

Consider A, B, C. Compare those sets:

1.  $A \cap (B \cup C)$  and  $(A \cap B) \cup (A \cap C)$
2.  $A \cup (B \cap C)$  and  $(A \cup B) \cap (A \cup C)$

1. Let  $x \in A \cap (B \cup C)$

$\Rightarrow x \in A$  and  $(x \in B \text{ or } x \in C)$

Applying the rule of replacement in classical logic

$\Rightarrow (x \in A \text{ and } x \in B) \text{ or } (x \in A \text{ and } x \in C)$

$\Rightarrow x \in (A \cap B) \cup (A \cap C)$

2. Let  $x \in A \cup (B \cap C)$

$\Rightarrow (x \in A \text{ or } x \in B) \text{ and } (x \in A \text{ or } x \in C)$

$\Rightarrow x \in (A \cup B) \cap (A \cup C)$