Ch5: Digital Circuits – Part 1

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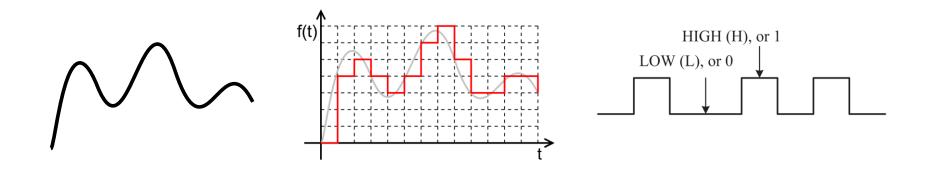
Amin Fakhari, Fall 2023

Number Systems

Number Systems

Analog and Digital Signals

In contrast to an **analog signal** that changes in a **continuous** manner, a **digital signal** exists only at specific **discrete** steps. Most digital signals have only two states (HIGH and LOW) and it is called a **binary signal** or **logic signal**.



Digital devices convert digital inputs into one or more digital outputs, and they are categorized as **Combinational Logic** or **Sequential Logic**.

Number Systems

The **base** (b) of a number system indicates the number of different symbols (d_i) that can be used to represent a digit.

$$(d_{n-1}\dots d_3d_2d_1d_0)_b = (d_{n-1}\cdot b^{n-1} + \dots + d_2\cdot b^2 + d_1\cdot b^1 + d_0\cdot b^0)$$
 Base b number system Decimal number

• To convert a number **from decimal to an arbitrary base**, the procedure is to successively divide the decimal number by the base and record the remainders after each division. The remainders, when written in reverse order from left to right, form the digits of the number represented in the new base.

Decimal number: b = 10, $d_i = 0 - 9$, Example: $123 = 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$

(Fractions may also be included if digits for negative powers of 10 are included: d_{-1} , d_{-2} ,...)

Number Systems



Binary Number System

Since the operation of **digital devices** is based on transistors that switch between two states: the **saturated state** (**ON**, **High**, **True**, or **1**) and the **cutoff state** (**OFF**, **Low**, **False**, or **0**), a base 2 number system called the **Binary Number System** is used to represent and manipulate numbers with digital devices.

Decimal to Binary:

Binary number: b = 2, $d_i = 0.1$, Example:

$$11110112 = 1 \cdot 26 + 1 \cdot 25 + 1 \cdot 24 + 1 \cdot 23 + 0 \cdot 22 + 1 \cdot 21 + 1 \cdot 20 = 123$$

Successive Divisions	Remainder	
123/2	1 LSF	— 3
61/2	1	
30/2	0	
15/2	1	
7/2	1	
3/2	1	
1/2	1 MS	В
Result	1111011	

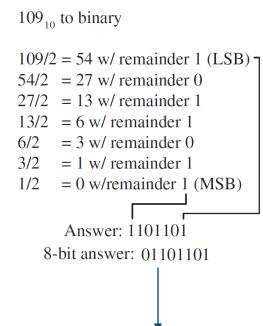
The digits of a binary number are also called **bits**. The first, or leftmost, bit is known as the **most significant bit** (**MSB**) because it represents the **largest** power of 2. The last, or rightmost, bit is known as the **least significant bit** (**LSB**) because it represents the **smallest** power of 2. A **group of 8 bits** is called a **byte** $(0\rightarrow 255)$.



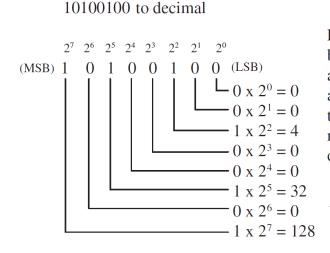
Example: Binary Number System

Binary-to-Decimal Conversion

Decimal-to-Binary Conversion



Take decimal number and keep dividing by 2, while keeping the remainders. The first remainder becomes the LSB, while the last one becomes the MSB.



Expand the binary number as shown and add up the terms. The result will be in decimal form.

Answer: 164₁₀

Note that most digital systems deal with 4, 8, 16, or 32 bits at a time. Hence, in decimal-to-binary conversions, you may need to put an additional 0 in front of the MSB (e.g., 1101101 -> 01101101).

Octal Number System

Because binary numbers can be long and cumbersome to write and display, often the Octal (Base 8) Number System or Hexadecimal (Base 16) Number System is used as an alternative representation.

$$247_8 \text{ (octal)} = 2 \times 8^2 + 4 \times 8^1 + 7 \times 8^0 = 167_{10} \text{ (decimal)}$$

Octal to Binary	Binary to Octal
537 ₈ to binary	111 001 100 ₂ to octal
5 3 7 (101 011 111)	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Answer: 101011111 ₂	Answer: 714 ₈

To convert a **binary number to octal**, divide the number into groups of **three digits** beginning with the LSB and replace each group with its octal equivalent.

Decimal	Binary	Octal
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	10
9	1001	11
10	1010	12
11	1011	13
12	1100	14
13	1101	15
14	1110	16
15	1111	17

$$123_{10} = 001 \ 111 \ 011_2 = 173_8$$



Hexadecimal Number System

In **Hexadecimal (Base 16) Number System**, the letters A through F are used to represent the digits larger than 9.

2D5₁₆ (hex) =
$$2 \times 16^2 + D$$
 (=13₁₀) $\times 16^1 + 9 \times 16^0 = 725_{10}$
Hex to Binary

Binary to Hex

3E9₁₆ to binary

1001 1111 1010 0111₂ to hex

0011 1110 1001₂

Answer: 9FA7₁₆



To convert a **binary number to hexadecimal**, divide the number into groups of **four digits** beginning with the LSB and replace each group with its hexadecimal equivalent.

Decimal	Binary	Octal	Hexadecima
0	0000	0	0
1	0001	1	1
2	0010	2	2
3	0011	3	3
4	0100	4	4
5	0101	5	5
6	0110	6	6
7	0111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	В
12	1100	14	С
13	1101	15	D
14	1110	16	E
15	1111	17	F

$$123_{10} = 0111\ 1011_2 = 7B_{16}$$

Number Systems



Binary Coded Decimal (BCD)

Binary Coded Decimal (BCD) system is used to represent each digit of a decimal number

as a 4-bit binary number.

	1	5	0
	/		\
	0001	0101	0000
150 _:	₁₀ = 00	01 01	01 0000 _(BCD)
	10 = 00 10 = 01		10 0011 _(BCD) 11 ₂

•	Although BCD is a convenient way to represent decimal numbers in
	a binary number format, it is inefficient for storing or transmitting
	multiple-digit numbers because only 10 of the 16 (24) possible states
	of the 4-bit number are used.

•	BCD is commonly used when outputting to decimal (0–9) displays, such as those
	(seven-segments) found in digital clocks and multimeters.

Decimal	Binary	BCD
0	0000	(0000 0000)
1	0001	0000 0001
2	0010	0000 0010
3	0011	0000 0011
4	0100	0000 0100
5	0101	0000 0101
6	0110	0000 0110
7	0111	0000 0111
8	1000	0000 1000
9	1001	0000 1001
10	1010	0001 0000
11	1011	0001 0001
12	1100	0001 0010
13	1101	0001 0011
14	1110	0001 0100
15	1111	0001 0101



ASCII Codes

American Standard Code for Information Interchange (ASCII) is an alphanumeric code used to transmit letters, symbols, numbers, and special nonprinting characters (e.g., ESC, DEL) represented in binary form between computers and computer peripherals (such as printers and keyboards).

- ASCII consists of 128 different 7-bit codes.
- The 7-bit codes are usually stored in an 8-bit byte.

A:
$$0100\ 0001 = 41_{16} = 65_{10}$$

B: $0100\ 0010 = 42_{16} = 66_{10}$
0: $0011\ 0000 = 30_{16} = 48_{10}$
1: $0011\ 0001 = 31_{16} = 49_{10}$

CHAR	DEC	HEX	7-BIT
@	64	40	100 0000
Α	65	41	100 0001
В	66	42	100 0010
С	67	43	100 0011
D	68	44	100 0100
E	69	45	100 0101
:			

https://en.wikipedia.org/wiki/ASCII



Binary Arithmetic: Binary Addition

Adding binary numbers $(x_b + y_b)$ is just like adding decimal numbers. Whenever the result of adding one column of numbers is greater than one digit, a 1 is carried over to the next column to be added. Here are the possibilities:

- 0 + 0 = 0
- 1 + 0 = 1
- 1 + 1 = 2 which is 10 in binary which is 0 with a carry of 1
- 1 + 1 + 1 (carry) = 3 which is 11 in binary which is 1 with a carry of 1

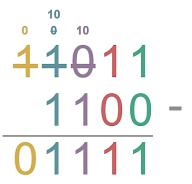
$$\begin{array}{r}
 11 \\
 9 \\
 + 3 \\
 \hline
 12 \\
 \hline
 12
 \end{array}$$

$$\begin{array}{r}
 1001 \\
 + 0011 \\
 \hline
 1100
 \end{array}$$

Binary Arithmetic: Binary Subtraction (1st Method)

Similar to binary addition, for binary subtraction $(x_b - y_b)$, we will work through the numbers, column by column, starting on the far right. Instead of carrying forward however, we will borrow backwards (when necessary). Here are the possibilities:

- 0 0 = 0
- 1 0 = 1
- 1 1 = 0
- 0 1 we can't do so we borrow 1 from the next column. This makes it 10 1 which is 1.

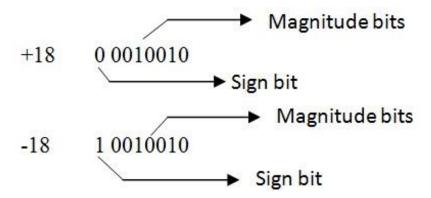


This method can be used only when $x_b \ge y_b$. Computers subtract binary digits using another approach that is to find the **negative value** of the second number and then add the numbers: $x_b + (-y_b)$.



Negative Binary Numbers: Sign-Magnitude Representation

One of the simplest methods is to represent negative binary numbers is **Sign-Magnitude Representation**. In this method, a bit, usually the MSB, to act as a **sign bit** is reserved. If the sign bit is **0**, the number is **positive**; if the sign bit is **1**, the number is **negative**.



Occasionally, you will see sign-magnitude numbers used in display and analog-to-digital applications, but you will hardly ever see them in circuits that perform arithmetic. Instead, **Two's Complement Representation** is usually used.

Negative Binary Numbers: Two's Complement Representation

In Two's Complement Representation,

- A **Positive** Number is the **same** as the actual binary number.
- A **Negative** Number is represented by a binary number, which when added to its corresponding positive equivalent results in zero.

Decimal to 2's Complement:

(Positive Number)

+41₁₀ to 2's Complement

- True Binary = 0010 1001
- 2's Complement = 0010 1001

(Negative Number)

 -41_{10} to 2's Complement

- True Binary $(41_{10}) = 0010 \ 1001$
- 1's Complement = 1101 0110 (1)
- Add 1: +1 (2)
- 2's Complement = 1101 0111
- 1) Take the 1's Complement: Complementing each bit of the true binary $(1 \rightarrow 0, 0 \rightarrow 1)$.
- 2) Add 1 to the 1's Complement number to get the magnitude bits. The **sign bit** will always end up being **1**.

Number Systems

-51₁₀



2**'**S

-8

Negative Binary Numbers: Two's Complement Representation

2's Complement to	Decimal:		DECIMAL	COMPLEMENT
• If the 2's comple	ment numbei	r is positive (sign bit = 0), perform a	+7	0000 0111
regular binary-to	-decimal con	version.	+6	0000 0110
			+5	0000 0101
• If the 2's comple	ment numbei	r is negative (sign bit = 1), the	+4	0000 0100
decimal sign will			+3	0000 0011
•	•	2's complement number.	+2	0000 0010
2) Add 1 to get the		•	+1	0000 0001
,	•	imal conversion and including	0	0000 0000
negative sign.	,	· · · · · · · · · · · · · · · · · · ·	-1	1111 1111
0 0			-2	1111 1110
21	1100 1101		-3	1111 1101
2's complement =	1100 1101	(4)	-4	1111 1100
Complement:	0011 0010	(1)	- 5	1111 1011
Add 1:	+1	(2)	-6	1111 1010
True Binary =	0011 0011	(3)	-7	1111 1001

Decimal =

Binary Arithmetic: Binary Subtraction (2nd Method)

The second method to subtract binary numbers (a - b) is to use the **two's complement representation**. That is, adding the numbers in this way: a + (-b).

- (i) Find the 2's complement representation of the number (-b).
- (ii) Add additional 0/1 to the left side of the positive/negative numbers if they don't have the same number of bits.
- (iii) Add the numbers a + (-b).
- (iv) If the final carry over of the sum is 1 (overflow bit), it is dropped, and the result is <u>positive</u>.
- (v) If there is no carry over, the result is negative.





Binary Arithmetic: Binary Multiplication

Binary multiplication is carried out in the same way as the decimal arithmetic. Here are the possibilities:

- $0 \times 0 = 0$
- $1 \times 0 = 0$
- $1 \times 1 = 1$

$$\begin{array}{cccc}
9 & 1001 \\
\times 3 & \times 0011 \\
\hline
27 & 1001 \\
& + 1001 \\
& + 0000 \\
& + 0000 \\
\hline
& 11011
\end{array}$$

	110	01
	1	10 X
	000	00
1	100	10
11	001	00
100	101	10

Binary division is also carried out in the same way as the decimal arithmetic.

Logic Gates and Combinational Logic

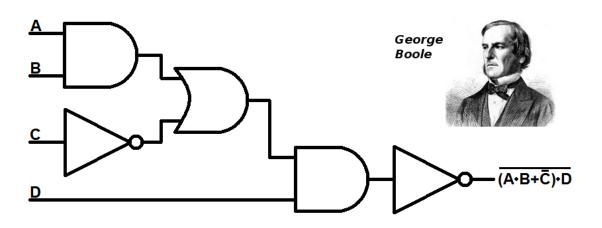
Number Systems



Logic Gates

Logic Gates are the building blocks of digital electronics. The fundamental logic gates include the NOT (INV), AND, NAND, OR, NOR, exclusive OR (XOR), and exclusive NOR (XNOR) gates.

The term **Combinational Logic** is used for the combining of two or more basic **Logic Gates** to form a required function. Outputs of **combinational logic** devices depend only on the **instantaneous values** of the inputs.



An online digital circuit simulator: https://logic.ly/demo/

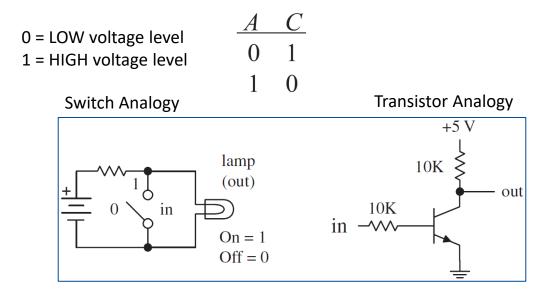
NOT (or INV) Gate

A NOT gate or INVerter outputs a logic level that is the opposite of the input logic level.

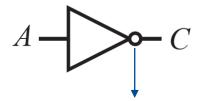
Operation: Inverting signal (complement)

Expression: $C = \bar{A}$

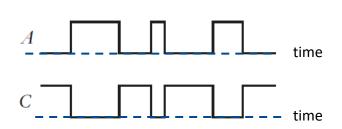
Truth Table: A table displaying all combinations of inputs and their corresponding outputs



• **Timing Diagram** helps to analyze complex logic circuits. It shows the simultaneous levels of every possible combination of inputs and corresponding outputs in a circuit vs. time.



A small circle at the input or output denotes signal inversion $(0\rightarrow 1, 1\rightarrow 0)$.



AND Gate

The output of an AND gate is HIGH only when both inputs are HIGH.

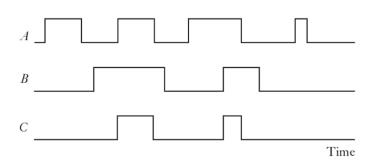
Operation: AND logic

Expression: $C = A \cdot B$

Truth Table:

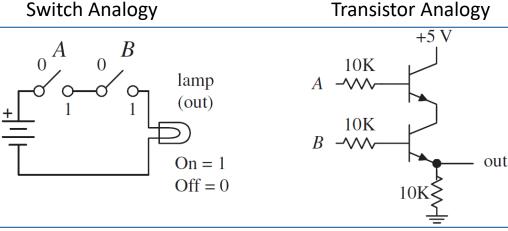
Number Systems

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Switch Analogy



NAND Gate

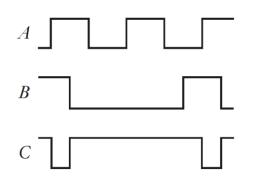
Combines the NOT function with an AND gate; output only goes LOW when both inputs are HIGH.

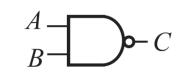
Operation: Inverted AND logic

Expression: $C = \overline{A \cdot B}$

Truth Table:

Number Systems

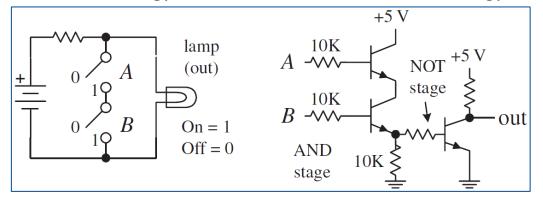








Transistor Analogy





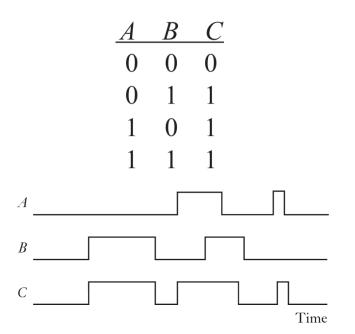
OR Gate

The output of an OR gate will go HIGH if one or both inputs goes HIGH. The output only goes LOW when both inputs are LOW.

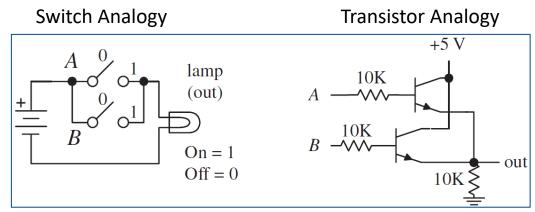
Operation: OR logic

Expression: C = A + B

Truth Table:







NOR Gate

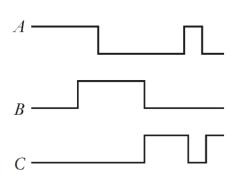
Combines the NOT function with an OR gate; output goes LOW if one or both inputs are LOW, output goes HIGH when both inputs are LOW.

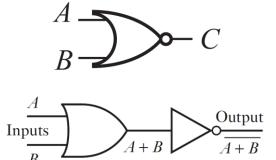
Operation: Inverted OR logic

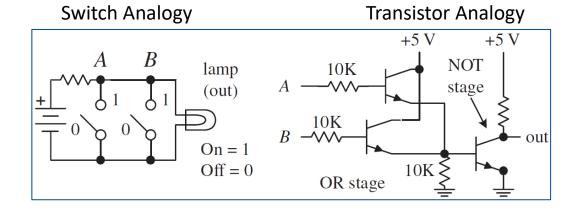
Expression: $C = \overline{A + B}$

Truth Table:

Number Systems







XOR (Exclusive OR) Gate

The output of an XOR gate goes HIGH if the inputs are different from each other.

Operation: Exclusive OR logic

Expression: $C = A \oplus B = (A + B) \cdot (\bar{A} + \bar{B}) = A \cdot \bar{B} + \bar{A} \cdot B$

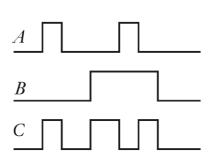
Truth Table:

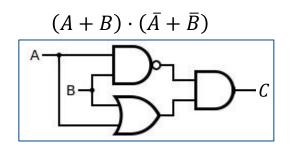
Number Systems

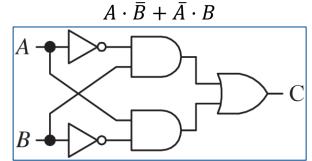
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$$A \longrightarrow C$$

Equivalent Circuits







XNOR (Exclusive NOR) Gate

Combines the NOT function with an XOR gate; output goes HIGH if the inputs are the same.

Operation: Exclusive NOR logic

Expression:
$$C = \overline{A \oplus B} = A \odot B = \overline{(A+B) \cdot (\overline{A} + \overline{B})} = A \cdot B + \overline{A} \cdot \overline{B}$$

Truth Table:

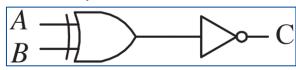
Number Systems

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\boldsymbol{A}	B	$\mid C \mid$
0	0	1
0	1	0
1	0	0
1	1	1

$$A \longrightarrow C$$

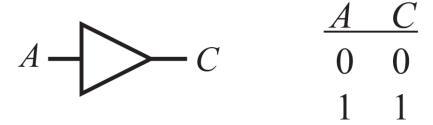
Equivalent Circuit





Buffer

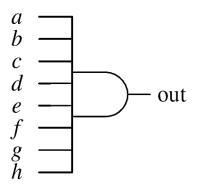
- A Buffer is used to increase the current supplied at the output while retaining the digital state.
- This is important if you wish to drive multiple digital inputs from a single output.
- A normal digital gate has a limited fan-out, which defines the maximum number of similar digital inputs that can be driven by the gate's output. The buffer overcomes fanout limitations by providing more output current.

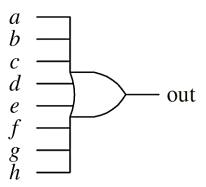


Multiple-Input Logic Gates

The **standard** AND, NAND, OR, NOR, and XOR gates have only two inputs, but other forms are available with more than two inputs.

- In the case of AND gate, the output is 1 if and only if all inputs are 1; otherwise, the output is 0.
- In the case of OR gate, the output is 0 if and only if all inputs are 0; otherwise, it is 1.
- In the case of XOR gate, the output is 0 if all of the inputs are 0 or if all of the inputs are 1; otherwise, it is 1.

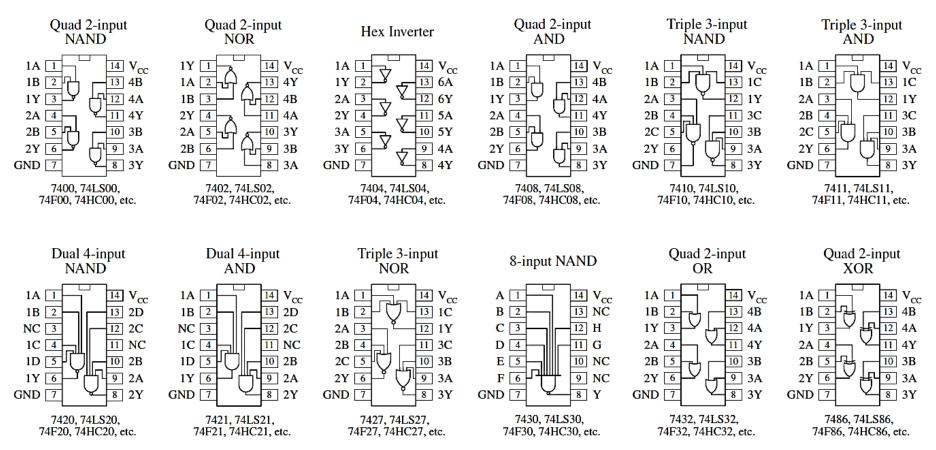




Number Systems

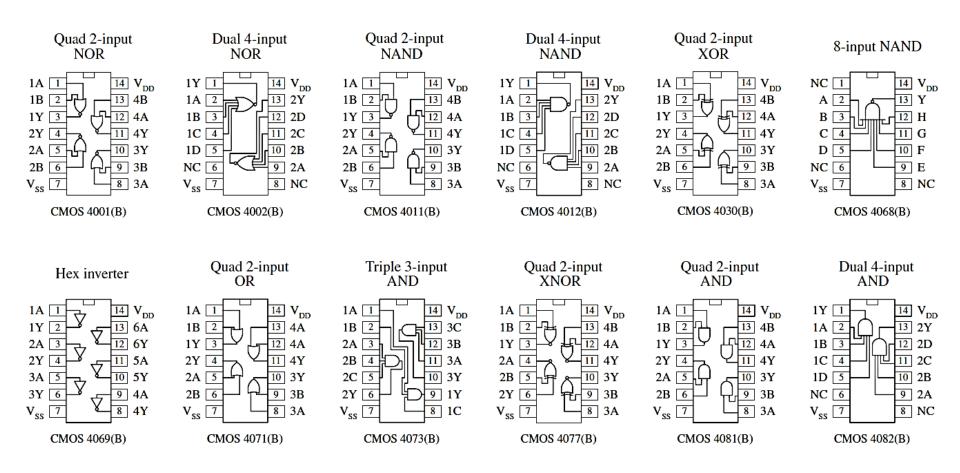
Digital Logic Gate ICs (Examples of TTL & CMOS 74XX Series)

The logic gates are manufactured as **Integrated Circuits**. The different manufacturers have standardized their numbering schemes so that the part numbers are the same regardless of the manufacturer.



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Digital Logic Gate ICs (Examples of CMOS 40XXB Series)

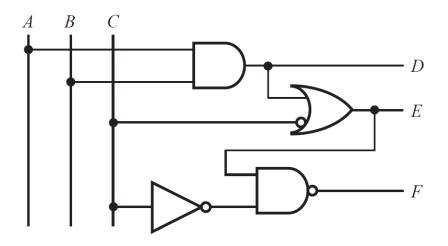


Number Systems



Example

Determine signal expressions and values in the following logic diagram.



Number Systems

Boolean Algebra is important in formulating mathematical expressions for logic circuits.

(+)
$$\Rightarrow$$
 OR , (\cdot) \Rightarrow AND , $(ar{X})$ \Rightarrow NOT

Fundamental Laws

OR	AND	NOT
A + 0 = A	$A \cdot 0 = 0$	
A + 1 = 1	$A \cdot 1 = A$	$\overline{\overline{A}} = A$
A + A = A	$A \cdot A = A$	(double inversion)
$A + \overline{A} = 1$	$A \cdot \overline{A} = 0$	

Commutative Laws

$$A + B = B + A$$
$$A \cdot B = B \cdot A$$

$$(A+B)+C = A+(B+C)$$

$$(A \cdot B) \cdot C = A \cdot (B \cdot C)$$

Distributive Laws

$$(A + B) + C = A + (B + C)$$
 $A \cdot (B + C) = (A \cdot B) + (A \cdot C)$

$$A + (B \cdot C) = (A + B) \cdot (A + C)$$

Number Systems

De Morgan's Laws:

$$\overline{A+B+C+\cdots} = \overline{A}\cdot\overline{B}\cdot\overline{C}\cdot\cdots$$

$$\overline{A \cdot B \cdot C \cdot \cdot \cdot \cdot} = \overline{A} + \overline{B} + \overline{C} + \cdot \cdot \cdot$$

or ∜

$$A + B + C + \cdots = \overline{\overline{A} \cdot \overline{B} \cdot \overline{C} \cdot \cdots}$$

$$A \cdot B \cdot C \cdot \cdot \cdot = \overline{\overline{A} + \overline{B} + \overline{C} + \cdot \cdot \cdot}$$

Other Useful Identities:

$$A + (A \cdot B) = A$$

$$A \cdot (A + B) = A$$

$$A + (\overline{A} \cdot B) = A + B$$

$$(A+B)\cdot (A+\overline{B}) = A$$

$$A + B + (A \cdot \overline{B}) = A + B$$

$$(A \cdot B) + (B \cdot C) + (\overline{B} \cdot C) = (A \cdot B) + C$$

$$(A \cdot B) + (A \cdot C) + (\overline{B} \cdot C) = (A \cdot B) + (\overline{B} \cdot C)$$

Number Systems

Truth tables can be very helpful in verifying an identity.

$$A + (\overline{A} \cdot B) = A + B$$

\boldsymbol{A}	\overline{A}	В	$\overline{A} \cdot B$	$A + \overline{A \cdot B}$	A + B
1	0	0	0	1	1
1	0	1	0	1	1
0	1	0	0	0	0
0	1	1	1	1	1

Number Systems



Example

Simplify the following expression using Boolean laws and identities.

$$X = (A \cdot B \cdot C) + (B \cdot C) + (\overline{A} \cdot B)$$

Number Systems



An application of combinational logic to a real engineering problem:

Design a circuit for a simple security system for a home in a way that an alarm to sound if someone breaks into the house through a door/window or if something is moving around the house. The user may also want to disable <u>portions of the alarm system</u>.

I. Defining Boolean variables for inputs and outputs of the circuit:

A: state of the door/window sensors

B: state of the motion detector

C D: 2-bit code to select the operating state by user defined by

- 0 1 the alarm will sound only if the doors/windows are disturbed (e.g., when occupants are sleeping).
- 10 the alarm will sound if the doors/windows are disturbed or if there is motion in the house (e.g., when occupants are away).
- 0 0 the alarm will not sound (normal state).

Y: output used to sound the alarm

(Inputs: *A*, *B*, *C*, and *D*; Output: *Y*)

II. Quasi-Logic Statement:

Number Systems

Activate the alarm (Y = 1) if A is high and the code C D is 0.1 or activate the alarm if A or B is high and the code is 10.

III. Boolean Expression:

$$Y = A \cdot (\overline{C} \cdot D) + (A + B) \cdot (C \cdot \overline{D})$$

Note: To create a product of 1 for the active control code 0 1, we need to form the expression $\bar{C} \cdot D$.

For this particular problem, by looking at a truth table, the equation can be **simplified**:

C	D	$(\overline{C}\cdot D)$	$(C\cdot \overline{D})$	$ \bar{C} \cdot D = D \ , C \cdot \overline{D} = C$
0	0	0	0	
1	0	0	1	
0	1	1	0	$\Rightarrow Y = (A \cdot D) + (A + B) \cdot C$

IV. Realization:

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After simplification, it may be desirable to manipulate the result further in order to convert all operations to a preferred type of gate (e.g., NOT, AND, NAND, OR, or NOR) to minimize the number of required logic gate IC components.

Converting from one gate type to another is easily accomplished with a repeated application of **De Morgan's Laws**.

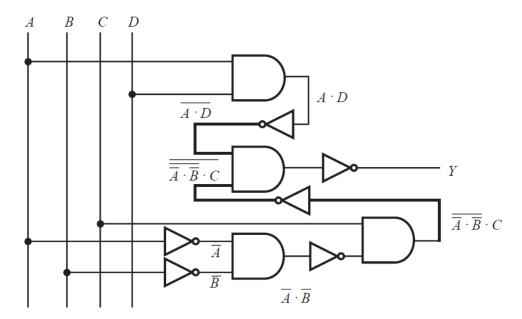
$$Y = (A \cdot D) + (A + B) \cdot C \xrightarrow{A + B + C + \cdots = \overline{A} \cdot \overline{B} \cdot \overline{C} \cdot \cdots} Y = (A \cdot D) + (\overline{\overline{A} \cdot \overline{B}}) \cdot C$$

$$Y = \overline{\overline{A \cdot D} \cdot (\overline{\overline{A} \cdot \overline{B}}) \cdot C}$$

V. Drawing the Circuit Diagram:

Since there are a total of 4 AND gates and 6 inverters, the circuit can be made with 2 ICs:

- one quad AND gate IC (e.g., the 7408), which contains four AND gates,
- one hex inverter IC (e.g., the 7404), which contains six inverters.



$$Y = \overline{\overline{A \cdot D} \cdot \overline{(\overline{A} \cdot \overline{B})} \cdot C}$$

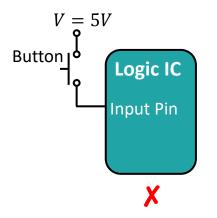
This solution is known as a hardware solution because it uses ICs to provide the desired logic. A software solution is to implement the logic using a program running on a microcontroller.

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Application

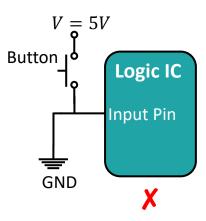
Pullup and Pulldown Resistors

To connect buttons to logic ICs, **Pullup** resistors are used to keep an input normally high and **Pulldown** resistors are used to keep an input normally low; otherwise, **Floating** or **Short Circuit** happens.



When the button is not pressed, the input pin is connected to nothing (the pin is said to be **Floating**). Thus, due to electrical noise on nearby pins, value of input pin fluctuates between high and low.

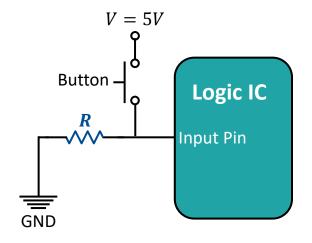
→ Unexpected results is read on the pin!



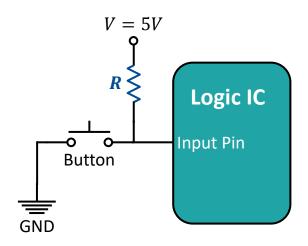
When the button is pressed, **Short Circuit** happens!

Pullup and Pulldown Resistors

Nearly all digital inputs use a **Pullup** or **Pulldown Resistor** to set the **default state** of the input pin.



Pulldown Resistor is used to make the initial state of input pin **LOW**

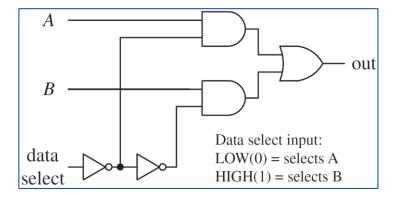


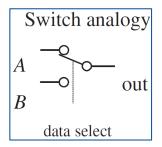
Pullup Resistor is used to make the initial state of input pin **HIGH**

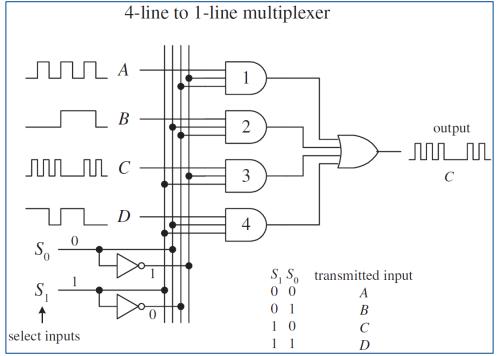
Typically, a pulldown resistor is around 100 to 1k and a pullup resistor is around 10k.

Multiplexers (Data Selectors)

Multiplexers (**Data Selectors**) act as digitally controlled switches similar to SPDT, SP4T, SP8T etc. switches.



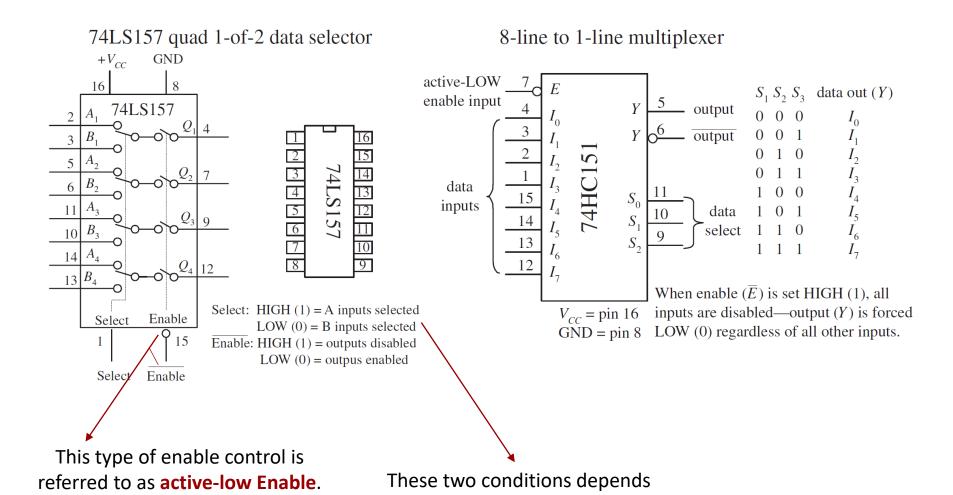




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Multiplexers (Data Selectors)

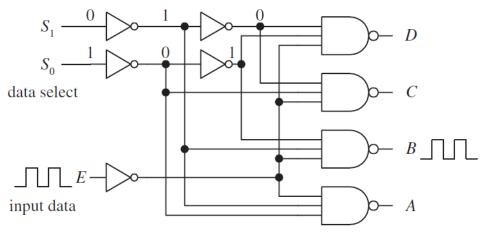


on the state of the **Enable** input.

Demultiplexers (Data Distributors)

Demultiplexer (or **Data Distributor**) is the opposite of Multiplexer. It takes a single data input and routes it to one of several possible outputs.

4-line demultiplexer logic circuit



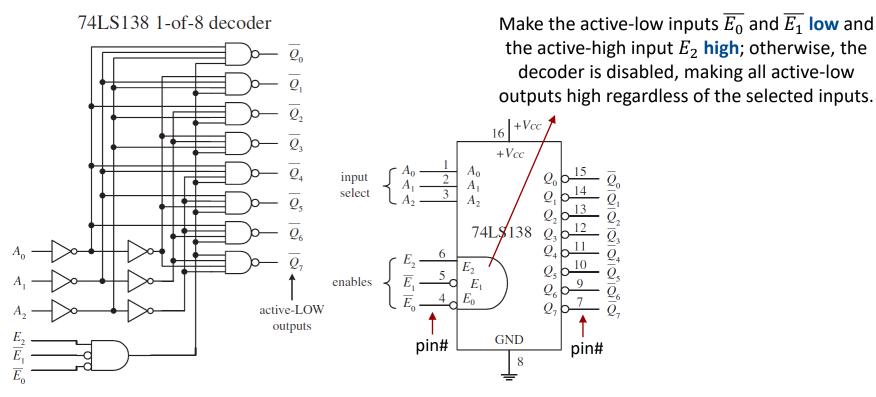
Control logic

$S_1 S_0$	input routed to:	
0 0	A	
0 1	B	disabled outputs
1 0	C	are held HIGH
1 1	D	

Decoders

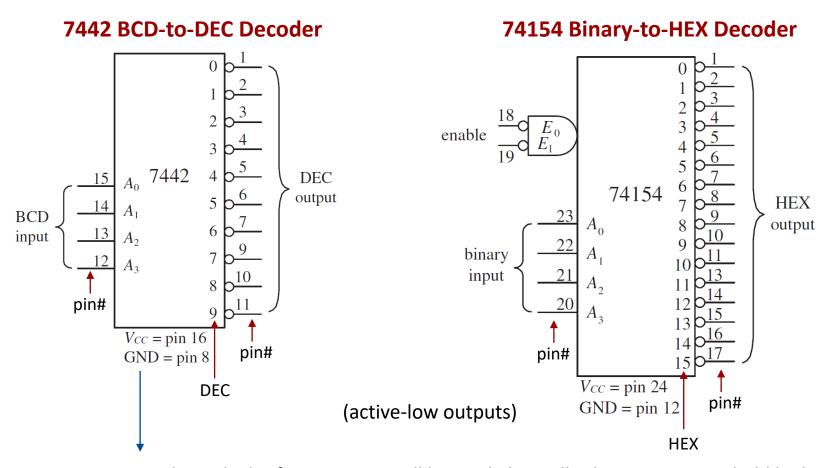
Decoder simply uses the data select inputs to choose which outputs, among many, are to be made high or low.

• 74138 uses 3 inputs to select which of eight outputs will be made low; all other outputs are held high (active-low output).





Decoders

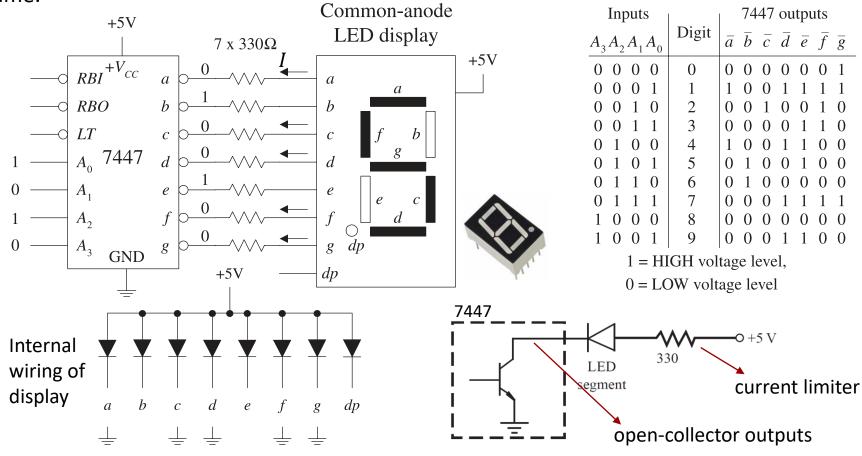


• Four inputs to select which of ten outputs will be made low; all other outputs are held high (active-low output).



Decoders

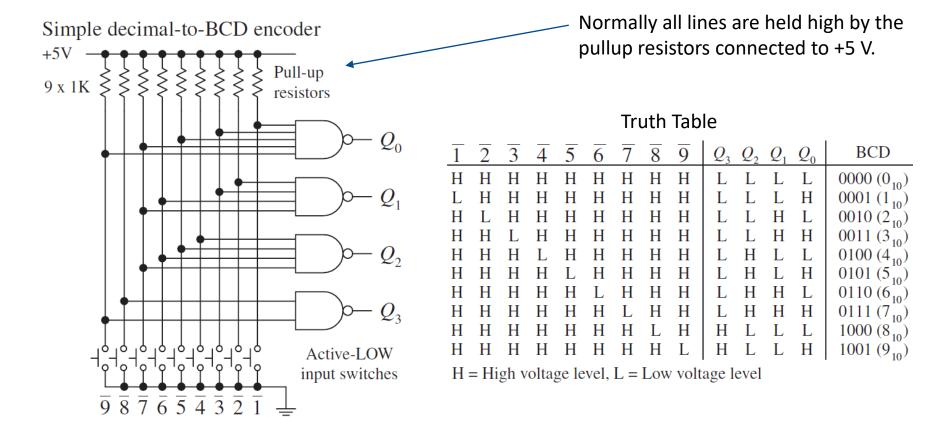
With 7447 **BCD-to-Seven-Segment decoder**, more than one output can be driven low at a time.





Encoders

Encoders are the opposite of decoders. They are used to generate a **coded output** from a <u>single</u> active numeric input.





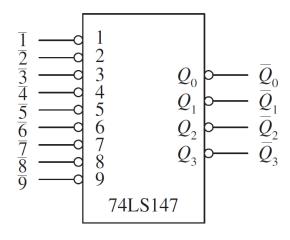
Encoders

74LS147 decimal-to-BCD **priority encoder**:

The term **priority** means that it is designed so that if two or more inputs are selected at the same time, it will select only the largerorder digit (e.g., if 3, 5, and 8 are selected at the same time, only the 8 will be output).

_	$\overline{2}$	- 2	$\overline{4}$	5	-	7	<u>o</u>	9	\overline{Q}_3	\overline{O}	\overline{Q}_1	\overline{O}	BCD (neg. logic)
1		<u> </u>	4	<u>J</u>	U		0	9	\mathcal{Q}_3	\mathcal{Q}_2	\mathcal{Q}_1	\mathcal{Q}_0	(neg. logic)
Н	Η	Η	Η	Η	Η	Η	Η	H	Н	Η	Η	Н	$1111(0_{10})$
X	X	X	X	X	X	X	X	L	L	Η	Η	L	$0110(9_{10})$
X	X	X	X	X	X	X	L	Η	L	Η	Η	Η	$0111(8_{10})$
X	X	X	X	X	X	L	Η	Η	Н	L	L	L	$1000 (7_{10}^{10})$
X	X	X	X	X	L	Η	Η	Η	Н	L	L	Η	1001 (6 ₁₀)
X	X	X	X	L	Η	Η	Η	Η	Н	L	Η	L	1.1010(5)
X	X	X	Ĺ	Η	Η	Η	Η	Η	Н	L	Η	Η	$1011(4_{10})$
X	X	Ĺ	H	H	Η	Η	H	Η	Н	Η	L	L	$1100 (3_{10}^{10})$
X	Ĺ	Η	Η	Η	Η	Η	Η	Η	Н	Η	L	Η	$ \begin{array}{c} 1100 (3_{10}) \\ 1101 (2_{10}) \end{array} $
L	Н	Н	Н	Н	Н	Н	Н	Н	Н	Н	Н	L	$1110 (1_{10}^{10})$

H = High voltage level, L = Low voltage level, X = don't care



• It has active-low outputs, i.e., output is expressed in **negative** true logic.

Other encoders:

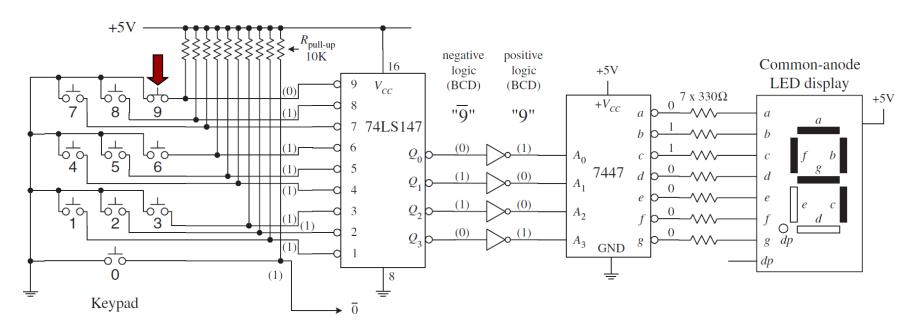
- 74148 octal-to-binary encoder
- 74184 BCD-to-binary encoder
- 74185 binary-to-BCD encoder

Number Systems



Encoders

Using an encoder and a decoder together to drive an LED display via a 0 through 9 keypad:



Note: For all logic ICs, by placing a load (e.g., LED) between +VCC and an output LOW, you can sink current through the load and into the output. By placing a load between an output HIGH and ground, you can source current from the output and sink it through the load. The limits to how much current an IC can source, or sink should be considered.