

Introduction to Graph ML

Graph ML

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Instructor

- Hadi Amiri
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What's This Course about?

- Graph Machine Learning
 - Networks
 - a pattern of inter-connections among a set of things!
 - deal with structure
 - Meta data
 - deal with various user generated content (text, images, videos, etc.,) in networks.
- We aim to learn about prediction algorithms that work well on networks.
 - Models, properties, design principles!

Graphs/Networks

- Communication Networks
 - Telco Nets
 - Messenger Nets
- Friendship Networks
 - Facebook
- Microblogs
 - Twitter
- Information Networks
 - Web!

Examples



Sample 1.

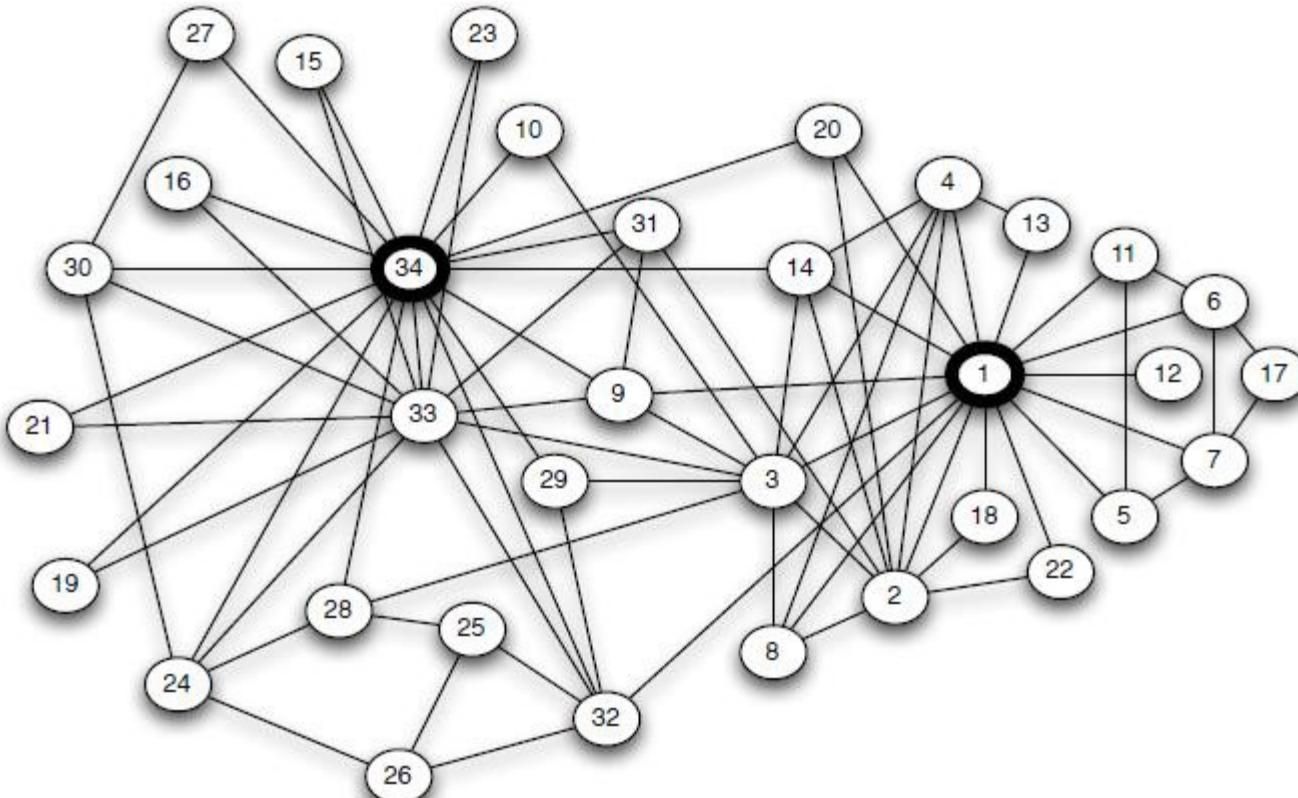


Figure 1.1: The social network of friendships within a 34-person karate club [421].

Sample 2.

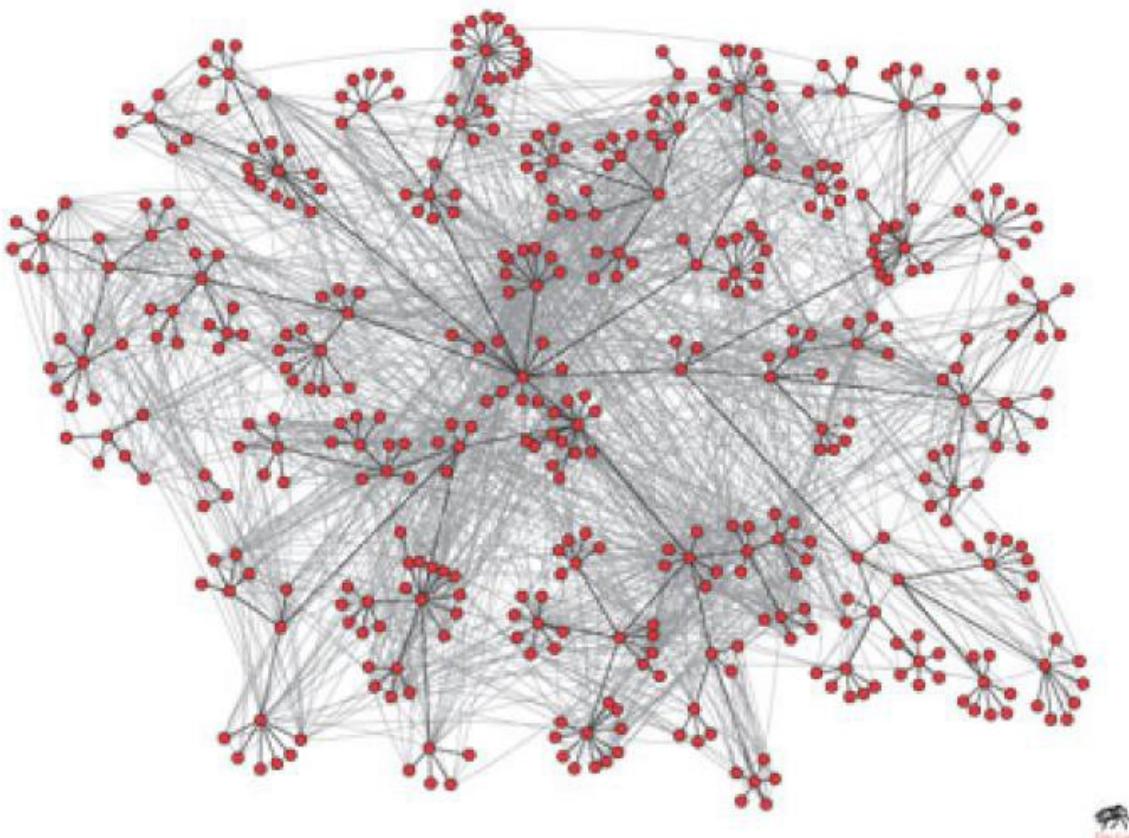


Figure 1.2: Social networks based on communication and interaction can also be constructed from the traces left by on-line data. In this case, the pattern of e-mail communication among 436 employees of Hewlett Packard Research Lab is superimposed on the official organizational hierarchy [6]. (Image from <http://www-personal.umich.edu/~ladamic/img/hplabsemailhierarchy.jpg>)

Sample 3.

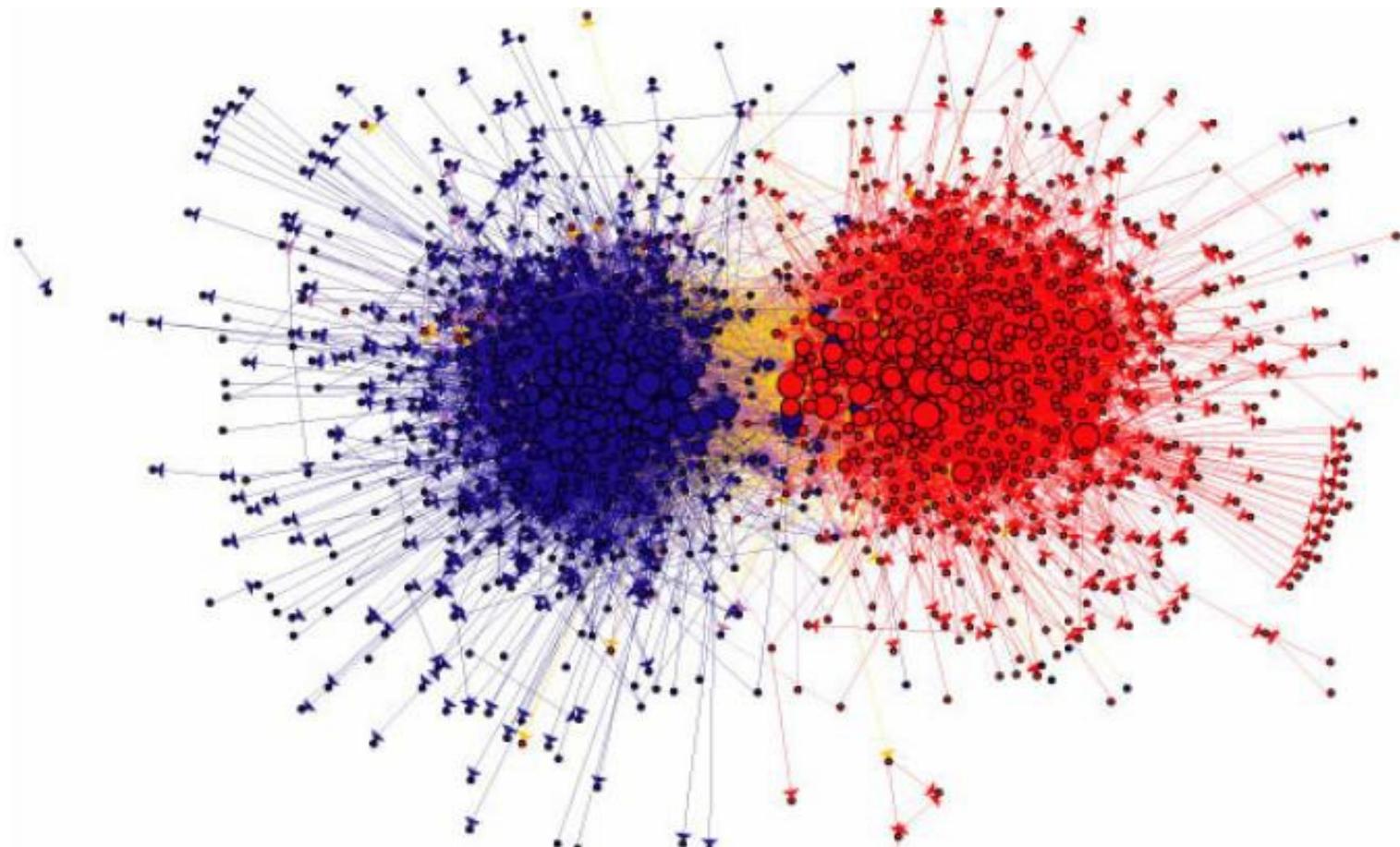


Figure 1.4: The links among Web pages can reveal densely-knit communities and prominent sites. In this case, the network structure of political blogs prior to the 2004 U.S. Presidential election reveals two natural and well-separated clusters [5]. (Image from <http://www-personal.umich.edu/ladamic/img/politicalblogs.jpg>)

Sample 4.

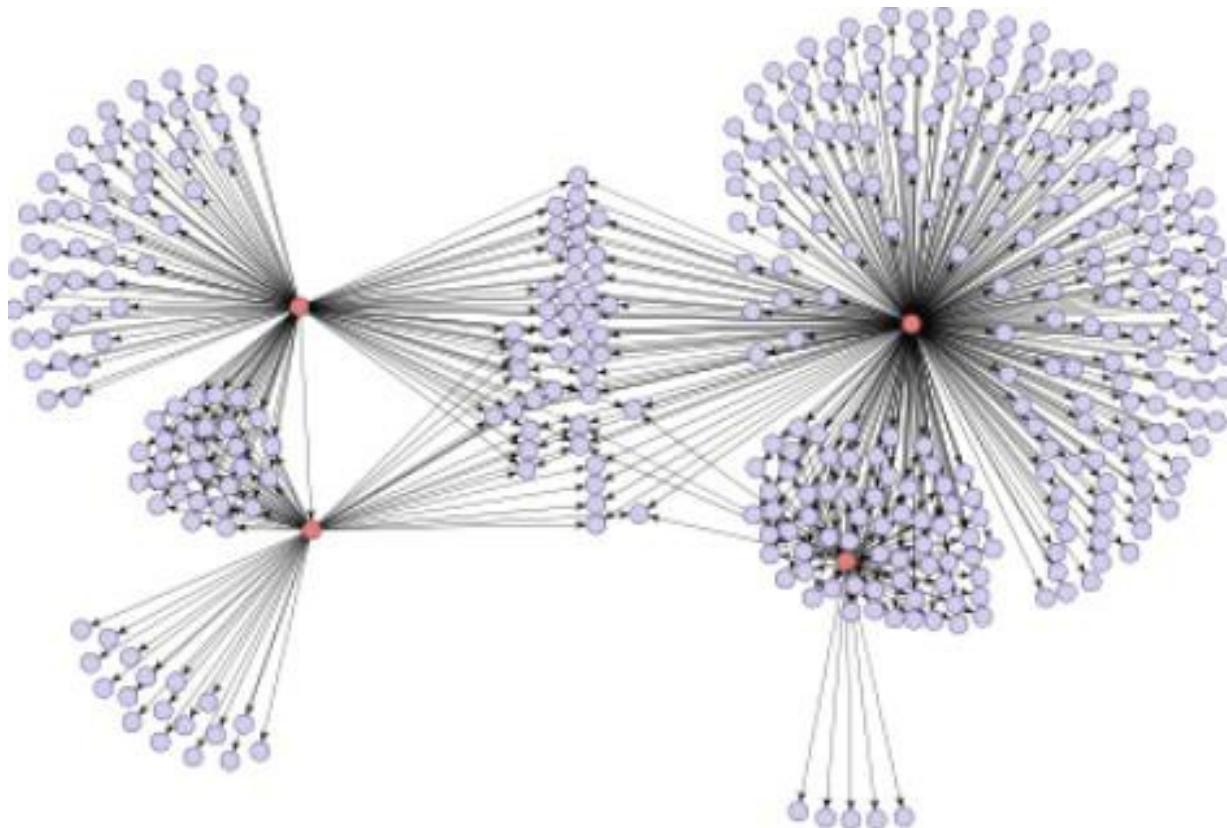


Figure 1.11: When people are influenced by the behaviors their neighbors in the network, the adoption of a new product or innovation can cascade through the network structure. Here, e-mail recommendations for a Japanese graphic novel spread in a kind of informational or social contagion. (Image from Leskovec et al. [271].)

Sample 5.

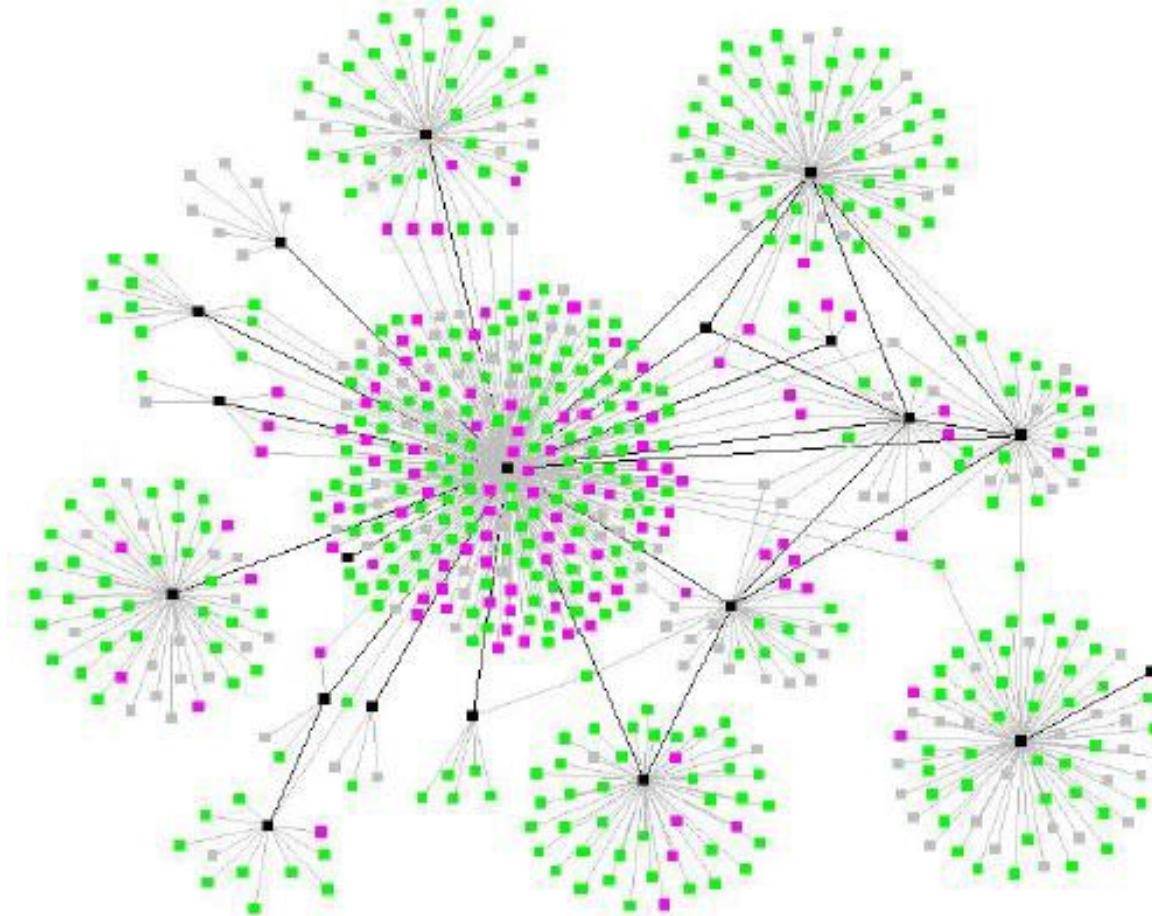
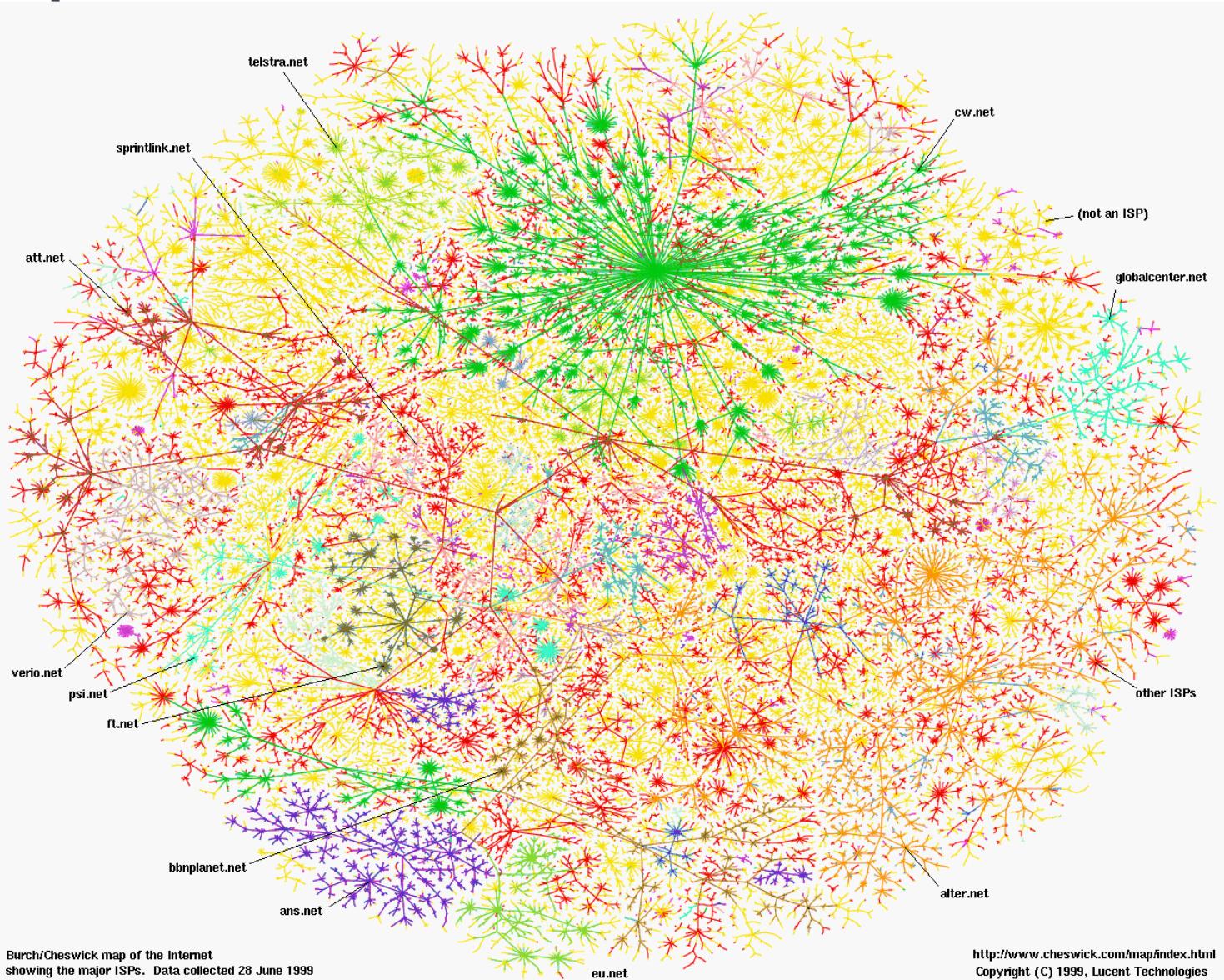


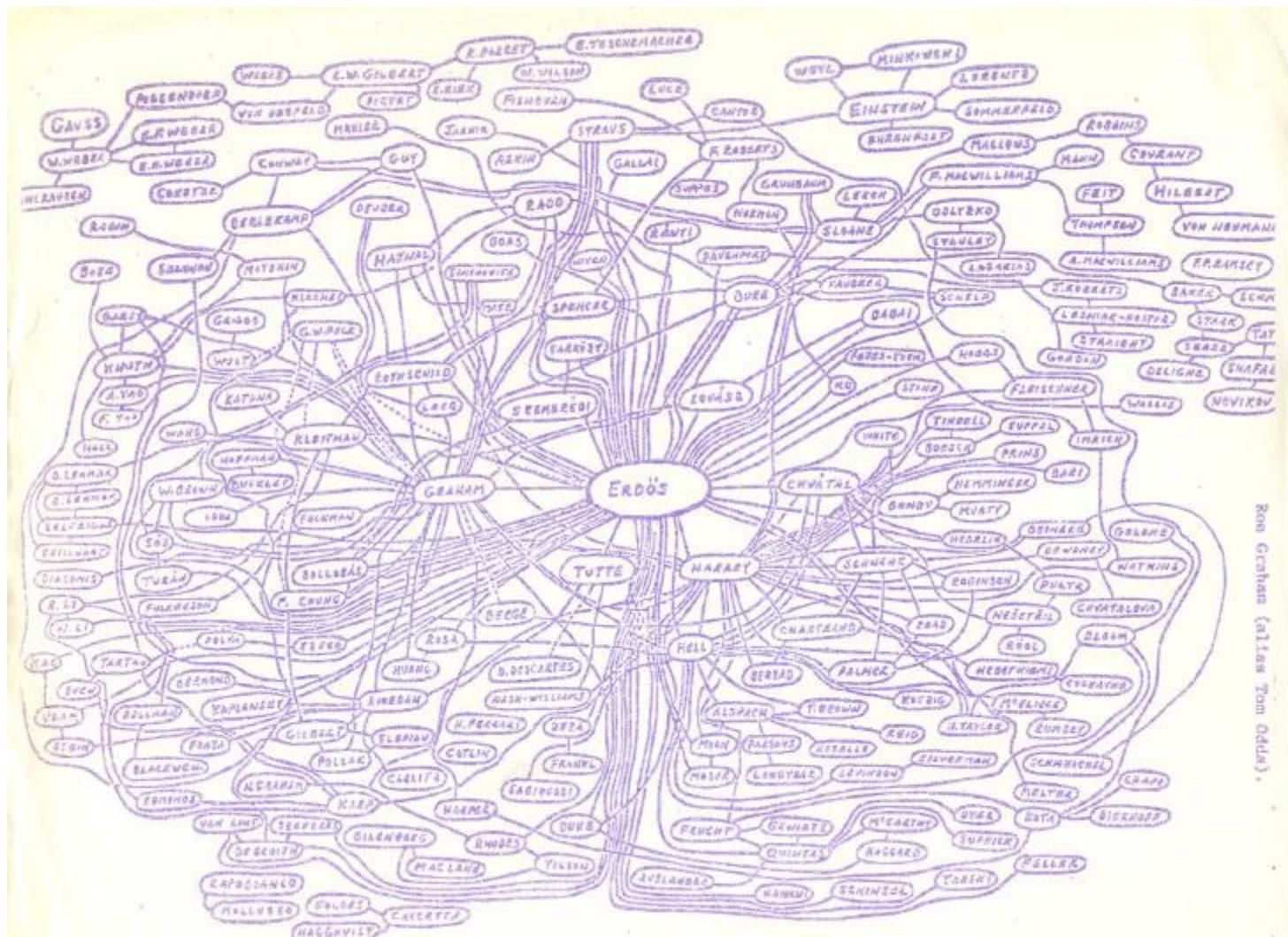
Figure 1.12: The spread of an epidemic disease (such as the tuberculosis outbreak shown here) is another form of cascading behavior in a network. The similarities and contrasts between biological and social contagion lead to interesting research questions. (Image from Andre et al. [16].)

Sample 6.

Network of Major ISPs.
1999



Sample 7.



Ron Graham (alias Tom Dula) «

Figure 2.12: Ron Graham's hand-drawn picture of a part of the mathematics collaboration graph, centered on Paul Erdős [189]. (Image from <http://www.oakland.edu/enp/cgraph.jpg>)

Sample 8.

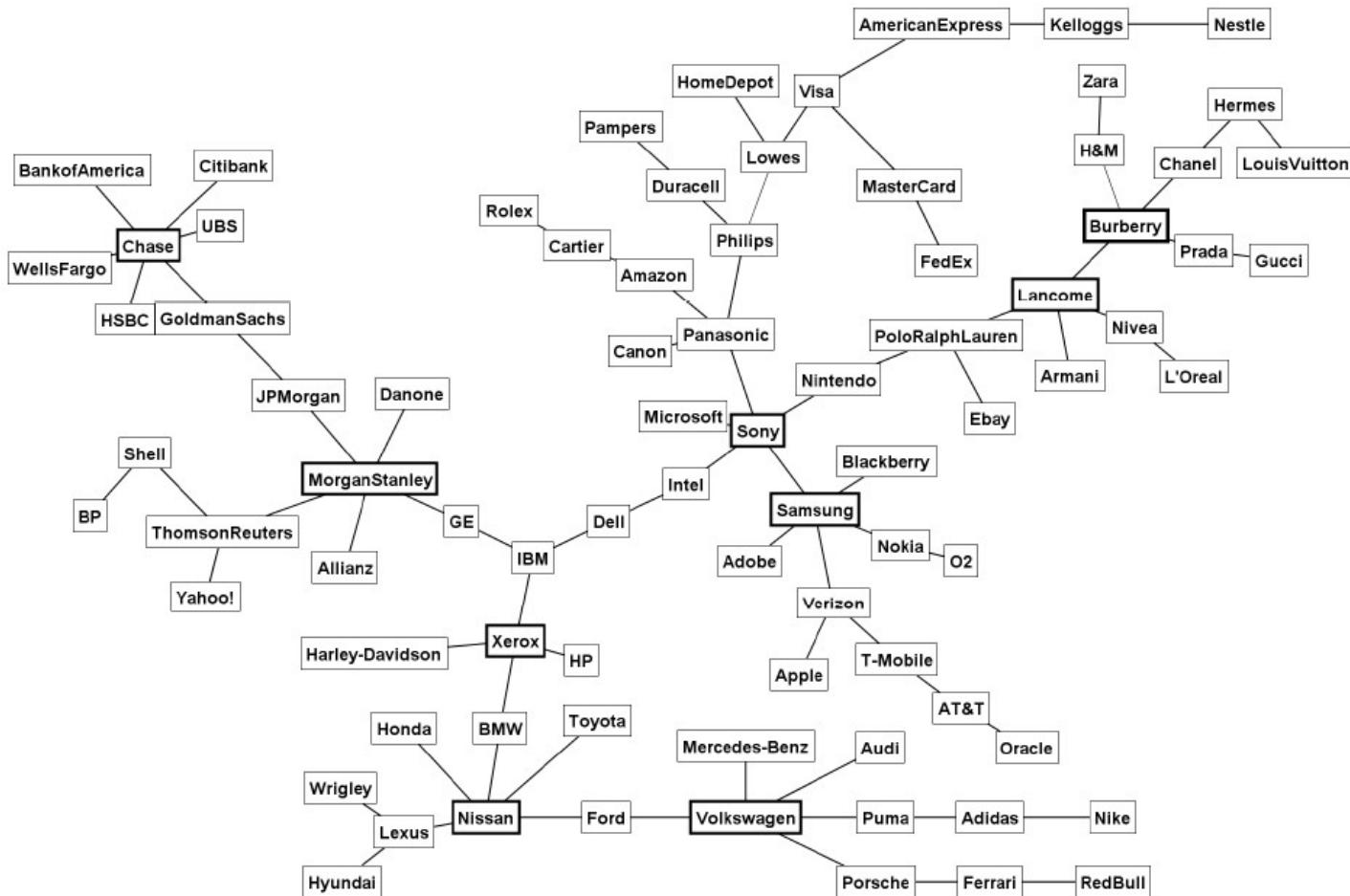


Figure 3. Minimum spanning tree (MST) of the most valued global brands. The MST of the brand network is the subset of edges that forms a tree reaching every brand such that the total length of all the edges is minimized. It is readily apparent that certain brands stand out prominently as hubs with connections to other brands radiating out from them. These hubs are generally the centers of well-formed market category groupings.

Sample 9.

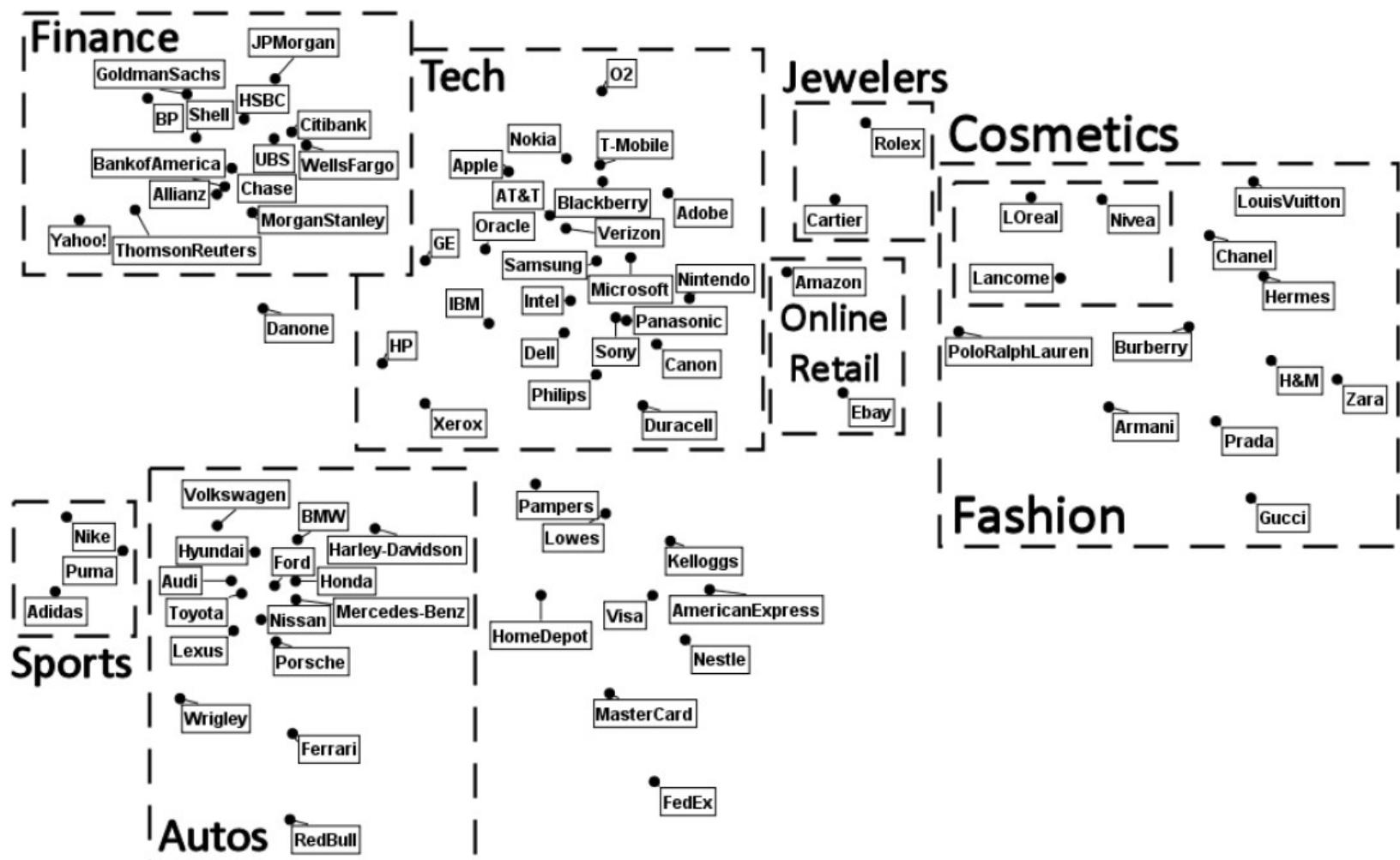
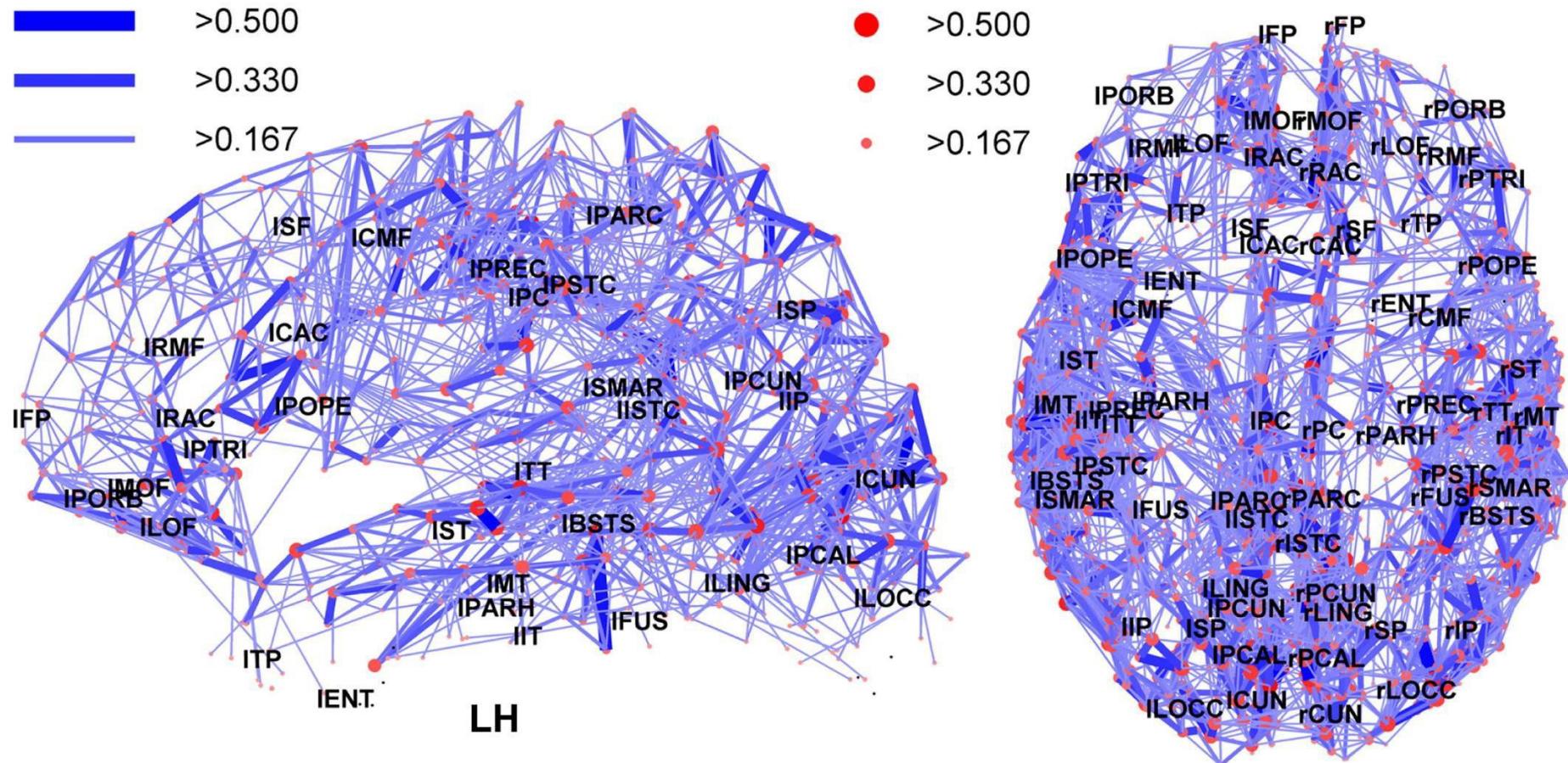


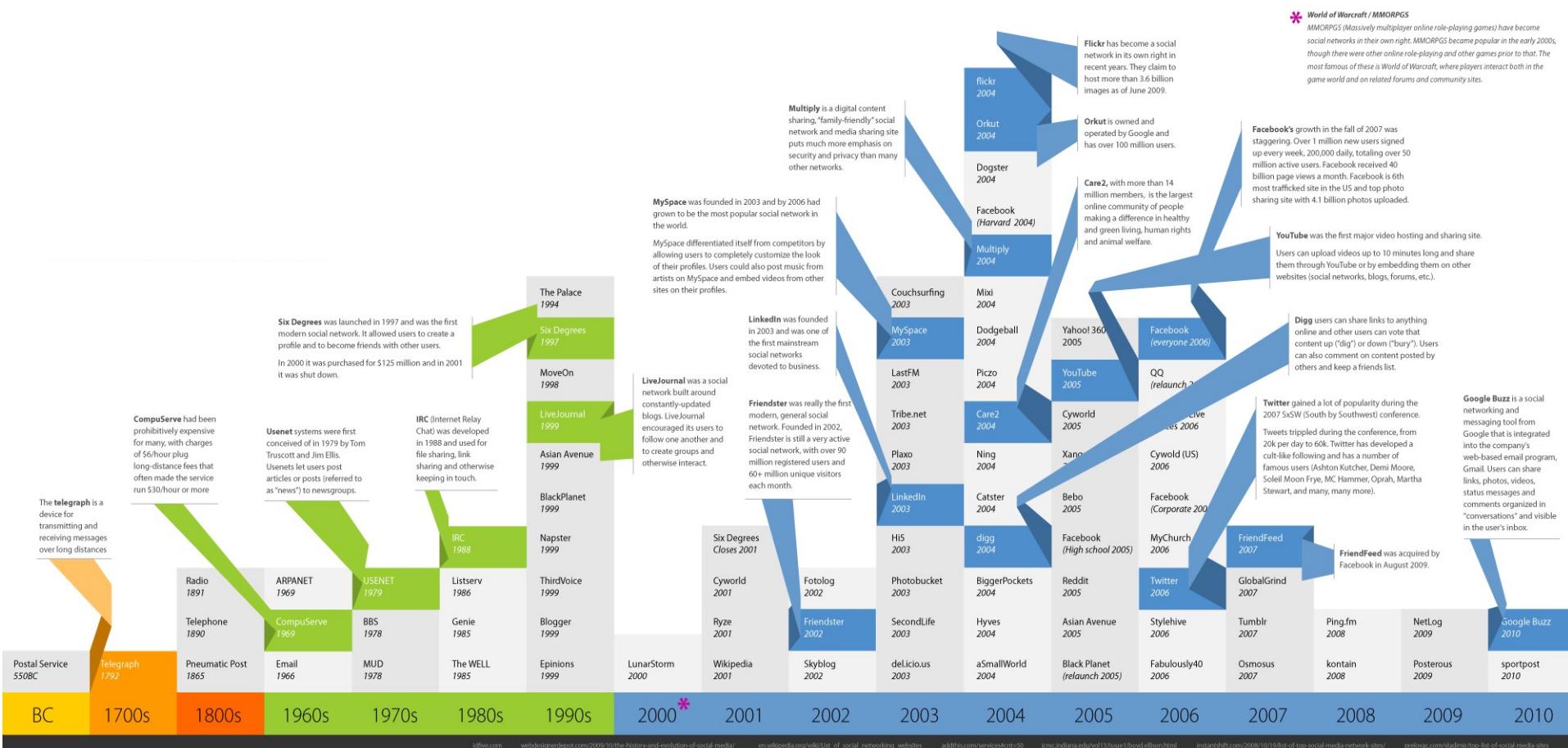
Figure 4. Map of brands. The minimum spanning tree augmented by triangulating each brand location from their nearest neighbors with forced-based layout yields a map high in face validity. Note the eight strong market category groupings outlined with broken lines.

Sample 10.

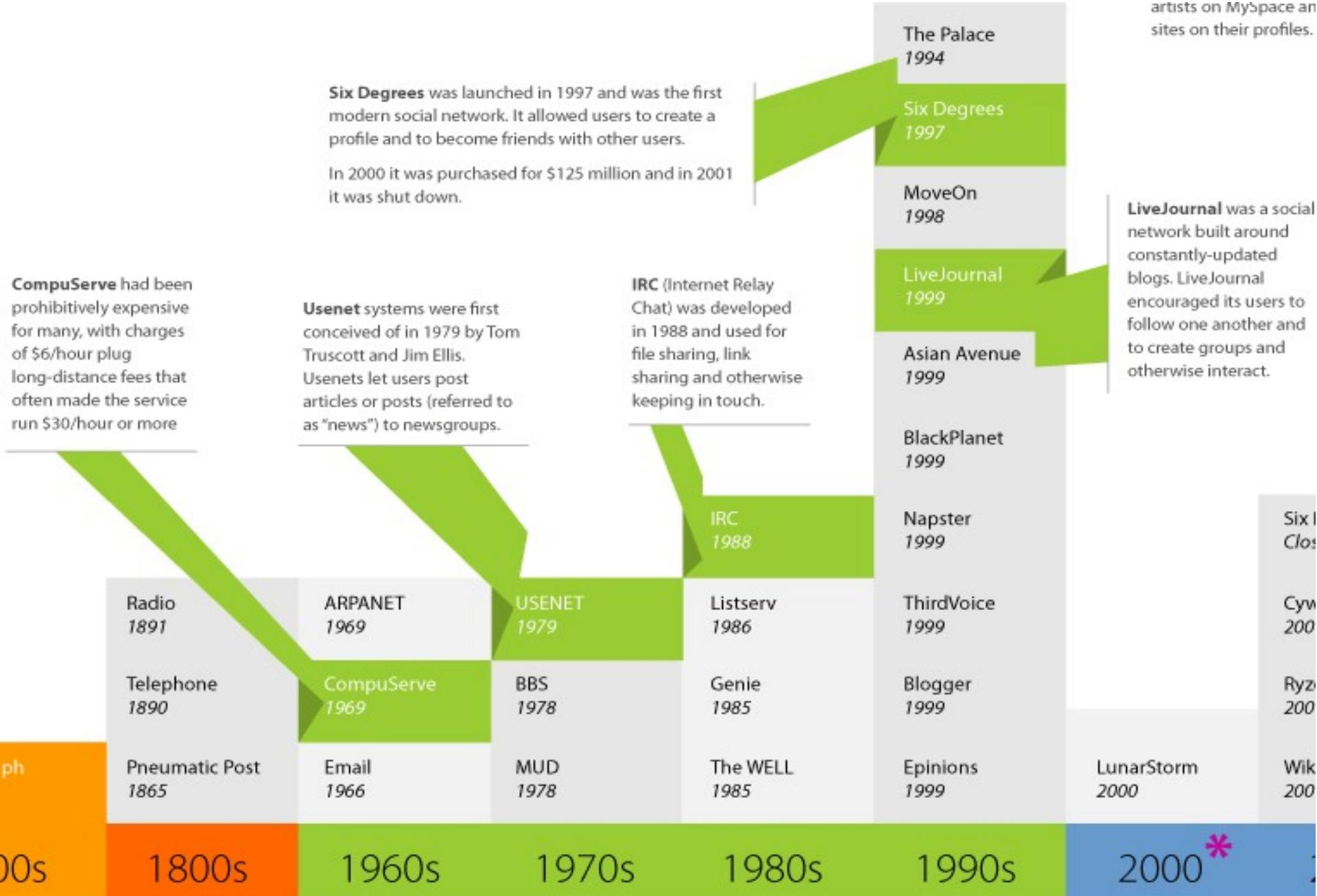


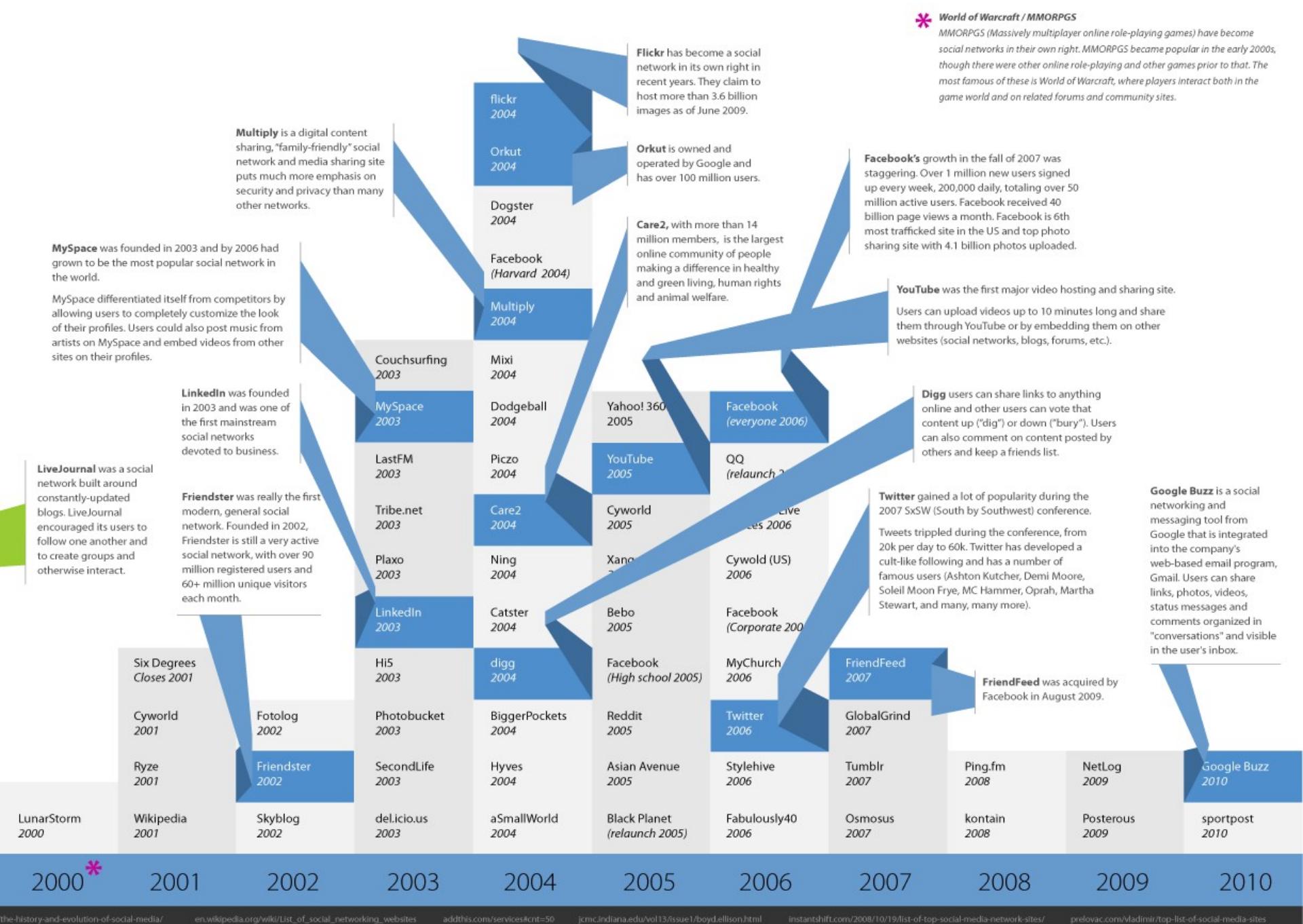
Network representation of brain connectivity: Dorsal and lateral views of the connectivity backbone of human brain. Labels indicating anatomical subregions are placed at their respective centers of mass. Nodes (individual ROIs) are coded according to strength and edges are coded according to connection weight.

How Long They've Been Around?



Source: <http://dustn.ty/stay-on-the-cutting-edge/>



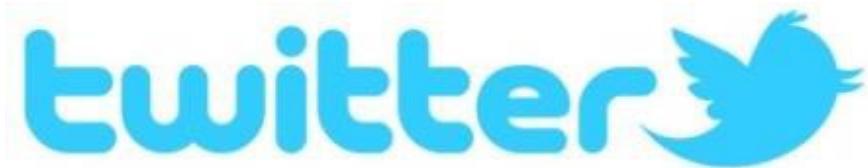


Why Should We Study Them?

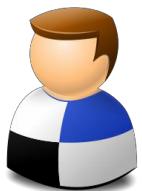
- Networks provide powerful ways of looking at complex data and systems:
 - Spread of news or diseases
 - Evolution of science
 - Structure of the Web
 - Markets & models of trades
- Networks help to understand if a principle holds across many settings and fields, and
- There are lots of them!

Cheap and high-resolution views into population behavior!

Let's Take a Closer Look at Twitter



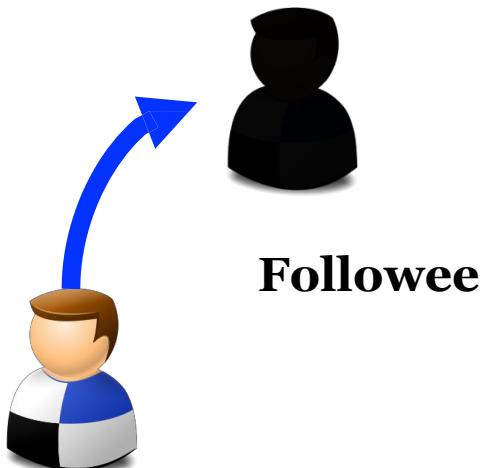
- Simple Structure



- Simple Structure

- Following

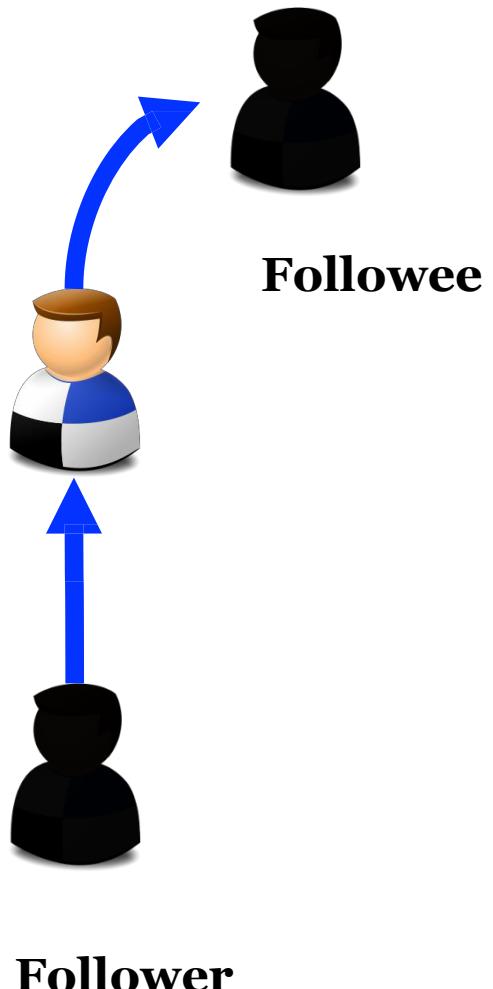
- To subscribe to other people's posts



- Simple Structure

- Following

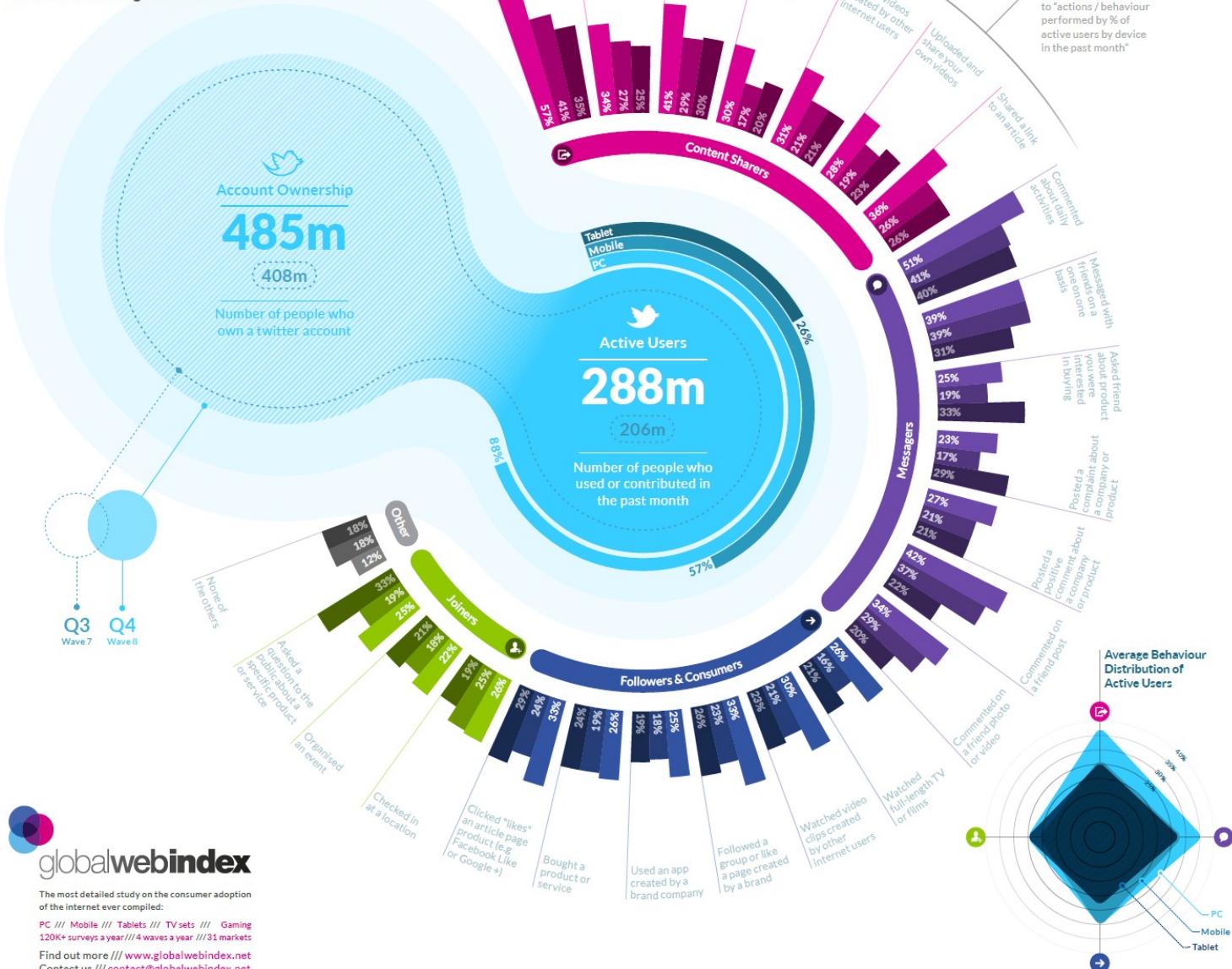
- To subscribe to other people's posts



TWITTER The Fastest Growing Social Platform

Twitter is now the fastest growing social platform increasing 40% between Q2 and Q4 2012. This means there are now **485m** account holders and **288m** active users.

FIND OUT MORE AT: globalwebindex.net





Account Ownership

485m

408m

Number of people who own a twitter account

88%

18%
18%
12%
Other



Tablet
Mobile
PC



Active Users

288m

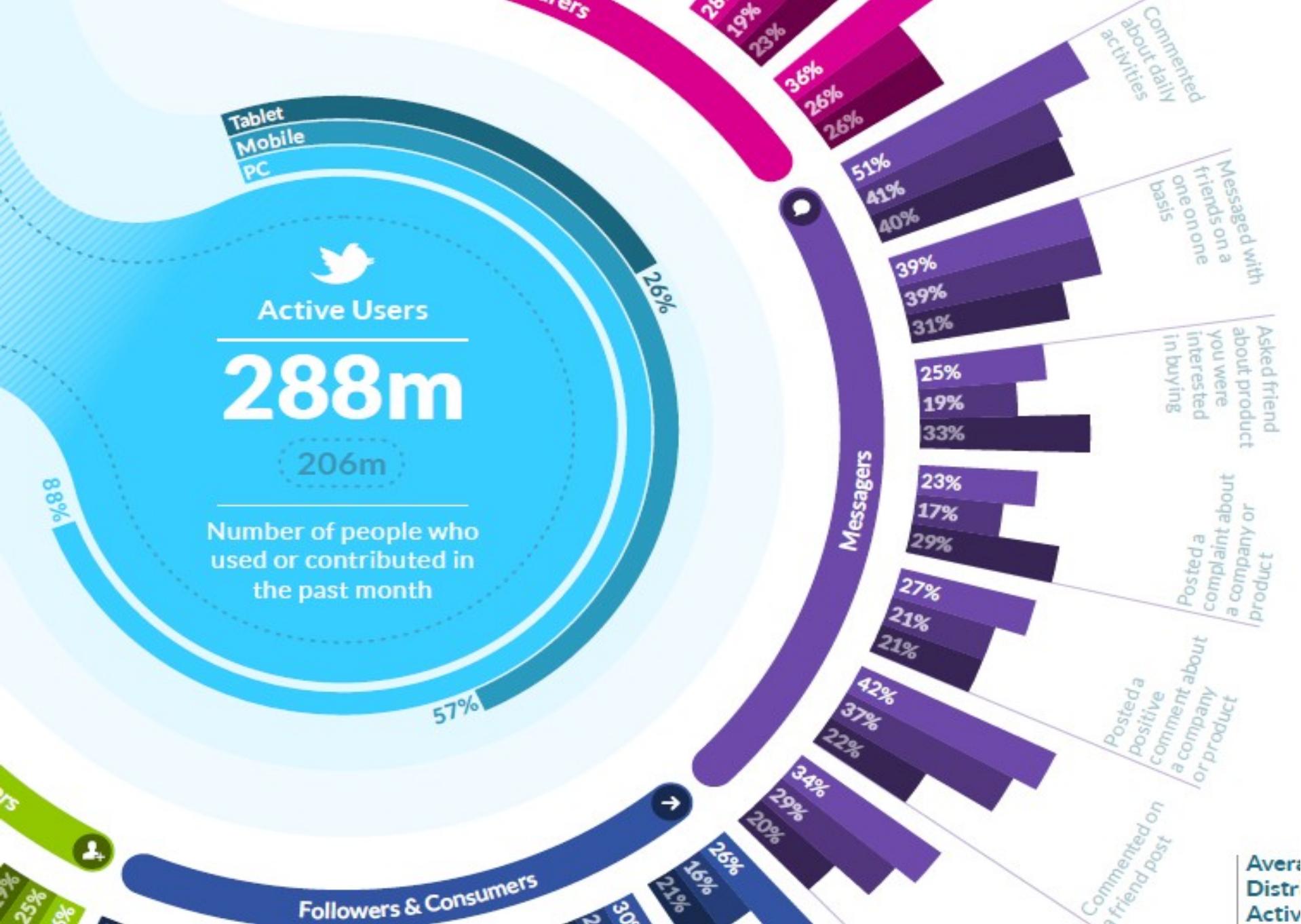
206m

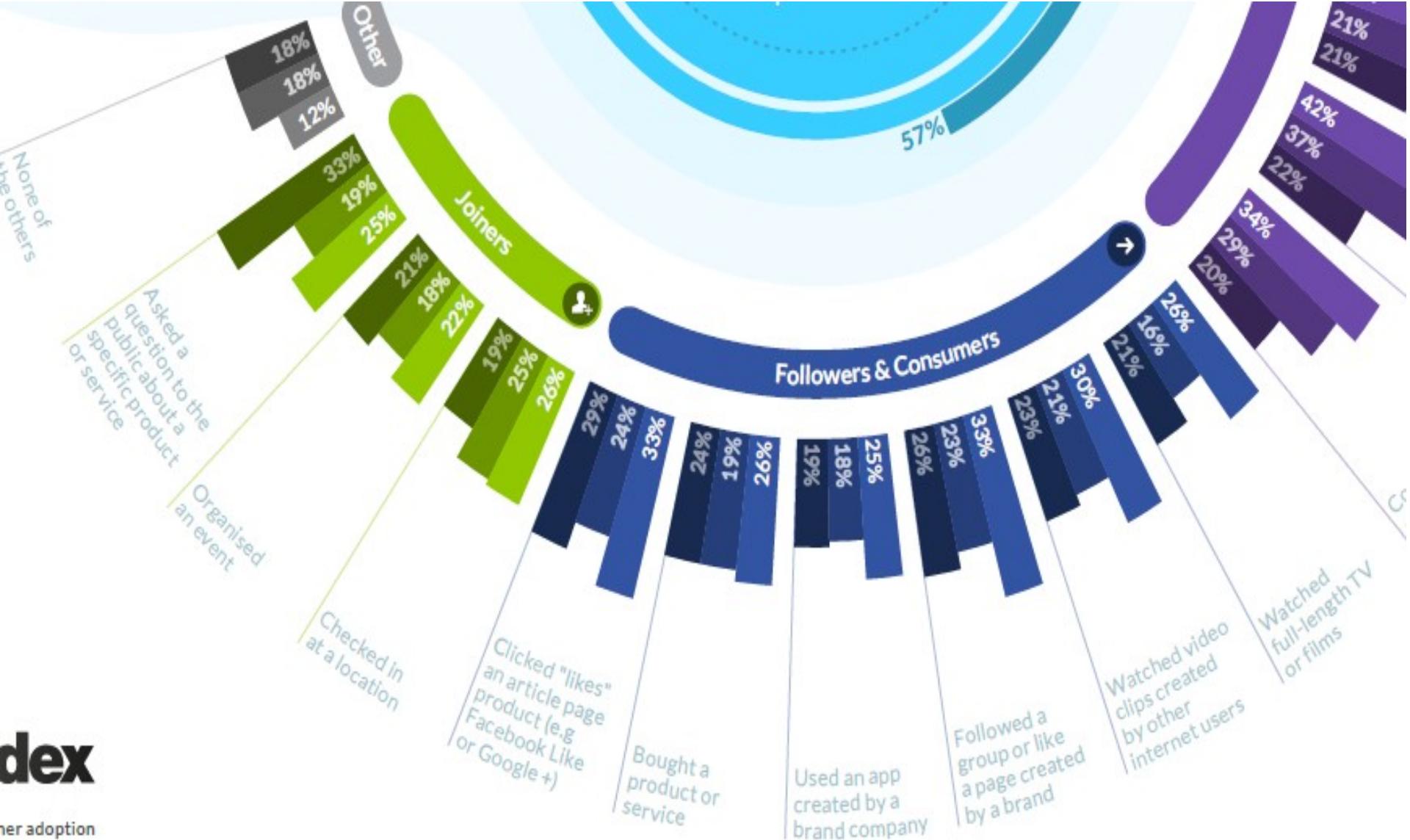
Number of people who used or contributed in the past month

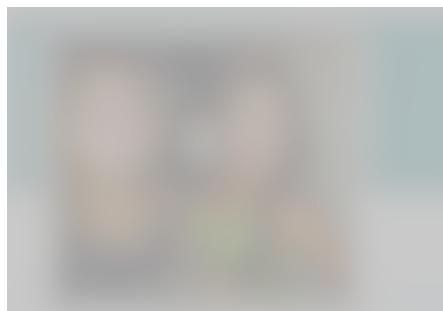
57%

al Platform







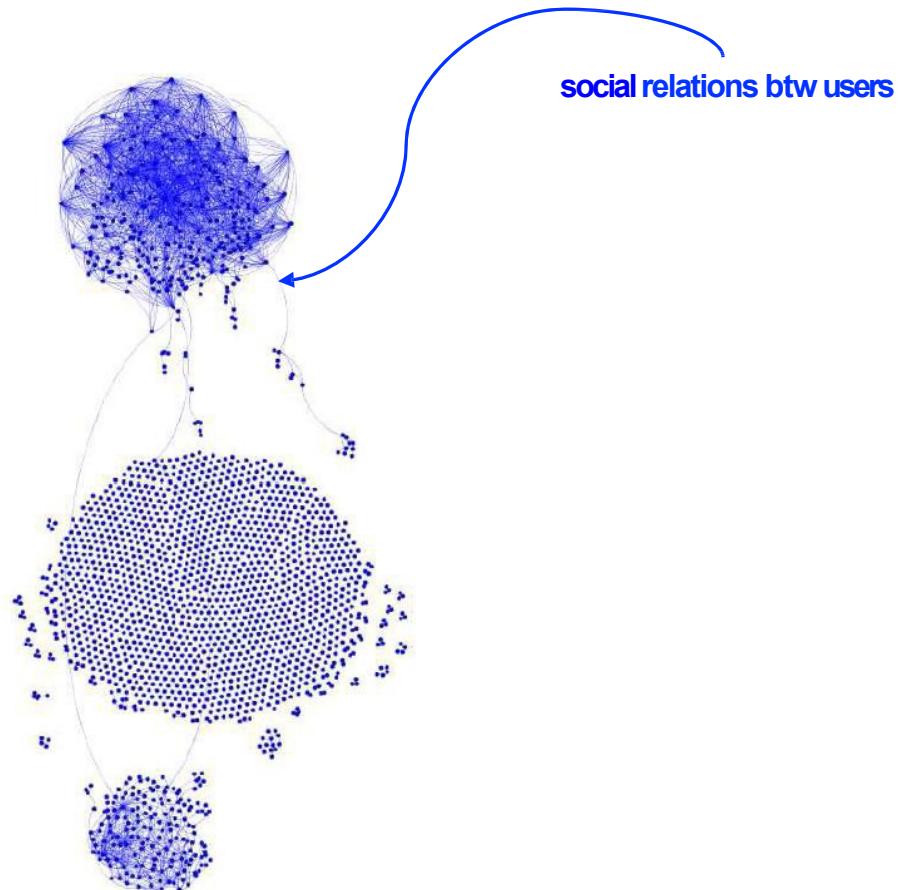


Joined July 2010

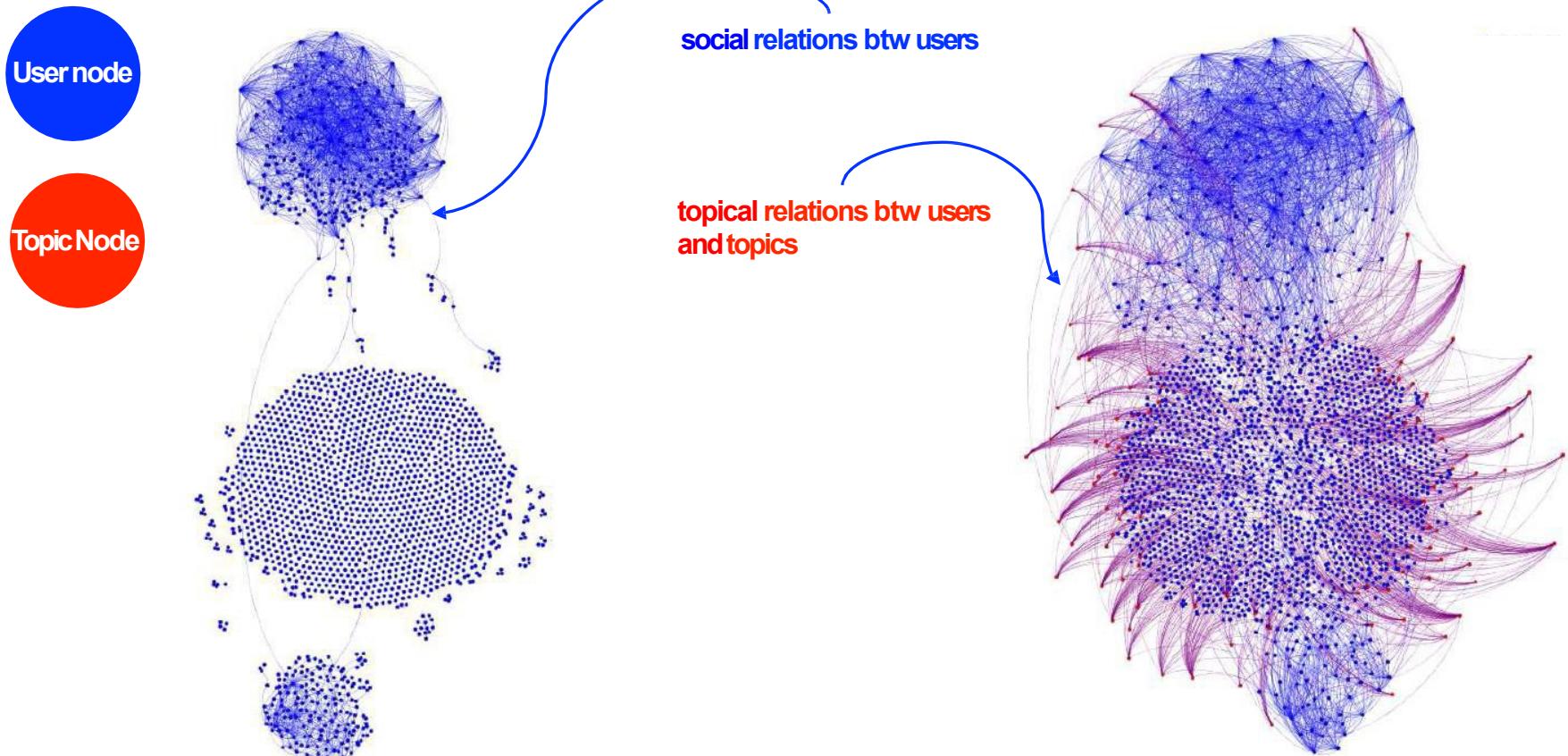
TWEETS	PHOTOS/ VIDEOS	FOLLOWING	FOLLOWERS	FAVORITES
47K	215	600	1219	368

```
object {21}
  created_at : Thu May 01 18:01:19 +0000 2014
  id : 461928366862376960
  id_str : 461928366862376960
  text : Debating if I should switch services with my family or if I should just stay on my own because I reallyyyy don't want to leave Verizon..
  truncated : false
  in_reply_to_status_id : null
  in_reply_to_status_id_str : null
  in_reply_to_user_id : null
  in_reply_to_user_id_str : null
  in_reply_to_screen_name : null
  user {40}
    geo : null
    coordinates : null
    place : null
    contributors : null
    retweet_count : 0
    favorite_count : 0
  entities {4}
    hashtags [0]
    symbols [0]
    urls [0]
    user_mentions [0]
  favorited : false
  retweeted : false
  lang : en
```

Net & Content Interactions



Net & Content Interactions



Network Characteristics

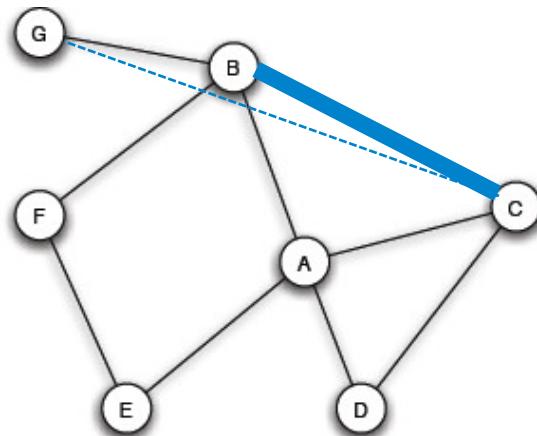
- Structure:
 - Network relations are often changing,
 - Weak/strong ties,
 - Often large but still a small world,
 - Popularity dynamics,
 - Cascades, etc.
- Content:
 - Streaming type,
 - High prevalence of user-generated/urban words,
 - Often short, context-less, and very noisy, and
 - Various languages.

What Do We Learn?

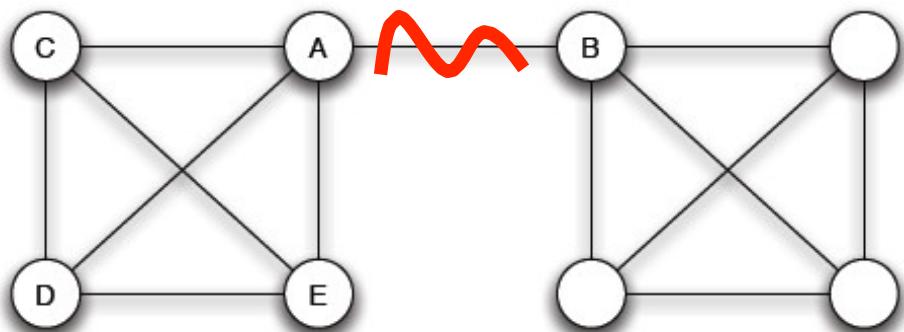
- Graph properties and features
- Node representation
- Graph representation
- Link prediction
- Cascade prediction
- Power laws and Popularity
- Meta Learning with graphs
- Applications
 - Language Analysis
 - Health Informatics
 - Search & Moment Retrieval
 - Trend Detection and Tracking, etc.

What Do We Learn? Cnt.

- Graph Features
 - Strong and Weak Ties



C-B is more likely to form or C-G?



Which link provides access to parts of the net that are unreachable by other means?

Are some nodes more important due to their position in networks?

What Do We Learn? Cnt.

- Graph Features
 - Distance metrics

common neighbors	$ \Gamma(x) \cap \Gamma(y) $
Jaccard's coefficient	$\frac{ \Gamma(x) \cap \Gamma(y) }{ \Gamma(x) \cup \Gamma(y) }$
Adamic/Adar	$\sum_{z \in \Gamma(x) \cap \Gamma(y)} \frac{1}{\log \Gamma(z) }$
preferential attachment	$ \Gamma(x) \cdot \Gamma(y) $
Katz $_{\beta}$	$\sum_{\ell=1}^{\infty} \beta^{\ell} \cdot \text{paths}_{x,y}^{(\ell)} $
where $\text{paths}_{x,y}^{(\ell)} := \{\text{paths of length exactly } \ell \text{ from } x \text{ to } y\}$ weighted: $\text{paths}_{x,y}^{(1)} := \text{number of collaborations between } x, y.$ unweighted: $\text{paths}_{x,y}^{(1)} := 1 \text{ iff } x \text{ and } y \text{ collaborate.}$	
hitting time	$-H_{x,y}$
stationary-normed	$-H_{x,y} \cdot \pi_y$
commute time	$-(H_{x,y} + H_{y,x})$
stationary-normed	$-(H_{x,y} \cdot \pi_y + H_{y,x} \cdot \pi_x)$
where $H_{x,y} := \text{expected time for random walk from } x \text{ to reach } y$ $\pi_y := \text{stationary-distribution weight of } y$ (proportion of time the random walk is at node y)	
rooted PageRank $_{\alpha}$	stationary distribution weight of y under the following random walk: with probability α , jump to x . with probability $1 - \alpha$, go to random neighbor of current node.
SimRank $_{\gamma}$	$\begin{cases} 1 & \text{if } x = y \\ \gamma \cdot \frac{\sum_{a \in \Gamma(x)} \sum_{b \in \Gamma(y)} \text{score}(a,b)}{ \Gamma(x) \cdot \Gamma(y) } & \text{otherwise} \end{cases}$

What Do We Learn? Cnt.

- Graph Features
 - The Structure of the Web
 - The Web contains a giant SCC

IN nodes:

can reach SCC but cannot be reached from it.

OUT nodes:

can be reached from SCC but cannot reach it.

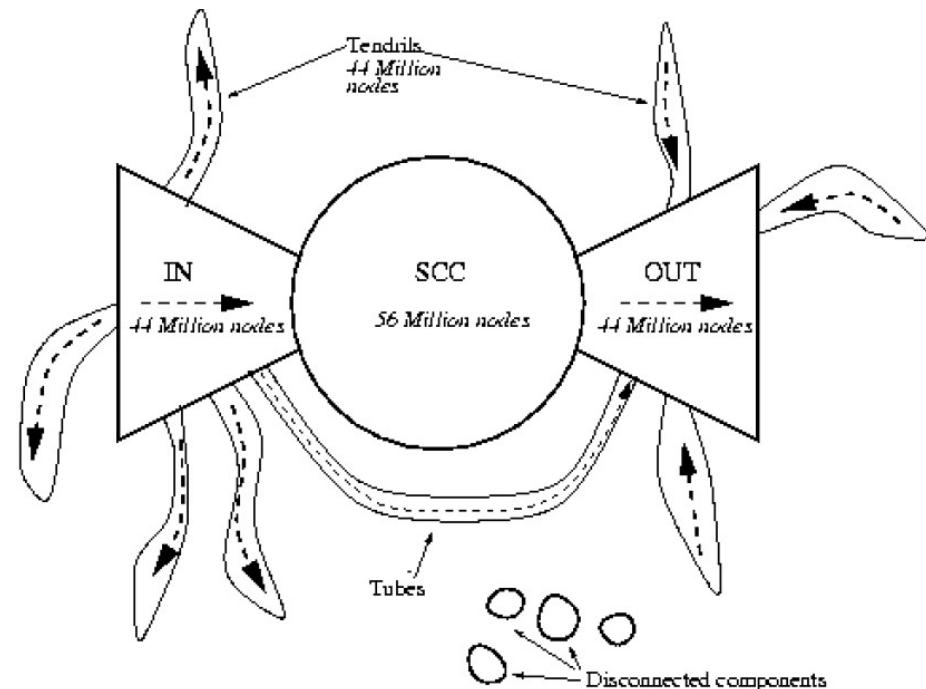
Tendrils nodes:

- reachable from IN but cannot reach SCC,
- can reach OUT but cannot be reached from SCC.

Tendrils nodes satisfying both (a) and (b), travel in "tube" from IN to OUT without touching SCC.

Disconnected nodes:

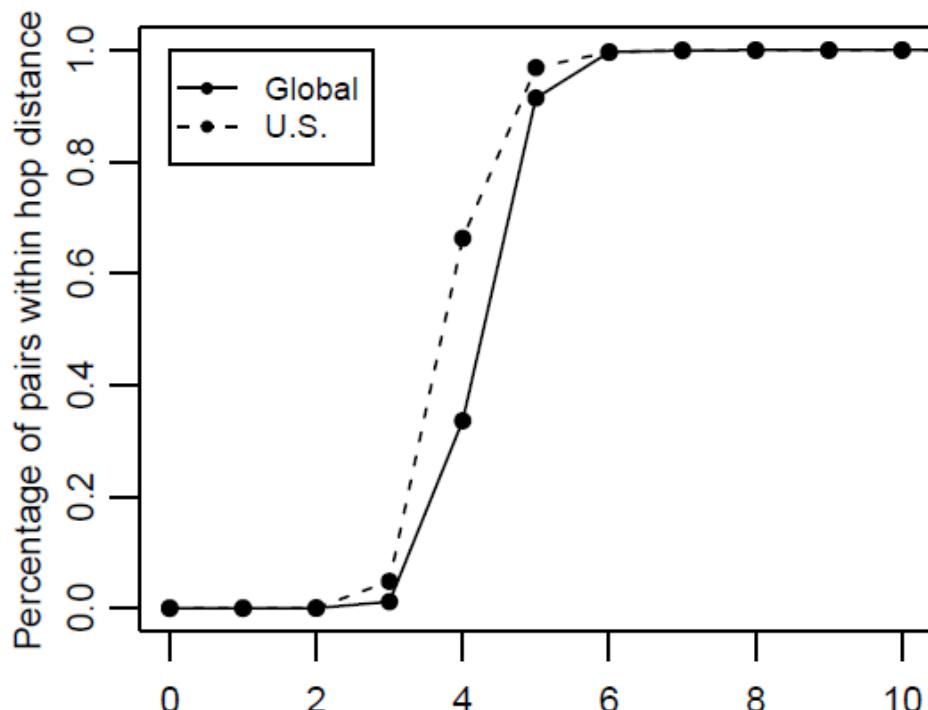
have no path to SCC ignoring directions



99.91% of individuals on FB belong to a single giant connected component

What Do We Learn? Cnt.

- Graph Features
 - Small World Phenomenon



Global

92.0%: within 5 degrees,
99.6%: within six degrees.

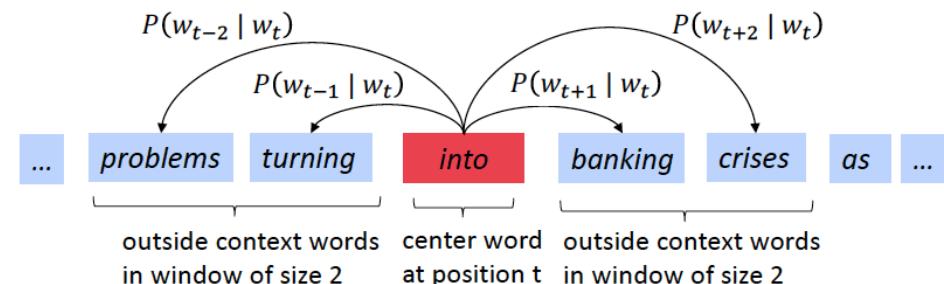
U.S. only

96.0%: within 5 degrees,
99.7%: within six degrees.

Figure 2. Diameter. The neighborhood function $N(h)$ showing the percentage of user pairs that are within h hops of each other. The average distance between users on Facebook in May 2011 was 4.7, while the average distance within the U.S. at the same time was 4.3.

What Do We Learn? Cnt.

- Node Representation



$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

- Update vectors so you can predict well

Nearest words to frog:

1. frogs
2. toad
3. litoria
4. leptodactylidae
5. rana
6. lizard
7. eleutherodactylus



litoria



leptodactylidae



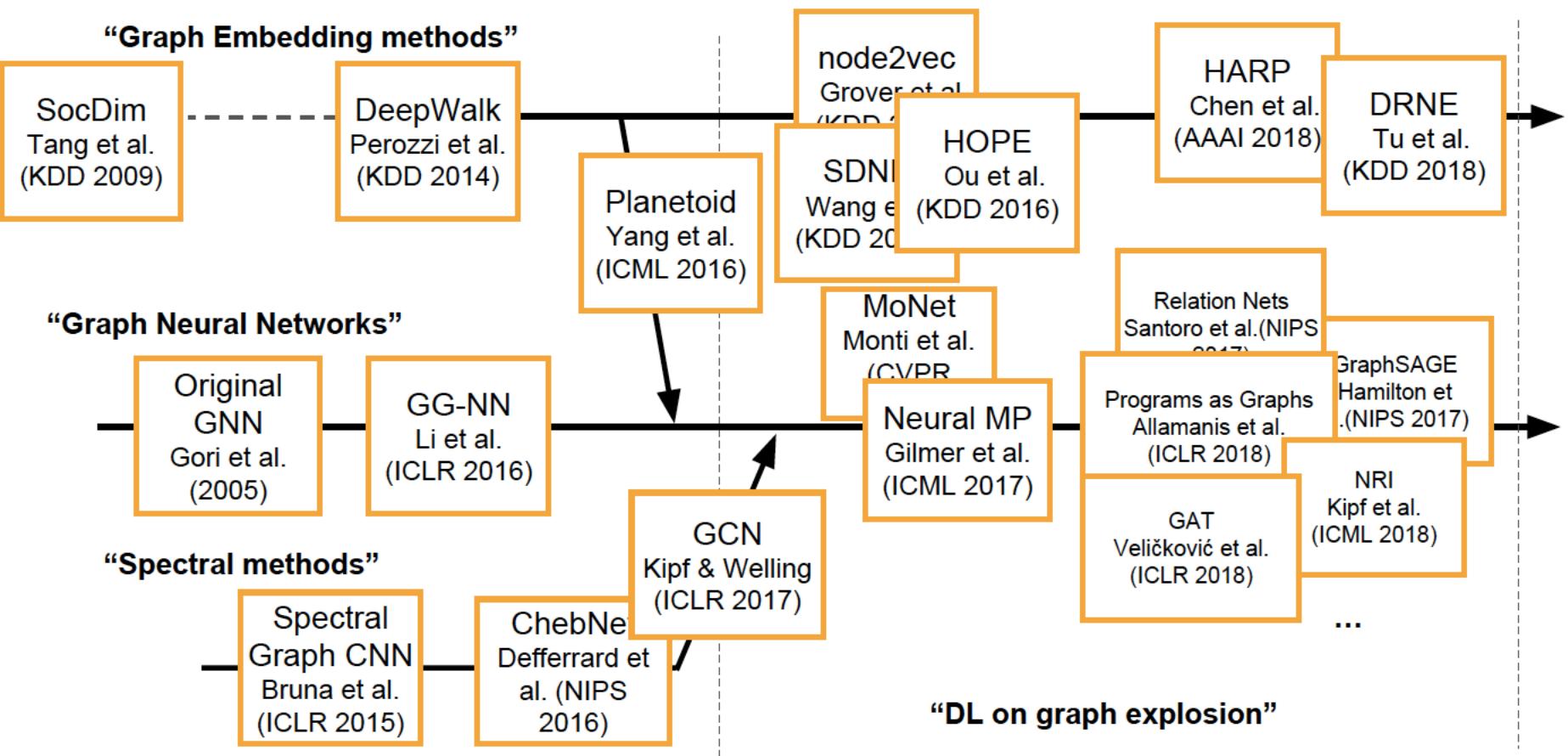
rana



eleutherodactylus

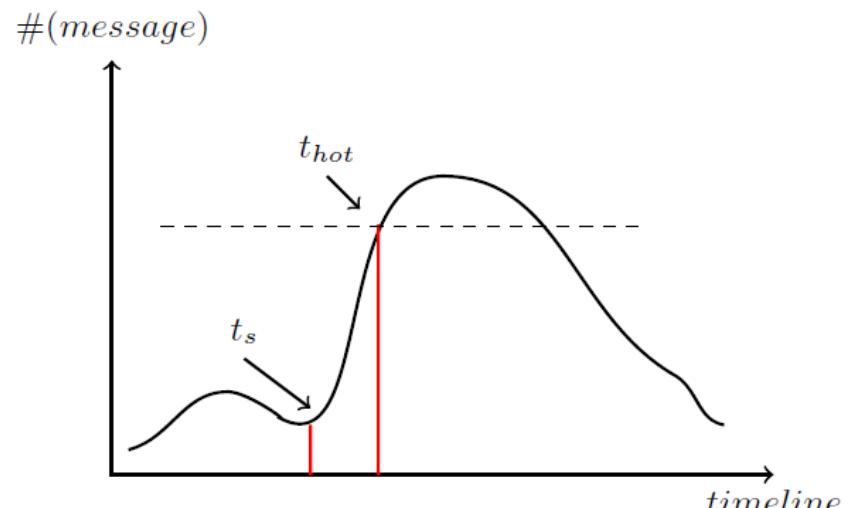
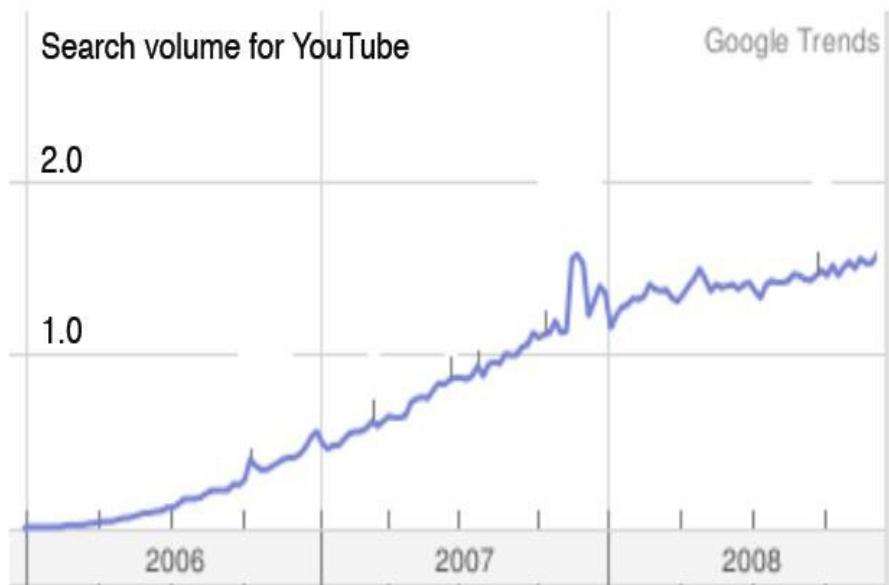
What Do We Learn? Cnt.

- Graph Representation



What Do We Learn? Cnt.

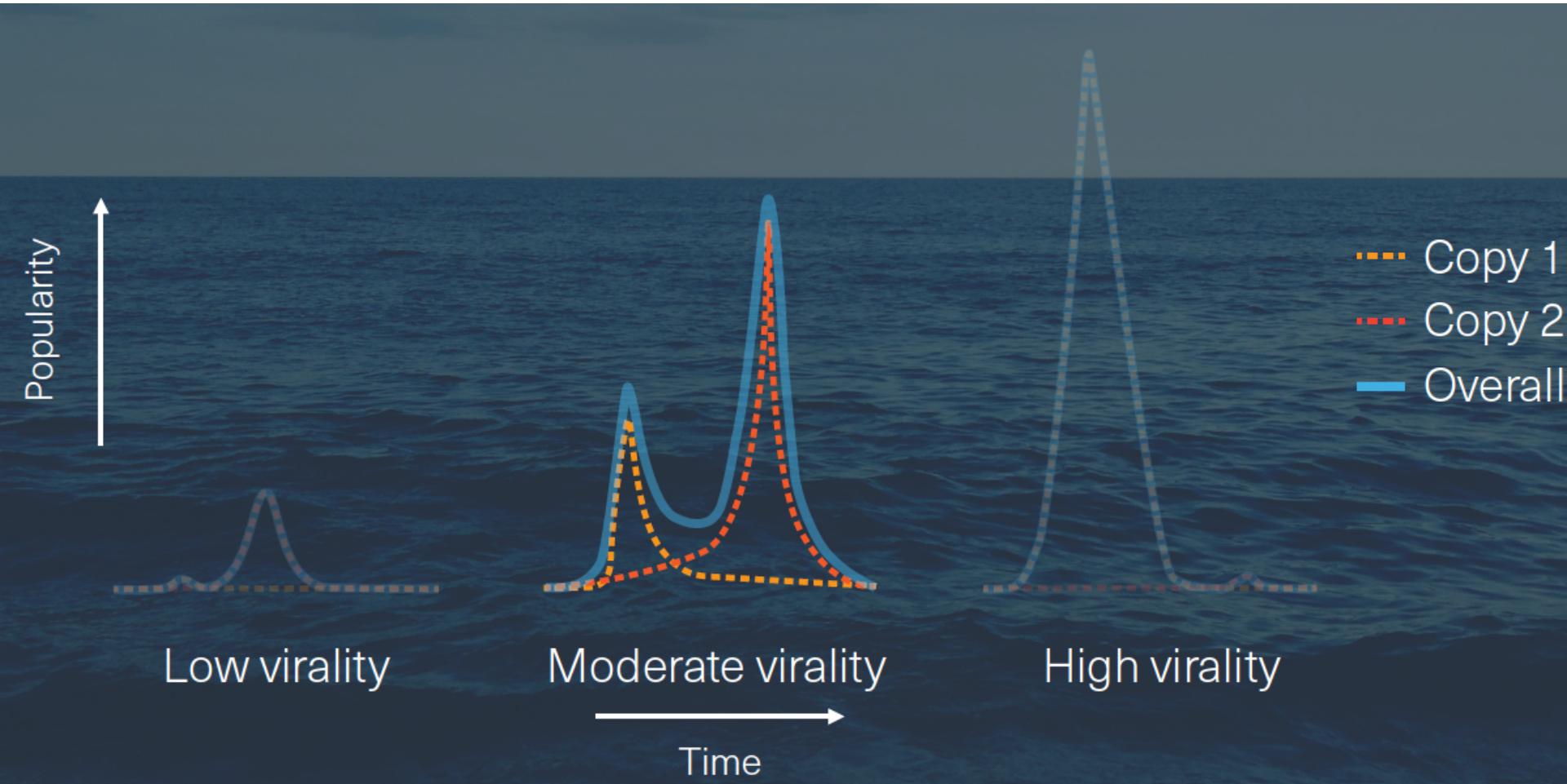
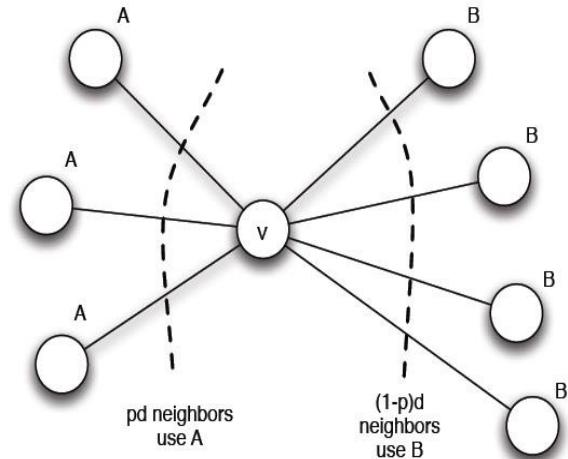
- Popularity prediction in networks



Is it that the rich always get richer? new ideas always get attention and become viral?

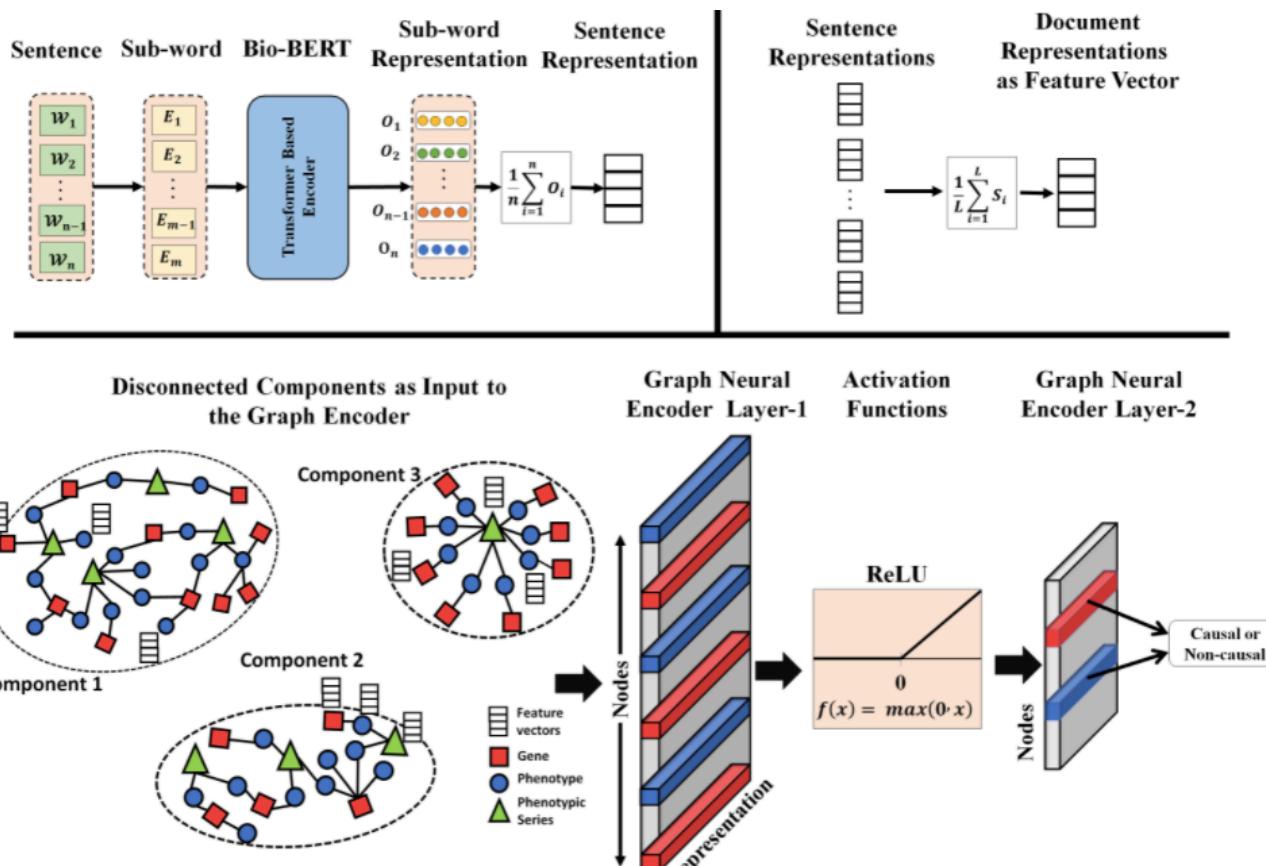
What Do We Learn? Cnt.

- Cascade Prediction



What Do We Learn? Cnt.

- Link Prediction
 - How can we predict links in networks?

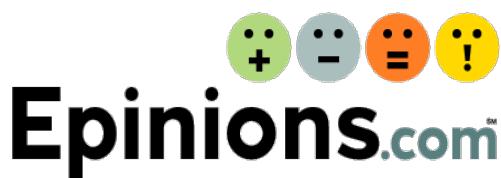


What Do We Learn? Cnt.

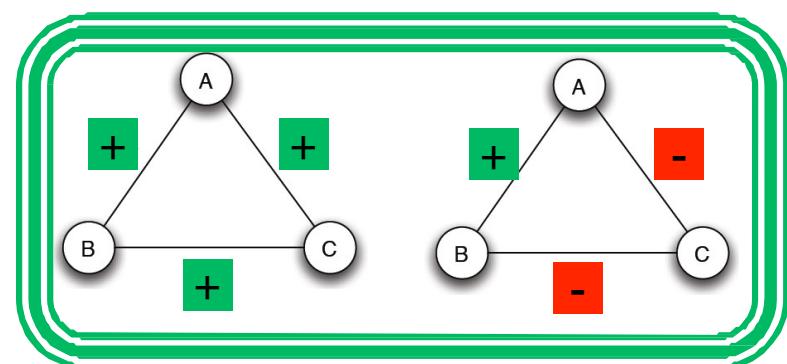
- Link Prediction
 - Take a network and annotate its links with
 - + sign representing friendship, and
 - - sign representing antagonism
 - How should we reason about such networks?
 - Say to understand the *tension* between these two forces!



Support / Oppose
relations



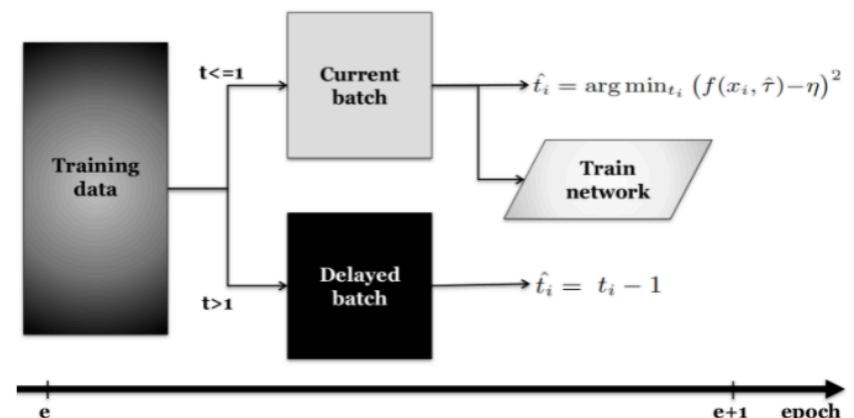
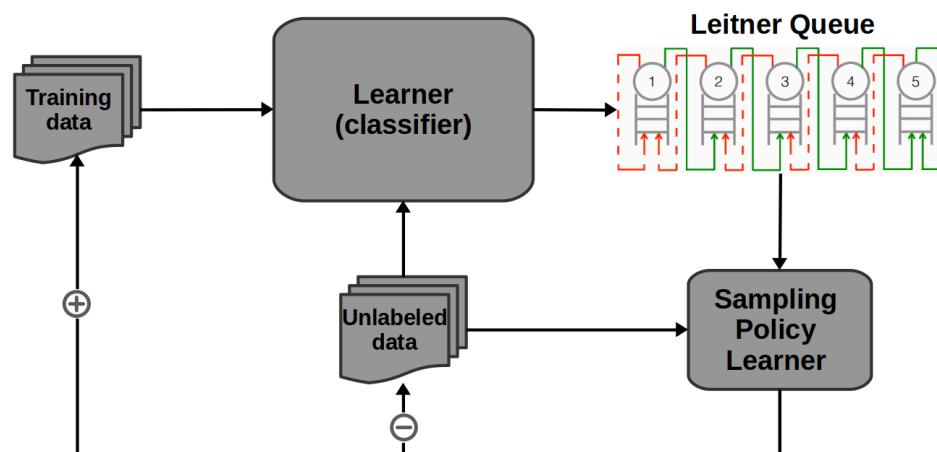
Trust / Distrust
relations



Balanced

What Do We Learn? Cnt.

- Meta Learning
 - Spaced repetition for training
 - Spotting spurious data
 - Neural self-training



Meta Learning

- Meta Learning
 - Curriculum learning with graphs

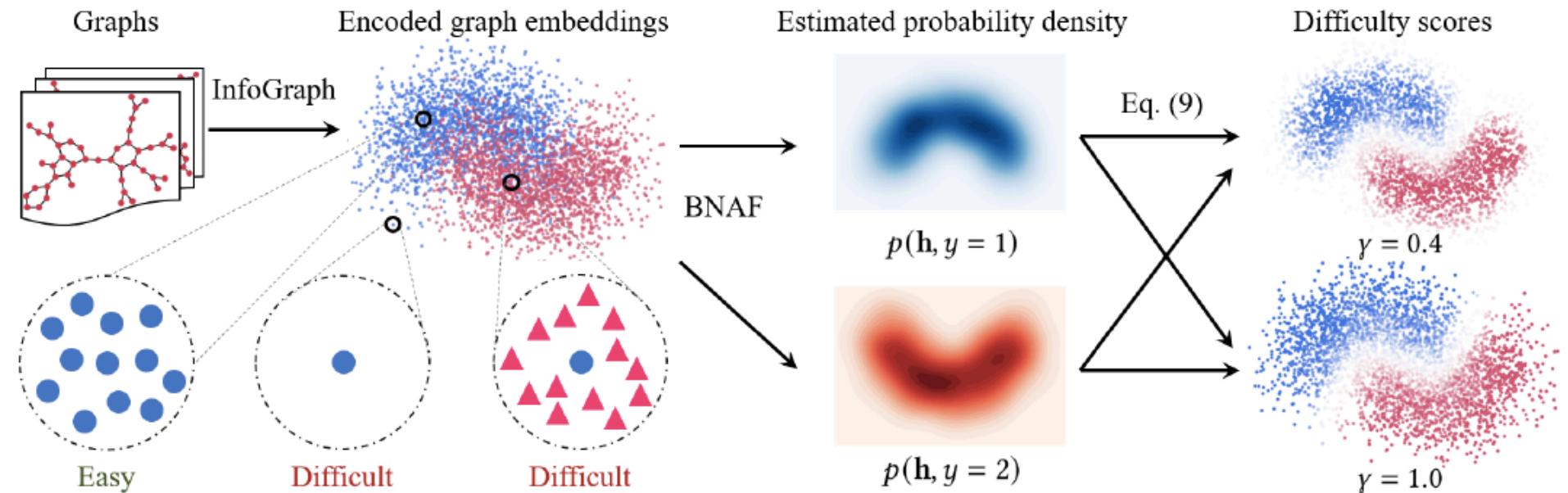


Figure 1: Infomax Curriculum Design. We use InfoGraph [49] to obtain graph representations, and BNAF [12] for density estimation. We calculate difficulty scores from intra-class and inter-class densities of Graph Embeddings (by Eq. (9)). Levels of transparency are positively related to difficulty scores. $\gamma = 0.4$ assigns higher difficulty values to outliers than $\gamma = 1.0$.

What Do We Learn? Cnt.

Time permitting

- Applications (*mainly given guest lectures*)
 - Health Informatics
 - Search and Factuality
 - Topic Detection and Tracking



Language query: a girl in orange first walks by the camera.

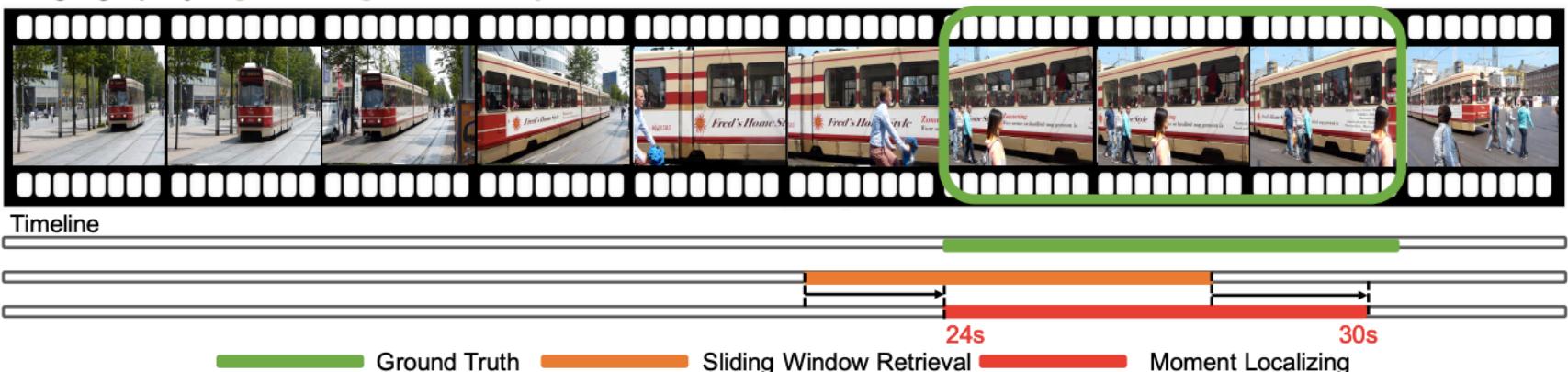
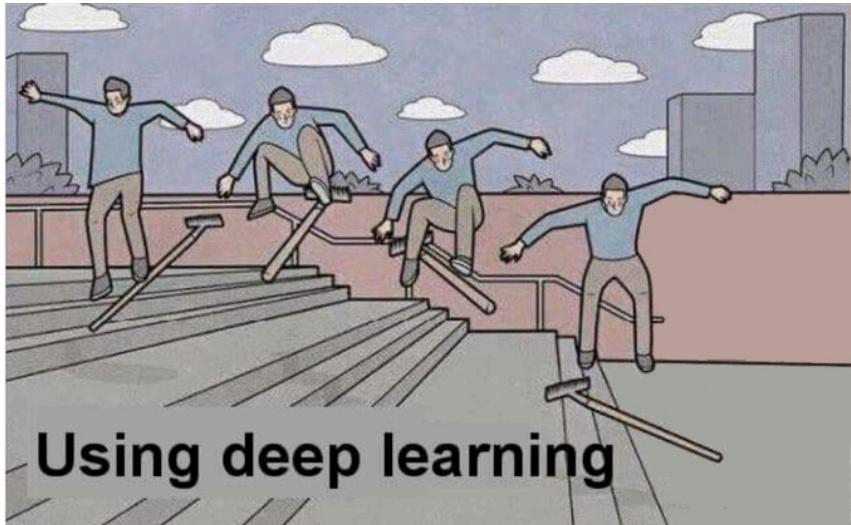
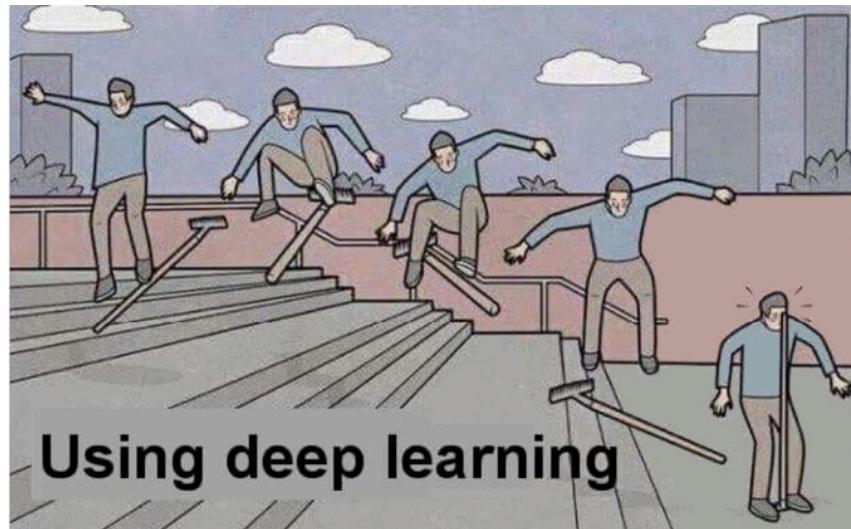


Figure 1: Temporal video moment localization is designed to localize a moment (the red bar) with a start point (24th s) and an end point (30th s) in the video according to the given language query. Here the green bar denotes the ground truth, the orange bar stands for the result of sliding window moment retrieval, and the red bar refers to the localizing result.





Reading

- Ch.01 Introduction [GRL]
- Ch.01 Overview [NCM]