

برای قرص خواهیم داشت:

پایستگی جرم ( $V^z=0$ ):

$$V^R \frac{\partial}{\partial R} (R^{3/2} - K R^{5/2}) + (R^{3/2} + K R^{5/2}) \left( \frac{\partial V^R}{\partial R} \right) = - (R^{3/2} + K R^{5/2}) \left[ V^R \left( \Gamma_{RR}^R + \Gamma_{\phi R}^\phi + \Gamma_{zR}^z \right) - \Gamma_{r0}^0 \right] + V^R \left[ \Gamma_{rz}^r + \Gamma_{\phi z}^\phi + \Gamma_{zz}^z \right] -$$

پایستگی تکانه شعاعی:

$$(R^{3/2} + K R^{5/2}) (u^{\hat{t}} \hat{t} 0)^2 \frac{\partial V^R}{\partial R} V^R + \left[ 1 + \frac{2m}{\sqrt{R^2 + z^2}} \right] \frac{\partial (K R^{5/2})}{\partial R} = - (R^{3/2} + K R^{5/2}) (u^{\hat{t}} \hat{t} 0)^2 \left[ \left( \Gamma_{00}^R \right) - 2 \Gamma_{0R}^0 V^R V^R + 2 V^\phi \Gamma_{0\phi}^R \right]$$

پایستگی تکانه زاویه ای:

$$- (R^{3/2} + K R^{5/2}) (u^{\hat{t}} \hat{t} 0)^2 \left[ 2 V^R \left( \Gamma_{tR}^\phi - \Gamma_{tR}^t V^\phi \right) + V^t V^R \left( \Gamma_{Rt}^\phi - \Gamma_{Rt}^t V^\phi \right) + V^R V^\phi \left( \Gamma_{\phi R}^\phi - \Gamma_{\phi R}^t V^\phi \right) + V^\phi V^R \left( \Gamma_{R\phi}^\phi - \Gamma_{R\phi}^t V^\phi \right) \right] u^{\hat{t}} \hat{t}$$

پایستگی تکانه ارتفاعی:

$$as J^R = 0, \frac{\partial}{\partial z} = 0, V^z = 0 \rightarrow 0 = 0$$

همینطور برای  $J$  در قرص داریم:

$$\left[ B_\phi(R) \right] + B_\phi \left( \frac{mR(R^5 + 2R^4 m - 2R^2 a^2 m)}{R^2(R^6 - 4R^4 m^2 + 4R^2 a^2 m^2)} - \frac{m}{R(R+2m)} - \frac{m}{R(R+2m)} \frac{R^3 m - R^4 + 2R^2 m^2 + 2a^2 m^2}{(R^4 - 4R^2 m^2 + 4a^2 m^2)} \right) \left( \frac{R^2}{R^2 + 2mR + 4m^2} \right) \\ \left[ B_\phi(R) \right] + B_\phi \left( \frac{mR(R^5 + 2R^4 m - 2R^2 a^2 m)}{R^2(R^6 - 4R^4 m^2 + 4R^2 a^2 m^2)} - \frac{m}{R(R+2m)} - \frac{m}{R(R+2m)} \frac{R^3 m - R^4 + 2R^2 m^2 + 2a^2 m^2}{(R^4 - 4R^2 m^2 + 4a^2 m^2)} \right) \left( \frac{R^2}{R^2 + 2mR + 4m^2} \right) \left\{ \right.$$

$$J^z = \frac{-c}{4\pi} \left[ \left( \frac{2R(R^2 + 2mR + 4m^2) - R^2(2R + 2m + 4m^2)}{(R^2 + 2mR + 4m^2)^2} \right) B_\phi(R) \right] + \left( \frac{R^2}{R^2 + 2mR + 4m^2} \right) \frac{\partial B_\phi(R)}{\partial R} + B_\phi \left( \frac{mR(R^5 + 2R^4 m - 2R^2 a^2 m)}{R^2(R^6 - 4R^4 m^2 + 4R^2 a^2 m^2)} - \frac{m}{R(R+2m)} \right)$$

$$J^z = \frac{-c}{4\pi} \left[ \left( \frac{R}{R^2 + 2mR + 4m^2} \right) B_\phi(R) \right] + \left( \frac{R^2}{R^2 + 2mR + 4m^2} \right) \frac{\partial B_\phi(R)}{\partial R} + B_\phi \left( \frac{mR(R^5 + 2R^4 m - 2R^2 a^2 m)}{R^2(R^6 - 4R^4 m^2 + 4R^2 a^2 m^2)} - \frac{m}{R(R+2m)} \right)$$

$$J^z \approx - \left[ \frac{B_\phi(R)}{R} + \frac{\partial B_\phi(R)}{\partial R} + B_\phi \left( \frac{1}{R^2} - \frac{m}{R(R+2m)} - \frac{m}{R(R+2m)} \frac{R^3 m - R^4 + 2R^2 m^2 + 2a^2 m^2}{(R^4 - 4R^2 m^2 + 4a^2 m^2)} \right) \right]$$

$$J^z \approx - \left[ \frac{B_\phi(R)}{R} + \frac{\partial B_\phi(R)}{\partial R} + \frac{B_\phi}{R^2} \right] = \frac{-\partial B_\phi}{\partial R} - B_\phi \left( \frac{1}{R} + \frac{1}{R^2} \right)$$

پایستگی جرم :

$$V^R \frac{\partial}{\partial R} (R^{3/2} - K R^{5/2}) + (R^{3/2} + K R^{5/2}) \left( \frac{\partial V^R}{\partial R} \right) = - (R^{3/2} + K R^{5/2}) \left[ V^R \left( \Gamma_{RR}^R + \Gamma_{\varphi R}^\varphi + \Gamma_{zR}^z \right) - \Gamma_{r0}^0 \right] + V^R \left[ \Gamma_{rz}^r + \Gamma_{\varphi z}^\varphi + \Gamma_{zz}^z \right] -$$

$$\frac{\partial V^R}{\partial R} = \frac{1}{4R} \dot{\phantom{0}}$$

پایستگی تکانه شعاعی:

$$(R^{3/2} + K R^{5/2}) (u \dot{\phantom{0}} \dot{\phantom{0}} 0)^2 \frac{\partial V^R}{\partial R} V^R + \left[ 1 + \frac{2m}{\sqrt{R^2 + z^2}} \right] \frac{\partial (K R^{5/2})}{\partial R} = - (R^{3/2} + K R^{5/2}) (u \dot{\phantom{0}} \dot{\phantom{0}} 0)^2 \left[ \left( \Gamma_{00}^R \right) - 2 \Gamma_{0R}^0 V^R V^R + 2 V^\varphi \Gamma_{0\varphi}^R \right]$$

$$B_\varphi \left[ \frac{-\partial B_\varphi}{\partial R} - B_\varphi \left( \frac{1}{R} + \frac{1}{R^2} \right) \right] (1 + 2u^R u^0) = \dot{\phantom{0}} - \left( R^{\frac{3}{2}} + K R^{\frac{5}{2}} \right) (u \dot{\phantom{0}} \dot{\phantom{0}} 0)^2 \left[ \left( \Gamma_{00}^R \right) - 2 \Gamma_{0R}^0 V^R V^R + 2 V^\varphi \Gamma_{0\varphi}^R + V^t V^R \left( \Gamma_{Rt}^t - \Gamma_{Rt}^0 V^R \right) \right]$$

$$\frac{\partial B_\varphi}{\partial R} = \frac{1}{B_\varphi (1 + 2u^R u^0)} \dot{\phantom{0}}$$

پایستگی تکانه زاویه ای:

$$- (R^{3/2} + K R^{5/2}) (u \dot{\phantom{0}} \dot{\phantom{0}} 0)^2 \left[ 2 V^R \left( \Gamma_{tR}^\varphi - \Gamma_{tR}^t V^\varphi \right) + V^t V^R \left( \Gamma_{Rt}^\varphi - \Gamma_{Rt}^t V^\varphi \right) + V^R V^\varphi \left( \Gamma_{\varphi R}^\varphi - \Gamma_{\varphi R}^t V^\varphi \right) + V^\varphi V^R \left( \Gamma_{R\varphi}^\varphi - \Gamma_{R\varphi}^t V^\varphi \right) \right] \dot{\phantom{0}} \dot{\phantom{0}}$$