

Package ‘SDRcausal’

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Title SDRcausal

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Description Provides two semiparametric estimators, semipar_imputation and semipar_ipw.

Encoding UTF-8

Imports stats, ggplot2

Suggests nloptr

LazyData true

License GPL (>= 2)

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R topics documented:

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aipw_variance	<i>Estimates Augmented Inverse Probability variance</i>
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Description

Variance of the Augmented IPW as in Ghosh, Ma, & De Luna (2020).

Usage

```
aipw_variance(
  x,
  y,
  treated,
  imp,
  ipw,
  bandwidth_scale1,
  bandwidth_scale0,
  bandwidth_scale_pr,
  kernel = "EPAN",
  explicit_bandwidth = TRUE,
  gauss_cutoff = 0.001,
  num_deriv_h = 1e-08,
  verbose = FALSE
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vector indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()
bandwidth_scale1	Scaling of the calculated bandwidth, m1
bandwidth_scale0	Scaling of the calculated bandwidth, m0
bandwidth_scale_pr	Scaling of the calculated bandwidth, pr
kernel	Specifies which kernel function to be used
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = bandwidth_scale * sd(x * beta) * n^{(1/5)}$.
gauss_cutoff	Cutoff value for Gaussian kernel
num_deriv_h	Step size of numerical derivative.
verbose	Specifies if the program should print output while running.

Value

The variance of Augmented IPW

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 10,
  bwc_prop_score = 18)

# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::aipw_variance(x, y, trt, imp, ipw,
  bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0,
  bandwidth_scale_pr = ipw$bw_pr)
```

b10_fun

Calculates B1/0

Description

Calculates Eq 2.8 or 2.10 in Ghosh, Ma, & De Luna (2020).

Usage

```
b10_fun(x, treated, dm, beta, kernel, bandwidth, gauss_cutoff)
```

Arguments

x	Projection of covariate matrix on CMS
treated	Binary vector indicating treatment.
dm	Derivative of imputed values
beta	CMS
kernel	Specifies which kernel function to be used
bandwidth	Specifies if bandwidth_scale will be used as the
gauss_cutoff	Cutoff value for Gaussian kernel

Value

B1/0 matrix

b_fun	<i>Calculates B1/0</i>
-------	------------------------

Description

Calculates Eq 2.8 or 2.10 in Ghosh, Ma, & De Luna (2020).

Usage

```
b_fun(x, treated, alpha_hat, h, kernel, bandwidth, bandwidth_pr, verbose)
```

Arguments

x	Projection of covariate matrix on CMS
treated	Treated
alpha_hat	Derivative of imputed values
h	CMS
kernel	Specifies which kernel function to be used
bandwidth	Kernel bandwidth
bandwidth_pr	Kernel bandwidth for probability
verbose	Specifies if the program should print output while running.

Value

B1/0 matrix

example_data	<i>Example data</i>
--------------	---------------------

Description

Data generated as in paper, study 1. Using the betas in betas data. Use beta1/0 for imputation as the initial guess of the central mean space (CMS) and alpha as the initial guess of the CMS for IPW.

Format

Data used in examples of the SDRcausal package

covariates covariate matrix

outcomes observed outcome vector

treated binary treatment vector

beta1_guess Starting guess for CMS for treated

beta0_guess Starting guess for CMS for untreated

alpha_guess Starting guess for CMS for propensity score

imp2_variance	<i>Estimates IMP2 variance</i>
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Description

Variance of IMP2 as in Ghosh, Ma, & De Luna (2020).

Usage

```
imp2_variance(
  x,
  y,
  treated,
  imp,
  ipw,
  bandwidth_scale1,
  bandwidth_scale0,
  kernel = "EPAN",
  explicit_bandwidth = TRUE,
  gauss_cutoff = 0.001
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vetor indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()
bandwidth_scale1	Scaling of the calculated bandwidth, or in case explicit_bandwidth the actual bandwidth. For m1 and beta1.
bandwidth_scale0	See bandwidth_scale1. For m0 and beta0.
kernel	Specifies which kernel function to be used
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = bandwidth_scale * sd(x * beta) * n^{(1/3)}$.
gauss_cutoff	Cutoff value for Gaussian kernel

Value

Variance of IMP

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 10,
  bwc_prop_score = 18)

# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::imp_variance(x, y, trt, imp, ipw,
  bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0)
```

```
improved_augmented_ipw
```

Improved Augmented IPW (IAIPW)

Description

Combines IPW and IMP estimators to form the improved augmented IPW, IAIPW as in Ghosh, Ma, & De Luna (2020).

Usage

```
improved_augmented_ipw(y, treated, imp, ipw)
```

Arguments

y	Observed response
treated	Binary vector indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()

Value

Average treatment effect (ATE) for the improved augmented IPW (IAIPW)

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 10,
  bwc_prop_score = 18)

# Calculate the variance of the Augmented IPW (AIPW)
iaipw <- SDRcausal::improved_augmented_ipw(y, trt, imp, ipw)
```

impute

Estimates imputed values based on CMS

Description

Performs semiparametric imputation based on the CMS calculated by `imp_dim_red`, as in Ghosh, Ma, & De Luna (2020).

Usage

```
impute(
  x,
  y,
  treated,
  beta_hat,
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  bandwidth_scale = 1,
  gauss_cutoff = 0.001,
  to_extrapolate = TRUE,
  to_truncate = TRUE,
  extrapolation_basis = as.integer(5),
  verbose = FALSE
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vector indicating treatment
beta_hat	Locally efficient CMS
kernel	Specifies which kernel function to be used
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = bandwidth_scale * sd(x * beta) * n^{1/3}$
bandwidth_scale	Kernel bandwidth
gauss_cutoff	Cutoff value for Gaussian kernel
to_extrapolate	Specifies whether to extrapolate or not
to_truncate	Specifies whether to extrapolate or not
extrapolation_basis	Number of data point to base extrapolation on.
verbose	Specifies if the program should print output while running

Value

A list containing the reduced space xb , the imputed values and their derivatives.

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess

# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt1 <- SDRcausal::treated
n <- as.integer(dim(x)[1])
trt0 <- as.integer(rep(1, times = n) - trt1)
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
```



```

# Perform semiparametric dimension reduction for treated
cms1 <- SDRcausal::imp_dim_red(x, y, trt1, b1,
  explicit_bandwidth = 1, bandwidth_scale = 1)

# Perform semiparametric dimension reduction for untreated
cms0 <- SDRcausal::imp_dim_red(x, y, trt0, b0,
  explicit_bandwidth = 1, bandwidth_scale = 1)

# Perform semiparametric imputation for treated
m1 <- SDRcausal::impute(x, y, trt1, cms1$fb,
  explicit_bandwidth = 1, bandwidth_scale = cms1$bw)

# Perform semiparametric imputation for untreated
m0 <- SDRcausal::impute(x, y, trt0, cms0$fb,
  explicit_bandwidth = 1, bandwidth_scale = cms0$bw)

```

imp_dim_red

*Estimates the Central Mean Space (CMS)***Description**

Semiparametric estimation of the Central Mean Space (CMS) as in Ghosh, Ma, & De Luna (2020). To be used with `SDRcausal::impute()`.

Usage

```

imp_dim_red(
  x,
  y,
  treated,
  beta_initial,
  solver = "optim",
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  bandwidth_scale = 1,
  gauss_cutoff = 0.001,
  penalty = 10,
  n_before_pen = 1,
  root_tol = 0.001,
  n_threads = 1,
  verbose = FALSE,
  ...
)

```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vetor indicating treatment
beta_initial	Initial guess of CMS

solver	Specifies which solver to be used. Current options optim and cobyla (from nloptr package).
kernel	Specifies which kernel function to be used, current options are: "EPAN", "QUARTIC", and "GAUSSIAN".
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = \text{bandwidth_scale} * \text{sd}(x * \text{beta}) * n^{1/5}$
bandwidth_scale	Scaling of the bandwidth or the actual bandwidth if explicit bandwidth.
gauss_cutoff	cutoff value for Gaussian kernel
penalty	Penalty for the optimizer if local linear regression fails. Added to the function value in solver as: $\text{penalty}^{(n - n_before_pen)}$, where n is the number of llr fails.
n_before_pen	Number of probabilities outside the range (0, 1) to accept during dimension reduction.
root_tol	Tolerance which makes the program warn if optim stops at a value higher than root_tol.
n_threads	Sets number of threads for parallel run. Set to 0 serial. If n_threads exceeds maximum number of threads, sets n_threads to max_threads - 1. To use max_threads, set to n_threads to max_threads of system.
verbose	Specifies if the program should print output while running.
...	Additional parameters passed to optim.

Value

A list containing the final beta, the bandwidth used, a warning if optim does not converge or converges to a value that is larger than root_tol, and the output of optim.

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

See Also

[stats::optim]

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt1 <- SDRcausal::treated
trt0 <- rep(1, length(trt1)) - trt1
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess

# Perform semiparametric dimension reduction for treated
cms1 <- SDRcausal::imp_dim_red(x, y, trt1, b1,
  explicit_bandwidth = TRUE, bandwidth_scale = 1)
```

```
# Perform semiparametric dimension reduction for untreated
cms0 <- SDRcausal::imp_dim_red(x, y, trt0, b0,
  explicit_bandwidth = TRUE, bandwidth_scale = 1)
```

imp_variance	<i>Estimates IMP variance</i>
--------------	-------------------------------

Description

Variance of the IMP as in Ghosh, Ma, & De Luna (2020).

Usage

```
imp_variance(
  x,
  y,
  treated,
  imp,
  ipw,
  bandwidth_scale1,
  bandwidth_scale0,
  kernel = "EPAN",
  explicit_bandwidth = TRUE,
  gauss_cutoff = 0.001
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vetor indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()
bandwidth_scale1	Scaling of the calculated bandwidth, or in case explicit_bandwidth the actual bandwidth. For m1 and beta1.
bandwidth_scale0	See bandwidth_scale1. For m0 and beta0.
kernel	Specifies which kernel function to be used
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = bandwidth_scale * sd(x * beta) * n^{(1/3)}$.
gauss_cutoff	Cutoff value for Gaussian kernel

Value

Variance of IMP

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 10,
  bwc_prop_score = 18)

# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::imp_variance(x, y, trt, imp, ipw,
  bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0)
```

ipw_augment

Combines IPW and IMP estimators to form the augmented IPW, AIPW

Description

Augmented IPW (AIPW) as in Ghosh, Ma, & De Luna (2020).

Usage

```
ipw_augment(y, treated, imp, ipw)
```

Arguments

y	Observed response
treated	Binary vector indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()

Value

Average treatment effect (ATE) for the augmented IPW (AIPW)

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 8,
  bwc_prop_score = 8)

# Calculate the variance of the Augmented IPW (AIPW)
aipw <- SDRcausal::improved_augmented_ipw(y, trt, imp, ipw)
```

ipw_dim_red

Estimates the Central Mean Space (CMS)

Description

Semiparametric estimation of the Central Mean Space (CMS) as in Ghosh, Ma, & De Luna (2020). To be used with `SDRcausal::propensity_score()`.

Usage

```
ipw_dim_red(
  x,
  treated,
  alpha_initial,
  solver = "optim",
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  bandwidth_scale = 1,
  gauss_cutoff = 0.001,
  penalty = 10,
  n_before_pen = 5,
  root_tol = 0.001,
  n_threads = 1,
```

```

    verbose = FALSE,
    ...
)

```

Arguments

<code>x</code>	Covariate matrix
<code>treated</code>	Binary vector indicating treatment
<code>alpha_initial</code>	Initial guess of CMS
<code>solver</code>	Specifies which solver to be used. Current options <code>optim</code> and <code>cobyla</code> (from <code>nloptr</code> package).
<code>kernel</code>	Specifies which kernel function to be used, current options are: "EPAN", "QUARTIC", and "GAUSSIAN".
<code>explicit_bandwidth</code>	Specifies if <code>bandwidth_scale</code> will be used explicitly as the bandwidth.
<code>bandwidth_scale</code>	Scaling of the calculated bandwidth, or in case of <code>explicit_bandwidth = TRUE</code> the bandwidth.
<code>gauss_cutoff</code>	cutoff value for Gaussian kernel
<code>penalty</code>	Penalty for the optimizer if a probability is outside (0, 1). Added to the function value in <code>optim</code> as: penalty^n , where n is the number of probabilities outside (0, 1).
<code>n_before_pen</code>	Number of probabilities outside the range (0, 1) to accept during dimension reduction.
<code>root_tol</code>	Tolerance which makes the program warn if <code>optim</code> stops at a value higher than <code>root_tol</code> .
<code>n_threads</code>	Sets number of threads for parallel run. Set to 0 serial. If <code>n_threads</code> exceeds maximum number of threads, sets <code>n_threads</code> to <code>max_threads - 1</code> . To use <code>max_threads</code> , set to <code>n_threads</code> to <code>max_threads</code> of system.
<code>verbose</code>	Specifies if the program should print output while running.
<code>...</code>	Additional parameters passed to solver.

Value

A list containing the final `alpha`, `bandwidth` used, and the output of `optim`

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

See Also

[stats::optim]

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
alp <- SDRcausal::alpha_guess

# Perform semiparametric dimension reduction for treated
cms <- SDRcausal::ipw_dim_red(x, trt, alp,
  explicit_bandwidth = TRUE, bandwidth_scale = 8)
```

ipw_variance	<i>Estimates IPW variance</i>
--------------	-------------------------------

Description

Variance of the IPW as in Ghosh, Ma, & De Luna (2020).

Usage

```
ipw_variance(
  x,
  y,
  treated,
  imp,
  ipw,
  bandwidth_scale,
  kernel = "EPAN",
  explicit_bandwidth = TRUE,
  gauss_cutoff = 0.001,
  num_deriv_h = 0.001,
  verbose = FALSE
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vector indicating treatment
imp	imp_output object from semipar_imputation()
ipw	ipw_output object from semipar_ipw()
bandwidth_scale	Scaling of the calculated bandwidth, or in case of
kernel	Specifies which kernel function to be used

explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = \text{bandwidth_scale} * \text{sd}(x * \text{beta}) * n^{1/3}$.
gauss_cutoff	Cutoff value for Gaussian kernel
num_deriv_h	Step size of numerical derivative.
verbose	Specifies if the program should print output while running.

Value

The variance of IPW

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 10,
  bwc_prop_score = 18)

# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::ipw_variance(x, y, trt, imp, ipw,
  bandwidth_scale = ipw$bw_pr)
```

nw_kernel_regress

The Nadaraya-Watson kernel estimator

Description

Gives the expected value of Y given $X = x$ by kernel regression according to the Nadaraya-Watson kernel estimator to get $E(Y|X)$. Note that y and x may be vectors or matrices, as long as $\text{dim}(x)[1] == \text{dim}(y)[1]$.

Usage

```
nw_kernel_regress(
  y,
  x,
  bandwidth = 1,
  kernel = "EPAN",
  gauss_cutoff = 0.001,
  verbose = FALSE
)
```

Arguments

y	Y in $E(Y X)$
x	X in $E(Y X)$
bandwidth	Kernel bandwidth
kernel	Indicates which kernel function to be used
gauss_cutoff	Cutoff value for Gaussian kernel
verbose	Specifies if the program should print output while running.

Value

Value of kernel regression

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes

# Estimating y given x,  $E(y | x)$ 
k <- nw_kernel_regress(y, x, bandwidth = 1)
```

plot_imp

Plots imputation output

Description

Plot function for visualisation of imputation output from `semipar_imputation`. Note: The function requires `ggplot2`.

Usage

```
plot_imp(x, y, treated, imp)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vetor indicating treatment
imp	imp_output object from semipar_imputation()

Value

A list of ggplot plots of observed and imputed values (pl_imp), imputed treated values vs CMS (pl_m1), and imputed untreated values vs CMS (pl_m0).

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Plotting
plots <- plot_imp(x, y, trt, imp)
```

plot_ipw

Plots IPW output

Description

Plot function for visualisation of IPW output from semipar_ipw. Note: The function requires ggplot2.

Usage

```
plot_ipw(treated, ipw)
```

Arguments

treated	Binary vetor indicating treatment
ipw	ipw_output object from semipar_ipw()

Value

ggplot plot of the propensity score vs CMS.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
alp <- SDRcausal::alpha_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

# Plotting
plots <- plot_imp(x, y, trt, imp)
```

propensity_score	<i>Estimates propensity score</i>
------------------	-----------------------------------

Description

Semiparametric estimation of the propensity score as in Ghosh, Ma, & De Luna (2020). To be used with `SDRcausal::ipw_dim_red()`.

Usage

```
propensity_score(
  x,
  treated,
  alpha_hat,
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  bandwidth_scale = 1,
  verbose = FALSE
)
```

Arguments

x	Covariate matrix
treated	Binary vetor indicating treatment
alpha_hat	Locally efficient CMS
kernel	Kernel specification

explicit_bandwidth Specifies if `bandwidth_scale` will be used as the bandwidth or if it will be calculated as $bw = bandwidth_scale * sd(x * beta) * n^{(1/3)}$.

bandwidth_scale Scaling of calculated bandwidth, or if `explicit_bandwidth = TRUE` used as the bandwidth.

verbose Specifies if the program should print output while running.

Value

A list containing the estimated propensity scores values and their derivatives, and the bandwidth used.

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
alp <- SDRcausal::alpha_guess

# Perform semiparametric dimension reduction
cms <- SDRcausal::ipw_dim_red(x, trt, alp,
  explicit_bandwidth = TRUE, bandwidth_scale = 8)

# Estimate propensity score
pr_score <- SDRcausal::propensity_score(x, trt, cms$fa,
  bandwidth_scale = 8)
```

semipar_imputation	<i>Estimates Average Treatment Effect (ATE) by imputation (IMP)</i>
--------------------	---

Description

Semiparametric estimation of the average treatment effect based on the imputation method described in Ghosh, Ma, & De Luna (2020).

Usage

```
semipar_imputation(
  x,
  y,
  treated1,
  beta_guess1,
```

```

    beta_guess0,
    solver = "optim",
    kernel = "EPAN",
    explicit_bandwidth = FALSE,
    recalc_bandwidth = FALSE,
    bwc_dim_red1 = 1,
    bwc_impute1 = 1,
    bwc_dim_red0 = 1,
    bwc_impute0 = 1,
    gauss_cutoff = 0.001,
    penalty = 10,
    n_before_pen = 5,
    to_extrapolate = TRUE,
    to_truncate = TRUE,
    extrapolation_basis = 5,
    n_threads = 1,
    verbose = TRUE,
    ...
)

```

Arguments

x	Covariate matrix
y	Response vector
treated1	Binary vector indicating treatment.
beta_guess1	Initial guess of beta for m1
beta_guess0	Initial guess of beta for m0
solver	Specifies which solver to be used. Current options optim and cobyla (from nloptr package).
kernel	Specifies which kernel function to be used, current options are: "EPAN", "QUARTIC", and "GAUSSIAN".
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = \text{bandwidth_scale} * \text{sd}(x * \text{beta}) * n^{(1/3)}$.
recalc_bandwidth	Specifies wheter the bandwidth should be recalculated after the estimation of alpha (ipw_dim_red).
bwc_dim_red1	Scaling of calculated bandwidth, or if explicit_bandwidth = TRUE used as the banddwidth. For dimension reduction (imp_dim_red).
bwc_impute1	Scaling of calculated bandwidth, or if explicit_bandwidth = TRUE used as the banddwidth. Recalculated if explicit_bandwidth = FALSE and recalc_bandwidth = TRUE. For imputation.
bwc_dim_red0	See bwc_dim_red1
bwc_impute0	See bwc_impute1
gauss_cutoff	Cutoff value for Gaussian kernel
penalty	Penalty for the optimizer if local linear regression fails. Added to the function value in solver as: $\text{penalty}^{(n - n_before_pen)}$, where n is the number of llr fails.
n_before_pen	Number of probabilities outside the range (0, 1) to accept during dimension reduction.

`to_extrapolate` Specifies wheter to extrapolate or not
`to_truncate` Specifies wheter to extrapolate or not
`extrapolation_basis` Number of data point to base extrapolation on.
`n_threads` Sets number of threads for parallel run. Set to 0 serial. If `n_threads` exceeds maximum number of threads, sets `n_threads` to `max_threads - 1`. To use `max_threads`, set to `n_threads` to `max_threads` of system.
`verbose` Specifies if the program should print output while running.
`...` Additional parameters passed to `optim`.

Value

A list containing the average treatment effect of the combination of observed and imputed values (`ate`), the average treatment effect based on the imputed values only (`ate2`), the imputed values for treated (`m1`) and untreated (`m0`), the and the output from `optim` (`op`).

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

See Also

[stats::optim]

Examples

```

# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess

# Perform semiparametric imputation
imp <- SDRcausal::semipar_imputation(x, y, trt, b1, b0,
  explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
  bwc_dim_red0 = 1, bwc_impute0 = 1)

```

semipar_ipw

Estimates average treatment effect through IPW

Description

Semiparametric estimation of the average treatment effect based on the IPW method described in Ghosh, Ma, & De Luna (2020).

Usage

```
semipar_ipw(
  x,
  y,
  treated,
  alpha_initial,
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  recalc_bandwidth = TRUE,
  bwc_dim_red = 1,
  bwc_prop_score = 10,
  gauss_cutoff = 0.001,
  penalty = 10,
  n_before_pen = 1,
  n_threads = 1,
  verbose = TRUE,
  ...
)
```

Arguments

x	Covariate matrix
y	Response vector
treated	Binary vector indicating treatment.
alpha_initial	Initial guess of beta for ml
kernel	Specifies which kernel function to be used, current options are: "EPAN", "QUARTIC", and "GAUSSIAN".
explicit_bandwidth	Specifies if bandwidth_scale will be used as the bandwidth or if it will be calculated as $bw = \text{bandwidth_scale} * \text{sd}(x * \text{beta}) * n^{(1/3)}$.
recalc_bandwidth	Specifies wheter the bandwidth should be recalculated after the estimation of alpha (ipw_dim_red)
bwc_dim_red	Scaling of calculated bandwidth, or if explicit_bandwidth = TRUE used as the banddwidth. For dimension reduction (ipw_dim_red).
bwc_prop_score	Scaling of calculated bandwidth, or if explicit_bandwidth = TRUE used as the banddwidth. Recalculated if explicit_bandwidth = FALSE and recalc_bandwidth = TRUE. For propensity score.
gauss_cutoff	cutoff value for Gaussian kernel
penalty	Penalty for the optimizer if a probability is outside (0, 1) during dimension reduction. Added to the function value in solver as: $\text{penalty}^{(n - n_before_pen)}$, where n is the number of probabilities outside (0, 1).
n_before_pen	Number of probabilities outside the range (0, 1) to accept during dimension reduction.
n_threads	Sets number of threads for parallel run. Set to 0 serial. If n_threads exceeds maximum number of threads, sets n_threads to max_threads - 1. To use max_threads, set to n_threads to max_threads of system.
verbose	Specifies if the program should print output while running.
...	Additional parameters passed to optim.

Value

A list containing the average treatment effect (ate), the propensity score (pr), the final alpha (fa), and the output from optim (op).

References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. *Statistica Sinica*, accepted.

See Also

[stats::optim]

Examples

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
alp <- SDRcausal::alpha_guess

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::semipar_ipw(x, y, trt, alp, bwc_dim_red = 8,
                             bwc_prop_score = 8)
```


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