

Article

# Anonymiced shareable data: Using mice to create and analyze multiply imputed synthetic data sets

Thom Volker<sup>1,\*</sup>, Gerko Vink<sup>1,†</sup>

- Utrecht University Department of Methodology and Statistics Padualaan 14, 3584CH Utrecht, the Netherlands;
- \* Correspondence: t.b.volker@uu.nl.
- † These authors contributed equally to this work.

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- structured abstracts, but without headings: 1) Background: Place the question addressed in a broad
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- treatments applied; 3) Results: Summarize the article's main findings; and 4) Conclusion: Indicate
- the main conclusions or interpretations. The abstract should be an objective representation of the
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#### 1. Introduction

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Open science, including open data, has been marked as the future of science [1], and the advantages of publicly available research data are numerous [2,3]. Collecting research data requires an enormous investment both in terms of time and monetary resources. Openly accessible research data bears the potential of increasing the scientific returns for the same data collection effort. Additionally, the fact that public funds are used for data collection results in increasing demand for the collected data. Nevertheless, the possibilities to distribute research data directly are often very limited due to restrictions on data privacy and data confidentiality. Although these regulations are much needed, privacy constraints are also ranked among the toughest challenges to overcome in the advancement of modern day social science research [4].

Anonymizing research data might seem a quick and appealing approach to limit the unique identification of participants. However, this approach is not sufficient to fulfil contemporary privacy and confidentiality requirements [5,6]. Over the years, several other techniques have been used to increase the confidentiality of research data, such as categorizing continuous variables, top coding values above an upper bound or adding random noise to the observed values [7]. However, these methods may distort the true data relation between variables, thereby reducing the data quality and the scientific returns for re-using the same data for further research.

An alternative solution has been proposed separately by Rubin [8] and Little [9]. Although their approaches differ to some extent, the overarching procedure is to use bonafide observed data to generate multiply imputed synthetic data sets that can be freely disclosed. While in practice, one

could see this as replacing the observed data values by multiple draws from the posterior predictive distribution of the observed data, based on some imputation model, Rubin would argue that these synthetic data values are merely draws from the same true data generating model. In that sense, the observed data is never replaced, but the population is resampled from the information captured in the (incomplete) sample. Using this approach, the researcher could replace the observed data set as a whole with multiple synthetic versions. Alternatively, the researcher could opt to only replace a subset of the observed data. For example, one can choose to only replace dimensions in the data that could be compared with publicly available data sets or registers. Likewise, synthetisation could be limited to those values that are disclosive, such as high incomes or high turnovers.

Conceptually, the synthetic data framework is based upon the building blocks of multiple imputation of missing data, as proposed by Rubin [10]. Instead of replacing just the missing values with multiple draws from the posterior predictive distribution, one could easily *overimpute* any observed sensitive values. Similarly to multiple imputation of missing data, the multiple synthetic data sets allow for correct statistical inferences, despite the fact that the analyses do not use the "true" value. The analyses over multiple synthetic data sets should be pooled into a single inference, so that the researcher can draw valid conclusions from the pooled results. To that respect, the variance should reflect the added variability that is induced by the imputation procedure.

Potentially, this approach could fulfill the needs for openly accessibly data, without running into barriers with regard to privacy and confidentiality constraints. However, there is no such thing as a free lunch: data collectors have to put effort in creating high-quality synthetic data. Also, the quality of the synthetic data is highly dependent on the imputation models, and using flawed models to generate synthetic data might bias subsequent analyses. Conversely, if the models used to create the synthetic data are able to preserve the relationships between the variables as in the original data, the synthetic data can be nearly as informative as the observed data. Thus, to fully exploit the benefits of synthetic data, the effort to actually create these high-quality data sets should be kept at a minimum.

To mitigate additional effort of creating synthetic data sets on behalf of the researcher, software aimed at multiple imputation of missing data can be employed. Especially if researchers used this software at an earlier stage in the research process, or acquired familiarity with it during earlier projects, the additional burden of creating synthetic data sets is relatively small. The R-package mice [11] implements multiple imputation of missing data in a straightforward and user-friendly manner. However, the functionality of mice is not restricted to the imputation of missing data, but allows to impute any value in the data: even observed values. Consequently, mice can be utilized for the creation of multiply imputed synthetic data sets.

After creating the multiply imputed synthetic data sets, the goal is to obtain valid statistical inferences in the spirit of Rubin [10] and Neyman [12]. In the missing data framework, this is done by performing statistical analyses on all imputed data sets, and pooling the results of the analyses according to Rubin's rules [10, pp.76]. In the synthetic data framework, the same procedure is followed, but with a slight twist: there are no values that remain constant over the synthetic data sets. The procedure of drawing valid inferences from multiple synthetic data sets is therefore slightly different.

In this manuscript we detail a workflow for synthesizing data with mice. First, the mice algorithm for the creation of synthetic data will be shortly explained. The aim is to generate synthetic sets that reassure the privacy and confidentiality of the participants. Second, a straightforward workflow for imputation of synthetic data with mice will be demonstrated. Third, we demonstrate the validity of the procedure through statistical simulation.

# 2. Generating synthetic data with mice

The mice package [11] in R [13] has been developed for multiple imputation of missing data. In this context, the aim is to replace missing values due to nonresponse by plausible values from the posterior predictive distribution of the variable containing the missings. Doing so, mice makes use of fully conditional specification [FCS; Van Buuren *et al.* [14]], which breaks down the multivariate distribution

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of the data  $\mathbf{Y} = (\mathbf{Y}_{obs}, \mathbf{Y}_{mis})$  into  $j = 1, 2, \ldots, k$  univariate conditional densities, where k denotes the number of columns in the data. Using FCS, a model is constructed for every incomplete variable and the missing values  $Y_{j,mis}$  are then imputed with draws from the posterior predictive distribution of  $P(Y_{j,mis}|\mathbf{Y}_{obs},\theta)$  on a variable-by-variable basis. Note that the predictor matrix  $Y_{-j}$  may contain yet imputed values from an earlier imputation step, and thus will be updated after every iteration. This procedure is applied m times, resulting in m completed data sets  $\mathbf{D} = (\mathbf{D}^{(1)}, \mathbf{D}^{(2)}, \ldots, \mathbf{D}^{(m)})$ , with  $\mathbf{D}^{(l)} = (\mathbf{Y}_{obs}, Y_{mis}^{(l)})$ .

In mice, the generation of multiply imputed data sets to solve for unobserved values is straightforward. The following pseudocode details the multiple imputation of the mice::boys data set [15] into the object imp with m = 10 imputated sets and maxit = 7 iterations for the algorithm to converge, using the default imputations methods for each column data class.

It is straightforward to extended the imputation approach to generate synthetic values. Rather than imputing missing data, the observed values are then replaced by synthetic draws from the posterior predictive distribution. For simplicity, assume that the data is completely observed (i.e.,  $\mathbf{Y} = \mathbf{Y}_{obs}$ ). Following the notation of Reiter and Raghunathan [16], let for n units denote  $Z_i = 1$  if any of the values of unit i = 1, 2, ..., n are to be replaced by imputations, and  $Z_i = 0$  otherwise, with  $\mathbf{Z} = (Z_1, Z_2, ..., Z_n)$ . Accordingly, the data consists of values that are to be replaced and values that are to be kept (i.e.,  $\mathbf{Y} = (\mathbf{Y}_{rep}, \mathbf{Y}_{nrep})$ ). Now, instead of imputing  $\mathbf{Y}_{mis}$  with draws from the posterior predictive distribution of  $P(Y_{j,mis}|\mathbf{Y}_{obs},\theta)$  as in the missing data case,  $\mathbf{Y}_{rep}$  is imputed from the posterior distribution of  $P(Y_{j,rep}^{(l)}|\mathbf{Y}_{-j}^{(l)},\mathbf{Z},\theta)$ , where l is an indicator for the synthetic data set (l=1,2,...,m). Note that synthetic values that are imputed at an earlier step can be used for imputing variable j. This process results in the synthetic data  $\mathbf{D} = (\mathbf{D}^{(1)}, \mathbf{D}^{(2)}, ..., \mathbf{D}^{(m)})$ .

For example, overimputing synthetic values for both the observed and missing cells in the mice::boys data set into the object syn, given the same imputation parameters as before, can be realized by the following code execution.

where the argument where requires a matrix of the same dimensions as the data, (i.e., a  $n \times k$  matrix) containing logicals  $z_{ij}$  that indicate which cells are selected to have their values replaced by draws from the posterior predictive distribution. This approach allows to *overimpute* a subset of the observed data, or - as in the above example - the observed data as a whole, resulting in a data set that partly or completely consists of synthetic data values.

Choosing an adequate imputation model to impute the data is paramount, as a flawed imputation model may drastically impact the validity of inferences. Imputation models should be as flexible as possible to capture most of the patterns in the data, and to model possibly unanticipated data characteristics [17,18]. Parametric methods, albeit easy to implement in practice, may be too restrictive to capture generally complex patterns in the data, especially in the case of nonlinear relations and interactions between multiple variables. Classification and regression trees [CART; Breiman *et al.* [19]] allow to model more complex patterns in the data, and have therefore been suggested as an

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appropriate imputation method [20–22]. Loosely speaking, CART sequentially splits the predictor space into non-overlapping regions in such a way that the within-region variance is as small as possible after every split. As such, CART does not impose any parametric distribution on the data, making it a widely applicable method that allows for a large variety of relationships within the data [23]. Given these appealing characteristics and the call for the use of flexible methods when multiply imputing data, we will focus our illustrations and evaluations of mice to method mice.impute.cart(), realized by:

In a nutshell, the above code shows the simplicity of creating m=10 synthetic data sets using mice. In practice, however, one should take some additional complicating factors into account. For example, one should account for deterministic relations in the data. Additionally, relations between variables may be described best using a different model than CART. Such factors are data dependent and should be considered by the imputer. In the next section, we will describe how the boys data can be adequately imputed. Additionally, we will show through simulations that this approach yields valid inferences.

# 3. Materials and Methods

We demonstrate the suitability of using mice for synthesization using a simulation study on the mice::boys data set. This data set consists of the values of 748 Dutch boys on the following 9 variables:

description
age in years
height (cm)
weight (kg)
body mass index
head circumference (cm)
genital Tanner stage G1-G5
pubic hair Tanner P1-P6
testicular volume (ml)
region

Unfortunately, this data set does not differ from the vast majority of collected data sets, in the sense that it suffers from missing data. For simplicity, the data is completed using the default mice imputation model for all predictors except bmi, which is passively imputed using its deterministic relation with weight and height.

```
# create a single imputed, completely observed `boys` data set
set.seed(123)

meth <- make.method(boys)
meth["bmi"] <- "~ I(wgt / (hgt / 100)^2)"
pred <- make.predictorMatrix(boys)</pre>
```

### 3.1. Simulation methods

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To induce sampling variance, 1000 bootstrap samples of the boys data will be synthesized with m=5 imputations. Synthetic values are generated using the CART imputation method for all columns, except for bmi. The deterministic relation bmi which will be synthesized passively based on the synthetic values for hgt and wgt to preserve the relation in the synthetic data. Additional parameters that come with the use of mice.impute.cart() are the complexity parameter cp and the minimum number of observations in any terminal node minbucket, that both constrain the flexibility of the imputation model. The values of the parameters cp and minbucket ought to adhere to the call for imputation models that are as flexible as possible. Appropriate values for these parameters, as well as the input for the predictorMatrix, depend on the data at hand. In the current example, the complexity parameter is specified at cp = 1e-08 rather than the default value 1e-04, and the minimum number of observations in each terminal node is set at minbucket = 3 rather than the default value 5. By allowing for more complexity in the imputation model, bias in the estimates from the synthetic data set is reduced. Additionally, since the missingness pattern is monotone, the number of iterations can be set to maxit = 1.

To assess the performance of mice for synthesizing data, we compare the bootstrapped samples with the synthetic versions of these bootstrapped samples. Specifically, univariate descriptive statistics, the correlation matrix, and two linear regression models as well as one ordered logistic regression model will be considered. Subsequently, the bias in the parameters and the 95% confidence interval coverage of the synthetic data will be examined. Similarly to multiple imputation of missing data, correct inferences from synthetic data requires correct pooling over the multiply imputed data sets.

Obtaining a final point estimate of the parameter of interest Q after imputation is fairly easy and no different from pooling in the case of missing data [10]. One can calculate the average of the m point estimates  $q^{(l)}$ 

$$\bar{q}_m = \sum_{l=1}^m \frac{q^{(l)}}{m}.$$

with  $l=1,\ldots,m$ .

Similarly to the missing data case, variances, and subsequently confidence intervals, should incorporate the increase in variance that is due to imputation [7,24]. Yet, the increase in variance due to imputation differs according to whether missing values are imputed or observed data is overimputed with missing values. Whereas the variance estimate after imputation of missing data needs to account for the fact that a certain amount of information in the data is missing, variance estimation from synthetic data does not suffer from this issue. The adjusted variance estimate that follows from using multiple synthetic data sets only suffers from the fact that a finite number of m synthetic data sets are used to resemble the observed data. Hence, the according variance estimate for synthetic data as developed by Reiter [24] yields

$$T=\bar{u}_m+\frac{b_m}{m},$$

$$b_m = \sum_{l=1}^m \frac{(q^{(l)} - \bar{q}_m)^2}{(m-1)},$$

162 and sampling variance

$$\bar{u}_m = \sum_{l=1}^{\infty} \frac{u^{(l)}}{m},$$

with  $u^{(l)}$  reflecting the variance estimate in the lth synthetic data set.

### 4. Results

This section may be divided by subheadings. It should provide a concise and precise description of the experimental results, their interpretation as well as the experimental conclusions that can be drawn.

- 168 4.1. Subsection Heading Here
- Subsection text here.
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- Bulleted lists look like this:
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- 176 1. First item
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**Figure 1.** This is a figure, Schemes follow the same formatting. If there are multiple panels, they should be listed as: (a) Description of what is contained in the first panel. (b) Description of what is contained in the second panel. Figures should be placed in the main text near to the first time they are cited. A caption on a single line should be centered.

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Title 1	Title 2	Title 3
entry 1	data	data
entry 2	data	data

This is an example of an equation:

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Example of a theorem:

**Theorem 1.** *Example text of a theorem.* 

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Example of a proof:

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#### 5. Discussion

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Authors should discuss the results and how they can be interpreted in perspective of previous studies and of the working hypotheses. The findings and their implications should be discussed in the broadest context possible. Future research directions may also be highlighted.

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This section is not mandatory, but can be added to the manuscript if the discussion is unusually long or complex.

#### 7. Patents

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207 Conflicts of Interest: 'The authors declare no conflict of interest.'

#### 208 Abbreviations

209 The following abbreviations are used in this manuscript:

MDPI Multidisciplinary Digital Publishing Institute

DOAJ Directory of open access journals

TLA Three letter acronym

LD linear dichroism

## 2 Appendix A

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# 213 Appendix A.1

The appendix is an optional section that can contain details and data supplemental to the main text. For example, explanations of experimental details that would disrupt the flow of the main text, but nonetheless remain crucial to understanding and reproducing the research shown; figures of replicates for experiments of which representative data is shown in the main text can be added here if

brief, or as Supplementary data. Mathematical proofs of results not central to the paper can be added as an appendix.

## 220 Appendix B

All appendix sections must be cited in the main text. In the appendixes, Figures, Tables, etc. should be labeled starting with 'A', e.g., Figure A1, Figure A2, etc.

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