

1. Basic Single-Path, Single Augmentation

Input Data: graph_data_1 = {
 's': {'a': {'capacity': 10, 'cost': 5}},
 'a': {'t': {'capacity': 10, 'cost': 2}}
}

Ans :: Max Flow: 10

Min Cost: $10 \times (5+2) = 70$

2. Capacity Bottleneck with Multiple Steps (Bottleneck Check)

```
graph_data_2 = {  
    's': {'a': {'capacity': 2, 'cost': 1}},  
    'a': {'b': {'capacity': 10, 'cost': 1}},  
    'b': {'t': {'capacity': 3, 'cost': 1}}  
}
```

Ans :: Total: Max Flow: 3, Min Cost: $6+3=9$

3. Prioritizing the Cheapest Path

Input Data:

```
graph_data_3 = {  
    's': {'a': {'capacity': 1, 'cost': 2}, 'b': {'capacity': 10, 'cost': 5}},  
    'a': {'t': {'capacity': 1, 'cost': 3}},  
    'b': {'t': {'capacity': 10, 'cost': 5}}  
}
```

Ans :: Total: Max Flow: 11, Min Cost: $(1 \times 5) + (10 \times 10) = 105$

4. Handling a Necessary Negative Cost Rerouting

Input Data:

```
graph_data_4 = {  
    's': {'a': {'capacity': 1, 'cost': 10}, 'b': {'capacity': 1, 'cost': 1}},  
    'a': {'t': {'capacity': 1, 'cost': 1}},  
    'b': {'a': {'capacity': 1, 'cost': -12}} # Negative cost edge!  
}
```

Ans :: Total: Max Flow: 1, Min Cost: -10 (A path can have negative net cost).

5. Checking for Unreachability

Input Data:

```
graph_data_5 = {  
    's': {'a': {'capacity': 1, 'cost': 5}, 'b': {'capacity': 10, 'cost': 1}},  
    'a': {'t': {'capacity': 1, 'cost': 5}}  
}
```

Ans :: Total: Max Flow: 1, Min Cost: 10