Outline

- Motivation
- word2vec
- Negative Sampling
- GloVe
- Applications

Word Embeddings

- It is useful to have numerical representations for words
  - Computers only really understand numbers
- Similar words should have similar numerical representations!
- A word will always have the same embedding no matter its context!

Word Embeddings

- It would not be great to have a single number for each word
  - The word ‘set’ has ~430 ways it can be used in English!
- Each word should thus be represented by an array of numbers
  - Hopefully, each possible use of a word is captured in this array, somehow
- Let’s assume each word is represented with an array of 300 numbers

Word Embeddings

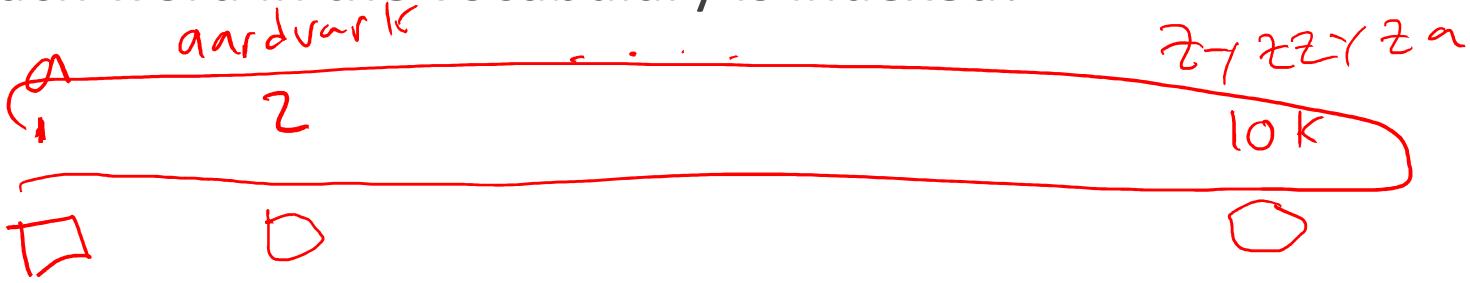
- How do we accomplish this?
  - Train a Neural Network model!
  - Goal of the model is to predict words
  - Train the embedding model using a large corpus of text
    - Something like all of Wikipedia
- Our model should learn:
  - Which words are similar
  - Which words appear together
- Extract some weights and biases from this network
  - These are our word embeddings!

Large Language Models

- There have been recent developments in word embeddings using Large Language Models (LLM)
  - The same word can have different embeddings, depending on the context
  - I set up a chess set to play a set of games.
- These are typically transformer-based embeddings
  - We'll talk about them later!

Setup

- To train a model for word embeddings we need a clean large corpus of text
  - Assume you have a corpus that has been tokenized and separated into blocks of text
    - Separate based on sentence or paragraph or …
- The number of tokens in this corpus is 10k
  - Vocabulary
  - Each word in the vocabulary is indexed!



Setup

- We now want to train a model to get meaningful embeddings for each token (word) in the vocabulary
- To train the model we need to understand a couple things
  - Context words
  - Target words

- My name is Dan and I work at UT.

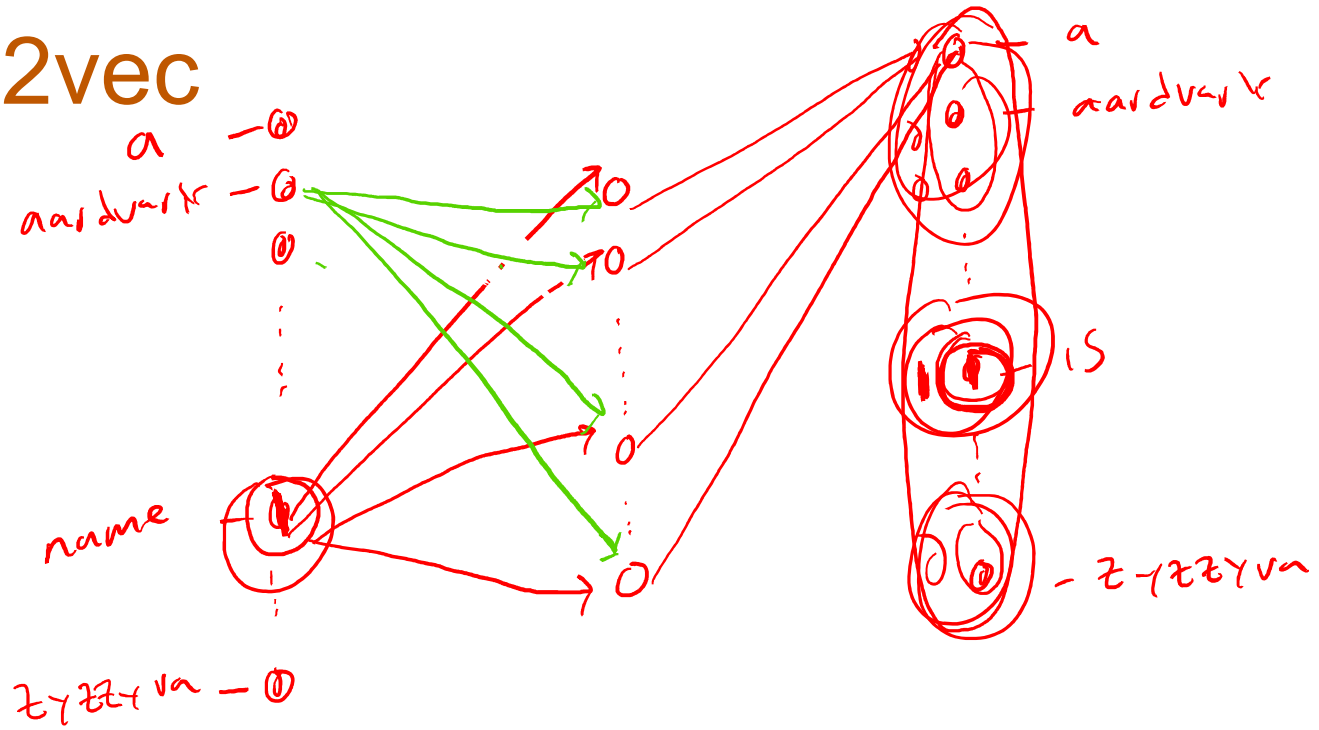
- Sampling – SGD

word2vec

- Build a neural network
  - 10k neurons on input layer
  - 300 neurons on hidden layer, no bias, no activation function
  - 10k neurons on output layer, softmax activation function

- All neural networks need data for inputs, x, and outputs, y

word2vec



- Eventually, the weights between the input layer and the hidden layer will contain the embeddings for each word

word2vec

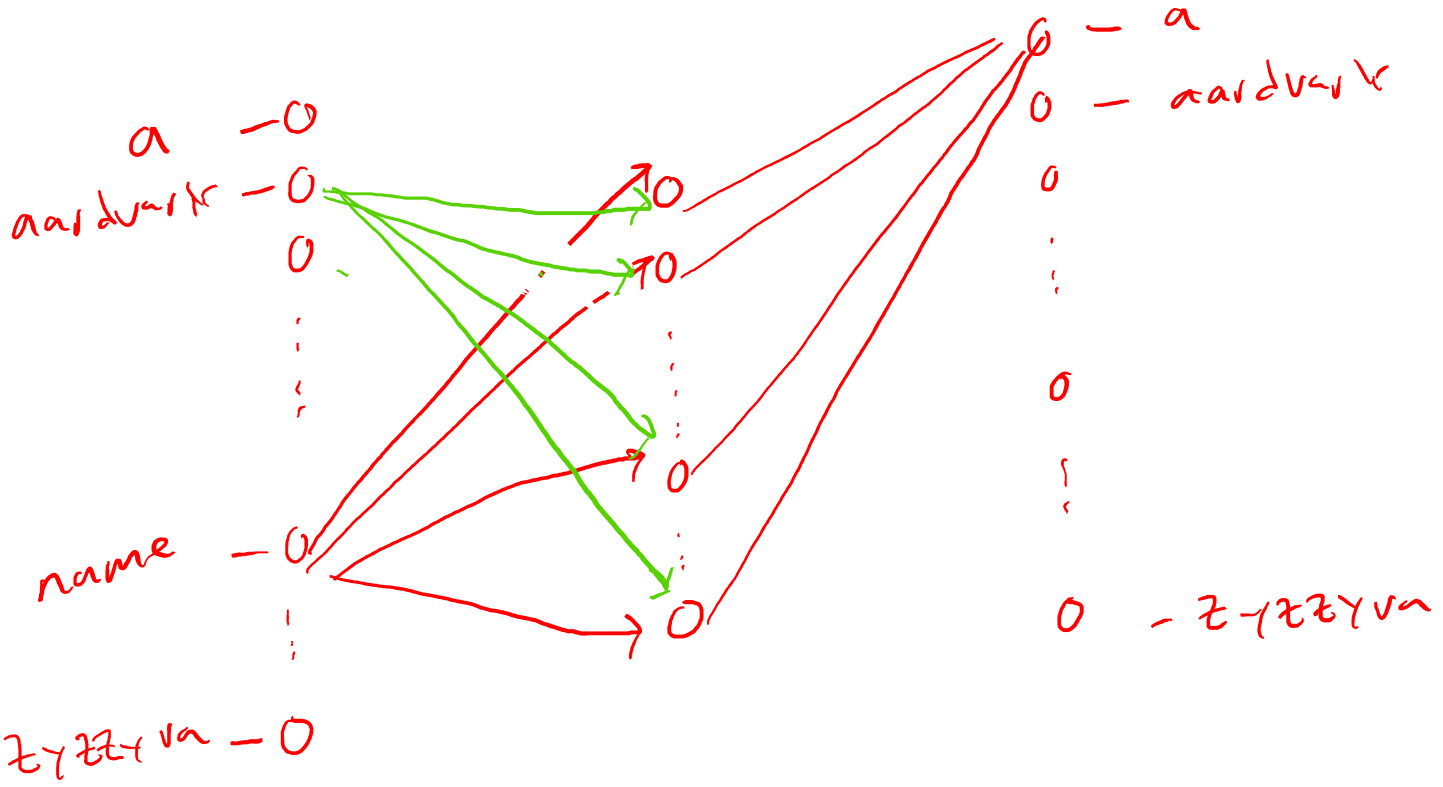
- The goal is to:
  - Plug in context words to the input
  - Have the neural network predict the target words
- Each output neuron will predict $\hat{y}$, the probability that each word is the target word for an input context

word2vec

- We need to train this neural network
- Simple idea:
  - Randomly grab a word (index j) from somewhere in the corpus, make it the context word
    - Set input neuron $x_j = 1$, all other input neurons are 0
  - Make the next word in the corpus the target word, index k
    - Set $y_k = 1$
  - Loss function for $\hat{y}_k$ vs y_k and SGD!
  - Repeat for many context/target pairs

word2vec

- My name is Dan and I work at UT.

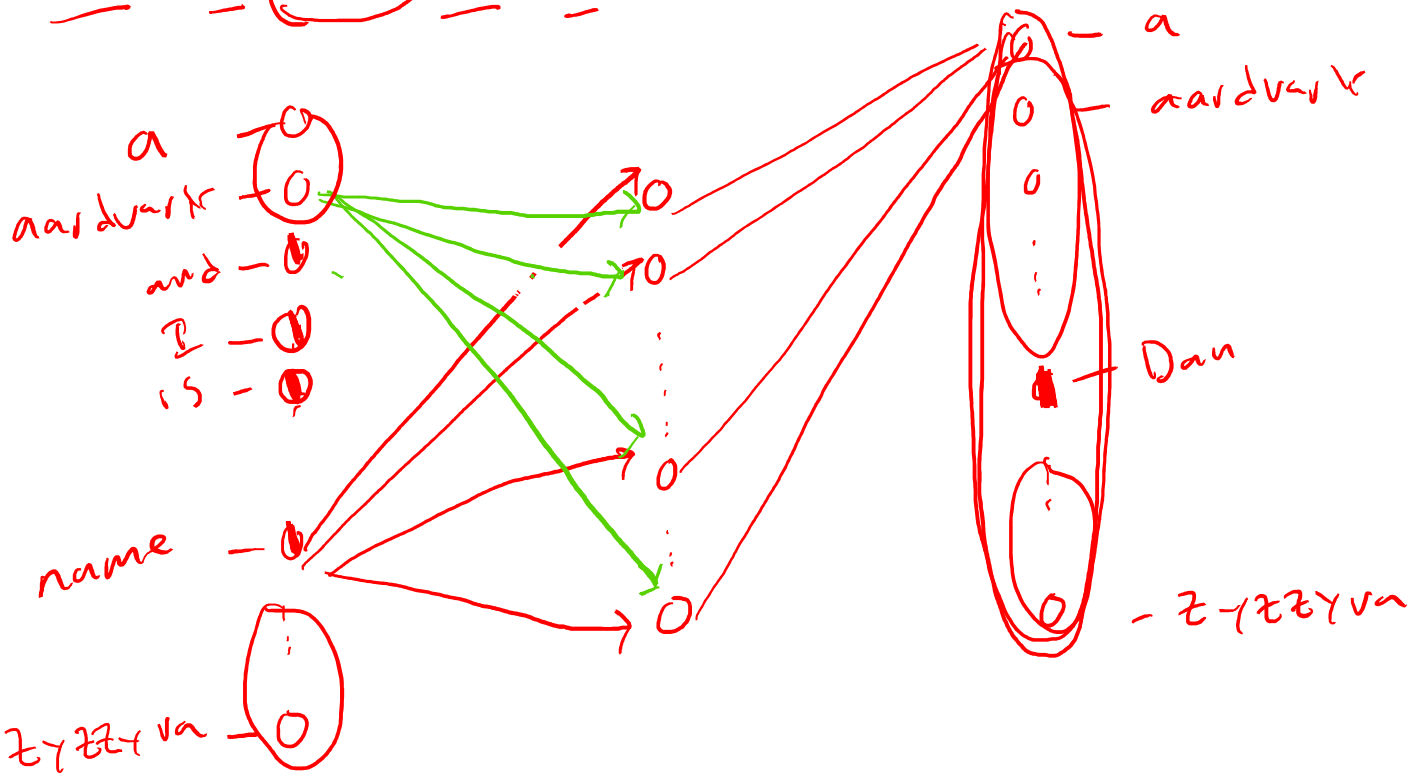


word2vec – Continuous Bag of Words (CBOW)

- With just 2 sequential words, we can't learn that much context
- Randomly pick a target word from the corpus, index k
  - Set $y_k = 1$
- Take a few words (hyperparameter) before and after the target as the context
  - For every word, j, in the context, set input neuron j = 1, all other input neurons = 0

CBOW

- My name is Dan and I work at UT.

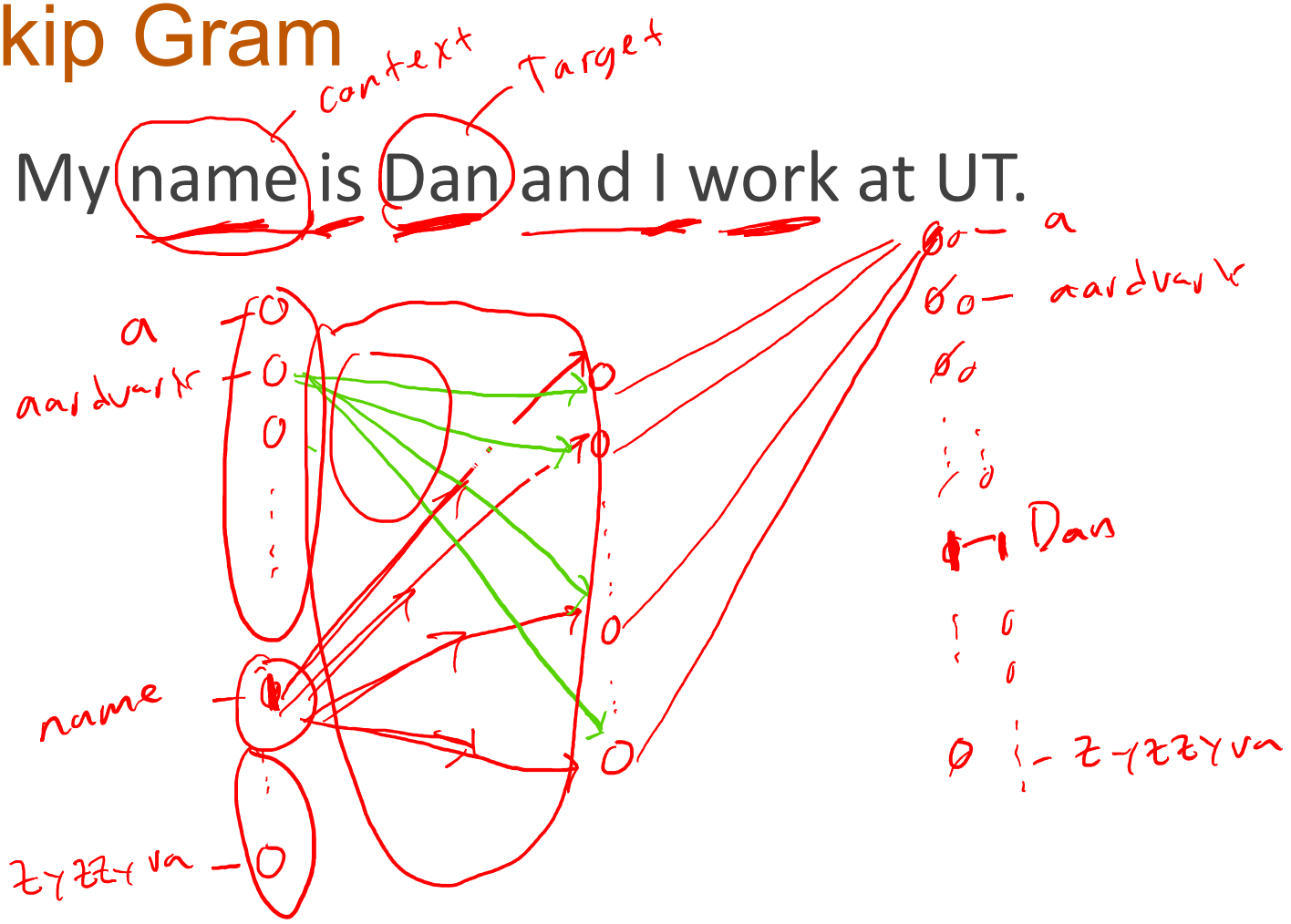


word2vec – Skip Gram

- Randomly pick a word from the corpus to be the target word, index k
  - Set $y_k = 1$
- Randomly pick a word within some range of the target to be the context word, index j
  - Set $x_j = 1$
- SGD

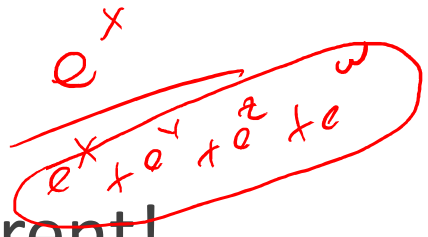
Skip Gram

- My name is Dan and I work at UT.



word2vec

- word2vec has ~ 10k X 300 X 2 = 6M parameters to estimate
- Softmax is very slow!
- Let's try something different!



Negative Sampling

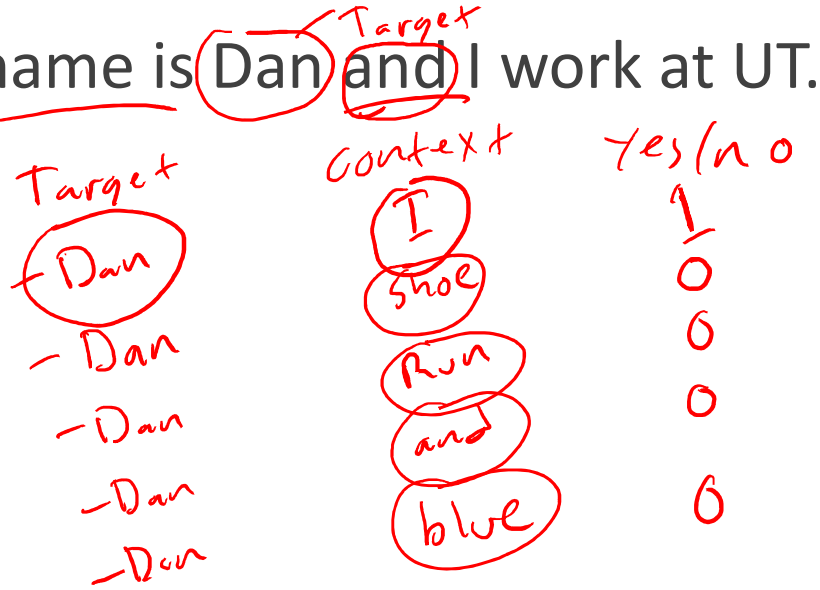
- Are 2 words part of a context/target pair?

- Build a neural network
  - 10k neurons on input layer
  - 300 neurons on hidden layer, no bias, no activation function
  - 10k neurons on output layer, sigmoid activation function

- For each target word, we're asking 10k yes/no questions!

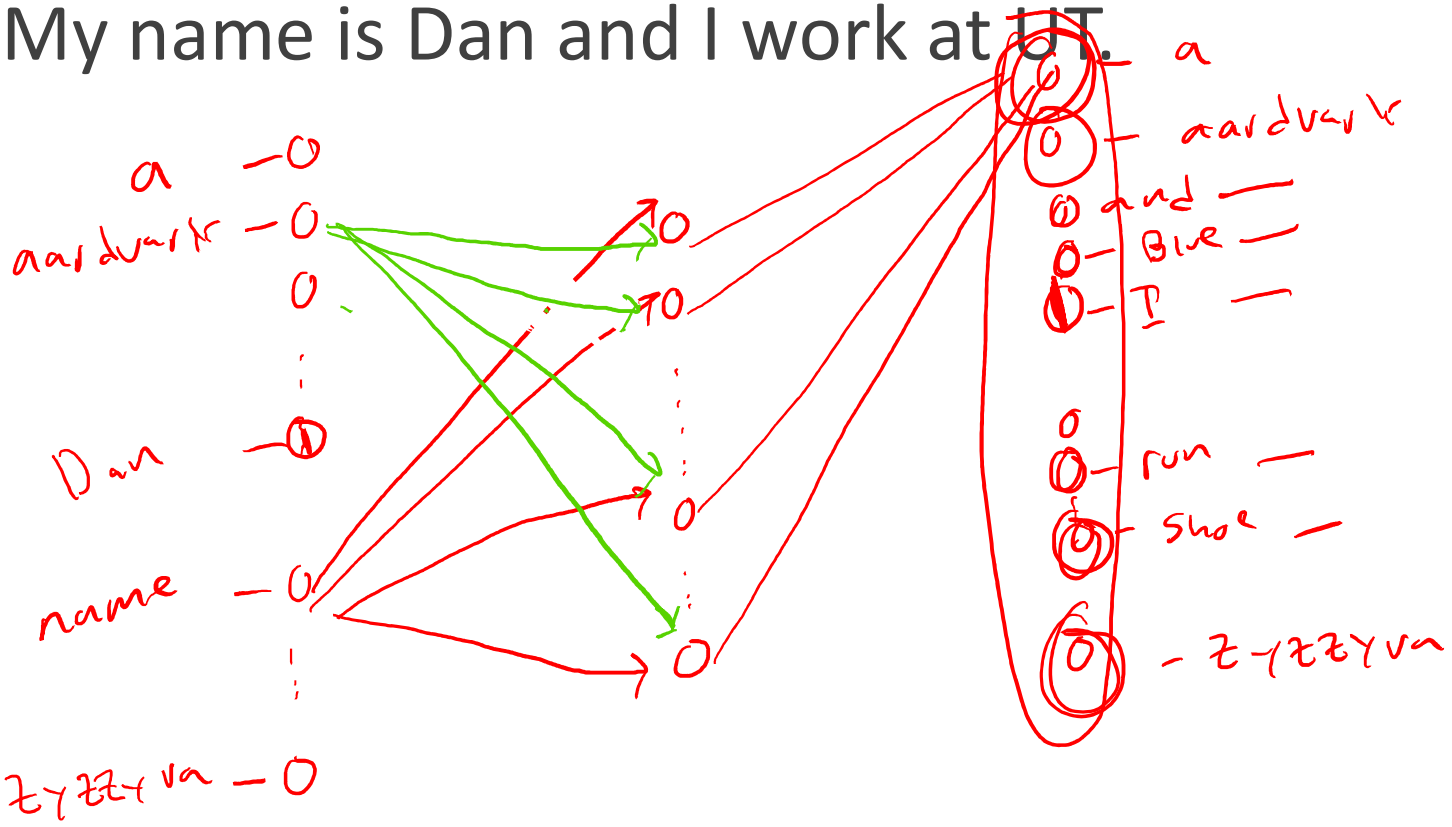
Negative Sampling

- Randomly pick a target word from the corpus
- Within some range of that word, pick a context word at random
- Randomly pick 4 other words from the vocabulary
- My name is Dan and I work at UT.



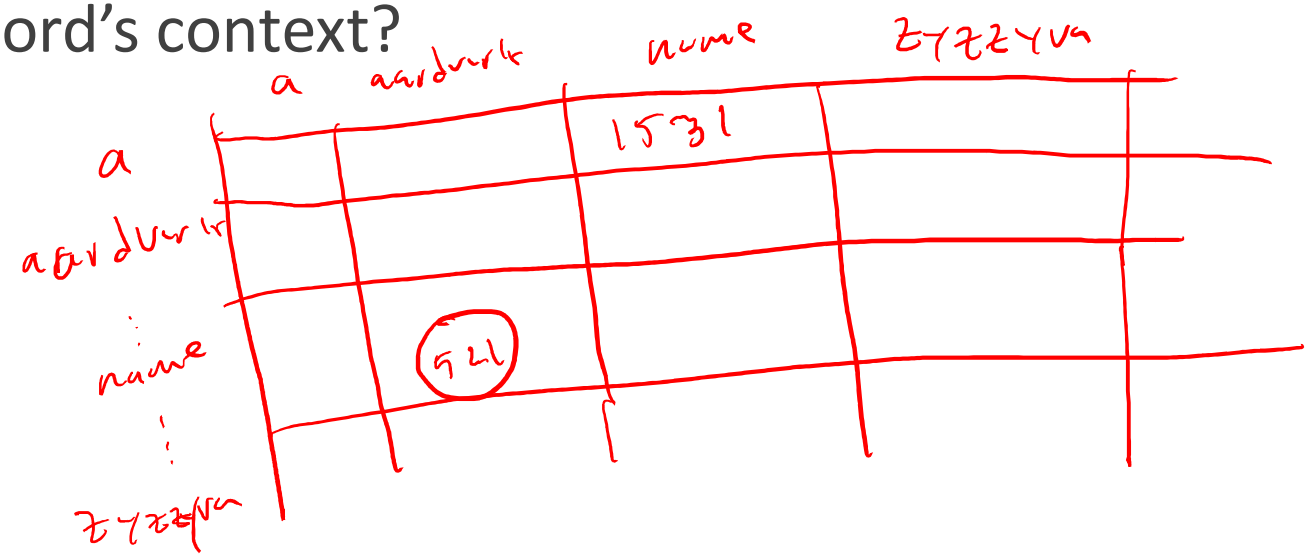
Negative Sampling

- My name is Dan and I work at UT.



GloVe

- word2vec and negative sampling only look locally at individual contexts
- GloVe is short for Global Vectors
- How many times does each word in the vocabulary show up in every other word's context?
  - y_{jk}

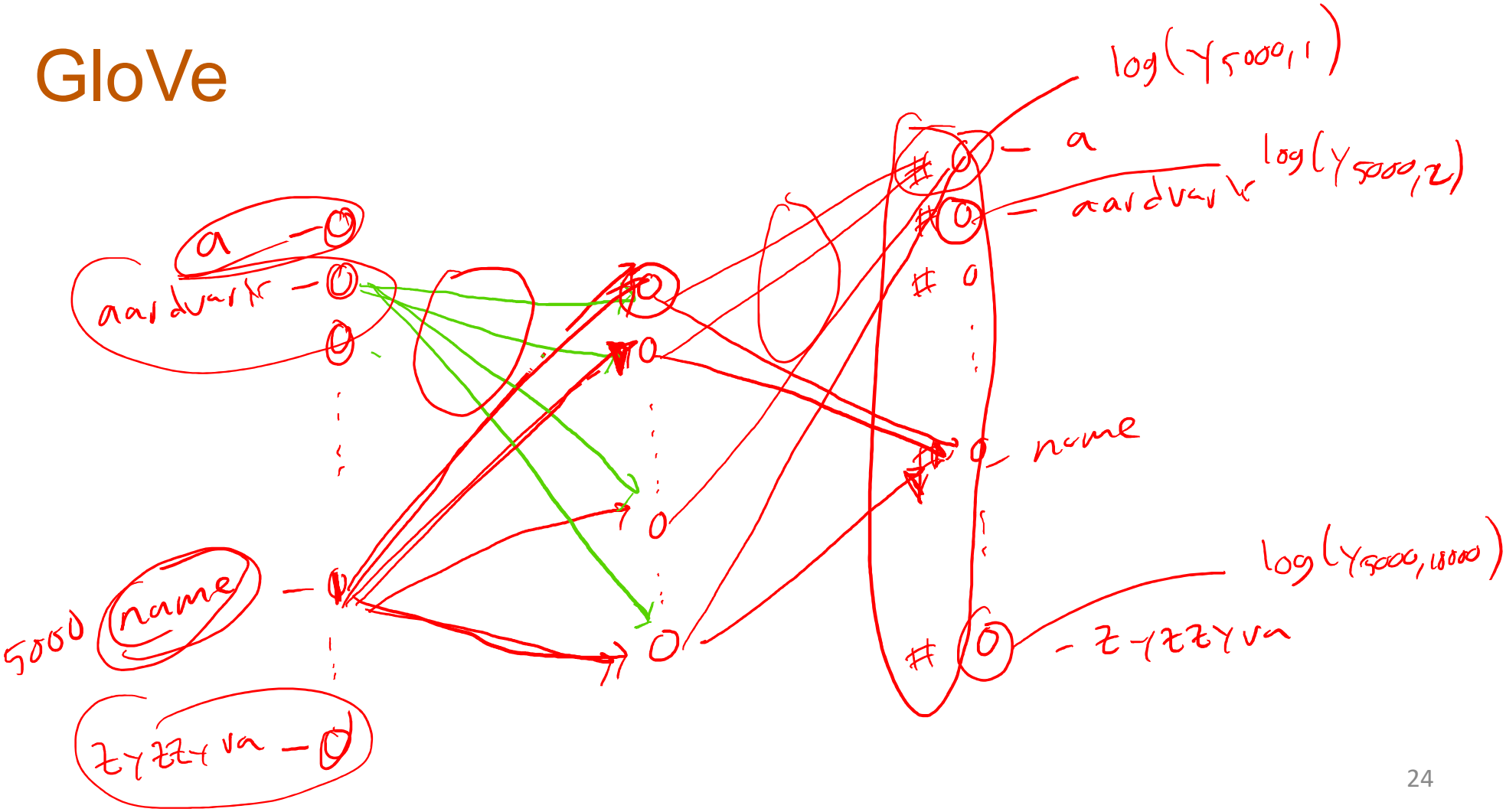


GloVe

- Build a neural network
  - 10k neurons on input layer
  - 300 neurons on hidden layer, no activation function
  - 10k neurons on output layer, no activation function

- For each target word, compare the output of NN to $\log(y_{jk})$

GloVe



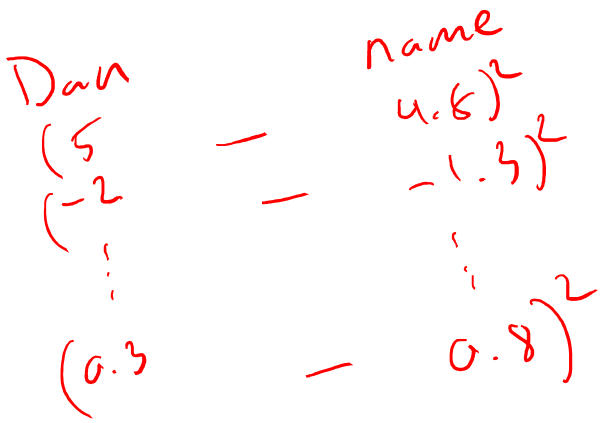
Word Embeddings

- Training our own word embeddings can be slow

- Fortunately, many people have done this already!
  - We can find other people's embeddings online
  - We will use the GenSim package in python for this

Implication

- Each word is now embedded so that
  - Similar words have similar embeddings
  - Words that appear together have similar embeddings
- That means we can measure the "distance" between words



$$\frac{5 * 4.8 + -2 * -1.3 + \cdots + 0.3 * 0.8}{\sqrt{5^2 + (-2)^2 + \cdots} * \sqrt{4.8^2 + (-1.3)^2 + \cdots}}$$

Application

- Text classification
  - Take output of embedding and use it as input for ML model
- Average the embeddings for each word in a block of text
  - Sentiment analysis

Application

- Semantic Synonym Search
  - Compare distance between words in vocabulary
- Search for ‘cabin’
  - Find results for ‘house’ too!

Semantic Sentence Search

- Average the embeddings for each word in a block of text
  - Stocks with high volatility are dangerous.
  - Equities that have large variability seem risky.
- We will see an application of this
- Later we will embed blocks of text, instead of just individual words

Summary

- There are several methods to create word embeddings
- They all fit some sort of machine learning model to get the embeddings
- The models are fit using a large corpus of text
- Word embeddings can be used for many down-stream tasks
  - Like semantic search