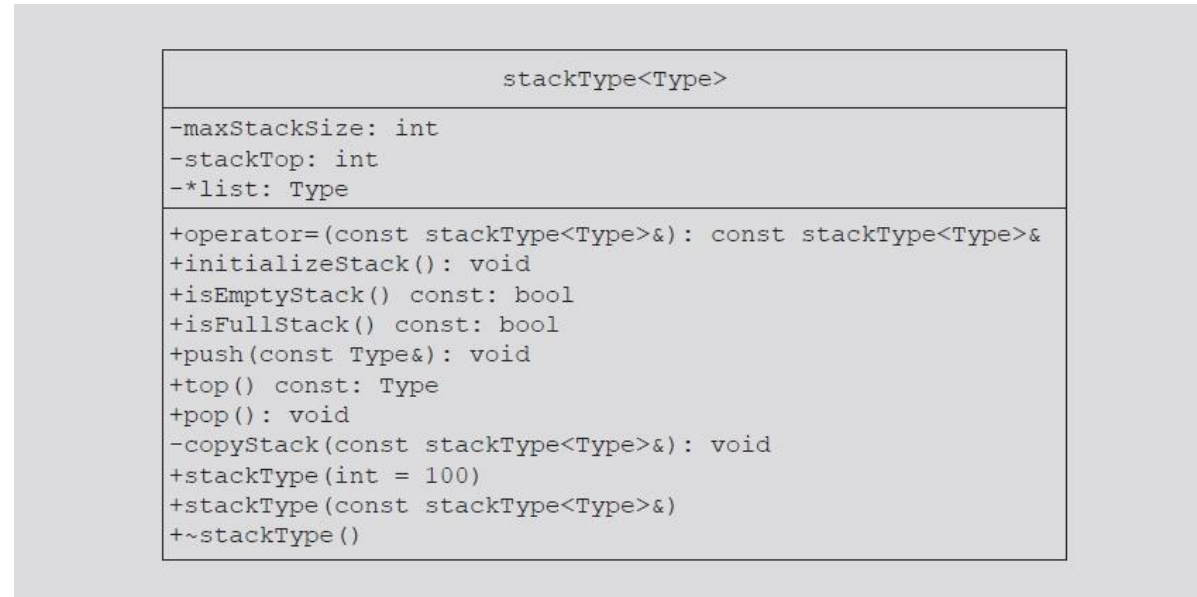


FIGURE 7-5 UML class diagram of the class `stackType`



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Implementation of Stacks as Arrays (cont'd.)

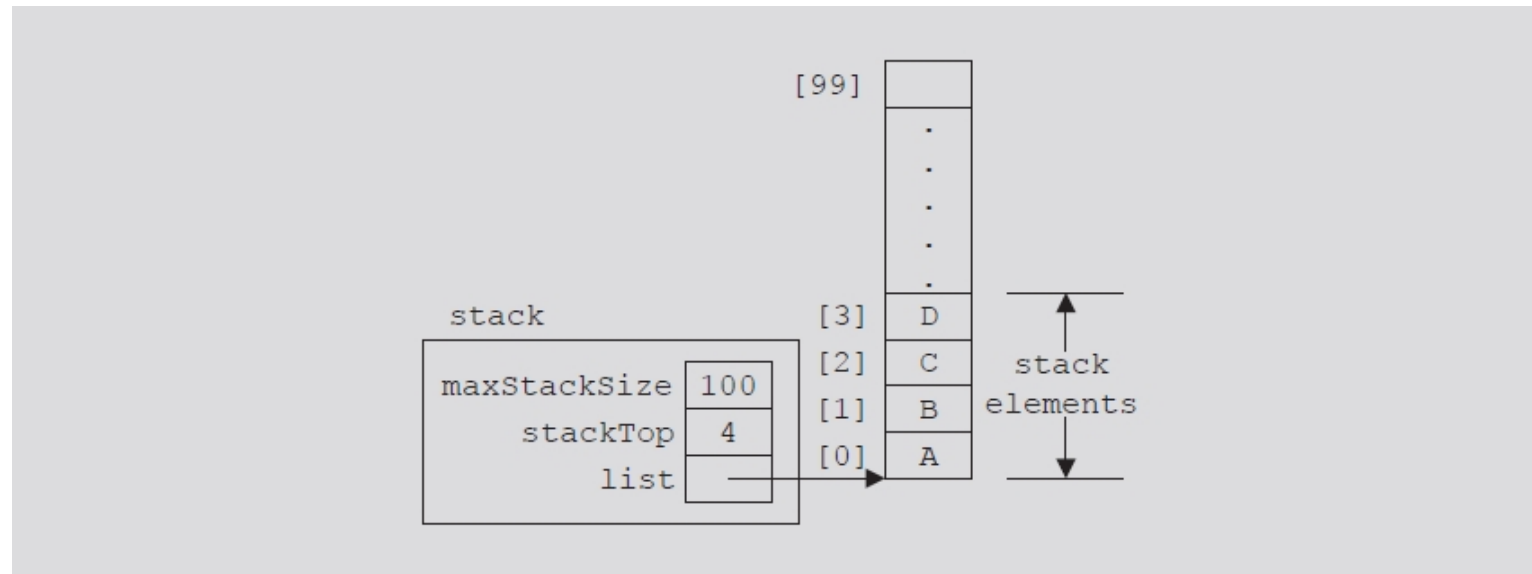
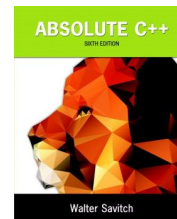


FIGURE 7-6 Example of a stack



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Initialize Stack

- Value of `stackTop` if stack empty
 - Set `stackTop` to zero to initialize the stack
- Definition of function `initializeStack`

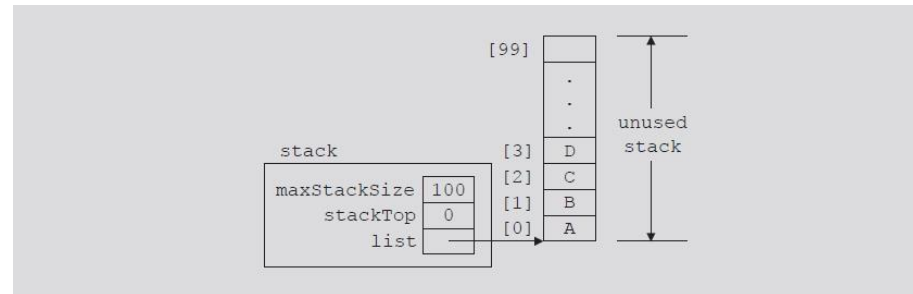
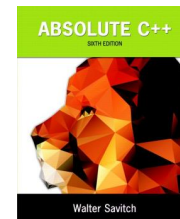


FIGURE 7-7 Empty stack

```
template <class Type>
void stackType<Type>::initializeStack()
{
    stackTop = 0;
} //end initializeStack
```

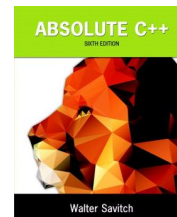


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Empty Stack

- Value of `stackTop` indicates if stack empty
 - If `stackTop = zero`: stack empty
 - Otherwise: stack not empty
- Definition of function `isEmptyStack`

```
template <class Type>
bool stackType<Type>::isEmptyStack() const
{
    return(stackTop == 0);
} //end isEmptyStack
```

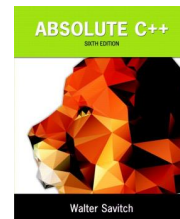


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Full Stack

- Stack full
 - If `stackTop` is equal to `maxStackSize`
- Definition of function `isFullStack`

```
template <class Type>
bool stackType<Type>::isFullStack() const
{
    return(stackTop == maxStackSize);
} //end isFullStack
```



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Push

- Two-step process
 - Store `newItem` in array component indicated by `stackTop`
 - Increment `stackTop`

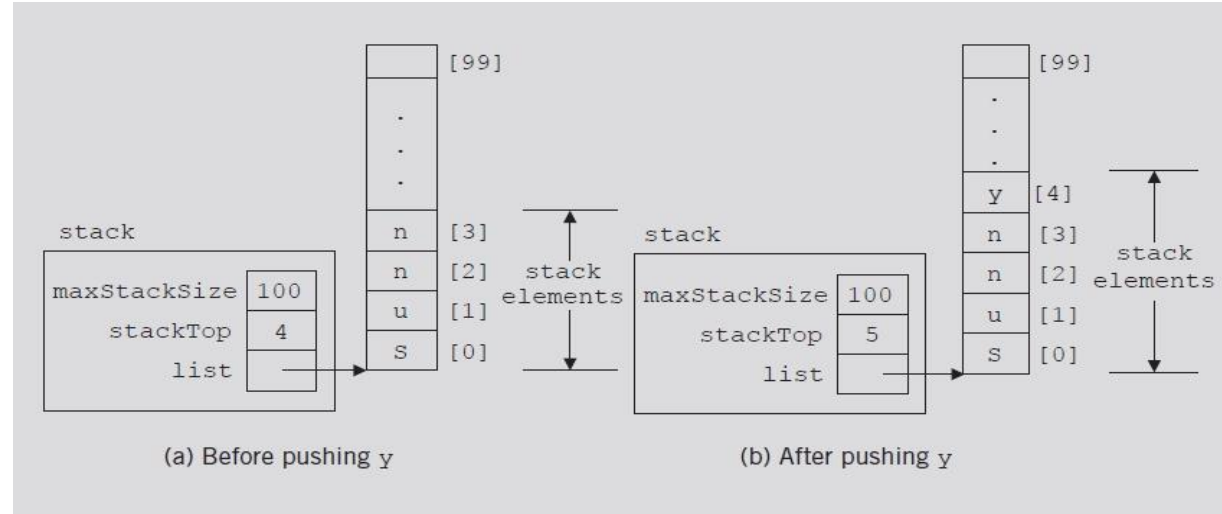
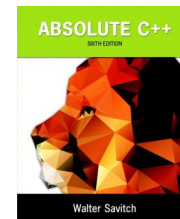


FIGURE 7-8 Stack before and after the `push` operation

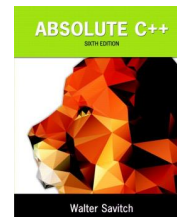


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Push (cont'd.)

- Definition of push operation

```
template <class Type>
void stackType<Type>::push(const Type& newItem)
{
    if (!isFullStack())
    {
        list[stackTop] = newItem; //add newItem at the top
        stackTop++; //increment stackTop
    }
    else
        cout << "Cannot add to a full stack." << endl;
} //end push
```



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Pop

- Remove (pop) element from stack
 - Decrement `stackTop` by one

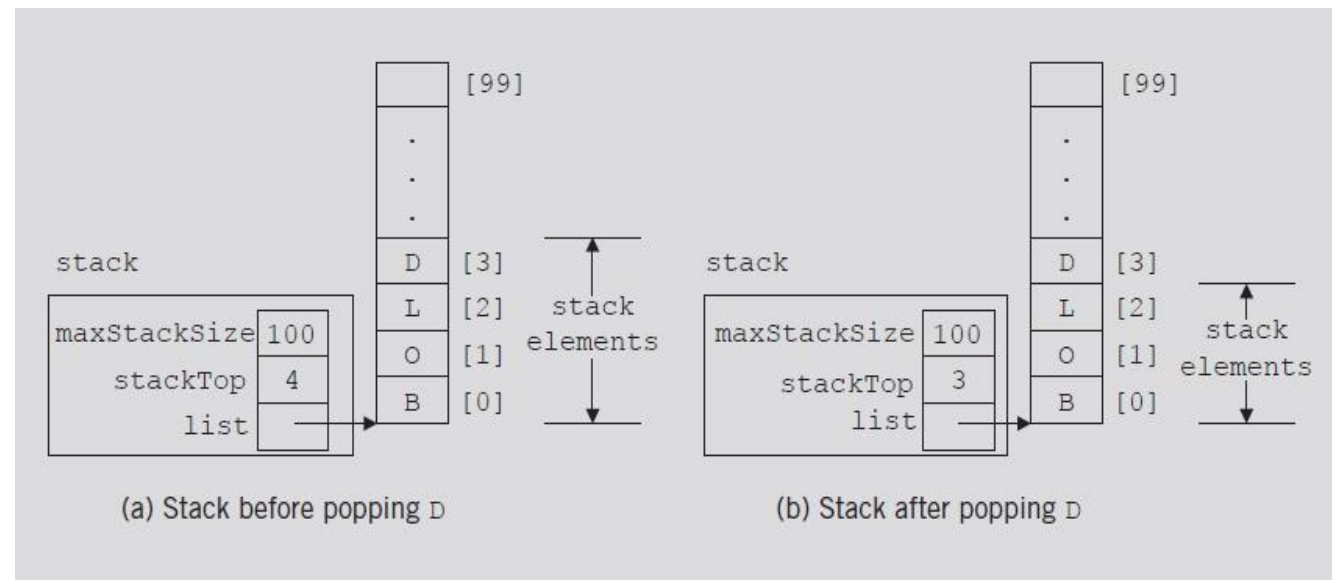
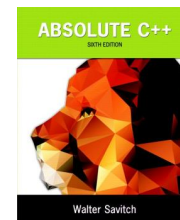


FIGURE 7-9 Stack before and after the `pop` operation

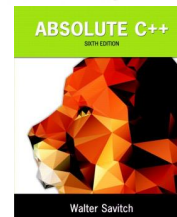


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Pop (cont'd.)

- Definition of `pop` operation
- Underflow
 - Removing an item from an empty stack
 - Check within `pop` operation (see below)
 - Check before calling function `pop`

```
template <class Type>
void stackType<Type>::pop()
{
    if (!isEmptyStack())
        stackTop--;    //decrement stackTop
    else
        cout << "Cannot remove from an empty stack." << endl;
} //end pop
```



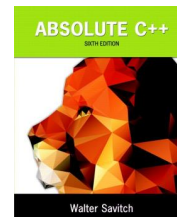
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Copy Stack

- Definition of function `copyStack`

```
template <class Type>
void stackType<Type>::copyStack(const stackType<Type>& otherStack)
{
    delete [] list;
    maxStackSize = otherStack.maxStackSize;
    stackTop = otherStack.stackTop;
    list = new Type[maxStackSize];

    //copy otherStack into this stack
    for (int j = 0; j < stackTop; j++)
        list[j] = otherStack.list[j];
} //end copyStack
```



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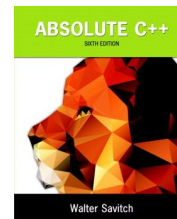
Constructor and Destructor

```
template <class Type>
stackType<Type>::stackType(int stackSize)
{
    if (stackSize <= 0)
    {
        cout << "Size of the array to hold the stack must "
              << "be positive." << endl;
        cout << "Creating an array of size 100." << endl;

        maxStackSize = 100;
    }
    else
        maxStackSize = stackSize;    //set the stack size to
                                     //the value specified by
                                     //the parameter stackSize

    stackTop = 0;                    //set stackTop to 0
    list = new Type[maxStackSize];   //create the array to
                                     //hold the stack elements
} //end constructor

template <class Type>
stackType<Type>::~~stackType() //destructor
{
    delete [] list; //deallocate the memory occupied
                  //by the array
} //end destructor
```



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Copy Constructor

- Definition of the copy constructor

```
template <class Type>
stackType<Type>::stackType(const stackType<Type>& otherStack)
{
    list = NULL;

    copyStack(otherStack);
} //end copy constructor
```



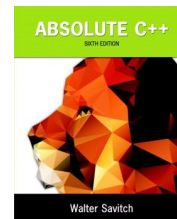
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Overloading the Assignment Operator (=)

- Classes with pointer member variables
 - Assignment operator must be explicitly overloaded
- Function definition to overload assignment

```
template <class Type>
const stackType<Type>& stackType<Type>::operator=
    (const stackType<Type>& otherStack)
{
    if (this != &otherStack) //avoid self-copy
        copyStack(otherStack);

    return *this;
} //end operator=
```



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Stack Header File

- `myStack.h`
 - Header file name containing `class` `stackType` definition

```
//Header file: myStack.h
```

```
#ifndef H_StackType  
#define H_StackType
```

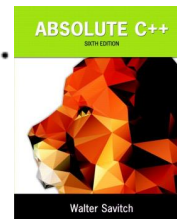
```
#include <iostream>  
#include <cassert>
```

```
#include "stackADT.h"
```

```
using namespace std;
```

```
//Place the definition of the class template stackType, as given  
//previously in this chapter, here.
```

```
//Place the definitions of the member functions as discussed here.  
#endif
```



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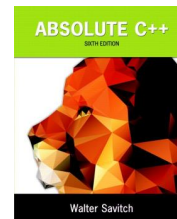
Implementation of Stacks as Linked List



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Linked Implementation of Stacks

- Disadvantage of array (linear) stack representation
 - Fixed number of elements can be pushed onto stack
- Solution
 - Use pointer variables to dynamically allocate, deallocate memory
 - Use linked list to dynamically organize data
- Value of `stackTop`: linear representation
 - Indicates number of elements in the stack
 - Gives index of the array
 - Value of `stackTop - 1`
 - Points to top item in the stack



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Implementing a Stack: Linked List

- Advantages:
 - always constant time to push or pop an element
 - can grow to an infinite size
- Disadvantages
 - the common case is the slowest of all the implementations
 - can grow to an infinite size
- Basic implementation
 - list is initially empty
 - *push()* method adds a new item to the head of the list
 - *pop()* method removes the head of the list



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Linked Implementation of Stacks (cont'd.)

- Value of `stackTop`: linked representation
 - Locates top element in the stack
 - Gives address (memory location) of the top element of the stack



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Linked Implementation of Stacks (cont'd.)

- Example 7-2
 - Stack: object of type `linkedStackType`

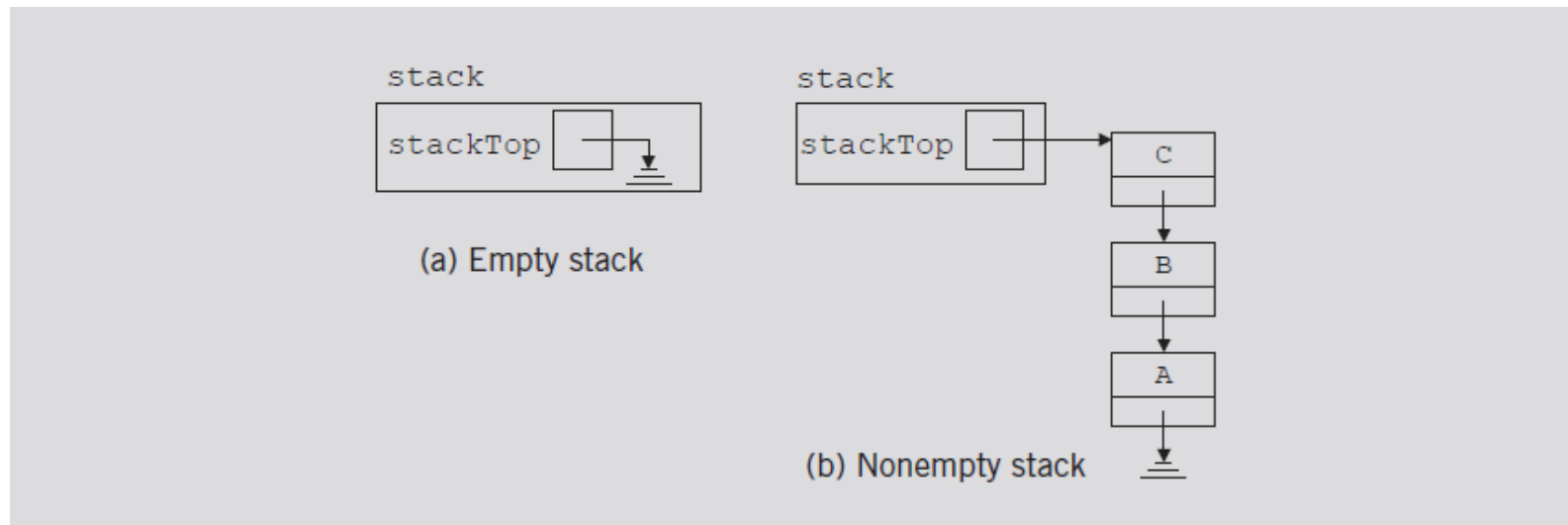
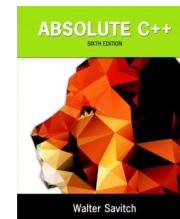


FIGURE 7-10 Empty and nonempty linked stacks



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Default Constructor

- When stack object declared
 - Initializes stack to an empty state
 - Sets `stackTop` to `NULL`
- Definition of the default constructor

```
template <class Type>
linkedStackType<Type>::linkedStackType()
{
    stackTop = NULL;
}
```

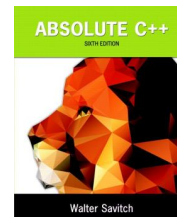


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Empty Stack and Full Stack

- Stack empty if `stackTop` is `NULL`
- Stack never full
 - Element memory allocated/deallocated dynamically
 - ```
template <class Type>
bool linkedStackType<Type>::isEmptyStack() const
{
 return(stackTop == NULL);
} //end isEmptyStack

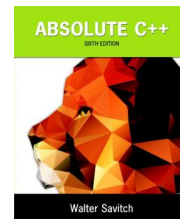
template <class Type>
bool linkedStackType<Type>::isFullStack() const
{
 return false;
} //end isFullStack
```



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# Initialize Stack

- Reinitializes stack to an empty state
- Because stack might contain elements and you are using a linked implementation of a stack
  - Must deallocate memory occupied by the stack elements, set `stackTop` to `NULL`
- Definition of the `initializeStack` function



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# Initialize Stack (cont'd.)

```
template <class Type>
void linkedStackType<Type>:: initializeStack()
{
 nodeType<Type> *temp; //pointer to delete the node

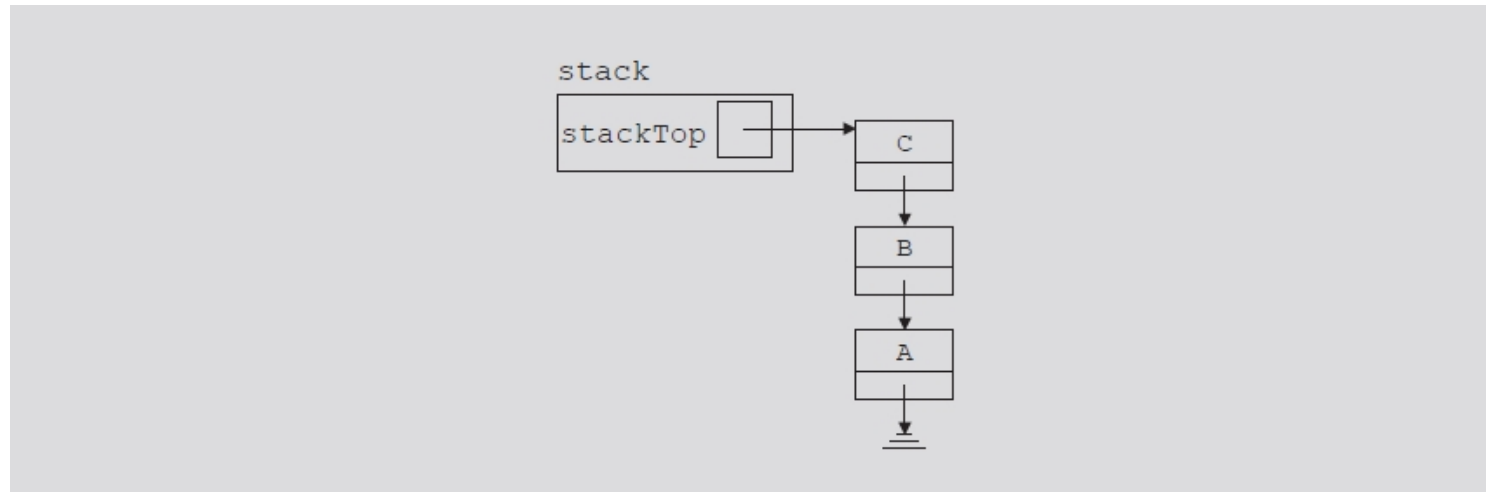
 while (stackTop != NULL) //while there are elements in
 //the stack
 {
 temp = stackTop; //set temp to point to the
 //current node
 stackTop = stackTop->link; //advance stackTop to the
 //next node
 delete temp; //deallocate memory occupied by temp
 }
} //end initializeStack
```



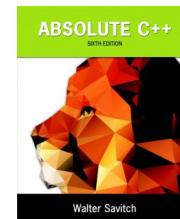
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# Push

- `newElement` added at the beginning of the linked list pointed to by `stackTop`
- Value of pointer `stackTop` updated

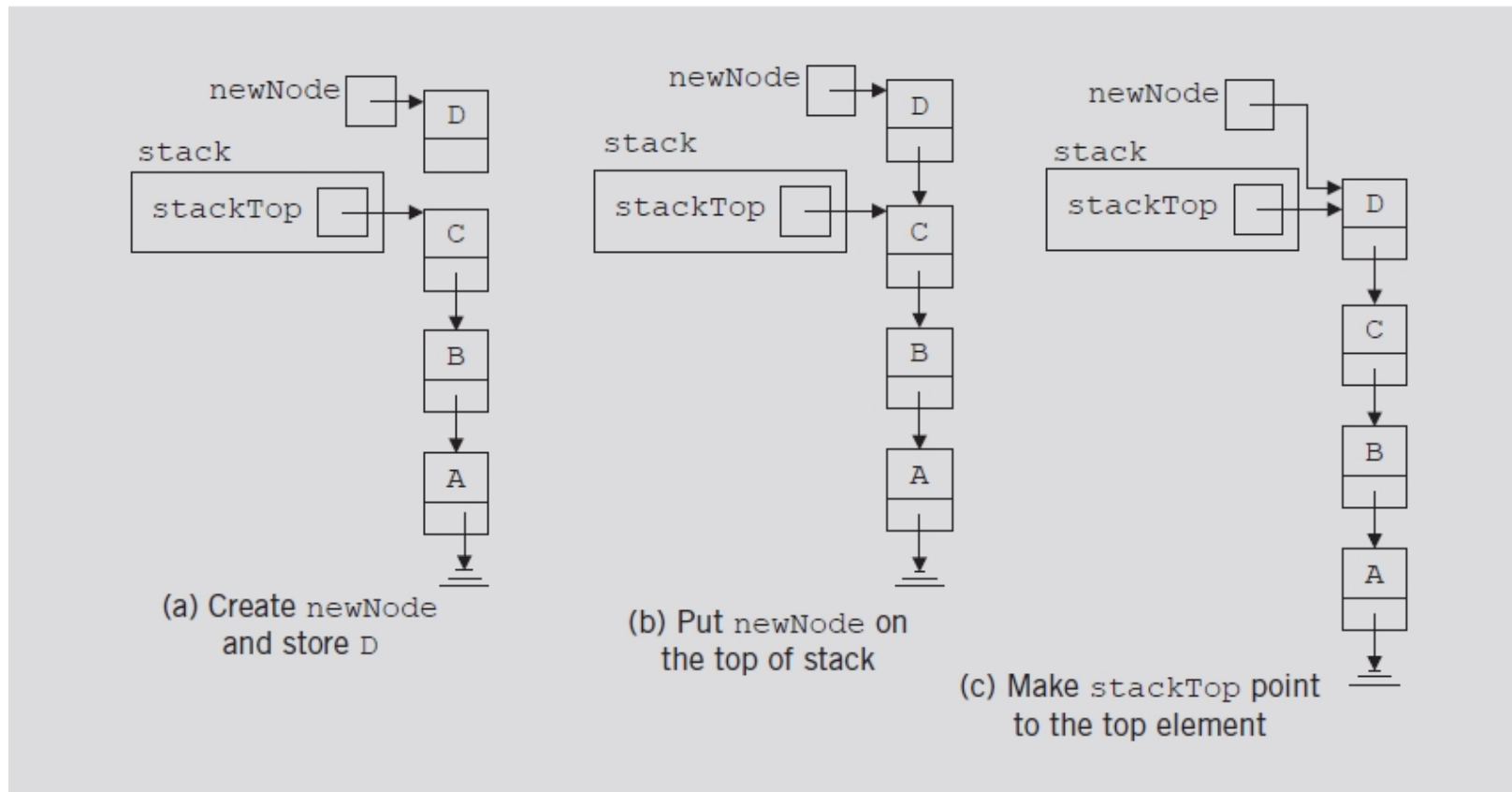


**FIGURE 7-11** Stack before the `push` operation



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# Push (cont'd.)



**FIGURE 7-12** Push operation



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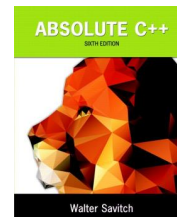
# Push (cont'd.)

- Definition of the `push` function

```
template <class Type>
void linkedStackType<Type>::push(const Type& newElement)
{
 nodeType<Type> *newNode; //pointer to create the new node

 newNode = new nodeType<Type>; //create the node

 newNode->info = newElement; //store newElement in the node
 newNode->link = stackTop; //insert newNode before stackTop
 stackTop = newNode; //set stackTop to point to the
 //top node
} //end push
```



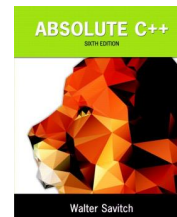
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# Return the Top Element

- Returns information of the node to which `stackTop` pointing
- Definition of the `top` function

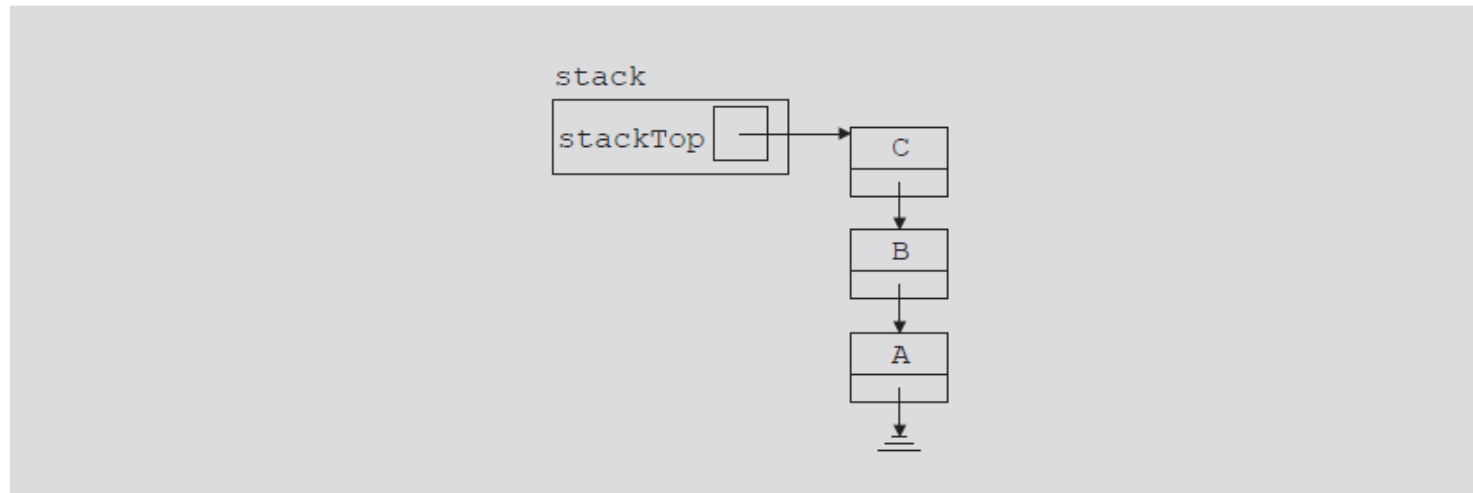
```
template <class Type>
Type linkedStackType<Type>::top() const
{
 assert(stackTop != NULL); //if stack is empty,
 //terminate the program
 return stackTop->info; //return the top element
} //end top
```



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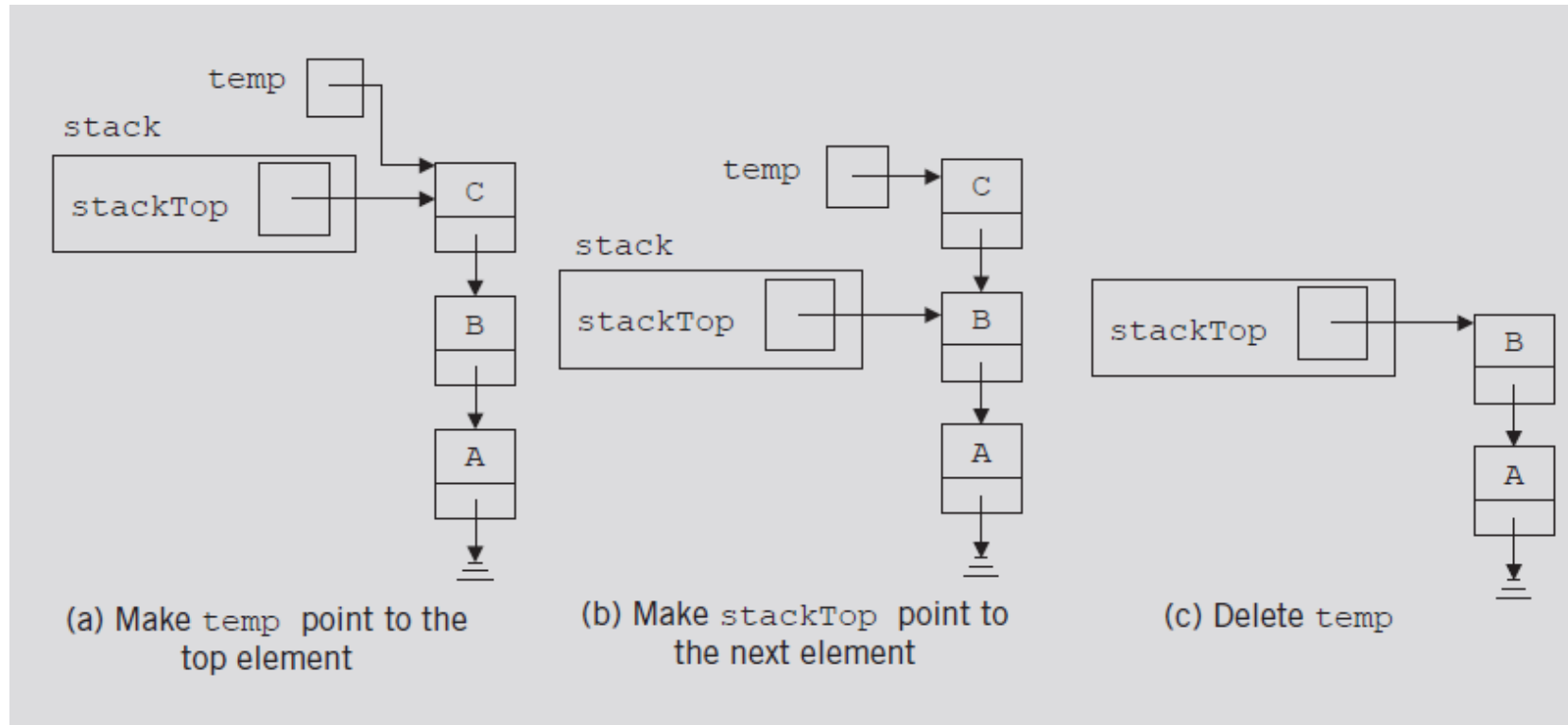
# Pop

- Removes top element of the stack
  - Node pointed to by `stackTop` removed
  - Value of pointer `stackTop` updated

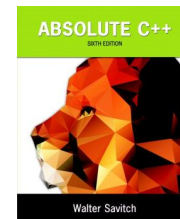


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# Pop (cont'd.)



**FIGURE 7-14** Pop operation



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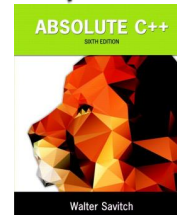
# Pop (cont'd.)

- Definition of the `pop` function

```
template <class Type>
void linkedStackType<Type>::pop()
{
 nodeType<Type> *temp; //pointer to deallocate memory

 if (stackTop != NULL)
 {
 temp = stackTop; //set temp to point to the top node

 stackTop = stackTop->link; //advance stackTop to the
 //next node
 delete temp; //delete the top node
 }
 else
 cout << "Cannot remove from an empty stack." << endl;
} //end pop
```



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# Copy Stack

- Makes an identical copy of a stack
- Definition similar to the definition of `copyList` for linked lists
- Definition of the `copyStack` function



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```

template <class Type>
void linkedStackType<Type>::copyStack
 (const linkedStackType<Type>& otherStack)
{
 nodeType<Type> *newNode, *current, *last;

 if (stackTop != NULL) //if stack is nonempty, make it empty
 initializeStack();

 if (otherStack.stackTop == NULL)
 stackTop = NULL;
 else
 {
 current = otherStack.stackTop; //set current to point
 //to the stack to be copied

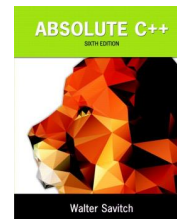
 //copy the stackTop element of the stack
 stackTop = new nodeType<Type>; //create the node

 stackTop->info = current->info; //copy the info
 stackTop->link = NULL; //set the link field to NULL
 last = stackTop; //set last to point to the node
 current = current->link; //set current to point to the
 //next node

 //copy the remaining stack
 while (current != NULL)
 {
 newNode = new nodeType<Type>;

 newNode->info = current->info;
 newNode->link = NULL;
 last->link = newNode;
 last = newNode;
 current = current->link;
 } //end while
 } //end else
} //end copyStack

```



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# Constructors and Destructors

- Definition of the functions to implement the copy constructor and the destructor

```
//copy constructor
template <class Type>
linkedStackType<Type>::linkedStackType(
 const linkedStackType<Type>& otherStack)
{
 stackTop = NULL;
 copyStack(otherStack);
} //end copy constructor
```

```
//destructor
template <class Type>
linkedStackType<Type>::~~linkedStackType()
{
 initializeStack();
} //end destructor
```



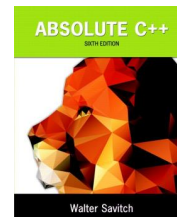
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# Overloading the Assignment Operator (=)

- Definition of the functions to overload the assignment operator

```
template <class Type>
const linkedStackType<Type>& linkedStackType<Type>::operator=
 (const linkedStackType<Type>& otherStack)
{
 if (this != &otherStack) //avoid self-copy
 copyStack(otherStack);

 return *this;
} //end operator=
```

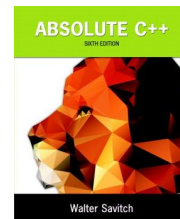


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# Stack Applications

- Stacks are a very common data structure
  - compilers
    - parsing data between delimiters (brackets)
  - operating systems
    - program stack
  - virtual machines
    - manipulating numbers
      - pop 2 numbers off stack, do work (such as add)
      - push result back on stack and repeat
  - artificial intelligence
    - finding a path



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# Application of Stacks: Postfix Expressions Calculator

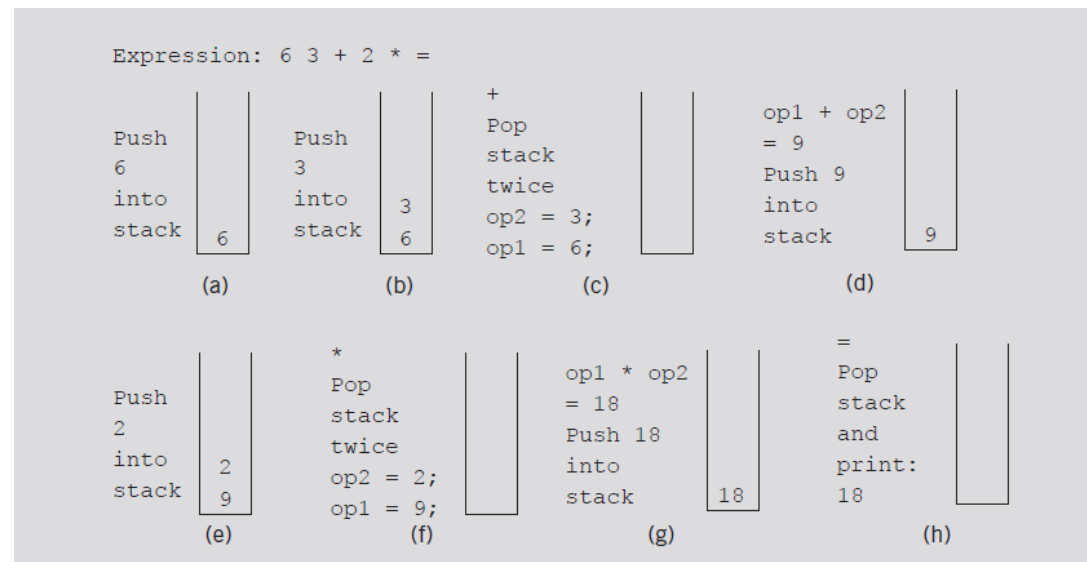
- Arithmetic notations
  - Infix notation: operator between operands
  - Prefix (Polish) notation: operator precedes operands
  - Reverse Polish notation: operator follows operands
- Stack use in compilers
  - Translate infix expressions into some form of postfix notation
  - Translate postfix expression into machine code



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# Application of Stacks: Postfix Expressions Calculator (cont'd.)

- Postfix expression:  $6\ 3\ +\ 2\ *\ =$



**FIGURE 7-15** Evaluating the postfix expression:  $6\ 3\ +\ 2\ *\ =$

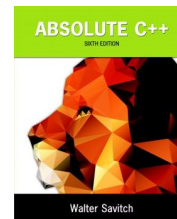


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# Application of Stacks: Postfix Expressions Calculator (cont'd.)

- Main algorithm pseudocode
  - Broken into four functions for simplicity
    - Function `evaluateExpression`
    - Function `evaluateOpr`
    - Function `discardExp`
    - Function `printResult`

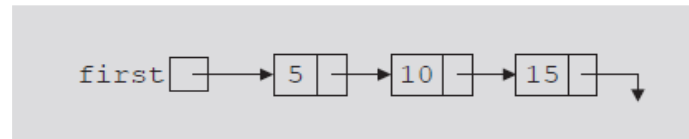
```
Read the first character
while not the end of input data
{
 a. initialize the stack
 b. process the expression
 c. output result
 d. get the next expression
}
```



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# Algorithm to Print a Linked List Backward

- Stack
  - Print a linked list backward
- Use linked implementation of stack



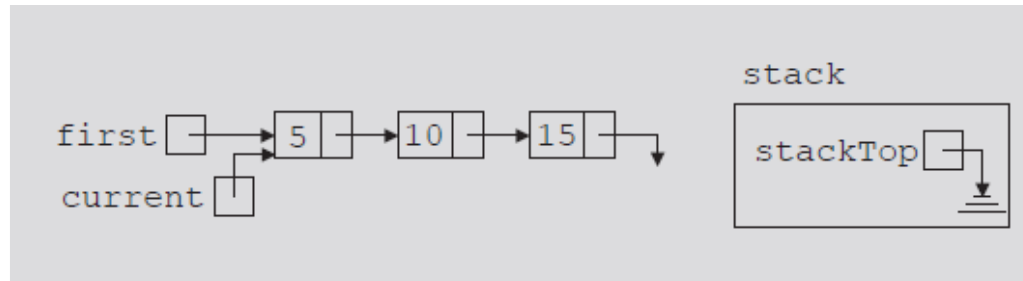
**FIGURE 7-16** Linked list

```
current = first; //Line 1

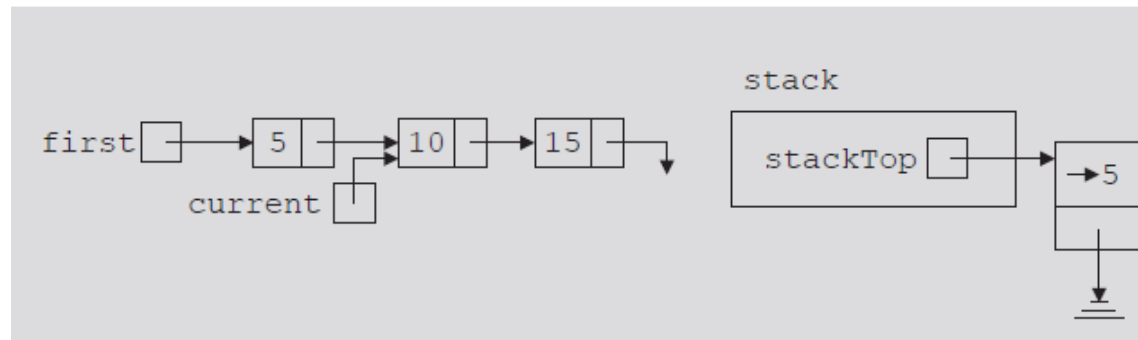
while (current != NULL) //Line 2
{ //Line 3
 stack.push(current); //Line 4
 current = current->link; //Line 5
} //Line 6
```



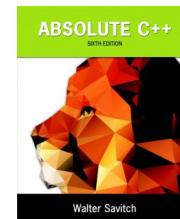
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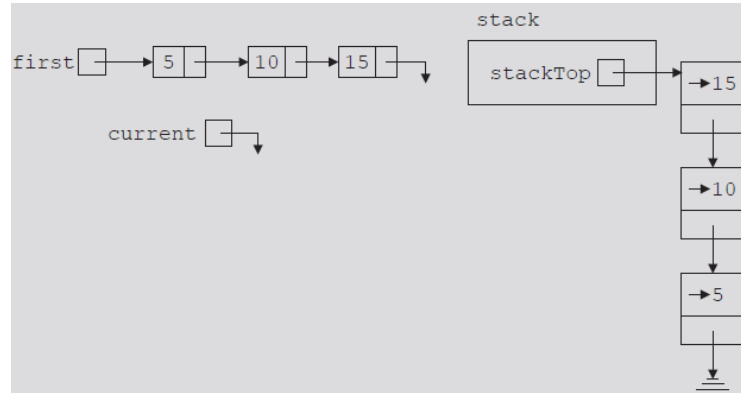
**FIGURE 7-17** List after the statement `current = first;` executes



**FIGURE 7-18** List and stack after the statements `stack.push(current);` and `current = current->link;` execute

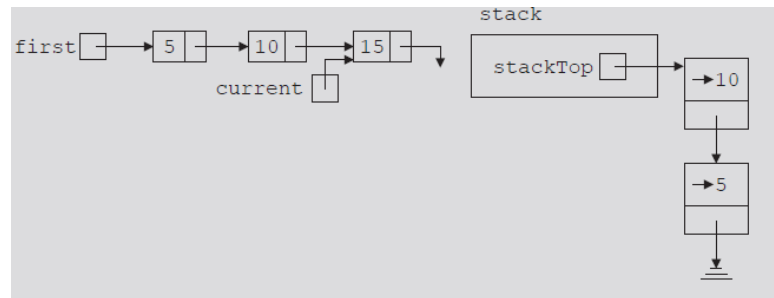


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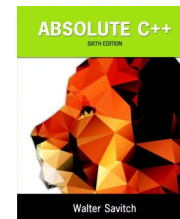


**FIGURE 7-19** List and stack after the while statement executes

```
while (!stack.isEmptyStack()) //Line 7
{ //Line 8
 current = stack.top(); //Line 9
 stack.pop(); //Line 10
 cout << current->info << " "; //Line 11
} //Line 12
```



**FIGURE 7-20** List and stack after the statements `current = stack.top();` and `stack.pop();` execute



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# Checking for Balanced Braces

- Example of curly braces in C++ language

- Balanced

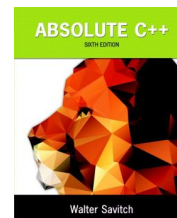
```
abc{defg{ijk}{l{mn}}op}qr
```

- Not balanced

```
abc{def}}{ghij{k}l}m
```

- Requirements for balanced braces

- For each }, must match an already encountered {
  - At end of string, must have matched each {

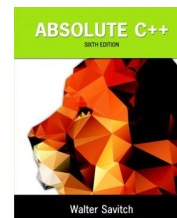




# Checking for Balanced Braces

- Initial draft of a solution.

```
for (each character in the string)
{
 if (the character is a '{')
 aStack.push('{')
 else if (the character is a '}')
 aStack.pop()
}
```



# Checking for Balanced Braces

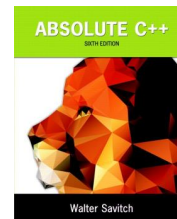
- Detailed pseudocode solution.

```
// Checks the string aString to verify that braces match.
// Returns true if aString contains matching braces, false otherwise.
checkBraces(aString: string): boolean
{
 aStack = a new empty stack
 balancedSoFar = true
 i = 0 // Tracks character position in string

 while (balancedSoFar and i < length of aString)
 {
 ch = character at position i in aString
 i++

 // Push an open brace
 if (ch is a '{')
 aStack.push('{')

 // Close brace
 else if (ch is a '}')
 {
```

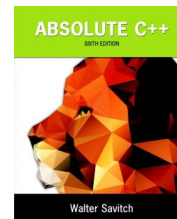


# Checking for Balanced Braces

- Detailed pseudocode solution.

```
// Close brace
else if (ch is a '}')
{
 if (!aStack.isEmpty())
 aStack.pop() // Pop a matching open brace
 else // No matching open brace
 balancedSoFar = false
}
// Ignore all characters other than braces
}

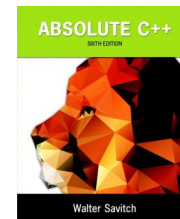
if (balancedSoFar and aStack.isEmpty())
 aString has balanced braces
else
 aString does not have balanced braces
}
```



# Checking for Balanced Braces

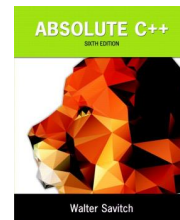
- Traces of algorithm that checks for balanced braces

| <u>Input string</u> | <u>Stack as algorithm executes</u> |    |    |    |                                                             |
|---------------------|------------------------------------|----|----|----|-------------------------------------------------------------|
| {a{b}c}             | 1.                                 | 2. | 3. | 4. | 1. push {                                                   |
|                     | {                                  | {  | {  |    | 2. push {                                                   |
|                     |                                    |    |    |    | 3. pop                                                      |
|                     |                                    |    |    |    | 4. pop                                                      |
|                     |                                    |    |    |    | stack empty -> balanced                                     |
| {a{bc}              | {                                  | {  | {  |    | 1. push {                                                   |
|                     |                                    |    |    |    | 2. push {                                                   |
|                     |                                    |    |    |    | 3. pop                                                      |
|                     |                                    |    |    |    | Stack not empty $\Rightarrow$ not balanced                  |
| {ab}c}              | {                                  |    |    |    | 1. push {                                                   |
|                     |                                    |    |    |    | 2. pop                                                      |
|                     |                                    |    |    |    | Stack empty when "}" encountered $\Rightarrow$ not balanced |



# Summary

- Stack
  - Last In First Out (LIFO) data structure
  - Implemented as array or linked list
  - Arrays: limited number of elements
  - Linked lists: allow dynamic element addition



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# Application(s)

## Queue Applications

### A “Palindrome”

- A string of characters that reads the same from left to right as it does from right to left.

“Nipson anomemata me monan opsin”

“NIΨON ANOMHMATA MH MONAN OΨIN”

To recognize a palindrome, a Queue can be used in conjunction with a Stack.

- A Stack reverses the order of occurrences.
- A Queue preserves the order of occurrences.



Church of St. Mary of Blachernae

# Application(s)

## Queue Applications

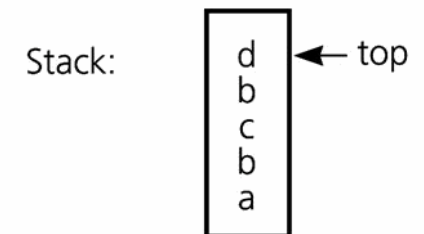
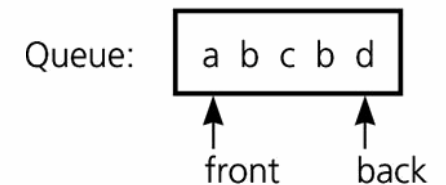
Recognizing a “Palindrome” – example:

- A non-recursive recognition algorithm for palindromes.

As we traverse the character string from left to right:

- Insert each character into both a queue and a stack.
- Compare the characters at the front of the queue and the top of the stack.

String:    abcbd



## Position-oriented ADTs

Position-oriented ADTs include:

- The List
- The Stack
- The Queue

## Stacks and Queues

- Only the end positions/entries can be accessed.

## Lists

- All positions/entries can be accessed.



## Position-oriented ADTs

Operations of stacks and queues can be paired off as:

- **createStack** and **createQueue**.
- Stack **empty** and Queue **empty**.
- **push** and **enqueue**.
- **pop** and **dequeue**.
- Stack **top** and Queue **front**.

ADT List operations generalize Stack and Queue operations:

- **size**.
- **insert**.
- **remove**.
- **retrieve**.

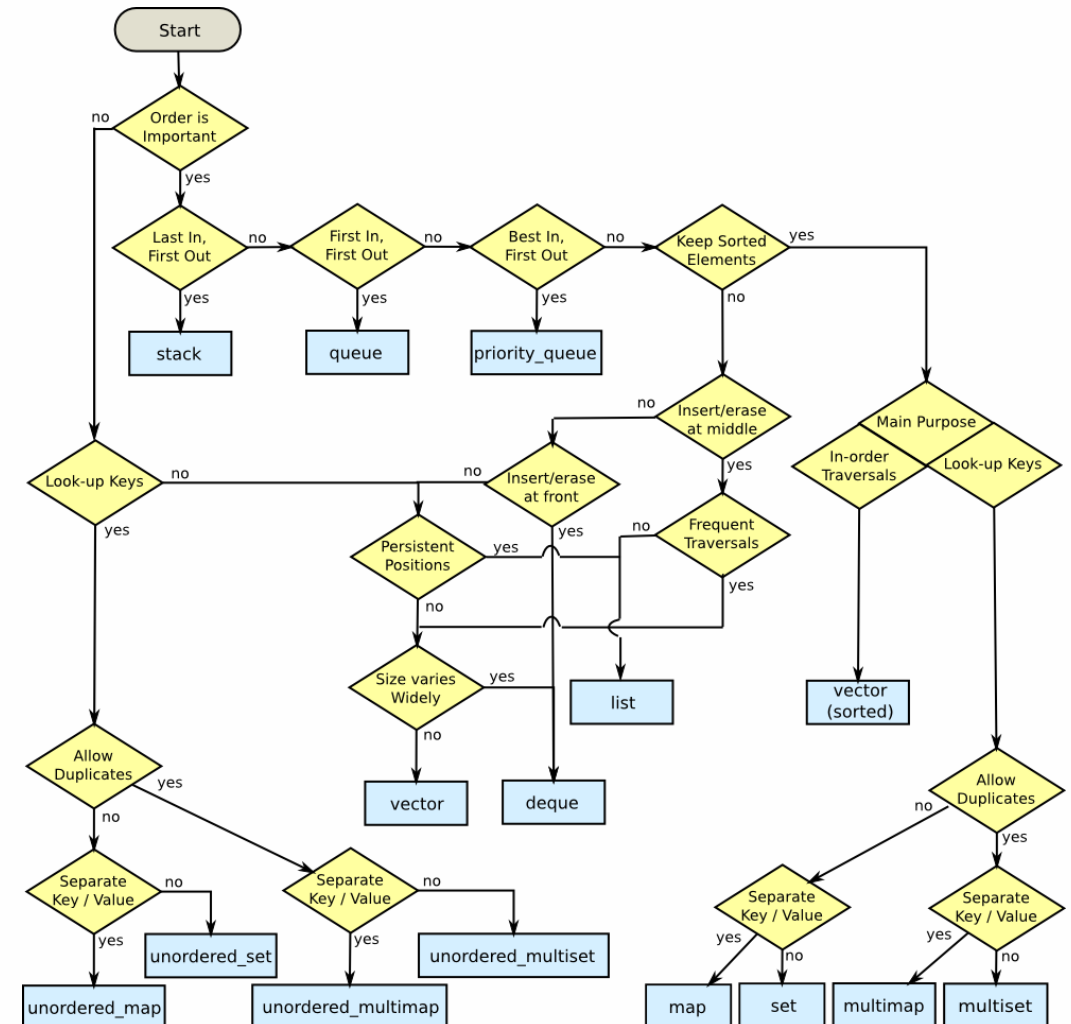
# Preliminary Discussion

## Data Structures – a *Cheatsheet*

Literally just scratched the surface:

- Array
- Stack
- Queue
- Not even Priority Queue yet ...
- List
- Usually Doubly-Linked List
- But a Forward-List also exists

Many more ...



**CS-202**

Time for Questions !