# **Graph traversals**

### **Definition**

A Graph consists of a finite set of vertices or nodes and set of Edges which connect a pair of nodes.

### Representation

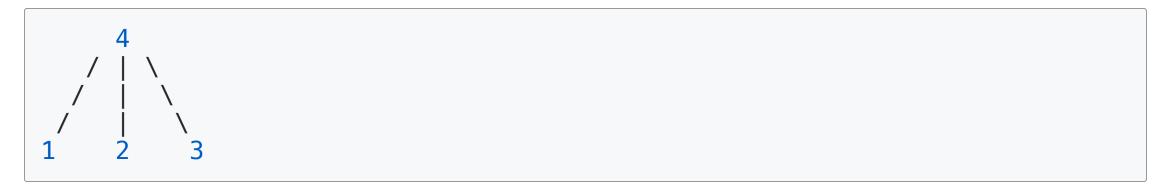
#### Adjacency matrix

Adjacency Matrix is a 2D array of size  $|V| \times |V|$  where V is the number of vertices in a graph. Let the 2D array be <code>adj[][]</code>, a slot <code>adj[i][j] = 1</code> indicates that there is an edge from vertex i to vertex j and 0 means no edge.

#### **Matrix**

```
[
    [0, 0, 0, 1],
    [0, 0, 0, 1],
    [0, 0, 0, 1],
    [1, 1, 1, 0]
]
```

#### Graph



#### Pros vs. Cons

#### Pros:

- Representation is easier to implement and follow
- ullet Removing an edge takes O(1) time
- $\bullet$  Queries like whether there is an edge from vertex  $[{\tt u}]$  to vertex  $[{\tt v}]$  are efficient and can be done O(1)

#### Cons:

- ullet Consumes more space  $O(V^2)$ . Even if the graph is sparse contains less number of edges, it consumes the same space
- ullet Adding a vertex is  $O(V^2)$  time

### Miscellaneous

We can sacrifice the O(1) to get a better space efficiency by using "Adjacency List".

#### Source

Other implementations include:

- "edge list" implementation where we have a list of Edge (Node, Node)
- combination of edge list and node list where we have list of Edge(Node's Id,
   Node's Id) and List<Node>

### Warm up

How to get neighbors of a particular node using an Adjacency Matrix?

```
List<Integer> neighbors(int[][] matrix, int i) {
   // TODO: note that we are given adjacency matrix or some 2D array of integer
   // and we want to find list of integer where they are connected with node `i`
   //
   //
}
```

### Solution

```
List<Integer> neighbors(int[][] matrix, int i) {
  List<Integer> neighbors = new LinkedList<>();
  for (int node : matrix[i]) {
    if (node == 1) {
        neighbors.add(node);
    }
  }
  return neighbors;
}
```

## **Breadth-first search (BFS)**

Algorithm for traversing or searching tree or graph data structures. It starts at the tree root, and explores all of the neighbor nodes at the present depth prior to moving on to the nodes at the next depth level.

## **BFS** implementation notes

- Do we need a Queue or Stack?
- How do we make sure we don't revisit the same node?

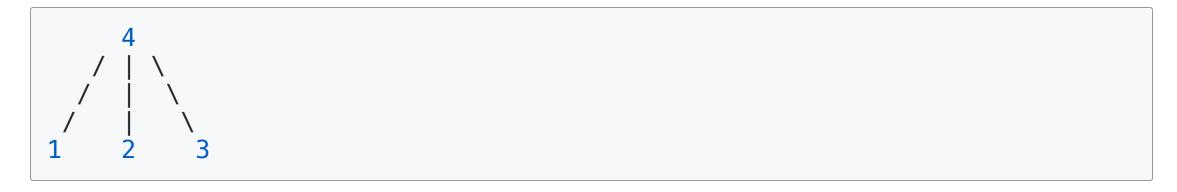
## **BFS** implementation in Java

```
List<Node> bfsTraversal(Node node) {
    if (node == null) return new LinkedList<Node>();
                                                                // if node is null then immediately
    LinkedList<Node> visited = new LinkedList<>();
                                                                 // list of visited nodes
    Queue<Node> queue = new LinkedList<>();
                                                                 // create queue of nodes
    queue.enqueue(node);
                                                                 // add `root` to the queue
    while (!queue.isEmptv()) {
                                                                 // while queue is not empty
       Node current = queue.dequeue();
                                                                 // dequeue a node
        if (visited.contains(current)) continue;
                                                                 // short-circuit if node already visited
        visited.add(current);
                                                                 // mark the node as visited
        List<Node> neighbors = getNeighbors(current);
                                                                 // get neighbors of current node
        for (Node neighbor: neighbors) {
            if (!visited.contains(neighbor)) {
                                                                 // we only add unvisited neighbors
                                                                 // engueue the next neighbor for traversal
                queue.add(neighbor);
    return visited;
                                                                 // return traversal list
```

### **Exercise**

Let's analyze the queue if we attempt to do a BFS traversal starting from node "1"

or bfsTraversal(node 1)



### Solution

```
visited: {
                      } queue: { 1
                                      } // start by adding the node to queue
                                      } // dequeue 1 and mark 1 as visited
} // enqueue un-visited neighbors of
                      } queue: {
} queue: { 4
visited: { 1
visited: { 1
                                          // enqueue un-visited neighbors of 1
                      } queue: {     } // mark 4 as visited
visited: { 1, 4
                      } queue: { 2, 3 }
visited: { 1, 4
                                           // enqueue un-visited neighbors of 4
                                           // [2, 3] <- enqueue(2)
                                                     <- enqueue(3)
visited: { 1, 4, 2 } queue: { 3 } // dequeue 2 and mark 2 as visited
                                      } // dequeue 3 mark 3 as visited
visited: { 1, 4, 2, 3 } queue: {
```

## Depth-first search (DFS)

Algorithm for traversing or searching tree or graph data structures. The algorithm starts at the root node and explores as far as possible along each branch before backtracking.

# **DFS** implementation notes

• Do we need a Queue or Stack?

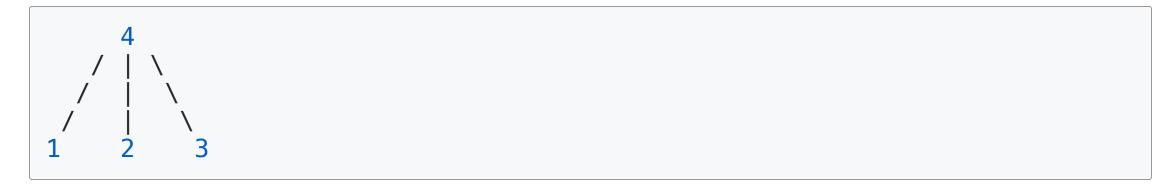
## **DFS Implementation in Java**

```
public List<Node> dfsTraversal(Node node) {
   LinkedList<Node> visited = new LinkedList<>();  // list of visited nodes
                                           // Initialize an empty stack
   Stack<Node> stack = new LinkedList<>();
   stack.push(node);
                                               // add the node to the top of the stack
   while (!stack.isEmpty()) {
      Node current = stack.pop();
                                           // pop the top current from the stack
       if (visited.contains(current)) continue; // short-circuit if node already visited
       visited.add(current);
                                               // add current node as visited
       List<Node> neighbors = getNeighbors(current); // get neighbors of current node
       for (Node neighbor: neighbors) {
          stack.push(neighbor);
                                            // engueue the next neighbor for traversal
                                               // return traversal list
   return visited;
```

### **Exercise**

Let's analyze the stack if we attempt to do a DFS traversal starting from node "1"

or dfsTraversal(node 1)



### Solution