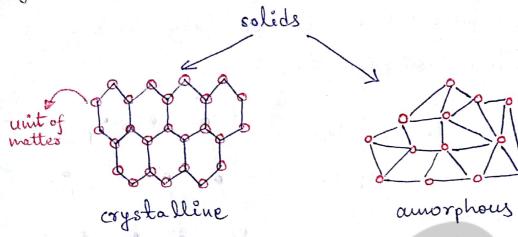
STATE PHYSICS

Crystal structure, direct lattice & (un) holy grail



(i) Amorphous solid: no order in arrangement of unit of matter (atoms, molecules etc). XRD shows liquid like proporty.

what's "solid"? -> elasticity

stress
$$\sigma = k \frac{\pi}{l}$$

 $\alpha = displacement$
 $\beta = -l^2 k \frac{\pi}{l}$
 $\beta = -k \ln \alpha = -k \pi$

$$\vec{x} = \frac{k_B T}{R} = \frac{k_B T}{K \ell}$$
So if $K \to 0$, $\vec{x} \to \infty$

-> rigidily amorphous solids \to highly viscous, super cooled liquids.

Example pitch, plastie, silicate glass.

SALIENT FEATURES

- (i) molecular motion is irregular but distance is more or less same with dastic solid.
- (ii) no regular shape > conductivity, elasticity, tensile strength is isotropic

(iii) no long range order. short range/ medium rauge order possible.

(w) no starp melting point.

There are polycrystalline substances which are composed of many small domains/regions of single crystals. Crystalline substances are distinguished from amorphous solids by their anisotropic behaviour (direction dependent).

Ideal crystal o infinite repetition of identical structure in space.

Periodic arrangement of unit (atoms, molecules, ions) in a (0,0) \rightarrow a coystal is alled the lattice, defined by three fundamental translation vectors \vec{a} , \vec{b} , \vec{c} . / basis vectors

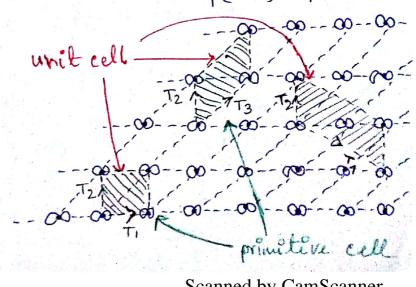
Atomie position vector
$$\vec{r} = \vec{r} + \vec{T}$$

$$= \vec{r} + n_1 \vec{a} + n_2 \vec{b} + n_3 \vec{c}$$

where n, n2, n3 are integers. primitive lattice & Unit cell

Unit cell is volume from which entire crystal can be constructed by translational repitition. (OABC parallelogram) primitive cell is a type of unit cell that contain I lattice

point at corners 1 minimum in volume = [(axb)·e]



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Basis in crystal stoucture, every lattice point is associated with an unit assembly of atoms/molecules/ions. This unit is called basis.

Basis can contain even hundreds I thousands of molecules.

A translation operation leaves the crystal invariant. $f(\vec{r}) = f(\vec{r} + \vec{T})$

physical: number density
$$n(\vec{r}) = \sum_{\vec{r}} \delta(\vec{r} - \vec{T})$$

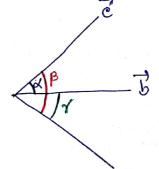
significance (point mass atom)
$$density p(\vec{r}) = \sum_{\vec{r}} m_{\alpha} \delta(\vec{r} - \vec{T} - \vec{c}_{\alpha})$$

where my is man of atom at lattice site cy.

$$p(\vec{r}) = p(\vec{r} + \vec{T})$$

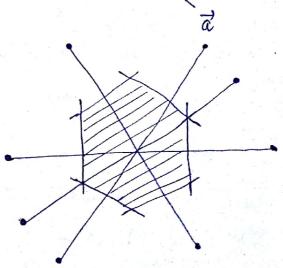
For cubie structure
$$|\vec{\omega}| = |\vec{b}| = |\vec{c}|$$

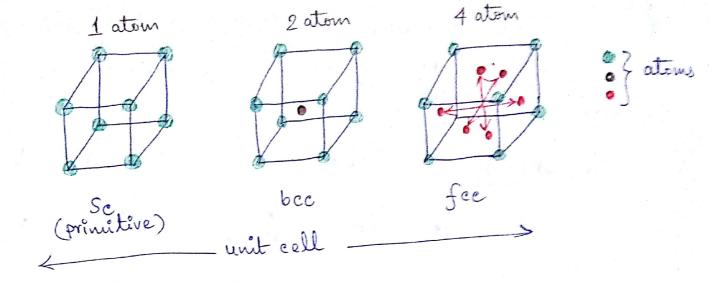
 $\alpha = \beta = \delta = \frac{\pi}{2}$



Wigner_Sielz primitive cell

- 1. Draw lines connecting nearby lattice points.
- 2. Draw planes/lines at midpoint of line I perpendicular to it.
 This is WS primitive cell.





Elements of symmetry

A symmetry operation transforms the crystal to itself.

(i) Translation $\vec{7} = \vec{7} + \vec{7}$ \wedge \wedge \wedge

in Rotation nø = 27

N = multiplicity of rotation axis.

= 1,2,3,4, x,6. A 2D square lattice has 4-fold rotational

(iii) Reflection mirror inage

(w) Inversion

(only for 3D lattice)

Symmetry operation performed about a point/line are called point group symmetry. 3 type of point group (i) plane of symmetry (reflection), (ii) axis of symmetry (rotation), (iii) centre of symmetry (inversion)

5-fold rotational symmetry: quasicrystals. But why 5-fold rotational symmetry is not permissible in ogstal structure?

