
CIS 721 - Real-Time Systems

Lecture 4: On-Line Scheduling

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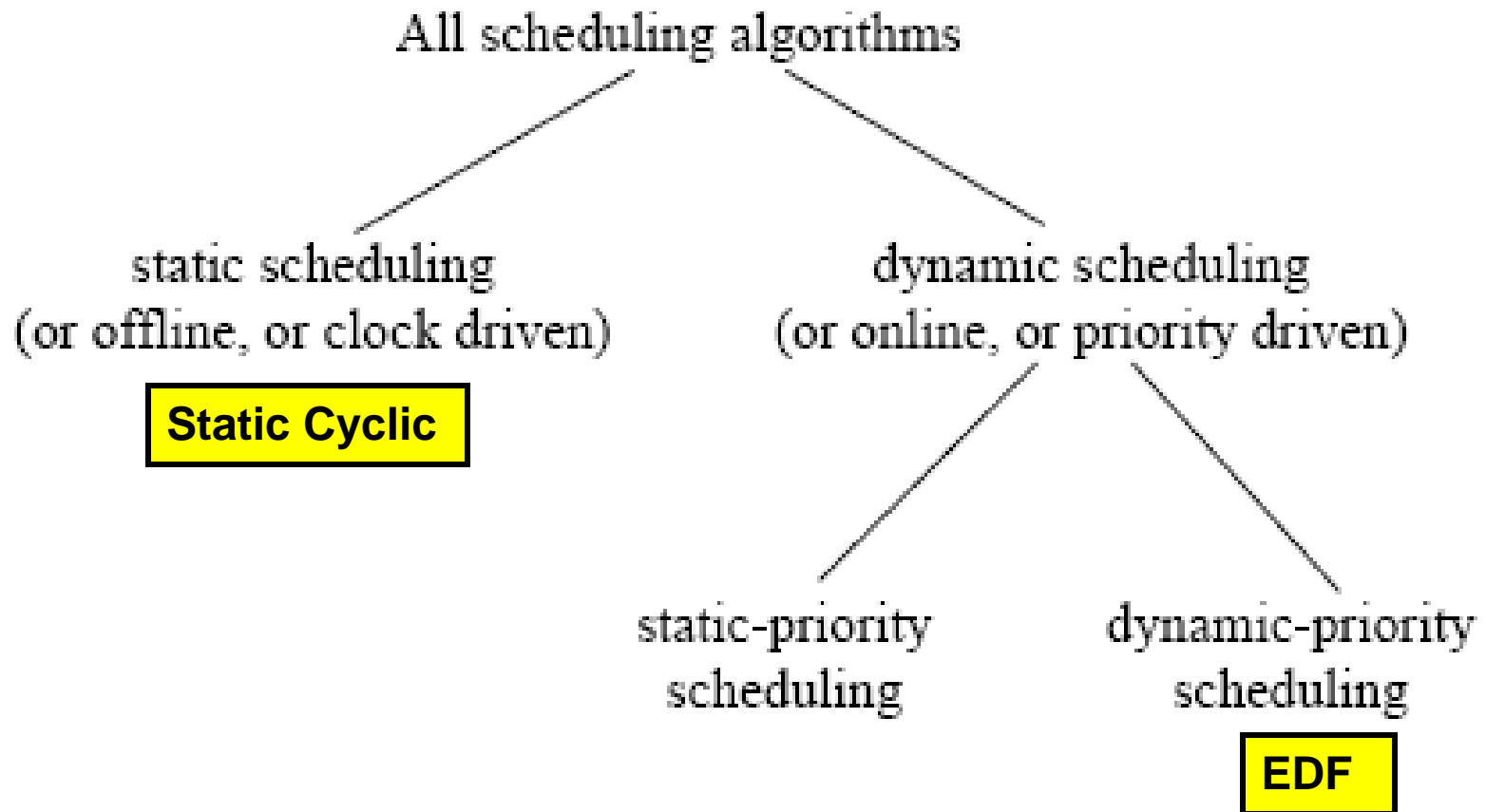
Outline

- **Approaches For Real-Time Scheduling (Ch. 4)**
 - **Off-line Scheduling**
 - **On-line Scheduling**
 - **EDF**
 - **Competitive Factor Theorem**
 - **Clock-Driven Scheduling (Ch. 5)**
 - **Priority-Driven Scheduling (Ch.6-7)**
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Schedules

- A **schedule** is an assignment of jobs to available processors. In a **feasible schedule**, every job starts at or after its release time and completes by its deadline in a **hard** real-time system.
- A scheduling algorithm is **optimal** if it always produces a feasible schedule if such a schedule exists.

Classification of Scheduling Algorithms



EDF is optimal for scheduling preemptive tasks on a single processor.

Temporal Parameters

- J_i : **job** – a unit of work
 - T_i (or τ_i): **task** - a set of related jobs
 - A **periodic task** is sequence of invocations of jobs with identical parameters.
 - r_i : **release time** of job J_i
 - d_i : **absolute deadline** of job J_i
 - D_i : **relative deadline** (or just **deadline**) of job J_i
 - e_i : (Maximum) **execution time** of job J_i
-

Periodic Task Model

- **Tasks:** T_1, \dots, T_n
- Each consists of a set of **jobs**: $T_i = \{J_{i1}, J_{i2}, \dots\}$
- ϕ_i : **phase** of task T_i = time when its first job is released
- p_i : **period** of T_i = minimum inter-release time
- H : **hyperperiod** $H = \text{lcm}(p_1, \dots, p_n)$
- e_i : **execution time** of T_i
- u_i : **utilization** of task T_i is given by $u_i = e_i / p_i$
- D_i : (relative) **deadline** of T_i , typically $D_i = p_i$

Periodic Task

- We refer to a periodic task T_i with phase ϕ_i , period p_i , execution time e_i , and relative deadline D_i by the 4-tuple (ϕ_i, p_i, e_i, D_i) .
- Example: $(1, 10, 3, 6)$
- By default, the phase of each task is 0, and its relative deadline is equal to its period.
- Example: $(0, 10, 3, 10) = (10, 3)$.

Sample Periodic Task Set

- Task 1: (12, 3)
 - Task 2: (6, 3)
 - Task 3: (12, 2)
-
- Hyperperiod $H = \text{lcm}(12, 6, 12) = 12$
 - Potential frame sizes? 3 or 6
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Clock-Driven Example

\$ hi_pr < cyclic2.input > cyclic2.output

INPUT:

p max 8 12

n 1 s

n 8 t

a 1 2 3

a 1 3 3

a 1 4 3

a 1 5 2

a 2 6 6

a 2 7 6

a 3 6 6

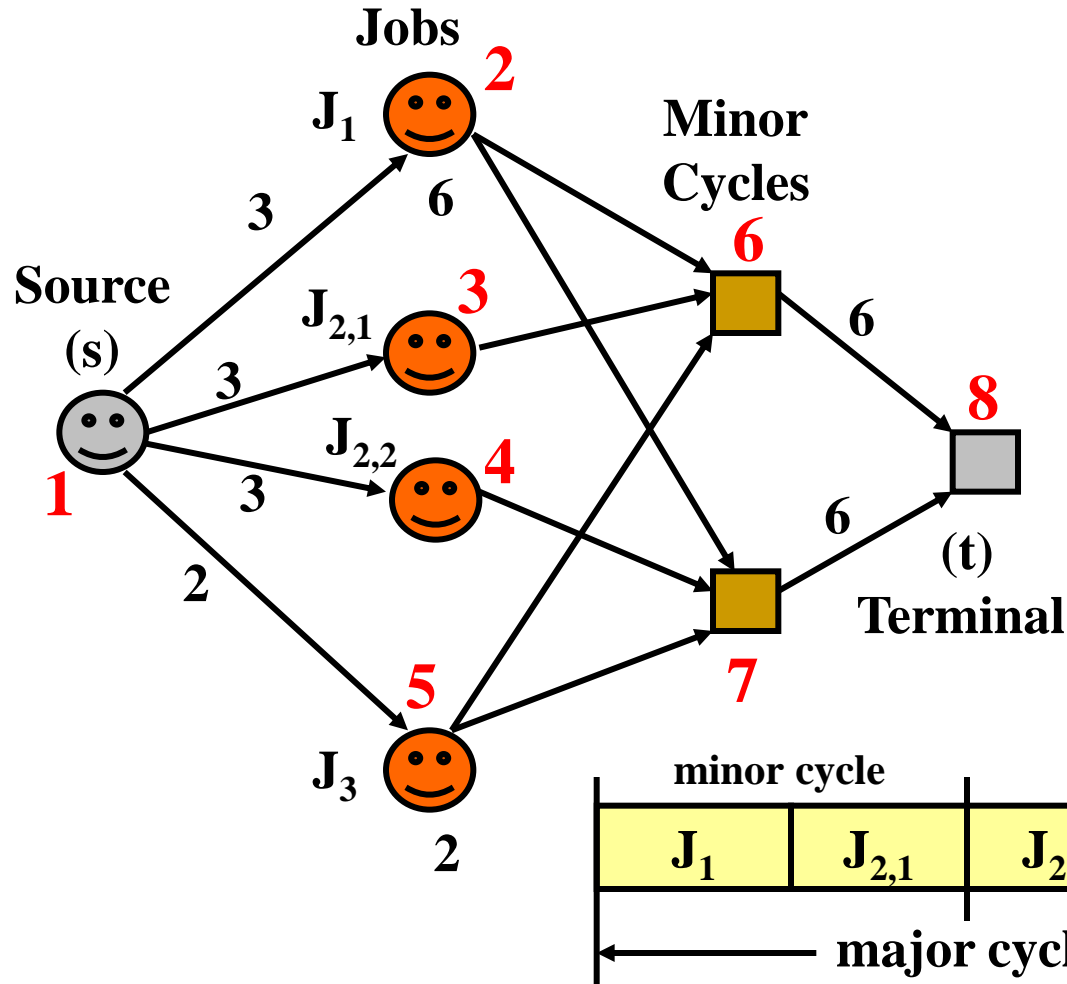
a 4 7 6

a 5 6 6

a 5 7 6

a 6 8 6

a 7 8 6



OUTPUT:

max flow:11

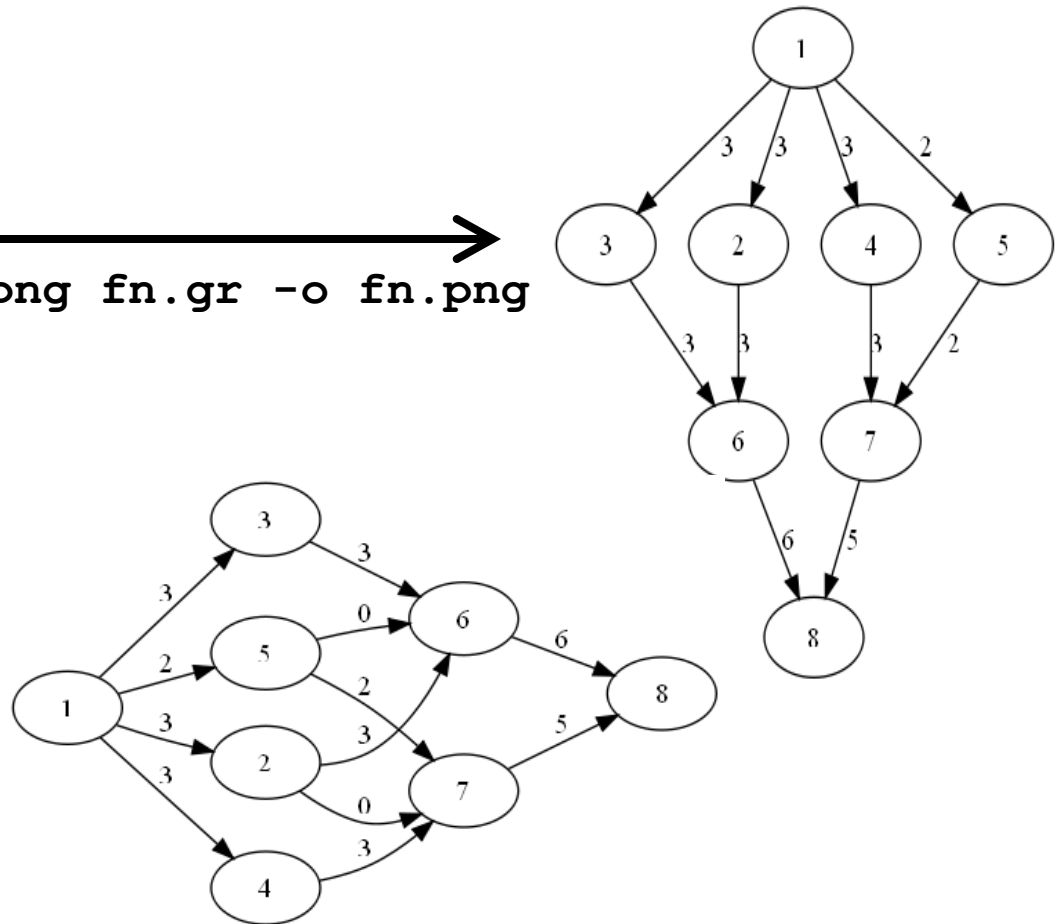
c flow values

f	1	2	3
f	1	4	3
f	1	3	3
f	1	5	2
f	2	6	3
f	2	7	0
f	3	6	3
f	4	7	3
f	5	7	2
f	5	6	0
f	6	8	6
f	7	8	5
c			

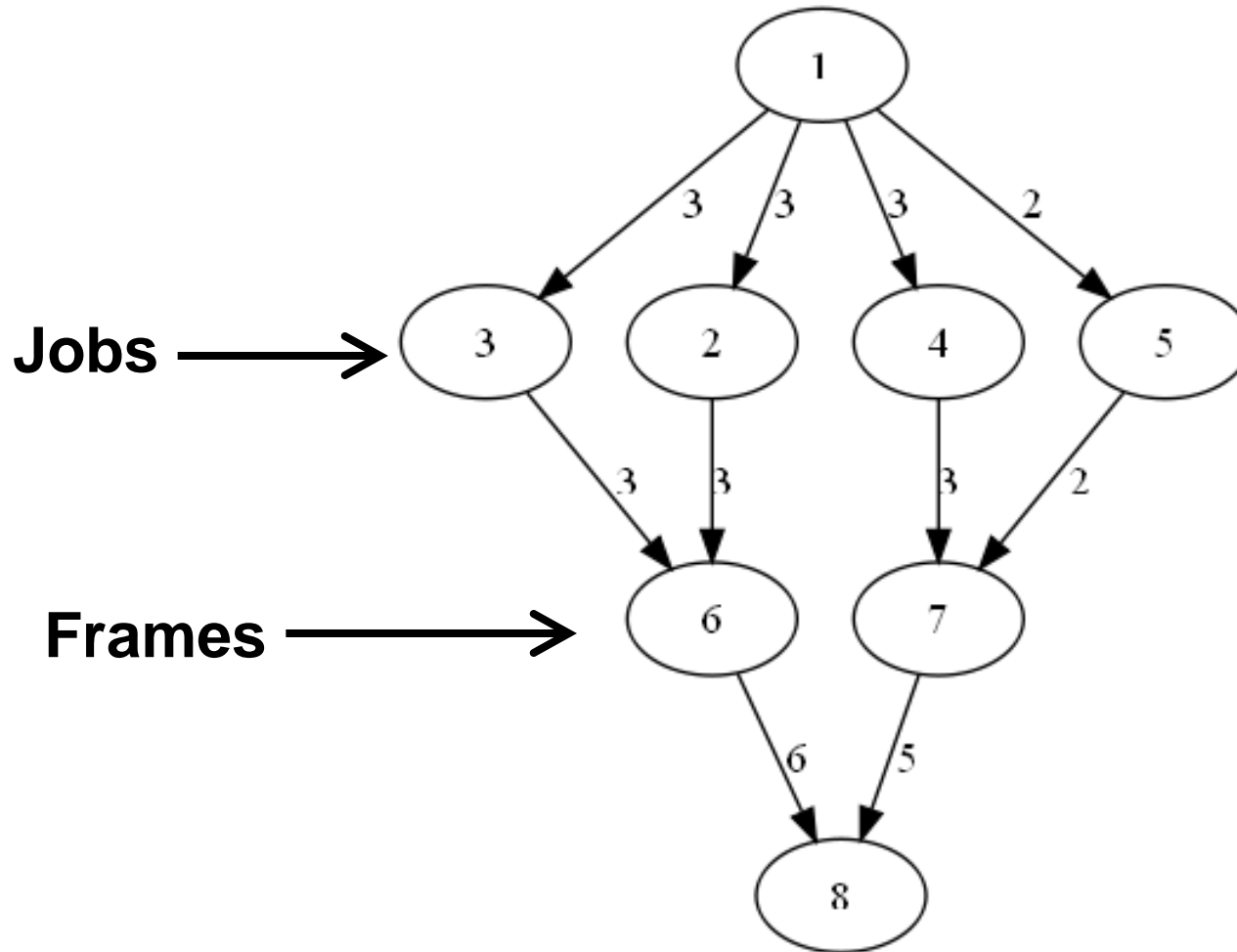
Resulting Graphics File

```
digraph g {  
  1 -> 2 [label=3]  
  1 -> 4 [label=3]  
  1 -> 3 [label=3]  
  1 -> 5 [label=2]  
  2 -> 6 [label=3]  
  3 -> 6 [label=3]  
  4 -> 7 [label=3]  
  5 -> 7 [label=2]  
  6 -> 8 [label=6]  
  7 -> 8 [label=5]  
  { rank=same; 2; 3; 4; 5;}  
  { rank=same; 6; 7;}  
}
```

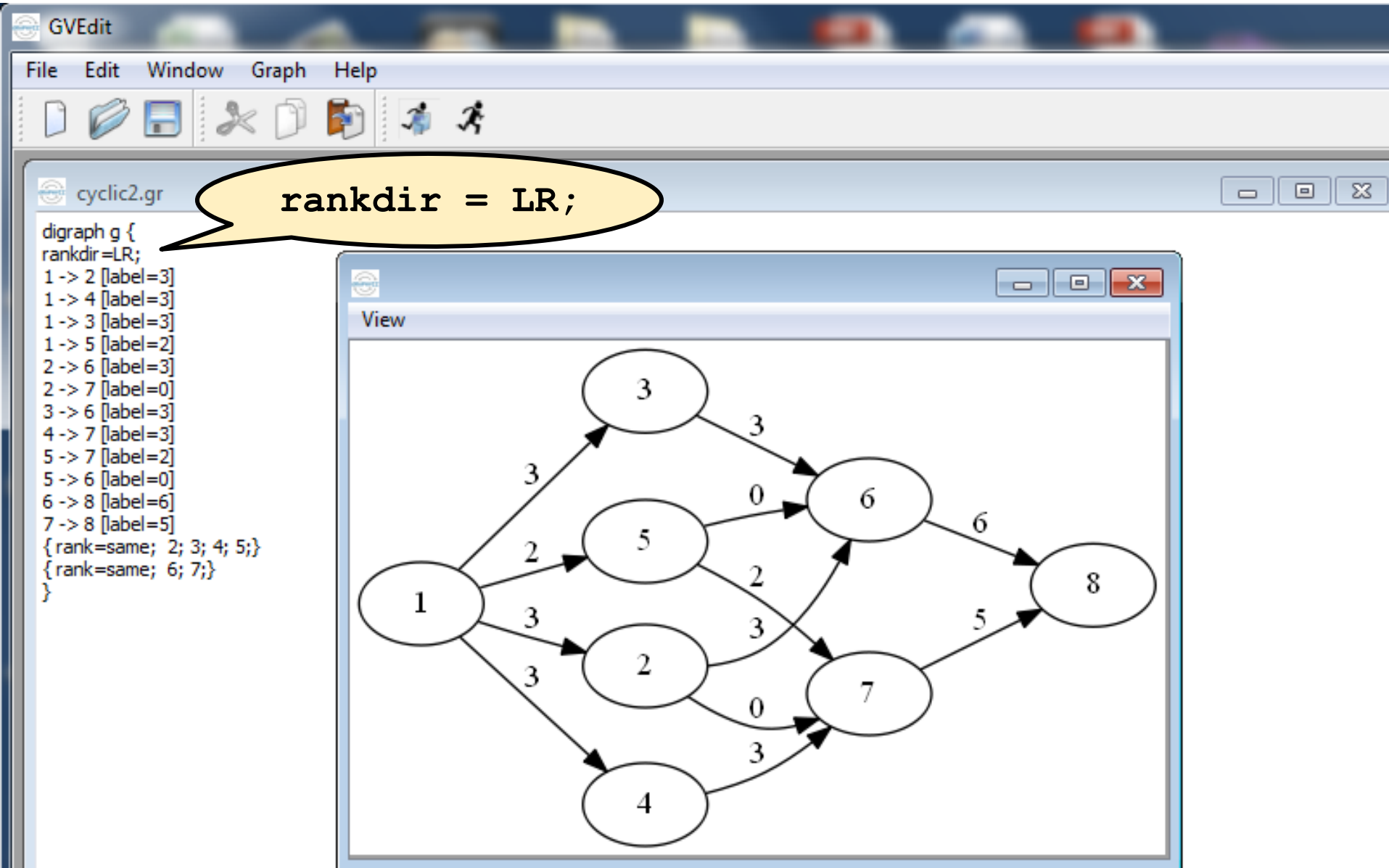
dot -Tpng fn.gr -o fn.png



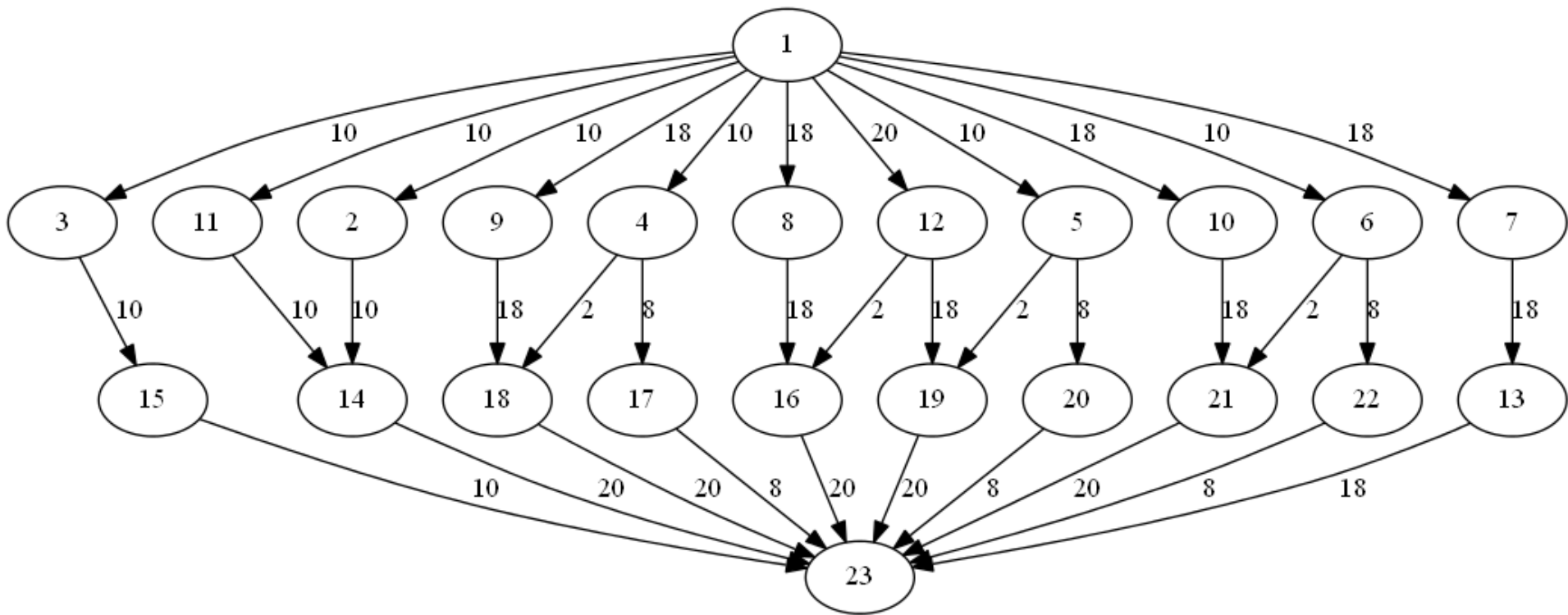
Output generated



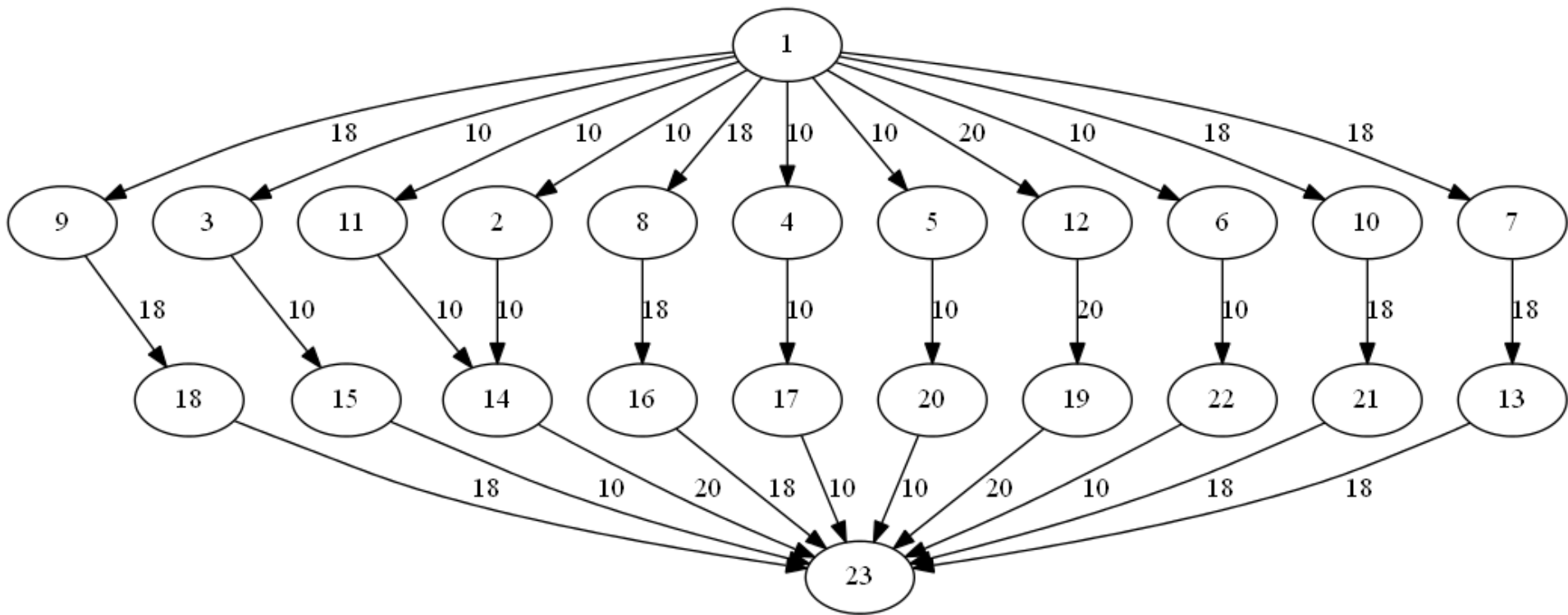
GraphViz Editor: GVEdit



Another Example



Another Example - Constrained



On-line Scheduling

- Scheduling is performed **on-line** if the scheduler makes decisions without knowledge of the jobs to be released in the future.
- EDF is an example of an on-line scheduling algorithm.
- The system is **overloaded** if the jobs cannot be feasibly scheduled even by a clairvoyant scheduler. During an overload, some jobs must be discarded in order to allow other jobs to complete.

EDF Algorithm

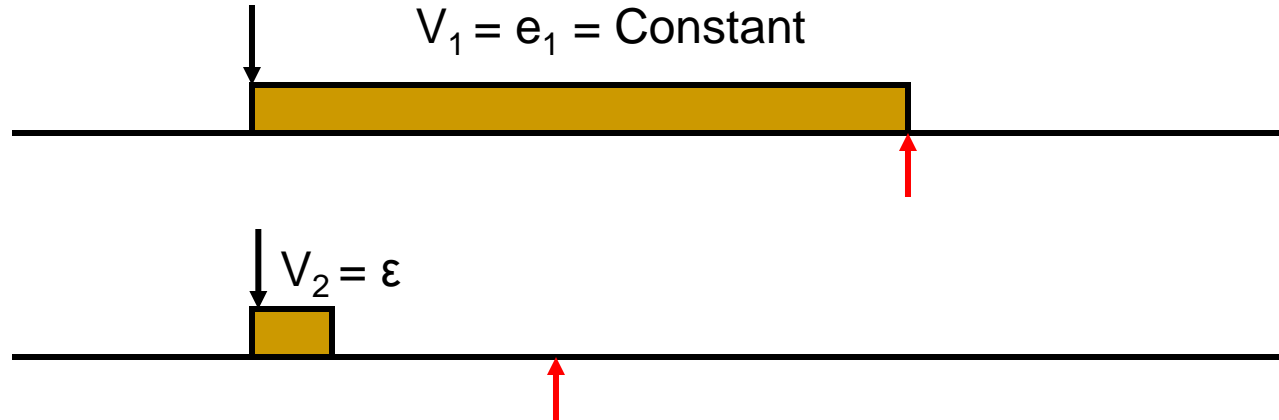
- **Earliest-Deadline-First (EDF) algorithm:**
 - At any time, execute the available job with the **earliest deadline**.
- **Theorem: (Optimality of EDF):** In a system with **one processor** and **preemption** allowed, EDF is optimal; that is, EDF can produce a feasible schedule for a given job set J with arbitrary release times and deadlines, if a feasible schedule exists.
- **Proof:** Apply schedule transformations and remove idle time.

Competitive Factor

- For hard real-time systems, the **value of a job** is defined to be the execution time of the job if the job completes by its deadline.
- The **value of a schedule** of a sequence of jobs is the sum of the values of all jobs in the sequence.
- An on-line algorithm has a **competitive factor c** iff the value of the schedule of any finite sequence of jobs produced by the algorithm is at least c times the value of the schedule produced by an optimal, clairvoyant algorithm.

Competitive Factor of EDF

- The competitive factor of EDF is 0.

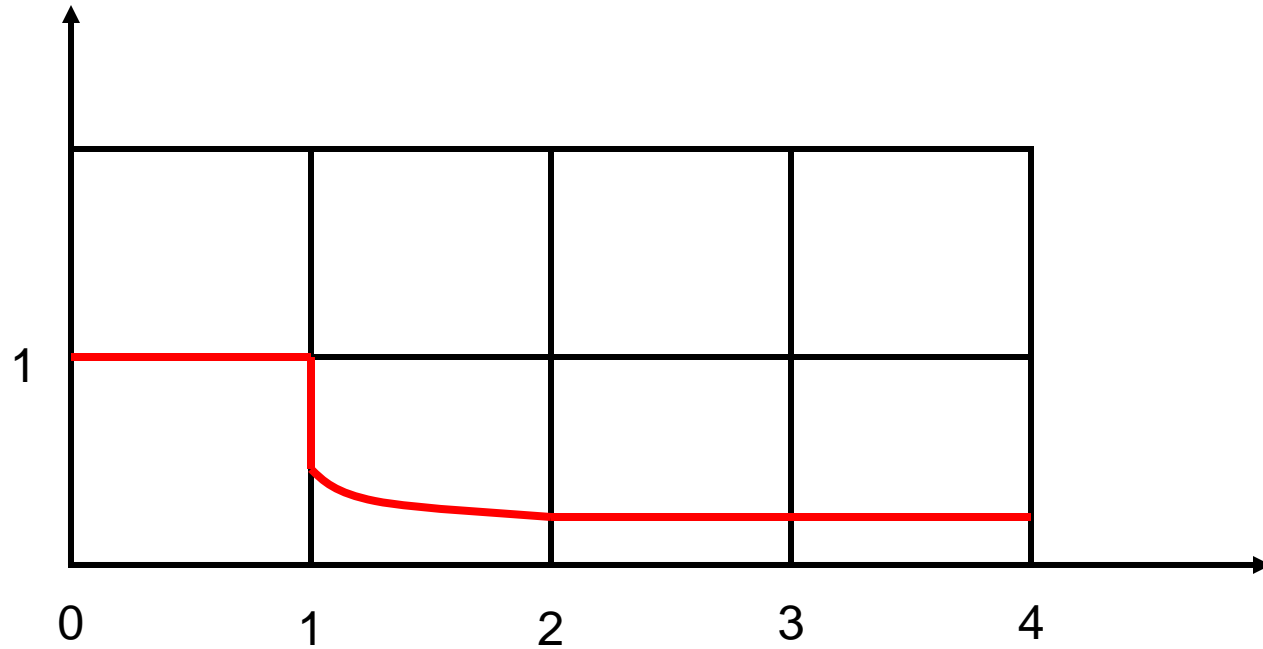


The value of an EDF schedule is V_2 whereas the value of an optimal schedule is V_1 . The competitive factor of $\text{EDF} = V_2 / V_1$ approaches 0 as ϵ approaches 0.

On-line Scheduling Limitations – Or how bad is it?

- **Theorem:** No on-line scheduling algorithm can achieve a competitive factor greater than 0.25 when the system is overloaded.
- Proof: [Baruah, et al., 1991]
[Competitive_Factor_Theorem.pdf](#)
- Note: Even when the system is only slightly overloaded (e.g., slightly more than 100% utilization), no on-line algorithm can achieve a competitive factor greater than 0.385.

Maximum Competitive Factor



Summary

- Read Ch. 4-6.
- Homework #1.