## $\begin{array}{c} \underline{\text{Homework 4}} \\ \text{CIS 770: Formal Language Theory} \end{array}$

Assigned: Feburary 26, 2016 Due on: March 8, 2013

**Instructions:** This homework has 2 problems that can be solved individually. Please follow the homework guidelines given on the class website. Solutions not following these guidelines will not be graded.

**Recommended Reading:** Lectures 8, 9, 10 and 11.

**Problem 1.** [Category: Comprehension+Design] Let  $L = \mathbf{L}(1*0(00 \cup 01 \cup 1)(0 \cup 1)*)$ .

- 1. List all the suffix languages of L, explain why your answer covers all the suffix languages. [5 points]
- 2. Draw the minimum state DFA  $M^L$  accepting L. [5 points]

**Problem 2.** [Category: Comprehension] Given a homomorphism  $h: \Sigma^* \to \Delta^*$  and a language  $L \subseteq \Sigma^*$  define  $h(L) = \{h(w) | w \in L\} \subseteq \Delta^*$ .

- 1. Pove that for all strings  $x, y \in \Sigma^*, h(xy) = h(x)h(y)$ . [5 points]
- 2. Prove  $h(L_1 \cup L_2) = h(L_1) \cup h(L_2)$ . [5 points]
- 3. Proof  $h(L_1 \circ L_2) = h(L_1) \circ h(L_2)$ . [5 points]