



Expected frequency and joint probability

Contingency table

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	200	60	260
Ginger	100	10	110
	300	70	370

Expected

	Cats	Dogs
Brown	$260 \times 300 / 370$	$260 \times 70 / 370$
Ginger	$110 \times 300 / 370$	$110 \times 70 / 370$

Contingency table

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	200	60	260
Ginger	100	10	110
	300	70	370

Expected

	Cats	Dogs
Brown	210.8	49.19
Ginger	89.19	20.81

Probability

Divide by number of observations

Observed			
	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Expected		
	Cats	Dogs
Brown	?	?
Ginger	?	?

Marginal Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed			Expected		
	Cats	Dogs		Cats	Dogs
Brown	0.541	0.162	0.703	?	?
Ginger	0.270	0.027	0.297	?	?
	0.811	0.189	370		

Marginals

- Probability that we take an animal from our population and it is a cat.
- Probability that we take an animal from our population and it is ginger.

Joint Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed			
	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

Expected		
	Cats	Dogs
Brown	?	?
Ginger	?	?

The **joint probability**, is the probability of two events occurring together.

- P(brown, cat)
- P(brown, dog)
- P(ginger, cat)
- P(ginger, dog)

Joint Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

Expected

	Cats	Dogs
Brown	?	?
Ginger	?	?

$$P(A \cap B) = P(A) \times P(B)$$

Joint Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

Expected

	Cats	Dogs
Brown	$p(\text{cat}) \times p(\text{Brown})$	$p(\text{dog}) \times p(\text{Brown})$
Ginger	$p(\text{cat}) \times p(\text{ginger})$	$p(\text{dog}) \times p(\text{ginger})$

$$P(A \cap B) = P(A) \times P(B)$$

Joint Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed		
	Cats	Dogs
Brown	0.541	0.162
Ginger	0.270	0.027
	0.811	0.189
		370

Expected		
	Cats	Dogs
Brown	0.811×0.703	0.189×0.703
Ginger	0.811×0.297	0.189×0.297

$$P(A \cap B) = P(A) \times P(B)$$

Joint Probability

$$E = (\text{Row x Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

Expected

	Cats	Dogs
Brown	0.570	0.133
Ginger	0.241	0.056

$$P(A \cap B) = P(A) \times P(B)$$

Joint Probability

$$E = (\text{Row} \times \text{Column}) / \text{Total}$$

Observed

	Cats	Dogs	
Brown	0.541	0.162	0.703
Ginger	0.270	0.027	0.297
	0.811	0.189	370

Expected

	Cats	Dogs
Brown	210.8	49.19
Ginger	89.19	20.81

Multiply by number of observations

$$P(A \cap B) = P(A) \times P(B)$$

THANK YOU

www.trainindata.com