

Big O's

$O(1)$ Constant - no loops

$O(\log N)$ Logarithmic - usually searching algorithms have $\log n$ if they are sorted (Binary Search)

$O(n)$ Linear - for loops, while loops through n items

$O(n \log(n))$ Log Linear - usually sorting operations

$O(n^2)$ Quadratic - every element in a collection needs to be compared to every other element. Two nested loops

$O(2^n)$ Exponential - recursive algorithms that solve a problem of size N

$O(n!)$ Factorial - you are adding a loop for every element

Iterating through half a collection is still $O(n)$

Two separate collections: $O(a * b)$

Big O	Name	Description
1	Constant	statement, one line of code
$\log(n)$	Logarithmic	Divide and conquer (binary search)
n	Linear	Loop
$n * \log(n)$	Linearithmic	Effective sorting algorithms
n^2	Quadratic	Double loop
n^3	Cubic	Triple loop
2^n	Exponential	Complex full search

What Can Cause Time in a Function?

- Operations (+, -, *, /)
- Comparisons (<, >, ==)
- Looping (for, while)
- Outside Function call (function())

Sorting Algorithms

Sorting Algorithms	Space complexity	Time complexity	Time complexity
	Worst case	Best case	Worst case
Insertion Sort	$O(1)$	$O(n)$	$O(n^2)$
Selection Sort	$O(1)$	$O(n^2)$	$O(n^2)$
Bubble Sort	$O(1)$	$O(n)$	$O(n^2)$
Mergesort	$O(n)$	$O(n \log n)$	$O(n \log n)$
Quicksort	$O(\log n)$	$O(n \log n)$	$O(n^2)$
Heapsort	$O(1)$	$O(n \log n)$	$O(n \log n)$

Common Data Structure Operations

Worst Case→	Access	Search	Insertion	Deletion	Space Complexity
Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Stack	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Queue	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Singly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Doubly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Hash Table	N/A	$O(n)$	$O(n)$	$O(n)$	$O(n)$

Rule Book

Rule 1: Always worst Case

Rule 2: Remove Constants

Rule 3:

- Different inputs should have different variables: $O(a + b)$.
- A and B arrays nested would be: $O(a * b)$

+ for steps in order

* for nested steps

Rule 4: Drop Non-dominant terms

What Causes Space Complexity?

- Variables
- Data Structures
- Function Call
- Allocations