



TEXAS A&M UNIVERSITY

Engineering

# Autonomous Trolley Localization

Amir Darwesh, Jacob Hartzer, Subodh Misra, and Keith Sponsler

MEEN 689: Robotic Perception - 22 April 2020

# Outline

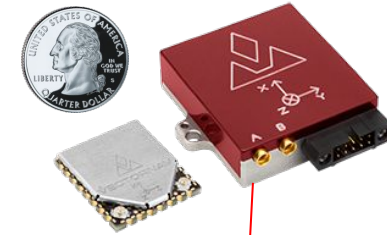


- Introduction
- Theory
- Data Collection
- Data Analysis
- Conclusions

# Introduction

## System

- Drive-by-wire 6 passenger Golf Cart
- Sensors include:
  - Vectornav Navigation System (VN300)
    - Raw GPS - 5 Hz
    - Raw Accelerometer/Gyro (IMU) - 50 Hz
    - **Fused Solution (INS) (50 Hz)**
  - PacMOD drive-by-wire module
    - Steering Wheel Angle - 30 Hz
    - Wheel Velocity - 30 Hz



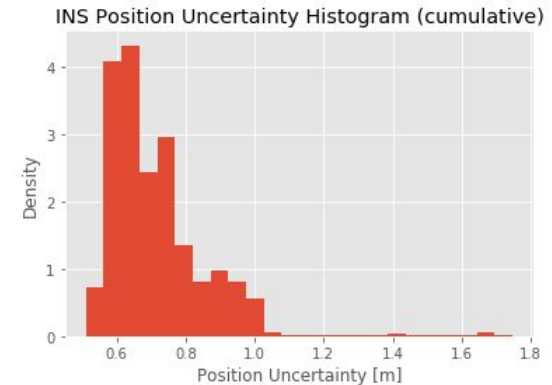
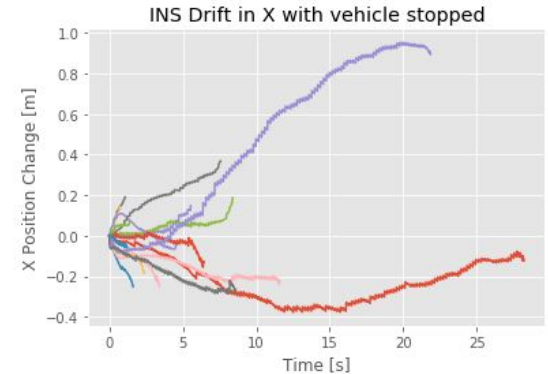
# Introduction

## Problem Statement

- Current localization methods are limited to the **INS** solution uncertainty (**0.2-1.5 m**)
- **INS** solution accuracy is very susceptible to atmospheric conditions, trees, buildings, and overpasses.
- **INS** solutions can “jump”, particularly while at rest, and can cause improper control actions.

## Objective

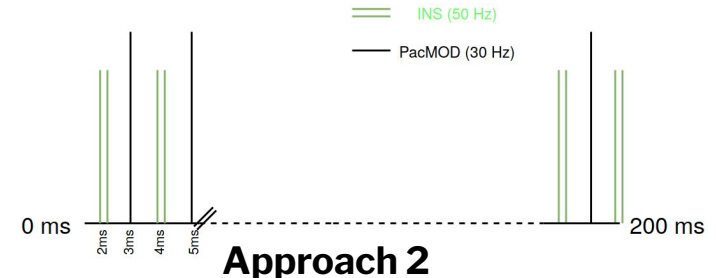
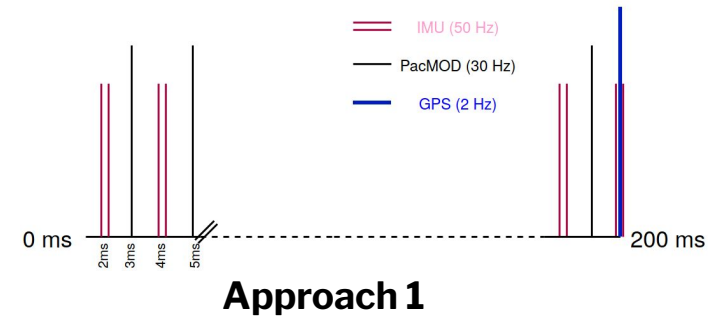
Combine Vectornav measurements with a physics based vehicle model to avoid these susceptibilities.



## Approach

- Two different approaches are taken
  - Combine **raw** IMU, Gyro, GPS measurements with the vehicle model based on PacMOD measurements
  - Combine manufacturer fused (IMU, Gyro, GPS) **INS** measurements with the vehicle model based on PacMOD measurements
- Robotic Operating System (ROS) & Python for real time implementation
- MATLAB for 3D version

## Measurement Update Cycle



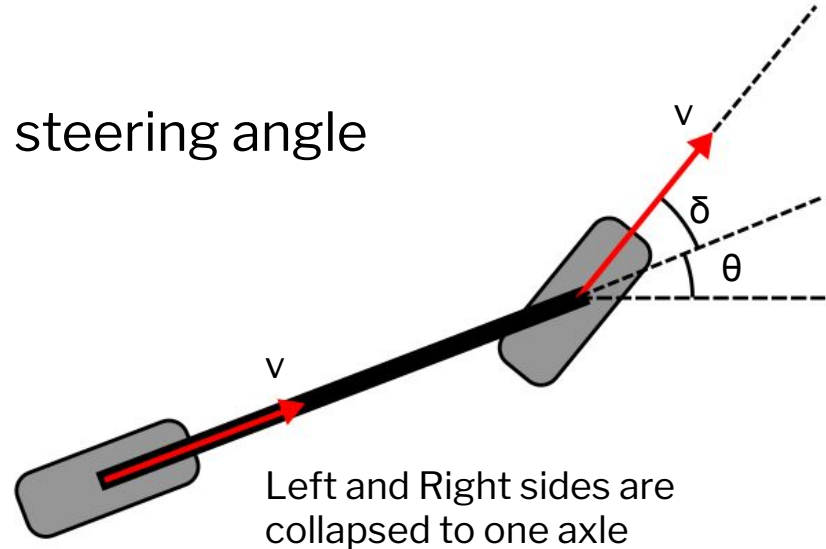
# Theory - Kinematic “Bicycle” Model

- Simplifies full vehicle
- Ignores slip and dynamics
- Depends only on velocity and steering angle

$$\dot{x}_r = v \cos \theta$$

$$\dot{y}_r = v \sin \theta$$

$$\dot{\theta} = \frac{v}{L} \tan \delta$$



# Theory - Kalman Filter

- Also known as Linear Quadratic Estimation (LQE)
- A two-step, recursive, real-time algorithm
- Equals the MAP in linear systems
- Assumes errors are Gaussian

State:

$$\mathbf{x} = \begin{bmatrix} x \text{ position } p_x \\ y \text{ position } p_y \\ \text{heading } \theta \\ x \text{ velocity } v_x \\ y \text{ velocity } v_y \\ \text{heading rate } \dot{\theta} \end{bmatrix}$$

Prediction Step:

$$\begin{aligned} \hat{\mathbf{x}}_{k|k-1} &= \mathbf{F}_k \hat{\mathbf{x}}_{k-1|k-1} + \mathbf{B}_k \mathbf{u}_k \\ \mathbf{P}_{k|k-1} &= \mathbf{F}_k \mathbf{P}_{k-1|k-1} \mathbf{F}_k^T + \mathbf{Q}_k \end{aligned}$$

Measurement Step:

$$\begin{aligned} \tilde{\mathbf{y}}_k &= \mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_{k|k-1} \\ \mathbf{S}_k &= \mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^T + \mathbf{R}_k \\ \mathbf{K}_k &= \mathbf{P}_{k|k-1} \mathbf{H}_k^T \mathbf{S}_k^{-1} \\ \hat{\mathbf{x}}_{k|k} &= \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k \tilde{\mathbf{y}}_k \\ \mathbf{P}_{k|k} &= (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_{k|k-1} \end{aligned}$$

- Nonlinear systems can be linearized about current state
- More computationally expensive
- Extends to most dynamic systems

Prediction Step:

$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{f}(\hat{\mathbf{x}}_{k-1|k-1}, \mathbf{u}_k)$$

$$\mathbf{P}_{k|k-1} = \mathbf{F}_k \mathbf{P}_{k-1|k-1} \mathbf{F}_k^T + \mathbf{Q}_k$$

$$\mathbf{F}_k = \left. \frac{\partial \mathbf{f}}{\partial \mathbf{x}} \right|_{\hat{\mathbf{x}}_{k-1|k-1}, \mathbf{u}_k}$$

$$\mathbf{H}_k = \left. \frac{\partial \mathbf{h}}{\partial \mathbf{x}} \right|_{\hat{\mathbf{x}}_{k-1|k-1}}$$

Measurement Step:

$$\tilde{\mathbf{y}}_k = \mathbf{z}_k - \mathbf{h}(\hat{\mathbf{x}}_{k|k-1})$$

$$\mathbf{S}_k = \mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^T + \mathbf{R}_k$$

$$\mathbf{K}_k = \mathbf{P}_{k|k-1} \mathbf{H}_k^T \mathbf{S}_k^{-1}$$

$$\hat{\mathbf{x}}_{k|k} = \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k \tilde{\mathbf{y}}_k$$

$$\mathbf{P}_{k|k} = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_{k|k-1}$$



Accelerometer  
calibration model:

$$A = \begin{bmatrix} 1 & M_{XY} & M_{XZ} \\ M_{YX} & 1 & M_{YZ} \\ M_{ZX} & M_{ZY} & 1 \end{bmatrix} \begin{bmatrix} \frac{1}{S_X} & 0 & 0 \\ 0 & \frac{1}{S_X} & 0 \\ 0 & 0 & \frac{1}{S_X} \end{bmatrix} \left( \begin{bmatrix} B_X \\ B_Y \\ B_Z \end{bmatrix} + \begin{bmatrix} V_X \\ V_Y \\ V_Z \end{bmatrix} \right)$$

Gyroscope  
calibration model:

$$\omega = \begin{bmatrix} 1 & M_{XY} & M_{XZ} \\ M_{YX} & 1 & M_{YZ} \\ M_{ZX} & M_{ZY} & 1 \end{bmatrix} \begin{bmatrix} \frac{1}{S_X} & 0 & 0 \\ 0 & \frac{1}{S_X} & 0 \\ 0 & 0 & \frac{1}{S_X} \end{bmatrix} \left( \begin{bmatrix} B_X \\ B_Y \\ B_Z \end{bmatrix} + \begin{bmatrix} V_X \\ V_Y \\ V_Z \end{bmatrix} + \begin{bmatrix} H_{XX} & H_{XY} & H_{XZ} \\ H_{YX} & H_{YY} & H_{YZ} \\ H_{ZX} & H_{ZY} & H_{ZZ} \end{bmatrix} \begin{bmatrix} a_x \\ a_y \\ a_z \end{bmatrix} \right)$$

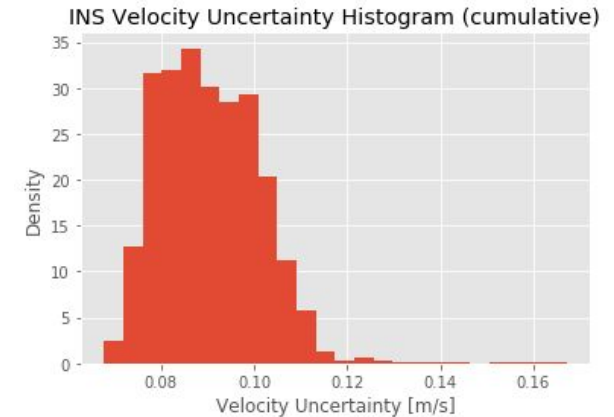
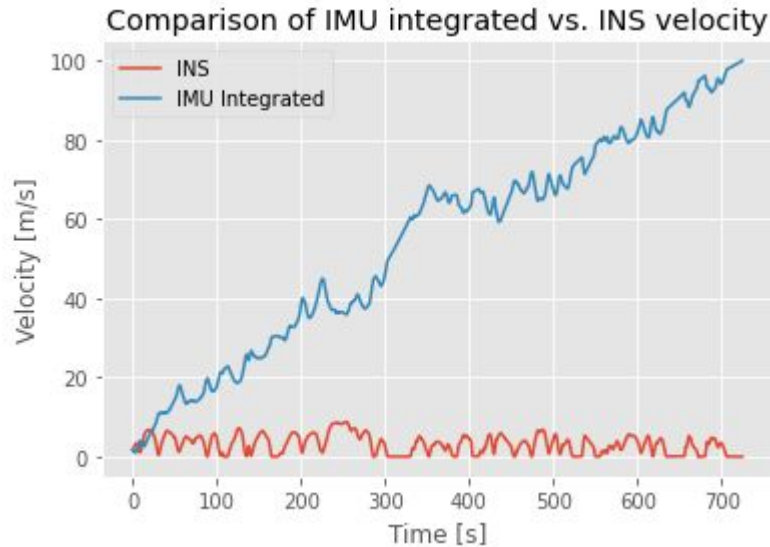
Assume the system is properly calibrated, just misaligned

- Removes scaling factors
- Orthogonal misalignment matrix

$$A = \begin{bmatrix} 1 & M_{XY} & M_{ZX} \\ M_{XY} & 1 & M_{YZ} \\ M_{ZX} & M_{YZ} & 1 \end{bmatrix} \left( \begin{bmatrix} B_X \\ B_Y \\ B_Z \end{bmatrix} + \begin{bmatrix} V_X \\ V_Y \\ V_Z \end{bmatrix} \right)$$

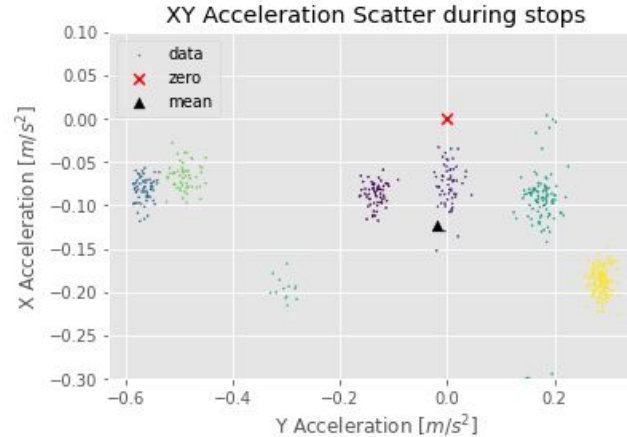
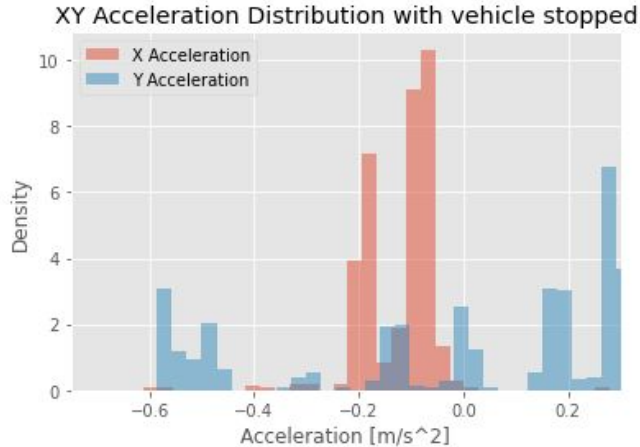
$$\omega = \begin{bmatrix} 1 & M_{XY} & M_{ZX} \\ M_{XY} & 1 & M_{YZ} \\ M_{ZX} & M_{YZ} & 1 \end{bmatrix} \left( \begin{bmatrix} B_X \\ B_Y \\ B_Z \end{bmatrix} + \begin{bmatrix} V_X \\ V_Y \\ V_Z \end{bmatrix} \right)$$

- Integrating for velocity drifts due to misalignment and bias



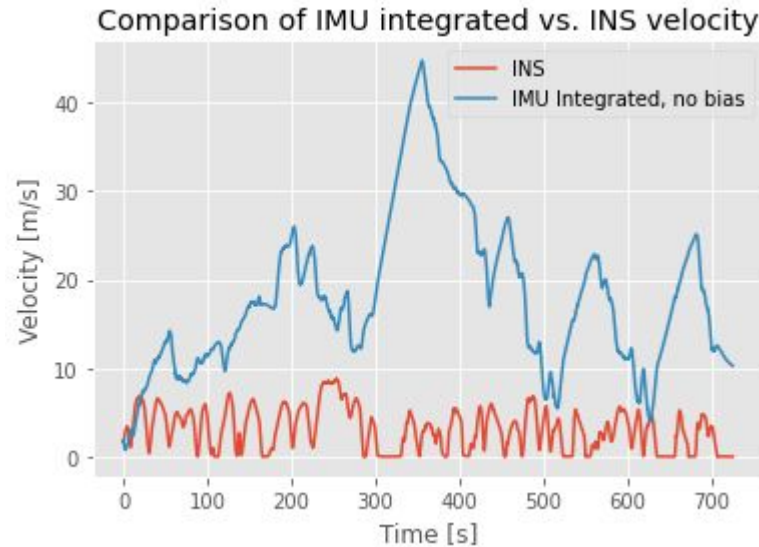
# Parameter Estimation - IMU Errors

- Biases are multimodal and dependent on road geometry
- This is very difficult to measure



MEAN  
x:  $-0.122 \text{ m/s}^2$   
y:  $-0.02 \text{ m/s}^2$

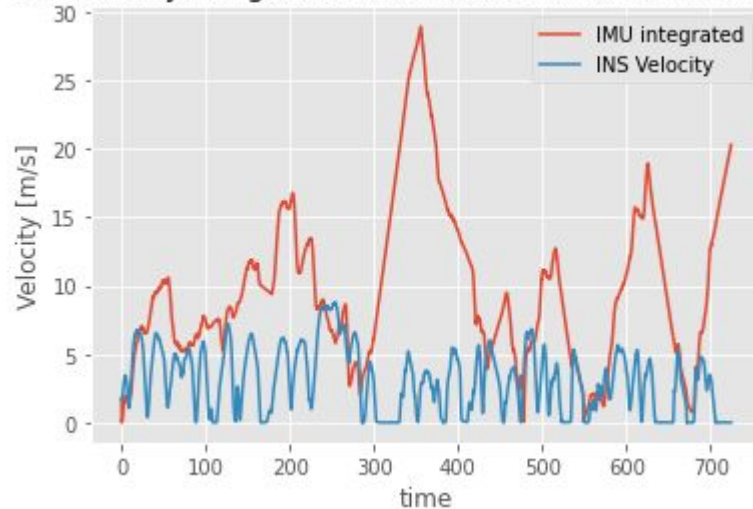
## Removing average bias does improve integration



# Parameter Estimation - IMU Errors

- Least Squares to minimize the velocity error

IMU Velocity integrated with bias and scale factor removal



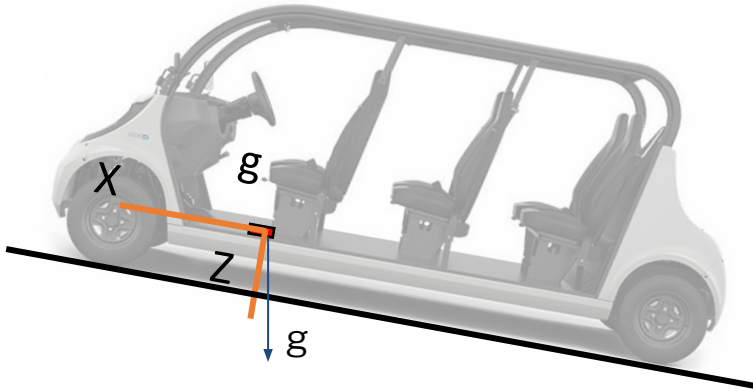
$$\begin{bmatrix} 0.9107 & 0.084 & -0.0053 \\ -0.0356 & 0.900 & -0.0016 \\ 0.0265 & -0.0435 & 0.9818 \end{bmatrix} \begin{bmatrix} V_X + 0.056 \\ V_Y + 0.1009 \\ V_Z - 0.200 \end{bmatrix}$$

# Parameter Estimation - Biases Example



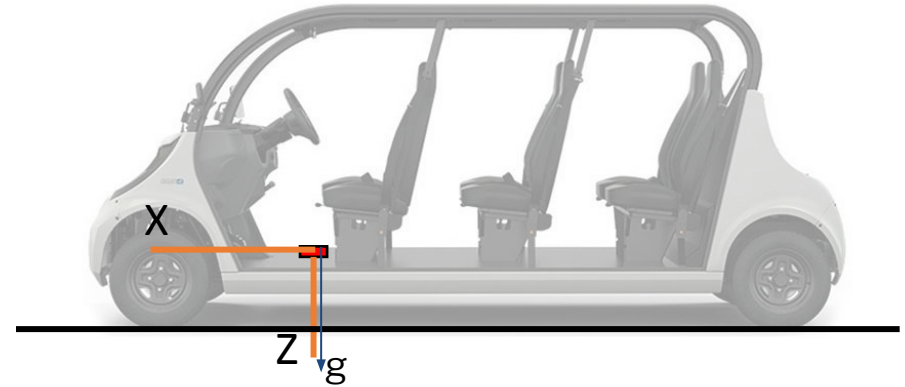
**EX:**

Golf Cart is pitched, gravity has components in X, Z



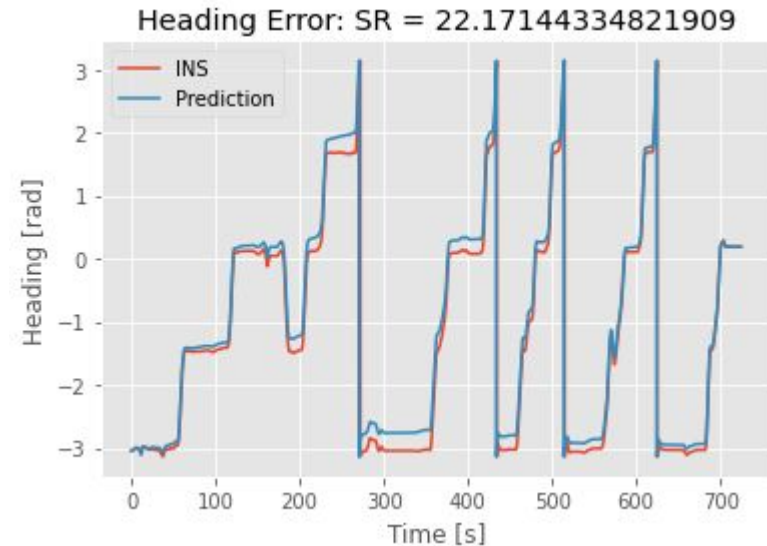
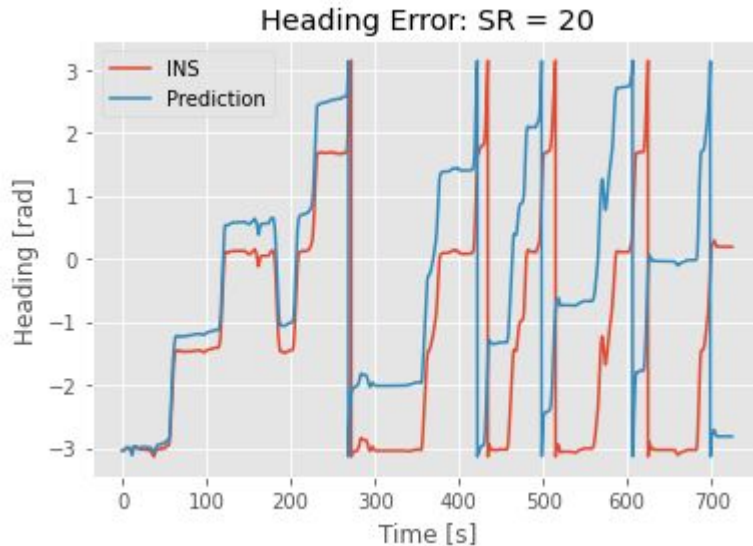
**EX:**

Golf Cart isn't pitched, gravity is entirely in Z axis



# Parameter Estimation - Steering Ratio

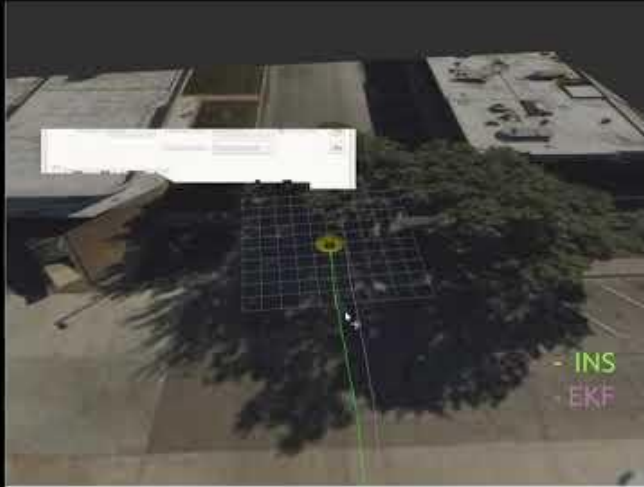
- Calibration of Steering Ratio
- Integrated Kinematic Bicycle Model vs INS
- Minimized final heading error



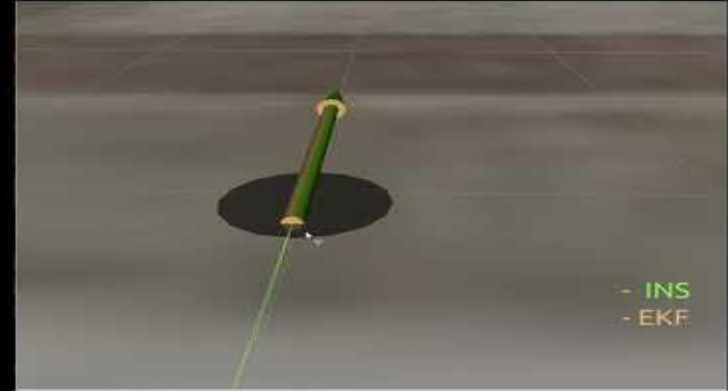


# Real Time Implementation

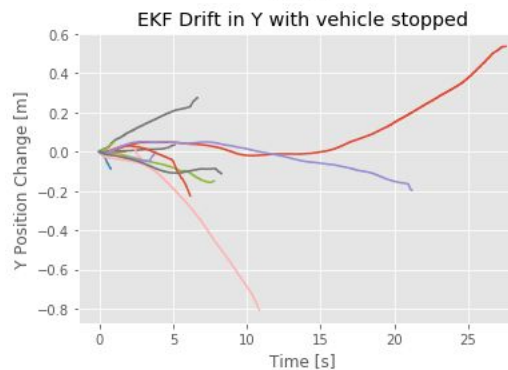
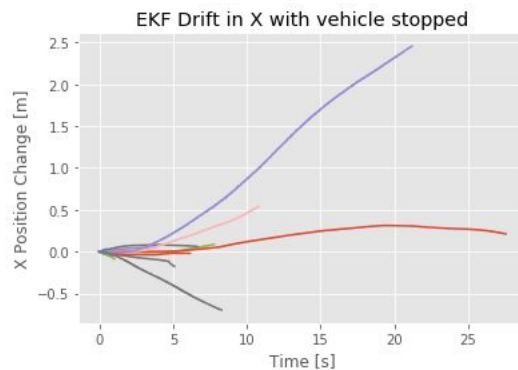
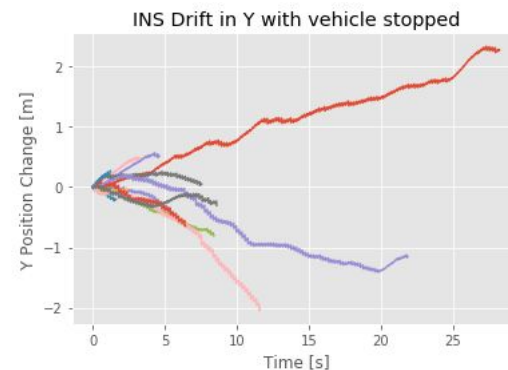
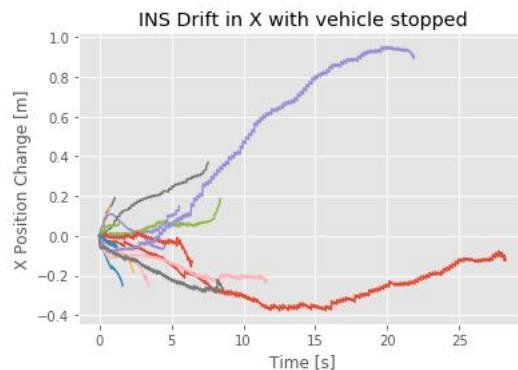
PacMOD + **(processed)** GPS, IMU



PacMOD + **INS**



# EKF results



## Accelerometer data

$$u_k = [a_{x_k}^b, a_{y_k}^b, a_{z_k}^b, p_k, q_k, r_k]^T$$

Transform acceleration to world frame and offset gravity

$$a^{NED} = R_z R_y R_z \begin{bmatrix} a_{x_k}^b \\ a_{y_k}^b \\ a_{z_k}^b \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ g \end{bmatrix}$$

Convert body rates to euler angle rates

$$\begin{bmatrix} \dot{\phi}_k \\ \dot{\theta}_k \\ \dot{\psi}_k \end{bmatrix} = \begin{bmatrix} \cos\theta_k \cos\psi_k & -\sin\psi_k & 0 \\ \cos\theta_k \sin\psi_k & \cos\psi_k & 0 \\ -\sin\theta_k & 0 & 1 \end{bmatrix}^{-1} \begin{bmatrix} p_k \\ q_k \\ r_k \end{bmatrix}$$

# Prediction



$$\hat{x}_k = f(x_{k-1}, u_k) = \begin{bmatrix} x_{k-1} + dt \times v_{x_{k-1}} + 0.5 \times dt^2 \times a_{x_k}^{NED} \\ y_{k-1} + dt \times v_{y_{k-1}} + 0.5 \times dt^2 \times a_{y_k}^{NED} \\ z_{k-1} + dt \times v_{z_{k-1}} + 0.5 \times dt^2 \times a_{z_k}^{NED} \\ v_{x_{k-1}} + dt \times a_{x_k}^{NED} \\ v_{y_{k-1}} + dt \times a_{y_k}^{NED} \\ v_{z_{k-1}} + dt \times a_{z_k}^{NED} \\ \phi_{k-1} + dt \times \dot{\phi}_k \\ \theta_{k-1} + dt \times \dot{\theta}_k \\ \psi_{k-1} + dt \times \dot{\psi}_k \end{bmatrix}$$

$$\hat{P}_k = F_k P_k F_k^T + B_k Q_k B_k^T$$

$$F_k = \left. \frac{\partial f}{\partial x} \right|_{(\hat{x}_{k-1}, u_k)}$$

$$B_k = \left. \frac{\partial f}{\partial u} \right|_{(\hat{x}_{k-1}, u_k)}$$

**GPS+Orientation Measurement**

$$H_k = \begin{bmatrix} \mathbf{I}_{3 \times 3} & \mathbf{0}_{3 \times 6} \\ \mathbf{0}_{3 \times 6} & \mathbf{I}_{3 \times 3} \end{bmatrix}$$

**State Correction**

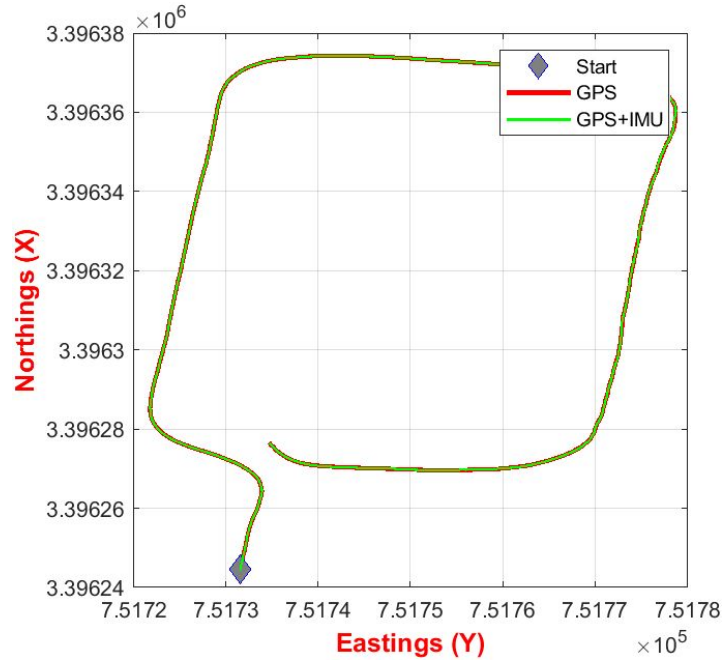
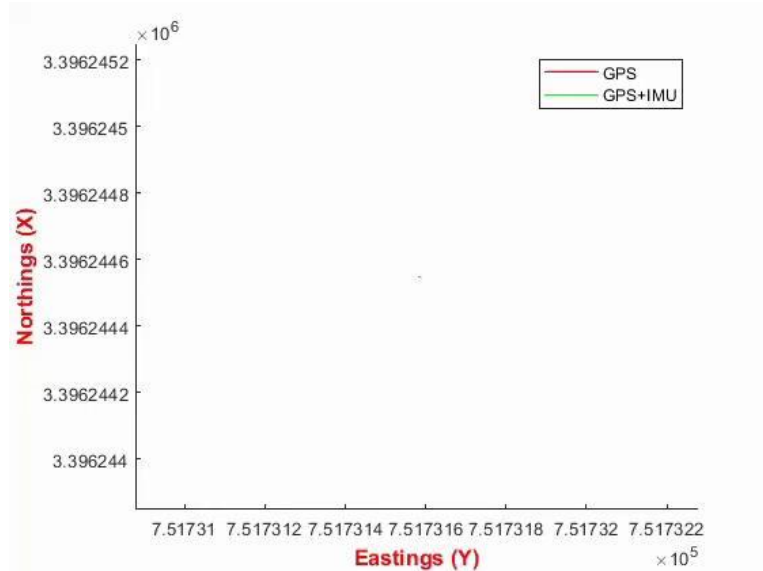
$$z_k = [x_k, y_k, z_k, \phi_k, \theta_k, \psi_k]^T$$

**Covariance Correction**

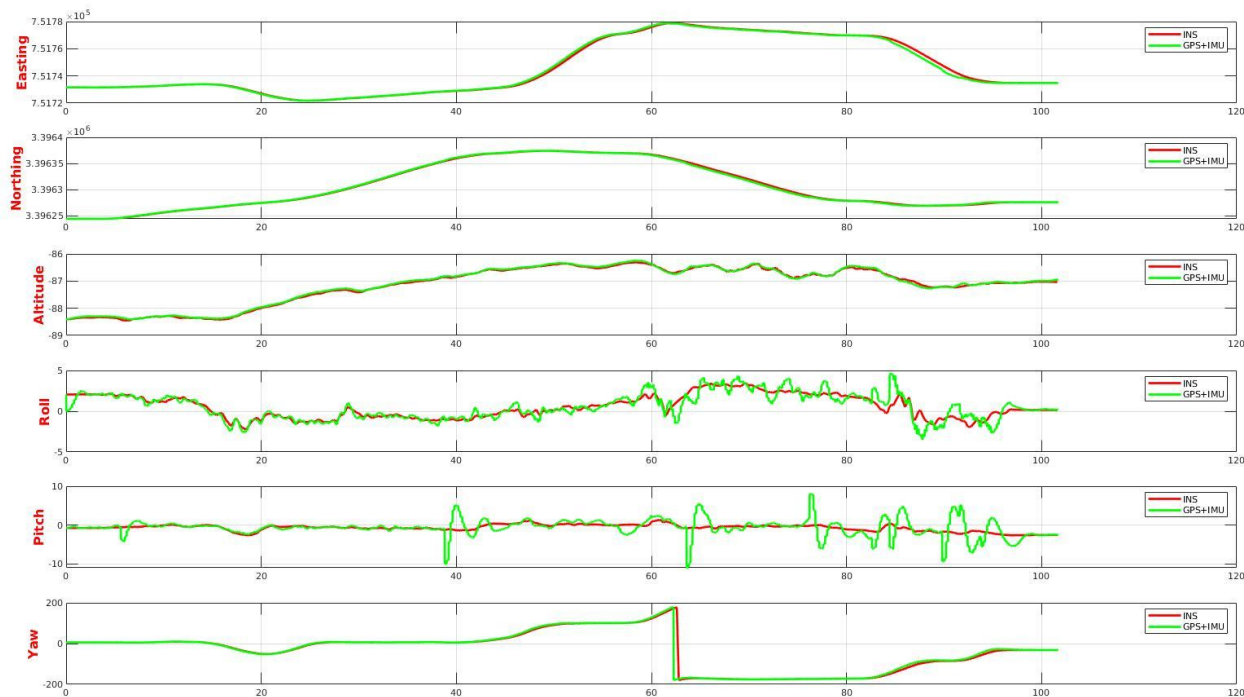
$$X_k = \hat{X}_k + K_k(z_k - H_k \hat{X}_k)$$

$$P_k = \hat{P}_k - K_k H_k \hat{P}_k$$

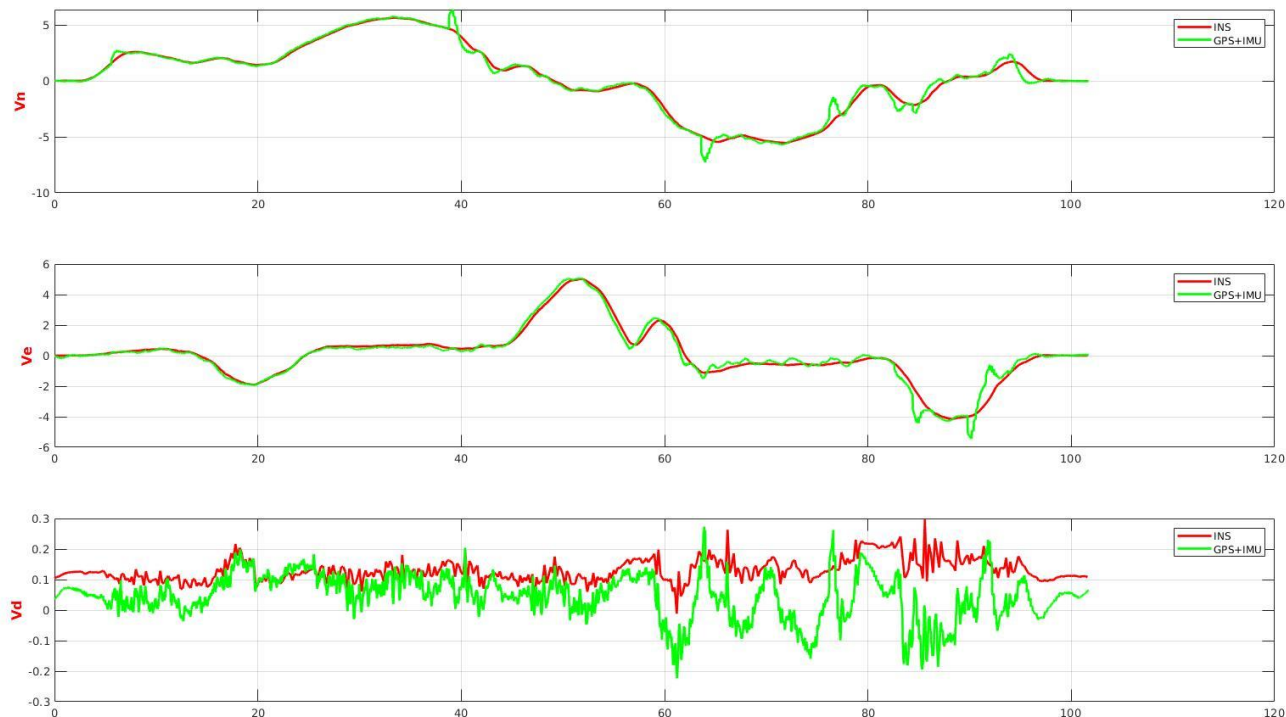
# 3D Results



# 3D Results

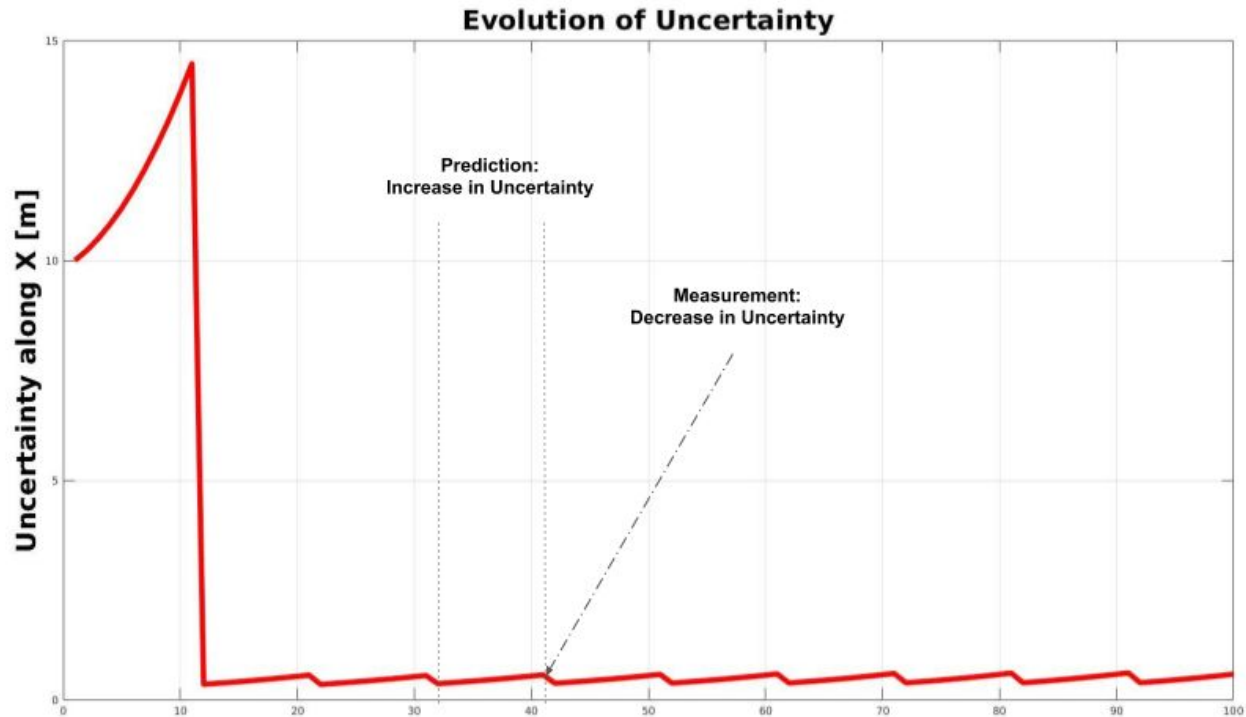


# 3D Results





# Evolution of State Uncertainty



# Conclusions



- Difficult to show accuracy improvements
- Would like to run more tests with filter running in real time
- Overall has lower covariance due to PACMod integration
- Able to filter in real time with golf cart data
- Smoother state estimate results
- Real time error estimation leads to filter instability

# References



- <https://www.vectornav.com/>
- <https://autonomoustuff.com/>
- [https://commons.wikimedia.org/wiki/File:Ros\\_logo.svg](https://commons.wikimedia.org/wiki/File:Ros_logo.svg)
- <https://tti.tamu.edu/news/self-driving-vehicles-begin-operating-in-downtown-bryan-texas/>
- Kalman, R.E. (1960). "A new approach to linear filtering and prediction problems" (PDF). *Journal of Basic Engineering*. 82 (1): 35–45.
- G.L. Smith; S.F. Schmidt and L.A. McGee (1962). "Application of statistical filter theory to the optimal estimation of position and velocity on board a circumlunar vehicle". National Aeronautics and Space Administration.



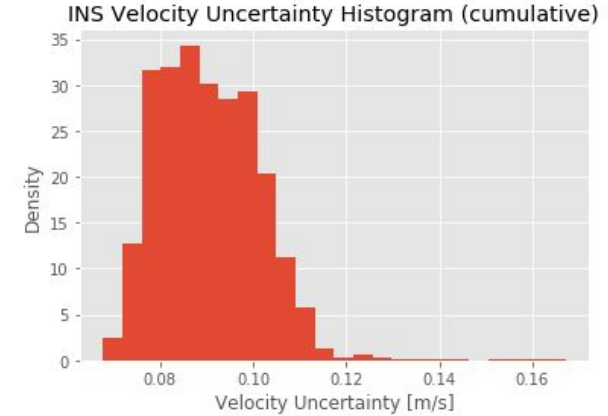
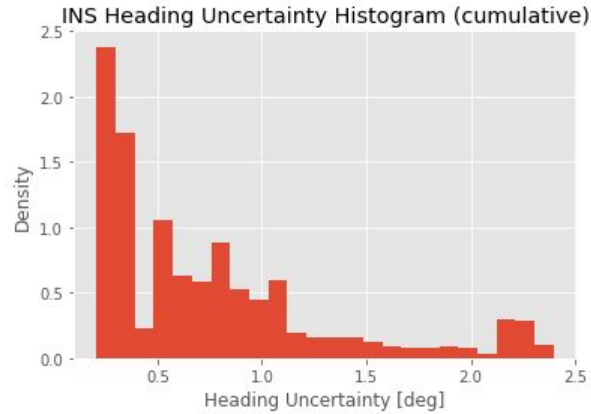
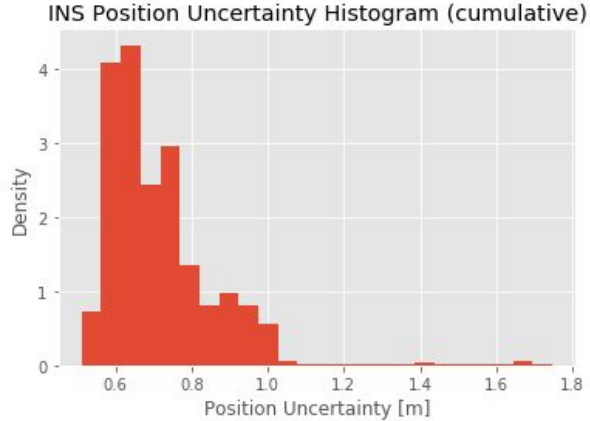
TEXAS A&M UNIVERSITY

Engineering

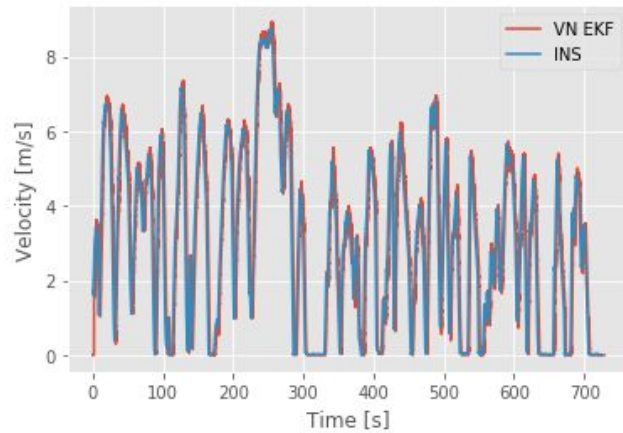
# Autonomous Trolley Localization

Thank you for your time

# Uncertainty Measurements



# vectornav EKF results



# Data Collection



TEXAS A&M UNIVERSITY  
Engineering

- Used Robot Operating System
- Robotics middleware
- Manages data messages between sources
- Can record and play back messages in real time



# Data Analysis - INS Drift

- Even without motion, the INS tends to drift position

