## Homework #3

Due on November 30, 2019 at 11:55pm

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## Problem 6

## Section a:

In these parts of problem , we evaluate some classification methods on digits which available in **scikit** library. In this section digit data is shown in below figures.

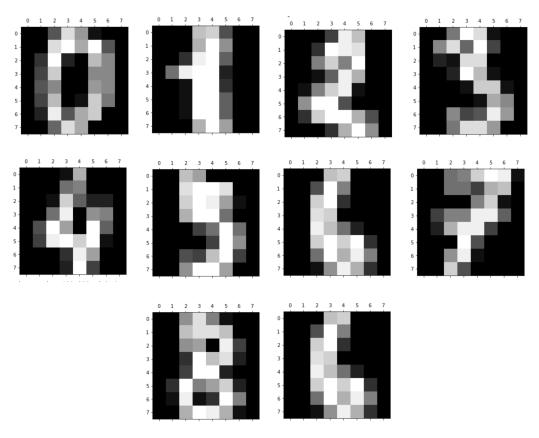


Figure 1: Digits

## Section b:

Results for various classification methods is shown bellow. As we can see logistic regression did better and achieved the best accuracy among others.

```
accuracy for QDA is 0.868888888888888
[[37 1 0 0 0 0 0 0 0 0]
 [ 0 35 0 0 0 0 0
                     0
                        2
                           0 1
  0 2 43 0 1 0 0
                     0 2 01
 [ 0
     0 0 43 0 0
                  0
                        2
                           0]
     1 0 0 33 0 0 5 0 0]
  0
     0
        0 10 1 32 0
                        7
                           11
  0
     2 0 0 0 0 42 0
                        2 01
  0
     0 0 0 0 0 0 48 0 0]
[ 0
     3 0 1 0 0 0 1 48
                           0]
     0 0 3 0 1 0 5 2 30]]
 [ 0
             precision
                        recall f1-score
                                          support
          0
                 1.00
                          0.97
                                    0.99
                                               38
          1
                 0.80
                          0.95
                                    0.86
                                               37
                 1.00
                          0.90
                                    0.95
          3
                 0.75
                          0.91
                                    0.83
                                               47
                 0.94
                          0.85
                                    0.89
                                               39
          5
                 0.97
                          0.60
                                    0.74
                                               53
          6
                 1.00
                          0.91
                                    0.95
                                               46
                 0.76
                          1.00
                                    0.86
          8
                 0.74
                          0.91
                                    0.81
                                               53
                 0.97
                                               41
                          0.73
                                    0.83
   accuracy
                                    0.87
                                              450
  macro avg
                 0.89
                          0.87
                                    0.87
                                              450
weighted avg
                 0.89
                          0.87
                                    0.87
                                              450
```

Figure 2: QDA results

```
accuracy for LDA is 0.94
[[38 0 0 0 0 0 0
                             0]
 [ 0 34 1
           0 0
                 0 0
                       0
                          1
                             1]
 0 ]
     0 48
           0
              0
                 0 0
                       0
                          0
                             0]
  0
     0
        0 43
             0
                 1
                    0
                       0
                             1]
  0
     1
        0
           0 37
                 0
                    0
                       1
                          0
                             0]
     0
        0
           0
             0 53 0
                       0
                             0]
  0
                          0
 0 ]
                             1]
     1
        0
           0
              0 0 44 0 0
 [ 0
        0
           0
              0
                 0
                   0 47 0
                            1]
  0
     7
        0
           0
             0 0 0 0 44 2]
 0 ]
           0 0 1 0 2 3 35]]
     0
        0
             precision
                          recall f1-score
                                            support
          0
                  1.00
                            1.00
                                      1.00
                                                  38
                  0.79
                            0.92
                                      0.85
                                                  37
          1
                  0.98
                            1.00
                                      0.99
                                                  48
                                      0.96
          3
                  1.00
                            0.91
                                                  47
          4
                  1.00
                            0.95
                                      0.97
                                                 39
          5
                  0.96
                            1.00
                                      0.98
                                                  53
          6
                  1.00
                            0.96
                                      0.98
                                                  46
          7
                  0.94
                            0.98
                                      0.96
                                                  48
          8
                  0.88
                            0.83
                                      0.85
                                                  53
                  0.85
                            0.85
                                      0.85
                                                  41
   accuracy
                                      0.94
                                                 450
  macro avg
                  0.94
                            0.94
                                      0.94
                                                 450
weighted avg
                  0.94
                            0.94
                                      0.94
                                                 450
```

Figure 3: LDA results

accuracy	for	Logist	ic I	Sear	ess	sion	is	0.96	
[[38 0	0 0	0 0		0	0	01		0.50	
[ 0 36	0 0	1 0	0	0	0	01			
[00]	48 0	0 0	0	0	0	0 ]			
0 0 ]	0 47	0 0	0	0	0	0]			
[ 0 1	0 0	38 0	0	0	0	0]			
0 0 ]	0 0	0 53	0	0	0	0]			
[ 0 1	0 0	0 1	43	0	1	0]			
0 0 ]	0 0	1 1	0	46	0	0]			
[ 0 3	1 0	0 0	0	0	47	2]			
0 0 ]	0 1	1 1	0	1	1	36]]			
		preci	sion	1	re	ecall	. 1	f1-score	support
	0		1.00			1.00		1.00	38
	1		0.88			0.97		0.92	37
						1.00		0.99	48
		0.98			1.00		0.99	47	
		0.93			0.97		0.95	39	
	5 0.95					1.00		0.97	53
	6 1.00				0.93		0.97	46	
	7		0.98			0.96		0.97	48
	8		0.96			0.89		0.92	53
	9		0.95	5		0.88	3	0.91	41
2001	×2011							0.96	450
accu	-		0 0/	-		0 06			
macro	_		0.96			0.96		0.96	450
weighted	avg		0.96	)		0.96	)	0.96	450

Figure 4: Logistic regression

After logistic regression , LDA did best on digits data and QDA has the lowest accuracy. Section  ${f c}:$ 

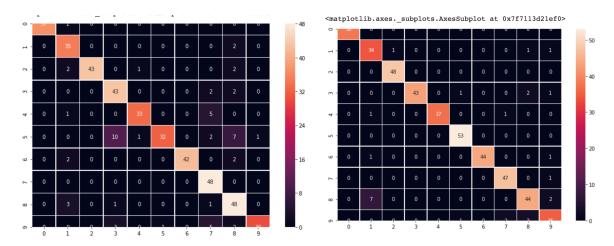
Confusion matrix is plotted bellow and accuracy for every digits also has shown.

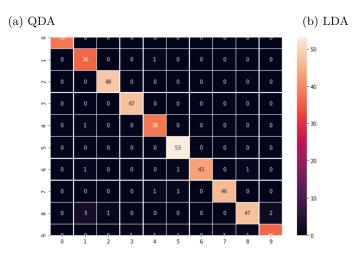
•	precision	recall	f1-score	support		precision	recall	f1-score	support
0	1.00	0.97	0.99	38	0	1.00	1.00	1.00	38
1	0.80	0.95	0.86	37	1	0.79	0.92	0.85	37
2	1.00	0.90	0.95	48	2	0.98	1.00	0.99	48
3	0.75	0.91	0.83	47	3	1.00	0.91	0.96	47
4	0.94	0.85	0.89	39	4	1.00	0.95	0.97	39
5	0.97	0.60	0.74	53	5	0.96	1.00	0.98	53
6	1.00	0.91	0.95	46	6	1.00	0.96	0.98	46
7	0.76	1.00	0.86	48	7	0.94	0.98	0.96	48
8	0.74	0.91	0.81	53	8	0.88	0.83	0.85	53
9	0.97	0.73	0.83	41	9	0.85	0.85	0.85	41
accuracy			0.87	450	accuracy			0.94	450
macro avg	0.89	0.87	0.87	450	macro avg	0.94	0.94	0.94	450
weighted avg	0.89	0.87	0.87	450	weighted avg	0.94	0.94	0.94	450

(a) QDA				(b)	LDA
	precision	recall	f1-score	support	
0	1.00	1.00	1.00	38	
1	0.88	0.97	0.92	37	
2	0.98	1.00	0.99	48	
3	0.98	1.00	0.99	47	
4	0.93	0.97	0.95	39	
5	0.95	1.00	0.97	53	
6	1.00	0.93	0.97	46	
7	0.98	0.96	0.97	48	
8	0.96	0.89	0.92	53	
9	0.95	0.88	0.91	41	
accuracy			0.96	450	
macro avg	0.96	0.96	0.96	450	
weighted avg	0.96	0.96	0.96	450	

(c) Logistic regression

For better illustration notice bellow figures.





(c) Logistic regression