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کنترل اتوماتیک خطی

امیررضا فرزین جید

$$x_1(s) = G_s R(s) - H_1(s) - H_r x_r(s) - 1$$

$$x_r(s) = G_1 x_1(s)$$

$$x_r(s) = G_r x_r(s) + D(s)$$

$$C(s) = G_r x_r(s)$$

معادله کلی  
C(s) →

$$x_r(s) = G_r G_1 x_1(s) + D(s)$$

$$x_r(s) = G_r G_1 (G_s R(s) - H_1(s) - H_r x_r(s)) + D(s)$$

$$\rightarrow C(s) \rightarrow G_r x_r(s) = G_r (G_r G_1 G_s R(s) - G_r G_1 H_1(s) - G_r G_1 H_r x_r(s) + D(s))$$

$$x_r(s) = \frac{C(s)}{G_r}$$

⇓

$$\Rightarrow \frac{C(s)}{R(s)} = \frac{G_r G_1 G_s}{1 + G_r G_1 G_s H_1 + G_r G_1 H_r}$$

C(s)

$$1 + G_r G_1 G_s H_1 + G_r G_1 H_r$$

$$= G_r G_1 G_s R(s) + G_r (D(s))$$

$$\frac{C(s)}{D(s)} = \frac{G_r}{1 + G_r G_1 G_s H_1 + G_r G_1 H_r}$$



- ۱۲

$$x = [u, w, q, \theta]^T \quad U = \delta_e \quad y = [u + w, q - \theta]^T$$

$$\dot{x} = Ax + Bu \quad y = Cx + Du$$

→  $\mu u \Rightarrow u = a_{11}u + a_{12}w + a_{13}q + a_{14}\theta + b_1 \delta_e$

$$\dot{w} \Rightarrow a_{21}u + a_{22}w + a_{23}q + a_{24}\theta + b_2 \delta_e$$

$$\dot{q} = a_{31}u + a_{32}w + a_{33}q + a_{34}\theta + b_3 \delta_e$$

$$\dot{\theta} = 0x u + 0x w + 1x q + 0x \theta + 0x \delta_e$$

ماتریس A =

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

ماتریس B =

$$\begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ 0 \end{bmatrix}$$

برای خروجی  $\theta$

$$C = [0 \ 0 \ 0 \ 1]$$

$$D = 0$$



(٣- الف)

$$q_c(s) = \frac{K_1}{s} (q_c(s) - K_f f(s))$$

$$\delta E(s) = \frac{1}{s+1} f_c(s)$$

$$f(s) = \frac{-K_A(1+STA)}{s^2 + 2\xi_{sp}\omega_{sp}s + \omega_{sp}^2} \delta E(s)$$

$$q_c(s) = \frac{-K_A(1+STA)K_1}{s(s+1)(s^2 + 2\xi_{sp}\omega_{sp}s + \omega_{sp}^2 + K_A(1+STA)K_fK_1)} q$$

(١)

$$s(s+1)(s^2 + 2\xi_{sp}\omega_{sp}s + \omega_{sp}^2) + K_A(1+STA)K_fK_1 = 0$$

$$\begin{aligned} \frac{d f q}{d t} + 1 + 2\xi_{sp}\omega_{sp} \frac{d^2 q}{d t^2} + (\omega_{sp}^2 + 2\xi_{sp}\omega_{sp}) \frac{d^3 q}{d t^3} + 1 \cdot \omega_{sp}^2 \frac{d^4 q}{d t^4} + K_A K_f \frac{d q}{d t} &= -K_A K_1 \\ &FC(4) \end{aligned}$$

$$\dot{x} = Ax + Bu \quad y = Cx$$

$$\dot{x}_1 = x_2 \quad \dot{x}_2 = x_3$$

$$\dot{x}_3 = x_4$$

$$\dot{x}_4 = a_1 x_4 - a_2 x_3 - a_3 x_2 + b_1 y(t)$$

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & -a_1 & -a_2 & -a_3 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 \\ 0 \\ 0 \\ b_1 \end{bmatrix}$$

$$C = [1 \ 0 \ 0 \ 0]$$

$$D = 0$$



بواسطی

$$\ddot{y} - y'' + 2y + 4y = 2\ddot{u} + 4\ddot{v} - 4 + 3u$$

$$y = x_1 \quad y' = x_2$$

$$x_1' = x_2 \quad x_2' = -2x_1 - 2x_2 + 2\ddot{u} + 4\ddot{v} - 4 + 3u$$

$$+ 4\ddot{v} - 4 + 3u$$

$$A = \begin{pmatrix} 0 & 1 \\ -2 & -2 \end{pmatrix}$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 2 & 4 & -1 & 3 \end{bmatrix}$$

$$C = [1 \ 0]$$

$$D = 0$$