



Sharif University of Technology  
Department of Computer Engineering

# Low Power Digital System Design

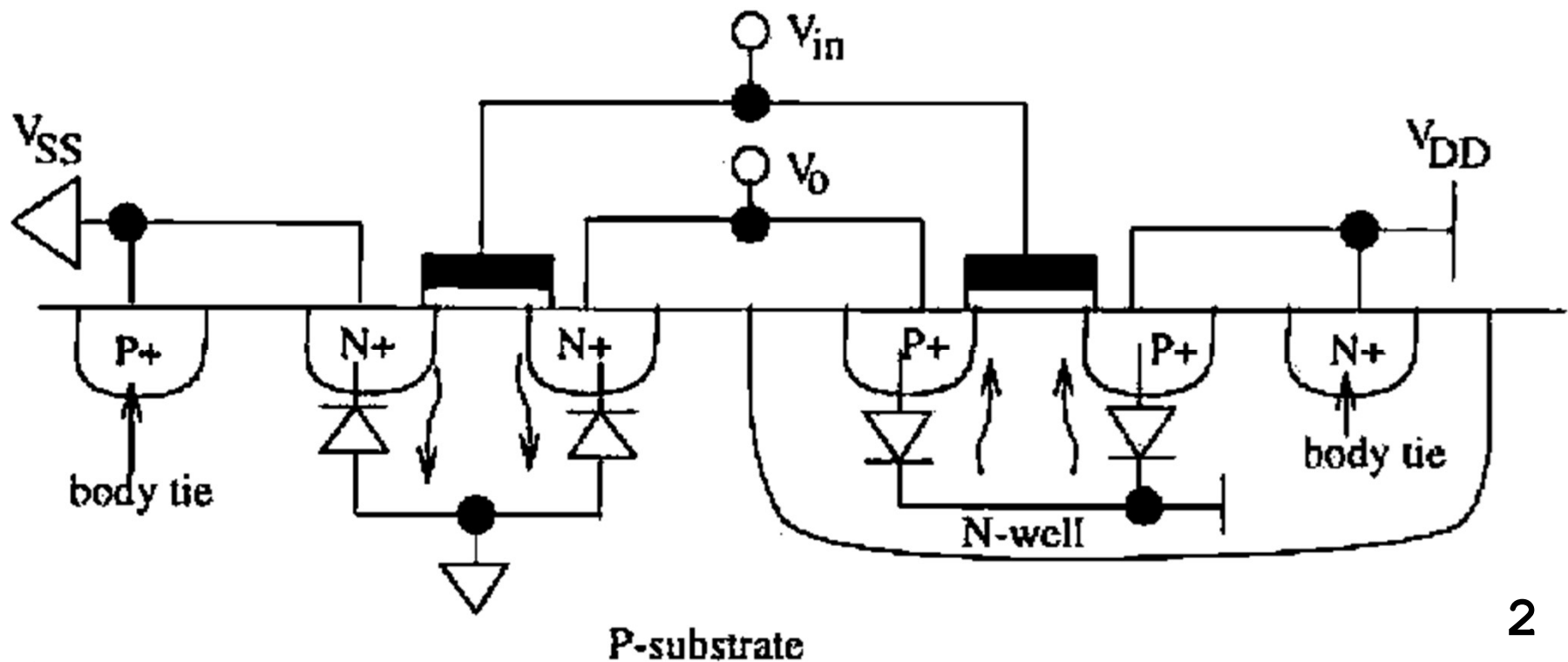
## Power Components (Cont.)

A. Ejlali

# Reverse Leakage Power

- The reverse leakage occurs when the parasitic diodes are reversely biased.

$$I_D = A \cdot J_S \left( e^{\frac{qV_{bias}}{KT}} - 1 \right)$$



## Reverse Leakage Power

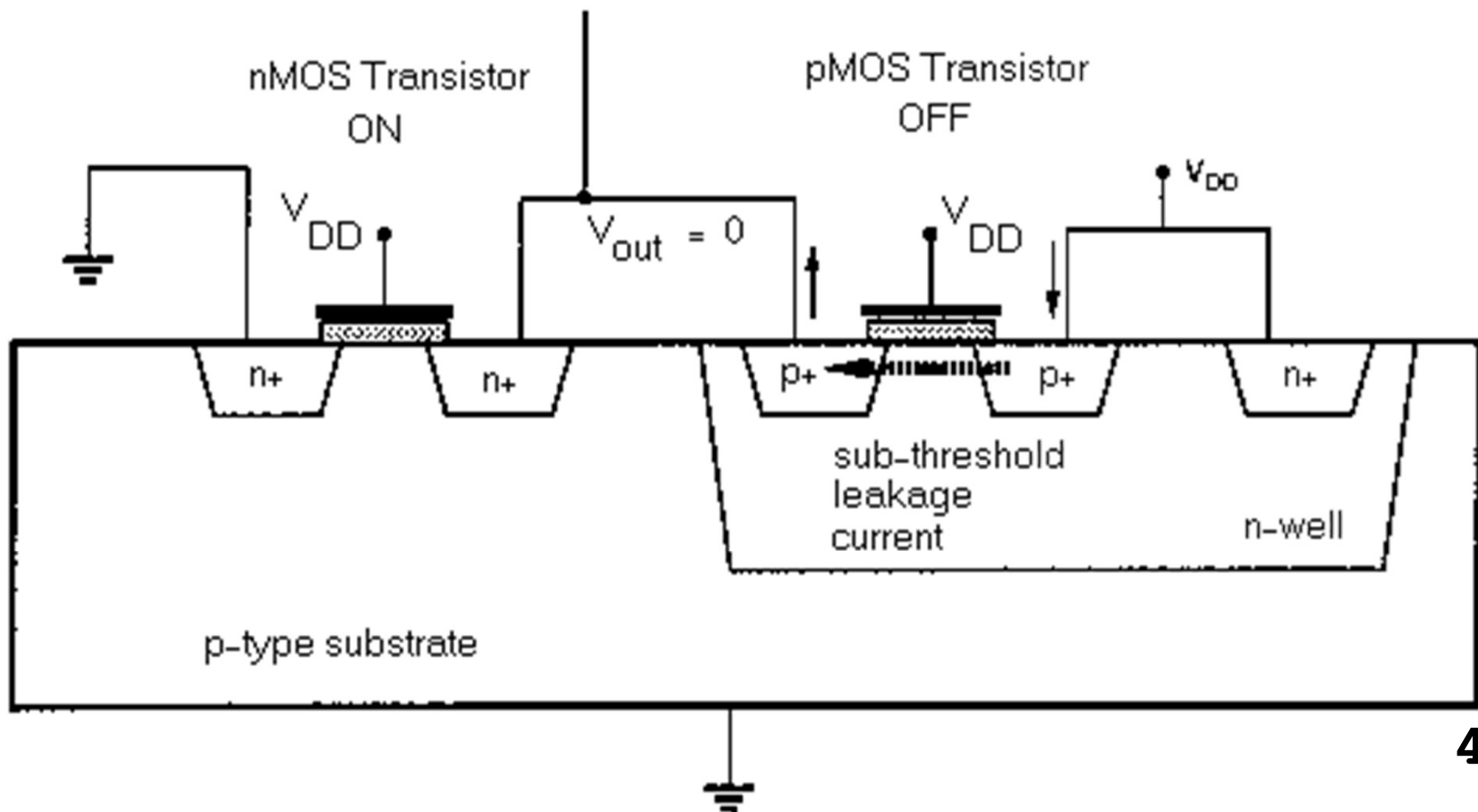
$$I_D = A \cdot J_S \left( e^{\frac{qV_{bias}}{KT}} - 1 \right)$$

- $A$  *Junction Area*
- $J_S$  Reverse saturation current density
- $q$  Electron's charge
- $K$  Boltzmann constant
- $T$  Temperature

$J_S$  increases quite significantly with temperature.

# Sub-threshold Leakage Power

- A MOS transistor in the sub-threshold region behaves similar to a bipolar device.



# Sub-threshold Leakage Power

$$I(\text{Sub-threshold}) = \beta(1 - \eta)V_T^2 \exp\left(\frac{V_{GS} - V_{th}}{\eta V_T}\right) \left[1 - \exp\left(-\frac{V_{DS}}{V_T}\right)\right]$$

where  $V_T = \frac{KT}{q}$

- Sub-threshold leakage power is the dominant static power component.
- Increasing almost 20 times for each new fabrication technology.

# Summary

$$P_{SW} = \alpha C_L V_{DD}^2 f$$

$$P_{SC} = \alpha \cdot \frac{\beta}{12} (V_{DD} - 2V_t)^3 \cdot t_{rf} \cdot f$$

$$P_{SUB} = V_{DD} \cdot \beta(1 - \eta)V_T^2 \exp\left(\frac{V_{GS} - V_{th}}{\eta V_T}\right) \left[1 - \exp\left(-\frac{V_{DS}}{V_T}\right)\right]$$

$$P_{Reverse} = V_{DD} \cdot A \cdot J_S$$

- In LPD, we consider the following factors:

Activity

Supply Voltage

Load Capacitance

Frequency

Rise time/fall time

Process Technology

Transistor size Threshold Voltage

Temperature

Scaling

Design Complexity

# Static Biasing Power

- Dissipated in non-CMOS families:
  - e.g., nMOS, Pseudo nMos, ...
- There are some circuits where static biasing can be beneficial in reducing the total power:
  - applicable for higher-frequency circuits.
- There is usually a large area savings as well.

