

CIS 721 - Real-Time Systems
Quiz #1
Spring 2014

Name: _____

Friday, Feb. 28, 2014

Please show all work on the quiz.

1. (30 points) Consider the following set of tasks scheduled using **preemptive** priority-based scheduling.

Task	Run Time (e_i)	Period (p_i)	Deadline (D_i)
A	8	24	24
B	3	12	12
C	2	8	8

- a) Suppose that the **rate monotonic (RM)** algorithm is used to assign priorities. In what order would these tasks be prioritized from highest to lowest priority? (Fill in the blanks with A, B, C)

Highest priority: _____, middle priority: _____, lowest priority: _____

- b) What is the total utilization, U , of all tasks? _____.
Can Liu and Layland's Test be used to try to check if the task set is schedulable? _____. If the test can be used, what conclusions, if any, can be made after applying Liu and Layland's Test? If the test cannot be applied, explain why not. Hint: $3 \cdot (2^{1/3} - 1) = 0.779763$.

- c) Use Response Time Analysis to determine if the task set is feasible. Show work.

- d) Draw the Gantt Chart (using the template shown below) showing how the tasks would be scheduled over one hyperperiod.

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2. (30 points) Consider the following set of tasks scheduled using **non-preemptive** priority-based scheduling. Assume that the **deadline monotonic (DM)** algorithm is used to assign priorities.

Task	Run Time (e_i)	Period (p_i)	Deadline (D_i)
A	2	5	5
B	2	10	10
C	3	20	9

- a) In what order would these tasks be prioritized from highest to lowest priority?

Highest priority: _____, middle priority: _____, lowest priority: _____

- b) What is the worst-case blocking time for each task?

$B_A =$ _____, $B_B =$ _____, $B_C =$ _____

- c) What conclusions (if any) can be made by applying a Utilization-Based Test to the given task set? Show work.

- d) Is the task set schedulable based on Response Time (Time-Based) Analysis? Show work.

3. (20 points) Preemption Thresholds: Suppose that the task sets shown above in **Problems 1 and 2** are scheduled using **priority-based scheduling with preemption thresholds**.

a) What does it mean for a task set to be simply periodic?

Is the task set shown in **Problem 1** simply periodic? _____

Is the task set shown in **Problem 2** simply periodic? _____

- b) Is there a particular assignment of **priorities and preemption thresholds** that makes the task set shown in **Problem 1** schedulable using **priority-based scheduling**? _____ If so, give an assignment using 3=high priority and 1=low priority:

- $\pi_A = \underline{\hspace{1cm}}$, $\gamma_A = \underline{\hspace{1cm}}$
- $\pi_B = \underline{\hspace{1cm}}$, $\gamma_B = \underline{\hspace{1cm}}$
- $\pi_C = \underline{\hspace{1cm}}$, $\gamma_C = \underline{\hspace{1cm}}$

- c) Is there a particular assignment of **priorities and preemption thresholds** that makes the task set shown in **Problem 2** schedulable using **priority-based scheduling**? _____ If so, give an assignment using 3=high priority and 1=low priority:

- $\pi_A = \underline{\hspace{1cm}}$, $\gamma_A = \underline{\hspace{1cm}}$
- $\pi_B = \underline{\hspace{1cm}}$, $\gamma_B = \underline{\hspace{1cm}}$
- $\pi_C = \underline{\hspace{1cm}}$, $\gamma_C = \underline{\hspace{1cm}}$

- d) Briefly describe an optimal algorithm to assign preemption thresholds for a given task set if the priorities are given.

4. (20 points) Consider the task set consisting of the following three preemptive, periodic tasks (denoted using the notation $\tau_i = (p_i, e_i, D_i)$):

$$\tau_1 = (12, 2, 6)$$

$$\tau_2 = (12, 4, 12)$$

$$\tau_3 = (24, 5, 12)$$

The system is to be scheduled and executed using a fixed cyclic schedule.

- a) Determine an appropriate frame size, and draw a network flow graph that can be used to find a fixed (static) cyclic schedule of the tasks. Hint: Remember to indicate the **maximum** allowable flows on all edges in the graph. Clearly indicate which nodes represent jobs and which nodes represent frames.

Frame Size = _____

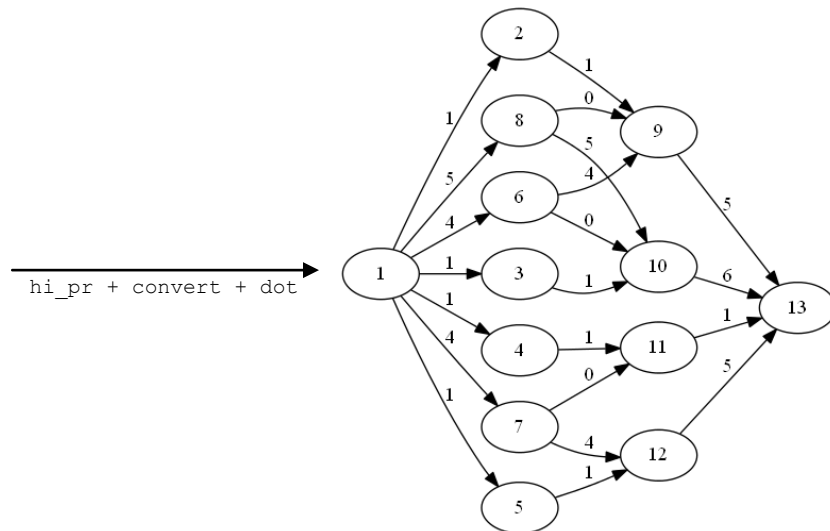
$$\tau_1 = (12, 2, 6)$$

$$\tau_2 = (12, 4, 12)$$

$$\tau_3 = (24, 5, 12)$$

- b) Suppose that the task set is modified so that $\tau_1 = (6, 1, 6)$. Further, suppose that a solution is obtained by using the following input file describing allowable flows in a directed graph, and by passing it as input to the maximum flow algorithm to compute a maximum flow of 17, with the corresponding flow values as shown in the graph:

```
p max 13 21
n 1 s
n 13 t
a 1 2 1
a 1 3 1
a 1 4 1
a 1 5 1
a 1 6 4
a 1 7 4
a 1 8 5
a 2 9 6
a 3 10 6
a 4 11 6
a 5 12 6
a 6 9 6
a 6 10 6
a 7 11 6
a 7 12 6
a 8 9 6
a 8 10 6
a 9 13 6
a 10 13 6
a 11 13 6
a 12 13 6
```



Draw a Gantt Chart showing the corresponding schedule that is represented by these flows.

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- c) Could the same solution be used for part b) if the jobs are non-preemptive? Explain briefly.