## **040: State**

When working through Chapter 6 (and these exercises) it is important to have a picture of the emerging story. This chapter, with the progression of exercises, shows you how we can arrive at an elegant abstraction in library design. We are starting with imperative generator of random numbers (no exercises about this), then we make it pure (the RNG state). Then again we observe that using it is tedious so, we start to see the random number generators as state transformers (Rand) and then we remark that the main functions manipulating them can just as well manipulate any state transformers, not only random number generators (we arrive at the State abstraction). To understand this story well, you will likely have to re-read the book in parallel to solving the exercises.

All exercises are to be solved by extending the file State.scala. It contains several modules inside, to avoid name clashes between different abstractions. Once done, please hand in the completed State.scala file.

**Exercise 1.** Write a function that uses RNG.nextInt to generate a random integer between 0 and Int.maxValue. Make sure to handle the corner case when nextInt returns Int.MinValue, which doesn't have a non-negative counterpart.<sup>1</sup>

```
def nonNegativeInt(rng: RNG): (Int, RNG)
```

Implement the function in the companion object of the RNG trait, file State.scala.

**Exercise 2.** Write a function to generate a Double between 0 and 1, not including 1. Note: You can use Int.MaxValue to obtain the maximum positive integer value, and you can use x.toDouble to convert an x: Int to a Double.

```
def double(rng: RNG): (Double, RNG)
```

Write this function in the companion object of the RNG trait.<sup>2</sup> Ponder for a moment: is the distribution generated by your function uniform?

**Exercise 3.** Write functions to generate an (Int, Double) pair and a (Double, Int) pair, where integers are non-negative. You should be able to reuse the functions you've already written.

```
def intDouble (rng: RNG)
def doubleInt (rng: RNG)
```

Write all of these in the RNG companion object.<sup>3</sup>

Exercise 4. Write a function to generate a list of random integers.<sup>4</sup>

```
def ints(count: Int)(rng: RNG)
```

If you have not done it yet, please add explicit return type annotations to all above functions, and see that your solutions still type check. Notice that all functions written so far have the same format: f[A]: RNG =>(A,RNG), except that in the last case this type has been curried with one additional parameter. This motivates the generalization of the interface from now on, see Section 6.4 in the text book for the Rand[A] type. We shall develop an API for this type, like we did for Option. The API will allow us computing with random values, without explicitly carrying the generator state around.

<sup>&</sup>lt;sup>1</sup>Exercise 6.1 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>2</sup>Exercise 6.2 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>3</sup>Exercise 6.3 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>4</sup>Exercise 6.4 [Chiusano, Bjarnason 2014]

**Exercise 5.** Use map to reimplement double in a more elegant way. See exercise 2 above.

Observe how for Option we used the higher order API to avoid using pattern matching, and how here we use it to avoid being explicit about the state (and also to avoid decomposing, a.k.a. pattern matching, the results of random generators into value and new state).<sup>5</sup>

**Exercise 6.** Write the implementation of map2 based on the following signature. This function takes two actions, ra and rb, and a function f for combining their results, and returns a new action that combines them:<sup>6</sup>

```
def map2[A,B,C](ra: Rand[A], rb: Rand[B])(f: (A, B) =>C): Rand[C]
```

**Exercise 7.** Implement sequence for combining a List of transitions into a single transition. Use it to reimplement the ints function you wrote before. For the latter, you can use the standard library function List.fill(n)(x) to make a list with x repeated n times.<sup>7</sup>

```
def sequence[A](fs: List[Rand[A]]): Rand[List[A]]
```

Exercise 8. Implement flatMap, and then use it to implement nonNegativeLessThan.<sup>8</sup>

```
def flatMap[A,B](f: Rand[A])(g: A =>Rand[B]): Rand[B]
```

**Note**: for Option we used map to compose a partial computation with a total computation. In here we used map to compose a random generator with a deterministic function. Similarly for flatMap. Function, Option.flatMap was used to compose two partial computations. On Rand the flatMap function is used to compose two random generators.

**Exercise 9.** Now we shall observe that everything we have done so far can just as well be done for other states, than RNG. Read beginning of Chapter 6.5, before solving this exercise.

Generalize the functions unit, map, map2, flatMap, and sequence. Add them as methods on the State case class where possible. Otherwise you should put them in a State companion object.<sup>9</sup>

**Exercise 10.** We now connect the State and Streams. Recall from basics of computer science that automata and traces are intimately related: each automaton generates a language of traces. In our implementation automata are implemented using State and Streams can be used to represent traces.

Implement a function state2stream that given a state object and an initial state, produces a stream of values generated by this State object (this automaton).

This composition provides an alternative to using sequence suggested above.

**Exercise 11.** Use state2stream to generate a lazy stream of integer numbers. Finally, obtain a finite list of 10 random values from this stream.

Notice, how concise is the expression to obtain 10 random values from a generator using streams. This is because all our abstractions compose very well.

<sup>&</sup>lt;sup>5</sup>Exercise 6.5 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>6</sup>Exercise 6.6 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>7</sup>Exercise 6.7 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>8</sup>Exercise 6.8 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>9</sup>Exercise 6.10 [Chiusano, Bjarnason 2014]