

## Diversity Maximization in the Presence of Outliers (Supplementary File)

### Additional Experiment

**Result obtained by STREAMING.** Figure 1(a) illustrates an example of  $X$  consisting of points including outliers<sup>1</sup>, whereas Figure 1(b) shows a diverse set obtained by STREAMING. (As this  $X$  contains a small number of points, CORESET returns the same solution.) From Figure 1, STREAMING also returns only inliers, different from GMM (see Figure 2 of our main paper).

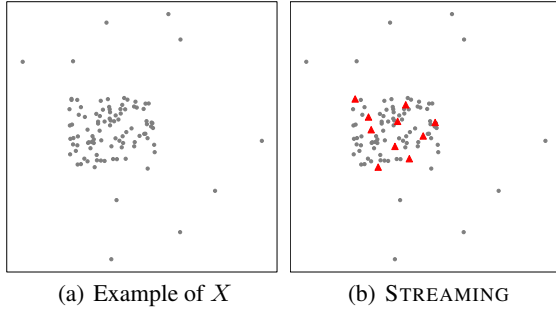


Figure 1: Result set obtained by STREAMING ( $k = 10$ )

**Result of GMM and PODS19.** Table 1 clearly shows that most points in  $S$  computed by GMM and PODS19 are outliers. This result demonstrates that simply running an existing algorithm for the problem of Max-Min diversification *without* outliers does not work.

Table 1: Average number of outliers in  $S$  ( $k = 100$ )

Algorithm	FCT	Household	KDD99	Mirai
GMM	99.00	99.00	99.00	99.00
PODS19	92.35	91.55	87.40	84.05

**Standard deviation result.** Table 2 reports the standard deviation w.r.t.  $div(S)$  of GREEDY, STREAMING, and CORESET. We used the default parameter setting. CORESET has a larger standard deviation than the others, and this result is actually reasonable. The coreset  $C$  has a much smaller number of points than  $n = |X|$ , thus  $div(S)$  of CORESET tends

Table 2: Standard deviation of  $div(S)$

Algorithm	FCT	Household	KDD99	Mirai
GREEDY	0.483	0.460	1.211	1.639
STREAMING	0.217	0.240	0.564	5.344
CORESET	2.345	1.506	4.307	4.444

to depend on the first random point of  $S$ . Since GREEDY and STREAMING use  $X$ , they do not have this tendency.

**Impact of success probability  $p$ .** Table 3 shows the average  $div(S) = \min_{x, x' \in S} dist(x, x')$  and running time [msec] of CORESET with different  $p$ . (Note that CORESET did not return any outliers for these values of  $p$ .)

We see that  $div(S)$  with  $p = 0.9$  is smaller than those with  $p = 0.95$  and  $p = 0.99$ . On the other hand, the running time becomes longer as  $p$  becomes larger. For the running time, this result is reasonable, since a smaller  $p$  constructs a coreset with a smaller size. (Recall that the time complexity of CORESET is  $O(kc)$ , where  $c$  is the coreset size.) This result is also reasonable for  $div(S)$ . Given a larger  $p$ , a coreset contains more points in  $X$ , so  $\min_{x, x' \in S} dist(x, x')$  tends to be larger.

Table 3: CORESET’s average  $div(S)$  and running time [msec] ( $k = 100$  and  $z = 200$ )

$p$	FCT		Household	
	$div(S)$	Time	$div(S)$	Time
0.90	48.996	1.369	36.916	1.553
0.95	50.158	5.323	38.369	5.823
0.99	51.425	13.422	39.294	27.239

$p$	KDD99		Mirai	
	$div(S)$	Time	$div(S)$	Time
0.90	73.690	3.253	101.880	30.500
0.95	77.064	8.523	106.352	97.760
0.99	80.153	54.130	107.272	476.063

<sup>1</sup>This is the same set as that in Figure 2 of our main paper.