

Let  $(p, q) \in \mathbb{Z}$   $p \wedge q = 1$  and  $\frac{p}{q} = \sqrt{2}$   
 $\Rightarrow p^2 = 2q^2$   
 $\Rightarrow 2|p$  and  $2|q$  Contradiction ■