

Let X a set, $E = P(X)$, we define R as:

$$\forall (A, B) \in E^2, ARB \iff A \subset B$$

Proove that R is an order relation.

Let $A \in E$
 $\Rightarrow A \subset A$
 $\Rightarrow R$ is reflexive

Let $(A, B, C) \in E^3, A \subset B$ and $B \subset C$
 $\Rightarrow A \subset C$
 $\Rightarrow R$ is transitive

Let $(A, B) \in E^2, A \subset B$ and $B \subset A$
 $\Rightarrow A = B$
 $\Rightarrow R$ is antisymmetric

Let $(x, y) \in E^2 \mid x \neq y$
 $\Rightarrow \{x\} \in P(E)$ and $\{y\} \in P(E)$ and $\{x\} \not\subset \{y\}$ and $\{y\} \not\subset \{x\}$
 $\Rightarrow R$ doesn't bring total order