

# Gates and Losses

$t=0,1,\dots,T$  temporal order

$d=0,1,\dots,D$  spatial order of ConvLSTM module

$\mathbf{X}$  = input to ConvLSTM module

$\mathbf{C}$  = cell gate

$\mathbf{H}$  = hidden state

$W$  = feedforward convolutional neural net

$\mathbf{X}_t^d$ , i.e. the output of ConvLSTM module at depth  $d$  and time  $t$ , depends on:

$\mathbf{X}_t^{d-1}$  input to ConvLSTM module

$\mathbf{H}_{t-1}^d$  temporal hidden state

$\mathbf{C}_{t-1}^d$  temporal cell gate

$$i_t^d = \sigma(W_{d,xi}(\mathbf{X}_t^{d-1}) + W_{d,hi}(\mathbf{H}_{t-1}^d)),$$

$$f_t^d = \sigma(W_{d,xf}(\mathbf{X}_t^{d-1}) + W_{d,hf}(\mathbf{H}_{t-1}^d)),$$

$$\tilde{C}_t^d = \tanh(W_{d,xc}(\mathbf{X}_t^{d-1}) + W_{d,hc}(\mathbf{H}_{t-1}^d)),$$

$$\mathbf{C}_t^d = f_t^d \circ \mathbf{C}_{t-1}^d + i_t^d \circ \tilde{C}_t^d.$$

$$o_t^d = \sigma(W_{d,xo}(\mathbf{X}_t^{d-1}) + W_{d,ho}(\mathbf{H}_{t-1}^d)),$$

$$\mathbf{H}_t^d = o_t^d \circ \tanh(\mathbf{C}_t^d),$$

$$\mathbf{X}_t^d = \mathbf{H}_t^d,$$

$$\mathbf{L} = \sum_{t=1}^T \gamma^t \mathbf{L}_t, \text{ where } \mathbf{L}_t = -\log \frac{e^{\mathbf{H}_t^{\mathbf{P}}[C]}}{\sum_j e^{\mathbf{H}_t^{\mathbf{P}}[j]}}.$$

