



Comparing Fair Ranking Metrics

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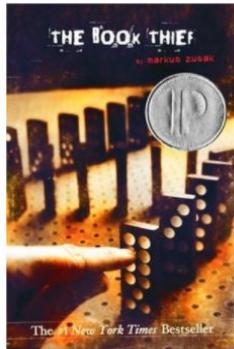
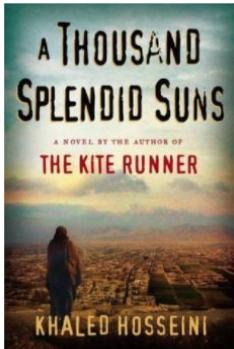
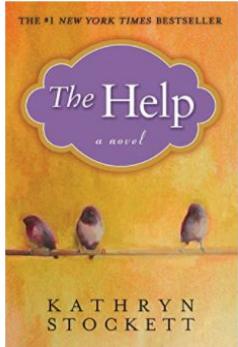
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Ranked List

Low order

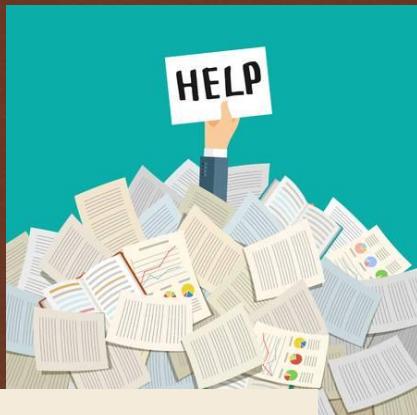
Protected Group



Non-Protected Group

Fair Ranking Metric Resources

1. Measuring Fairness in Ranked Output (Yang et. al.; SSDBM '17): **PreF Δ**
2. FA*IR: A Fair Top-k Ranking Algorithm (Zehlike et.al.; CIKM'17): **FAIR**
3. Equity of Attention: Amortizing Individual Fairness in Rankings (Biega et. al.; SIGIR'18): **IAA**
4. Fairness of Exposure in Ranking (Singh et.al.; KDD'18): **DP, EUR, RUR**
5. Quantifying the Impact of User Attention Fair Group Representation in Ranked List (Sapienzynski et. al.; WWW'19): **AWRF**
6. Fairness in Recommendation Ranking through Pairwise Comparisons (Beutal et.al.; SIGKDD'19): **PAIR**
7. Evaluating Stochastic Ranking with Expected Exposure (Diaz et.al.; CIKM'20): **EEL, EED, EER**
8. Pairwise Fairness for Ranking and Regression (Narasimhan et.al.; AAAI'20): **PAIR**



**Several metrics
to measure
unfairness**



**Difficulty finding
suitable metric(s)**



**Differences and
similarities
among metrics**

Focus of the talk

1

Describe and compare exposure and rank-fairness metrics

2

Identify gaps between their original presentation and the practicalities of applying them to recommender systems

3

Sensitivity analysis to assess the impact of design choices

Fairness Position



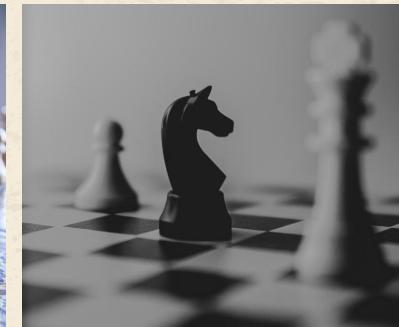
Consumer

Provider

Provider Fairness



Group



Individual

Group Fairness

Factors we considered

Fairness Goal

what does it mean to be fair

Group membership

binary or non-binary group association

Relevance

does the metric consider item relevance score

Weighting Strategy

attention/exposure in different position

- no relevance information
- no weighting model
- binary group membership

Prefix = 10



PreFΔ (Yang et. al)

- 10-item window
- prioritize the top order fairness



ΔND :

K



ΔRD :

X



ΔKL :

K

FAIR (Zehlike et. al)

- every prefix
- given minimum proportion determined by Binomial probabilities



Λ

$\geq p$

Attention/Exposure



AWRF (Sapienzynski et. al)

Expected cumulative exposure( x position weight) $\geq p$

- geometric attention decay
- non-binary group membership
- no relevance information
- uses a population estimator to compare

Population estimator is the group distribution in entire ranked list (true demographics)

Demographic Parity (Singh et.al)

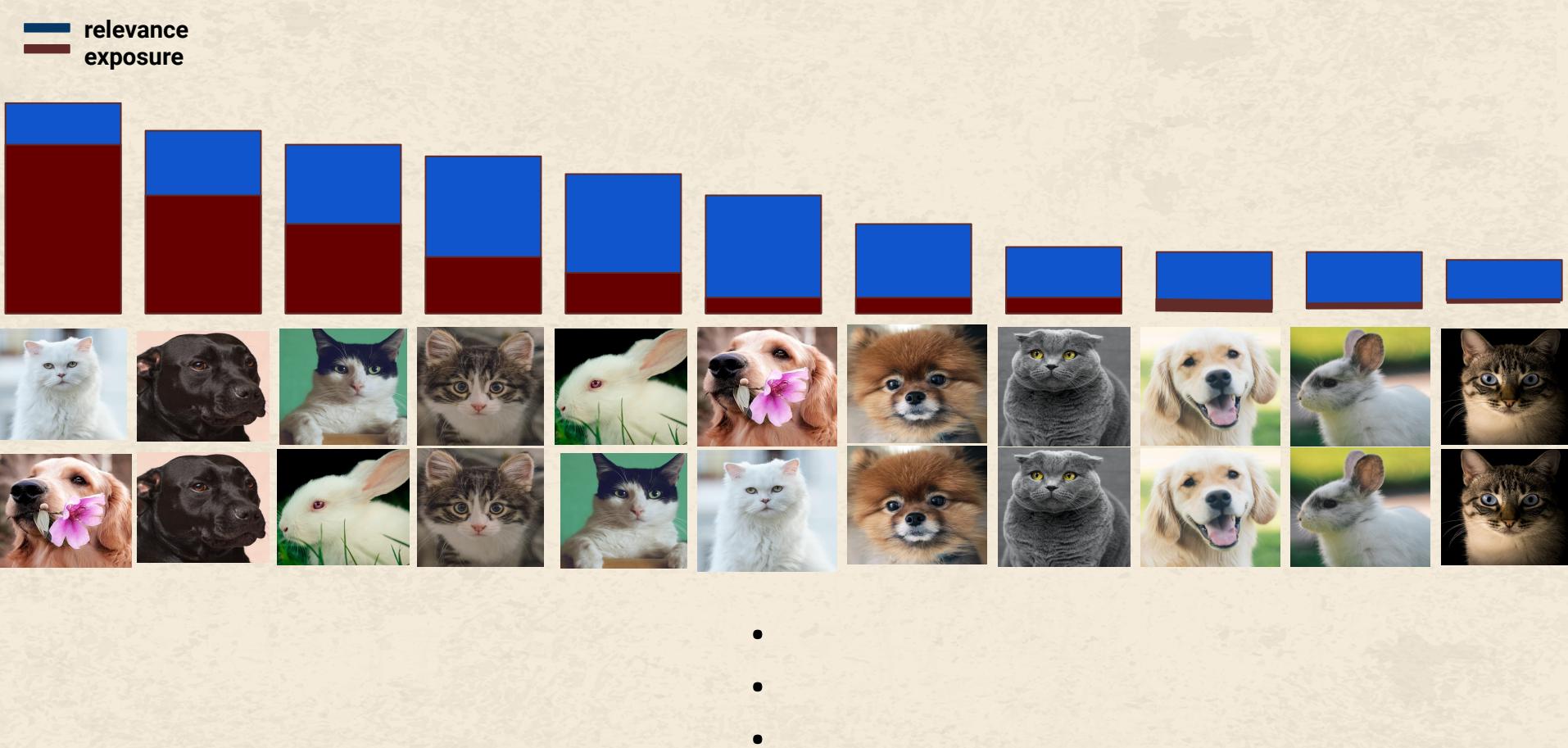
Exp  =Exp 

- logarithmic attention decay
- binary group membership

Expected-Exposure Disparity (Diaz et.al)

EED: Demographic Parity

- rbp & cascade attention decay
- non-binary group membership



Exposure should be proportional to relevance

DTR(EUR)

$$\frac{\text{Exp}}{\text{Utility}} = \frac{\text{Exp}}{\text{Utility}}$$


DIR(RUR)

$$\frac{\text{DCG}}{\text{Utility}} = \frac{\text{DCG}}{\text{Utility}}$$


(Singh et. al)

- probabilistic ranking
- logarithmic attention decay
- binary group membership

IAA (Biega et. al)

$$\frac{\sum \text{Attention}}{\sum \text{Relevance}} = \frac{\sum \text{Attention}}{\sum \text{Relevance}}$$

$$||\text{Attention-Relevance}||_1$$

- sequence of ranking
- geometric attention decay
- binary group membership

EE* (Diaz et. al)

EEL(Expected Exposure Loss):
 $||\text{target-system}||^2$

EER (Expected Exposure Relevance):
Exposure-relevance distribution

- stochastic ranking
- rbp & cascade attention decay
- non-binary group membership

Pair

(Beutal et. al; Narasimhan et.al.)

- single ranking
- uses relevance information
- non-Binary group membership
- pairwise comparison



Relevance \geq Relevance

InterACC:



IntraACC:



Relevance \geq Relevance

Browsing Model (Weighting Strategy)

patience parameter

visiting probability exponentially decreases with position

RBP

stopping probability

visiting probability exponentially decreases with position

Geometric

patience parameter
stopping probability

visiting probability depends on relevance of visited items

Cascade

visiting probability logarithmically decreases with position

Logarithmic

Metric(s)	Goal	Weighting	Relevance	Binary	
PreF Δ	Each prefix representative of whole ranking	✗	✗	Dep on Δ	Single-List metric
AWRF	Weighted representation matches population	Geometric	✗	✗	
FAIR	Each prefix matches target distribution	✗	✗	✓	
DP	Exposure equal across groups	Logarithmic	✗	✓	Distribution and sequence metric
EUR	Exposure proportional to relevance	Logarithmic	✓	✓	
RUR	Discounted gain proportional to relevance	Logarithmic	✓	✓	
IAA	Exposure proportional to predicted relevance	Geometric	Predicted	✗	
EEL, EER	Exposure matches ideal (from relevance)	Cascade, RBP	✓	✗	
EED	Exposure well-distributed	Cascade, RBP	✗	✗	
PAIR	Pairwise preference accurately modeled across groups	✗	✓	✗	

Challenges in implementation

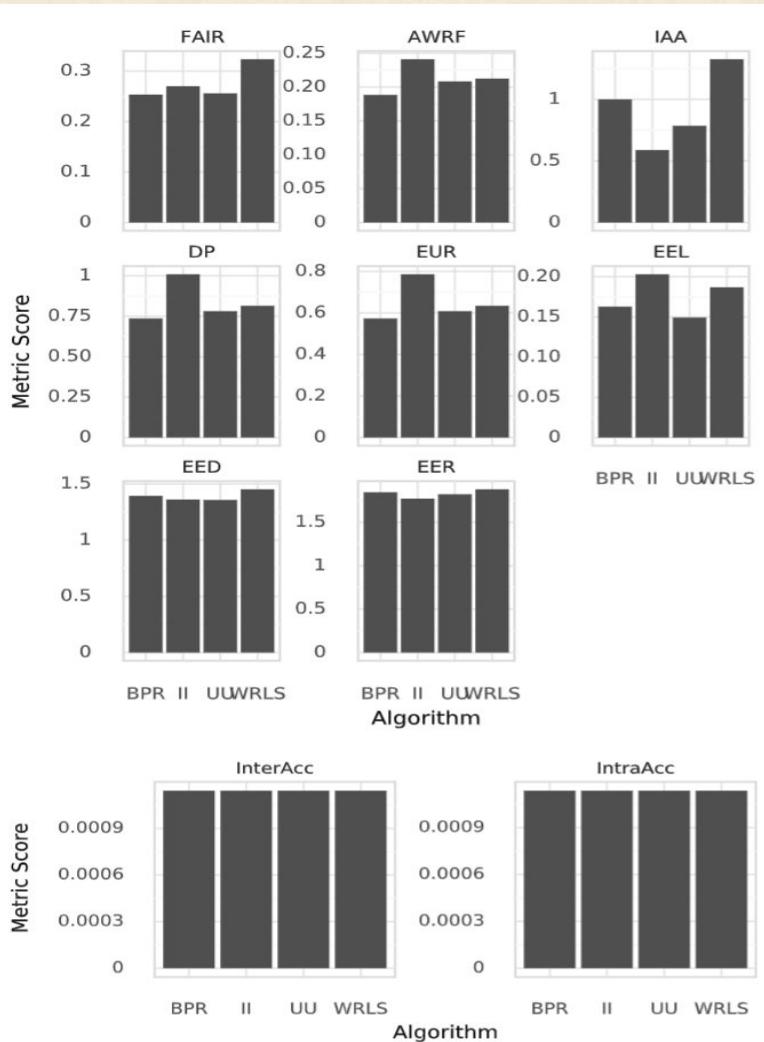


Missing Relevance Information

Missing Group Label

Extreme Imbalance

Parameter Setting



Comparative Analysis

- Algorithms did not show significant differences on most metrics
- No clear agreement

Sensitivity Analysis

Weighting Strategy

Algorithms did not show much difference (except EEL)

Parameter Changes

EE* and AWRF showed unstable response towards parameter change.

Takeaways

- **PreF Δ** and **RUR**: suffer from the missing data (sparsity) problem
- **RUR**: sensitive to imbalance retrieval across groups
- **FAIR, DP, EUR**, and **RUR**: not allowing non-binary protected attributes limits the applicability of those metrics in real data
- **PreF Δ , AWRF, FAIR, DP, EED**: do not consider relevance information
- **IAA**: exhibits a comparatively robust nature
- **DP** and **EUR**: show consistency in response to various parameter changes.
- **EE*** and **AWRF**: significantly sensitive towards the change of parameters

Summary

Defining metrics in unified framework

- Metrics are surprisingly similar

Implement the metrics in same experimental setup

- Missing data, missing relevance information, ranked list size are crucial/delicate factors in implementing metrics.

Sensitivity Analysis

- Metrics differ in their sensitivity towards external factors.
- High sensitivity towards design choices add complexity in the usability of metrics



Thank You