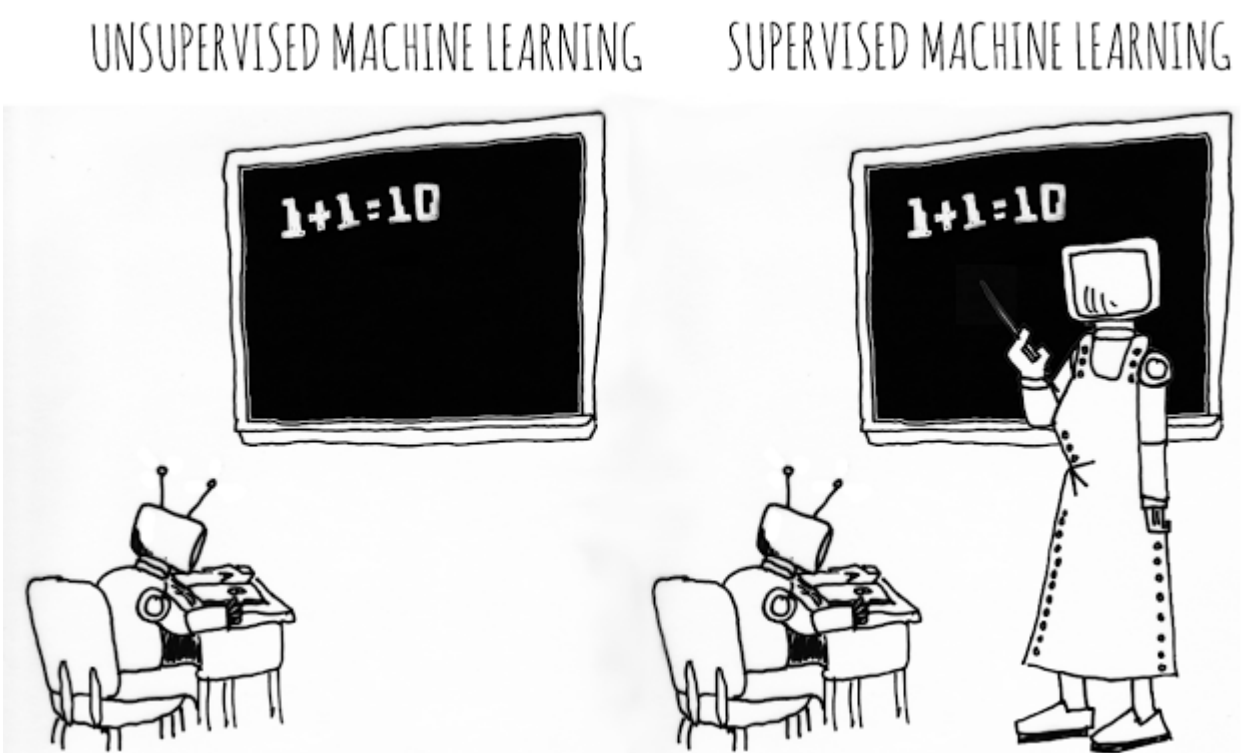


# Unsupervised Learning

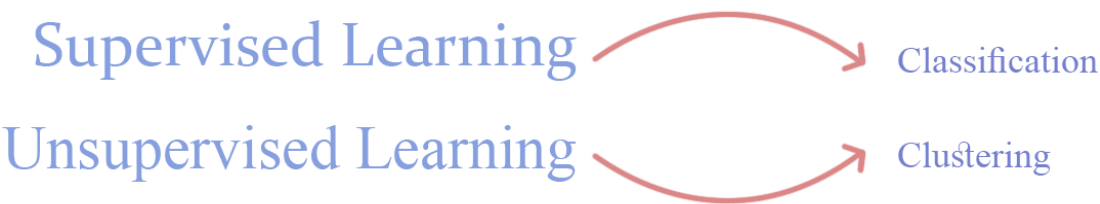
Unsupervised learning finds the pattern in data

Supervised learning :  $(x, y)$   
Unsupervised learning :  $(x)$



by David Taylor

<http://prooffreaderswhimsy.blogspot.com/2014/11/machine-learning.html>  
(<http://prooffreaderswhimsy.blogspot.com/2014/11/machine-learning.html>)

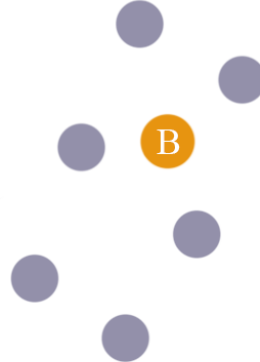
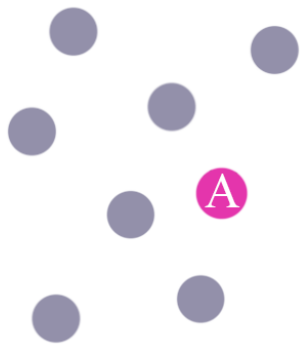


## K-Means

K-Means finds culster of samples

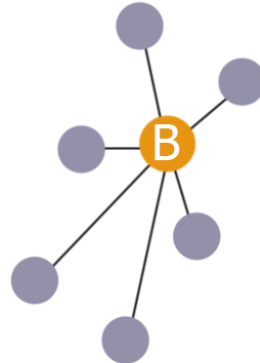
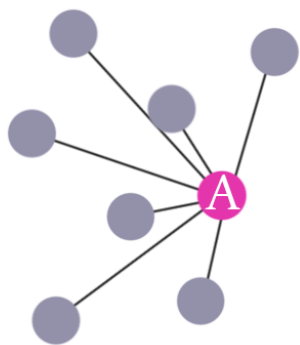
# K-Means

Step one : initialization



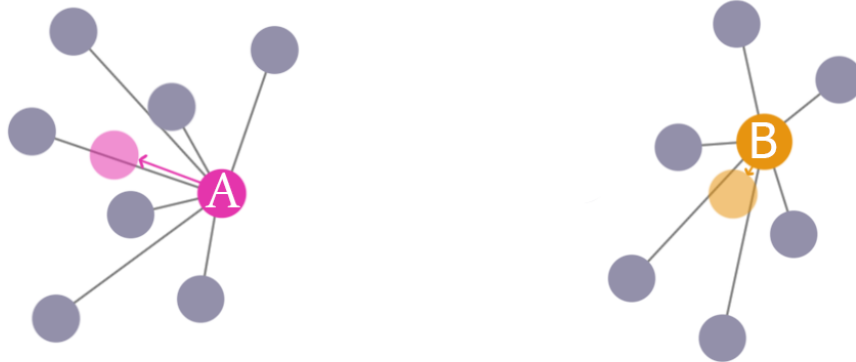
# K-Means

Step two : Assignment



# K-Means

## Step three : Update



### Visualizing K-Means algorithm :

<http://tech.nitoyon.com/en/blog/2013/11/07/k-means/> (<http://tech.nitoyon.com/en/blog/2013/11/07/k-means/>)

```
In [1]: import numpy as np
        from sklearn.datasets import load_iris
        from sklearn.cluster import KMeans
        import matplotlib.pyplot as plt
```

```
In [2]: iris = load_iris()
```

```
In [3]: iris.data
```

```
Out[3]: array([[ 5.1,  3.5,  1.4,  0.2],
 [ 4.9,  3. ,  1.4,  0.2],
 [ 4.7,  3.2,  1.3,  0.2],
 [ 4.6,  3.1,  1.5,  0.2],
 [ 5. ,  3.6,  1.4,  0.2],
 [ 5.4,  3.9,  1.7,  0.4],
 [ 4.6,  3.4,  1.4,  0.3],
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 [ 4.4,  2.9,  1.4,  0.2],
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 [ 5.4,  3.7,  1.5,  0.2],
 [ 4.8,  3.4,  1.6,  0.2],
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 [ 4.3,  3. ,  1.1,  0.1],
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 [ 5.7,  4.4,  1.5,  0.4],
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 [ 5.1,  3.7,  1.5,  0.4],
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 [ 5. ,  3.4,  1.6,  0.4],
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 [ 5.2,  3.4,  1.4,  0.2],
 [ 4.7,  3.2,  1.6,  0.2],
 [ 4.8,  3.1,  1.6,  0.2],
 [ 5.4,  3.4,  1.5,  0.4],
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 [ 5.5,  4.2,  1.4,  0.2],
 [ 4.9,  3.1,  1.5,  0.1],
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 [ 5.5,  3.5,  1.3,  0.2],
 [ 4.9,  3.1,  1.5,  0.1],
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 [ 5.1,  3.4,  1.5,  0.2],
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 [ 4.4,  3.2,  1.3,  0.2],
 [ 5. ,  3.5,  1.6,  0.6],
 [ 5.1,  3.8,  1.9,  0.4],
 [ 4.8,  3. ,  1.4,  0.3],
 [ 5.1,  3.8,  1.6,  0.2],
 [ 4.6,  3.2,  1.4,  0.2],
 [ 5.3,  3.7,  1.5,  0.2],
 [ 5. ,  3.3,  1.4,  0.2],
 [ 7. ,  3.2,  4.7,  1.4],
 [ 6.4,  3.2,  4.5,  1.5],
 [ 6.9,  3.1,  4.9,  1.5],
 [ 5.5,  2.3,  4. ,  1.3],
 [ 6.5,  2.8,  4.6,  1.5],
 [ 5.7,  2.8,  4.5,  1.3],
 [ 6.3,  3.3,  4.7,  1.6],
 [ 4.9,  2.4,  3.3,  1. ],
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 [ 6. ,  2.2,  4. ,  1. ],
 [ 6.1,  2.9,  4.7,  1.4],
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 [ 6.7,  3.1,  4.4,  1.4],
 [ 5.6,  3. ,  4.5,  1.5],
 [ 5.8,  2.7,  4.1,  1. ],
 [ 6.2,  2.2,  4.5,  1.5],
 [ 5.6,  2.5,  3.9,  1.1],
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 [ 6.1,  2.8,  4.7,  1.2],
```

[ 6.4, 2.9, 4.3, 1.3],  
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[ 6.8, 3. , 5.5, 2.1],  
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[ 5.8, 2.8, 5.1, 2.4],  
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[ 6.4, 2.8, 5.6, 2.1],  
[ 7.2, 3. , 5.8, 1.6],  
[ 7.4, 2.8, 6.1, 1.9],  
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[ 6.1, 2.6, 5.6, 1.4],  
[ 7.7, 3. , 6.1, 2.3],  
[ 6.3, 3.4, 5.6, 2.4],  
[ 6.4, 3.1, 5.5, 1.8],  
[ 6. , 3. , 4.8, 1.8],  
[ 6.9, 3.1, 5.4, 2.1],  
[ 6.7, 3.1, 5.6, 2.4],  
[ 6.9, 3.1, 5.1, 2.3],  
[ 5.8, 2.7, 5.1, 1.9],  
[ 6.8, 3.2, 5.9, 2.3],  
[ 6.7, 3.3, 5.7, 2.5],  
[ 6.7, 3. , 5.2, 2.3],  
[ 6.3, 2.5, 5. , 1.9],  
[ 6.5, 3. , 5.2, 2. ],

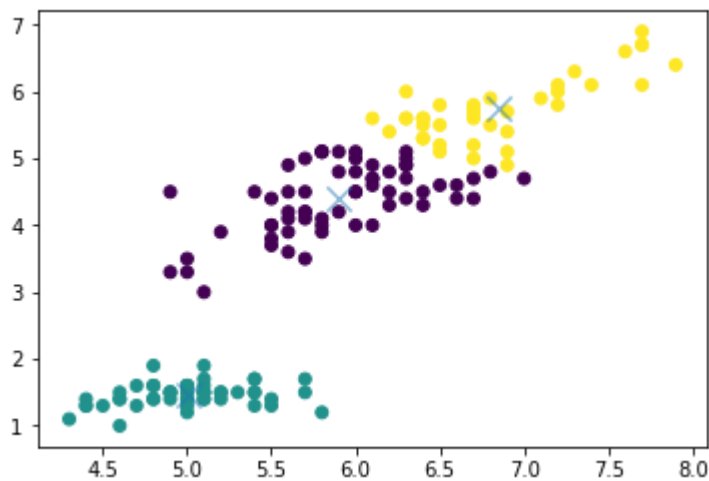
```
[ 6.2,  3.4,  5.4,  2.3],  
[ 5.9,  3. ,  5.1,  1.8]])
```

```
In [4]: kmn = KMeans(n_clusters=3)  
kmn.fit(iris.data)  
labels = kmn.predict(iris.data)
```

```
In [5]: labels
```

```
Out[5]: array([1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,  
              1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,  
              1, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
              0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
              0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 2, 2, 2, 0, 2, 2, 2, 2, 2, 0, 0,  
              2, 2, 2, 2, 0, 2, 0, 2, 0, 2, 2, 0, 0, 2, 2, 2, 2, 2, 0, 2, 2, 2,  
              0, 2, 2, 2, 0, 2, 2, 2, 0, 2, 2, 0])
```

```
In [6]: xs = iris.data[:,0]  
ys = iris.data[:,2]  
  
centroids = kmn.cluster_centers_  
  
plt.scatter(xs, ys, c=labels)  
plt.scatter(centroids[:,0],centroids[:,2],marker='x',s=150,alpha=0.5)  
plt.show()
```



## evaluation a clustering

**inertia** :distance from each sample to centroids of its cluster or how spread out the clusters.  
(Lower is better)

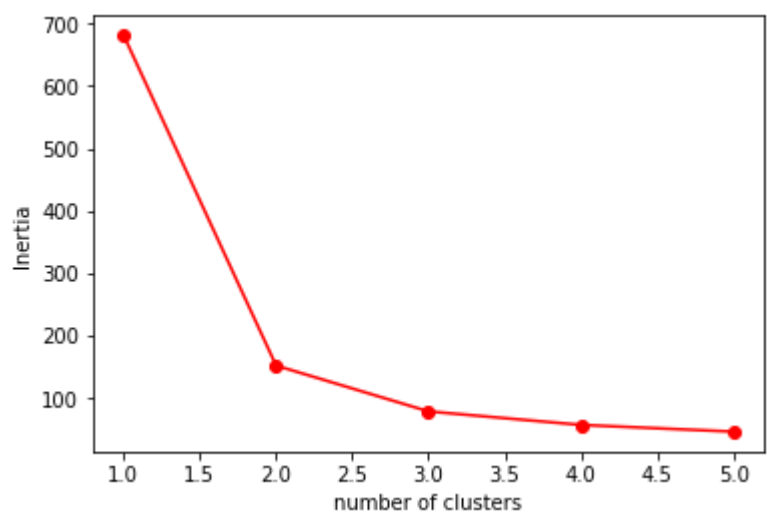
```
In [7]: print(kmn.inertia_)
```

```
78.9408414261
```

```
In [8]: inertia_list = []  
  
for k in np.arange(1, 6):  
    kmn = KMeans(n_clusters=k)  
    kmn.fit(iris.data)  
    inertia_list.append(kmn.inertia_)  
  
inertia_list
```

```
Out[8]: [680.82439999999997,  
         152.36870647733906,  
         78.940841426146022,  
         57.345409315718165,  
         46.535582051282049]
```

```
In [9]: plt.plot(np.arange(1,6),inertia_list,'ro-')
plt.xlabel('number of clusters')
plt.ylabel('Inertia')
plt.show()
```



## Hierarchical Clustering

Iran

India

France

Italy

Greece

- every country begins in a seperate cluster .
- at each step , the two closest clusters are merged .
- continue until all countries in a single cluster .

dendrogram.png

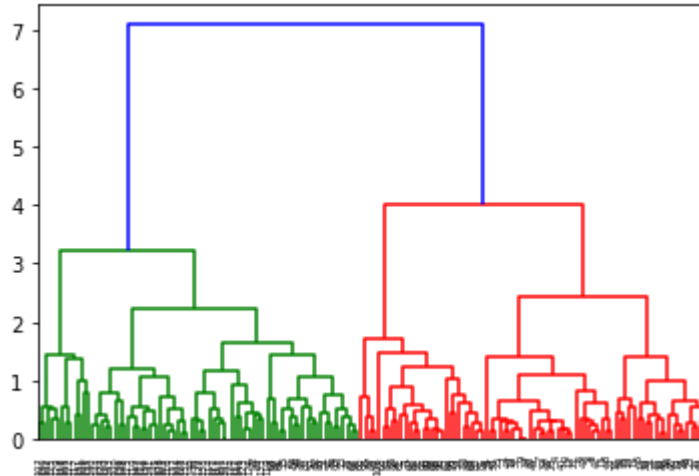
**Wikipedia :**  
a dendrogram (from Greek dendro "tree" and gramma "drawing") is a tree diagram frequently used to illustrate the arrangement of the clusters produced by hierarchical clustering.

This is a "bottom up" approach called **Agglomerative**.

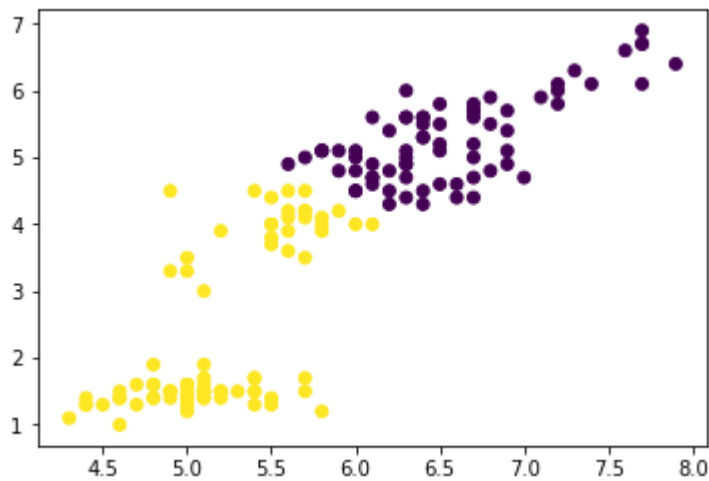


```
In [10]: from scipy.cluster.hierarchy import linkage,dendrogram,fcluster
import matplotlib.pyplot as plt
```

```
hir = linkage(iris.data,method='complete')
labels = fcluster(hir, 6, criterion='distance')
print(labels)
dendrogram(hir,leaf_rotation=90)
plt.show()
```

[illegible]

```
In [11]: plt.scatter(iris.data[:,0], iris.data[:,2], c=labels)
plt.show()
```

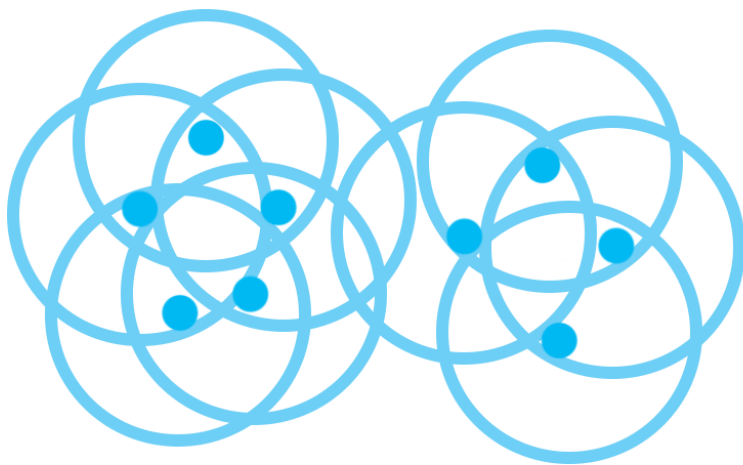


## Meanshift

MeanShift

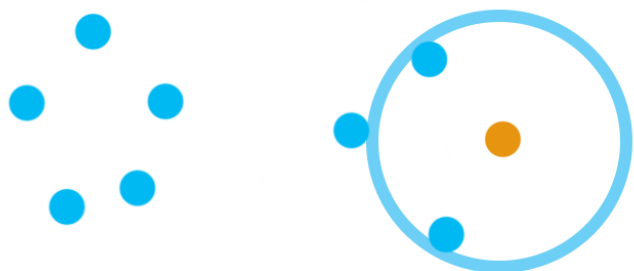


MeanShift



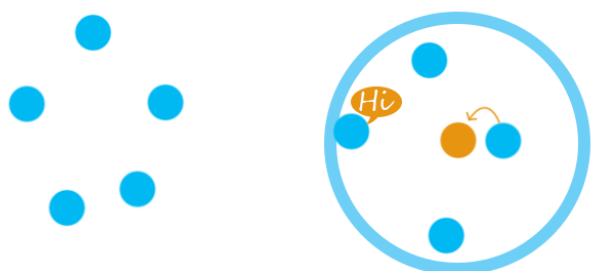
Bandwidth

MeanShift



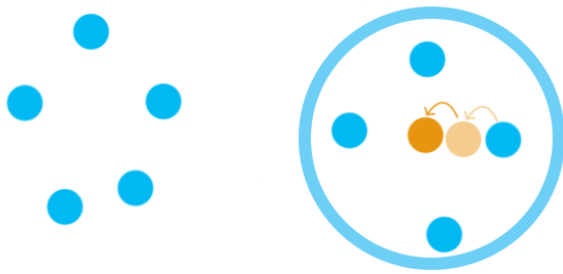
Bandwidth

MeanShift



Bandwidth

## MeanShift



## Bandwidth

```
In [12]: from sklearn.cluster import MeanShift
```

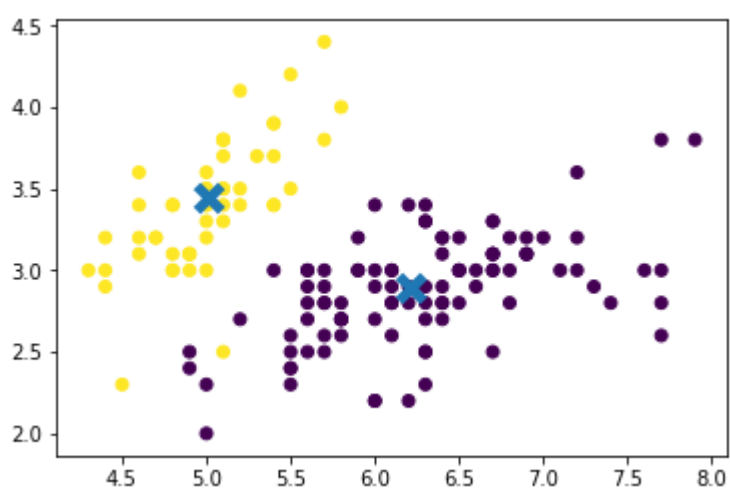
```
In [13]: x = iris.data
ms = MeanShift()
ms.fit(x)
labels = ms.labels_

cluster_center = ms.cluster_centers_
n_cluster = len(np.unique(labels))

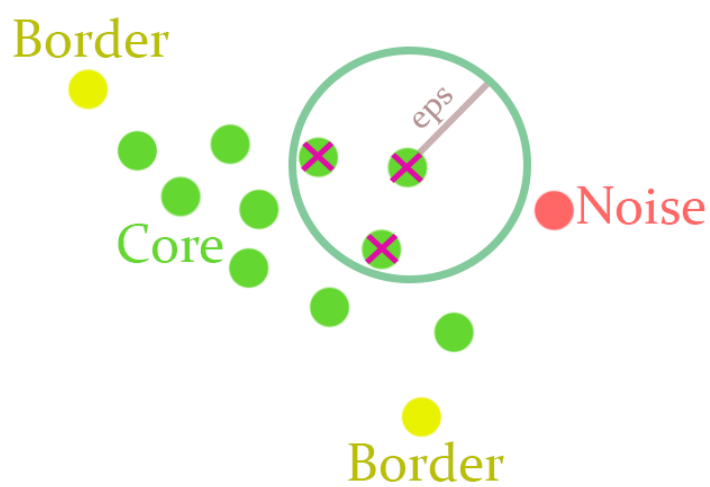
print('Number of estimated cluster:' ,n_cluster)

plt.scatter(x[:,0], x[:,1], c=labels)
plt.scatter(cluster_center[:,0], cluster_center[:,1], marker='x', s=150, linewidth=5, z
order=10)
plt.show()
```

Number of estimated cluster: 2



**DBSCAN : Density-Based Spatial Clustering of Applications with Noise**



## DBSCAN

MinSamples = 3

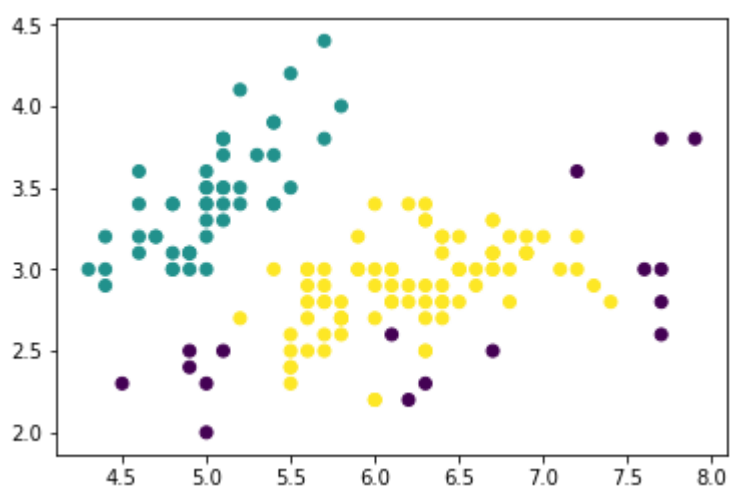


```
In [14]: from sklearn.cluster import DBSCAN
```

```
In [15]: dbscan = DBSCAN()
dbscan.fit(iris.data)
labels = dbscan.labels_
```

```
In [16]: xx = iris.data[:,0]
yy = iris.data[:,1]

plt.scatter(xx,yy, c=labels)
plt.show()
```



## Dimensity Reduction