```
0.00
CU Roll No.
CU Registration No. : xxxx
Description : Basics of Scipy
Author : AKB
Author
import numpy as np
from scipy.integrate import quad, odeint
import matplotlib.pyplot as plt
import warnings
warnings.filterwarnings("ignore")
# Integer case switch for different problems to solve (feel free to add)
gquad, radiodec, simhm, dfshm, vdpol, duff, lorentz = 0, 1, 0, 0, 0, 0, 0;
if(gguad):
   #====
   print ('~~ Use of Gauss Quadrature ~~')
   # function definition
   def f(x, a):
      return a*x**2
   # main
   a = 1:
   print ('Integral 0 to 2 x^2dx using Gauss Quadrature : ', quad(f,0,2, args=(a,)) )
                                            # Note the comma for single variable
if(radiodec):
#-----#
  print ('--- 1ST ORDER LINEAR ODE : dxdt + lambda x = 0; Radioactive Decay of Nuclear
Mass ~~~')#
   # function definition
   def f(x,t,lam):
      dxdt = -lam*x
      return dxdt
   # Alternatively, def f(x,t,lam): return -lam*x
   # main
   x0, lam = 100, 0.5 # initial number of particles and decay constant
   t0, tf = 0, 10
                            # initial and final time
   t = np.linspace(t0,tf,100) # create time interval with 100 points
   sol = odeint(f, x0, t, args=(lam,))
   # plot
   plt.figure(1)
   plt.semilogy(t, sol, 'gx', label='x(t)', lw=1, ms=4)
   plt.semilogy(t, x0*np.exp(-lam*t), 'r-', label=r'x_0e^{-\lambda t}, lw=.5, ms=2)
   plt.legend(loc='best', prop={'size':12}) # try plt.legend()
   plt.text(0, sol[len(sol)-1]*2, r'$\tau {1/2}='+str(np.log(2)/lam)+'$', fontsize=12)
   #plt.axis([0, 10, 0, 100])
   plt.grid()
   plt.title(r'Nulcear decay curve $(\lambda = '+str(lam)+')$', fontsize=12)
   plt.xlabel('Time', fontsize = 12); plt.xticks(fontsize = 14)
   plt.ylabel('Nuclear Mass', fontsize = 12); plt.yticks(fontsize = 14)
   #plt.savefig('plot/01_radiodecay.pdf')
   plt.show()
if(simhm):
```

```
print ('--- 2ND ORDER LINEAR ODE : SHM d2x/dt2 + kx = 0; dxdt = y, dydt = -kx ---')#
   # function definition
   def shm(u,t,k):
        x, y = u[0], u[1];
        dxdt, dydt = y, -k*x
        return np.array([dxdt, dydt])
   # main
   t = np.linspace(t0, tf, 1000)
   sol = odeint(shm, u0, t, args=(k,))
   x1 = sol[:,0]; y1 = sol[:,1]
   # plot
   plt.figure(2)
   plt.subplot(2,1,1)
   plt.plot(t, x1, 'ko', label='x(t)', lw=1, ms=2)
plt.plot(t, y1, 'r+', label='v(t)', lw=1, ms=3)
plt.legend(loc='best', prop={'size':12})
#plt.axis([0, 50, -1, 1])
   plt.grid()
   plt.axhline(lw=2, color='coral') # draw a horizontal line
plt.title(r'(SHM) $\frac{d^2x}{dt^2}+kx=0; $'+'k='+str(k), fontsize = 12);
plt.xlabel('Time', fontsize = 12); plt.xticks(fontsize = 12)
   plt.ylabel('X(t), V(t)', fontsize = 12); plt.yticks(fontsize = 12)
   plt.subplot(2,1,2)
   plt.plot(x1, y1, 'mo-.', label='Phase Diagram', lw=2, ms=2)
plt.plot(x1[0], y1[0], 'b*', label='Initial Value', lw=2, ms=12)
   plt.legend(loc='best', prop={'size':12})
   plt.grid()
   plt.axhline(lw=.5, color='coral') # draw a horizontal line
   plt.axvline(lw=.5, color='coral') # draw a vertical line
   plt.xlabel('X(t)', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('V(t)', fontsize = 12); plt.yticks(fontsize = 12)
   plt.show()
if(dfshm):
   print ('--- 2ND ORDER LINEAR ODE : Damped SHM d2x/dt2 + lambda*dx/dt + kx = 0; dxdt =
y, dydt = -kx-lambda y ~~~')
                                                 #
   print ('
                                     Forced SHM d2x/dt2 + lambda*dx/dt + kx = acos(wt); dxdt =
y, dydt = -kx-lambda y + acos(wt) \sim )#
   # function definition
   def dshm(u,t,k,lam):
        x = u[0]; y = u[1];
        dxdt = y
        dydt = -k*x - lam*y
        return np.array([dxdt, dydt])
   def fshm(u,t,k,lam,omega):
        x = u[0]; y = u[1];
        dxdt = y
        dydt = -k*x - lam*y - a*np.cos(omega*t)
```

```
return np.array([dxdt, dydt])
    # main
    u0 = [1, 0]
                                 # initial displacement and velocity
    k, lam = 0.5, 0.2 # Parameters for Damped Oscillation
a, omega = 0.1, 1.0 # Parameters for Forced Oscillation
    t0, tf = 0, 50 # initial and final time
    t = np.linspace(t0,tf,1000) # create time interval with 100 points
    sol = odeint(dshm, u0, t, args=(k,lam))
                                                                    # Damped
    x1 = sol[:,0]; y1 = sol[:,1]
    sol = odeint(fshm, u0, t, args=(k,lam,omega)) # Forced
    x2 = sol[:,0]; y2 = sol[:,1]
    # plot
    # Damped
    plt.figure(3)
    plt.subplot(2,2,1)
plt.subtot(2,2,1)
plt.plot(t, x1, 'kx', label='x(t) [Damped]', lw=2, ms=3)
plt.plot(t, y1, 'ro', label='v(t) [Damped]', lw=2, ms=3)
plt.title(r'$\lambda='+str(lam)+', k='+str(k)+'$'+r', $a='+str(a)+',
\lambda='+str(omega)+'$', fontsize=12)
plt.legend(loc='best', prop={'size':12})
    plt.grid()
    plt.axhline(lw=2, color='gray') # draw a horizontal line
    #plt.axis([0, 50, -1, 1])
    plt.ylabel(r'$\frac{d^2x}{dt^2}+\lambda\frac{dx}{dt}+kx=0$', fontsize = 12);
plt.yticks(fontsize = 12)
    plt.subplot(2,2,2)
    plt.plot(x1, y1, 'gx', label='Phase Diagram', lw=2, ms=2)
plt.plot(x1[0], y1[0], 'b*', label='Initial Value', lw=2, ms=12)
    plt.legend(loc='best', prop={'size':10})
    plt.grid()
    plt.axhline(lw=.5, color='coral') # draw a horizontal line
    plt.axvline(lw=.5, color='coral') # draw a vertical line
    plt.xlabel('X(t)', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('V(t)', fontsize = 12); plt.yticks(fontsize = 12)
    # Forced
    plt.subplot(2,2,3)
    ptt.susptot(2,2,5)
plt.plot(t, x2, 'kx', label='x(t) [Forced]', lw=2, ms=3)
plt.plot(t, y2, 'ro', label='v(t) [Forced]', lw=2, ms=3)
plt.legend(loc='best', prop={'size':12})
    plt.grid()
    plt.axhline(lw=2, color='gray') # draw a horizontal line
    #plt.axis([0, 50, -1, 1])
    plt.xlabel('Time', fontsize = 12); plt.xticks(fontsize = 12)
    plt.ylabel(r'$\frac{d^2x}{dt^2}+\lambda \frac{dx}{dt}+kx=acos(\lambda t) , fontsize =
12); plt.yticks(fontsize = 12)
    plt.subplot(2,2,4)
    plt.plot(x2, y2, 'mo-.', label='Phase Diagram', lw=2, ms=2)
plt.plot(x2[0], y2[0], 'b*', label='Initial Value', lw=2, ms=12)
    plt.legend(loc='best', prop={'size':10})
    plt.grid()
    plt.axhline(lw=.5, color='coral') # draw a horizontal line
plt.axvline(lw=.5, color='coral') # draw a vertical line
    plt.xlabel('X(t)', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('V(t)', fontsize = 12); plt.yticks(fontsize = 12)
    #plt.savefig('plot/01_dampshm.pdf')
    plt.show()
if(vdpol):
```

```
print ('--- 2ND ORDER NONLINEAR ODE (Vanderpol Oscillator) : d2x/dt2 - mu(1-x^2)*dx/dt
+ beta*x = 0 ~~~ ')
  print ('~~ dydt = x/mu & dxdt = mu(1-x^3/3-beta*y); [mu & beta > 0] ~~ ')
   # function definition
   def vanderpol(X, t, mu, beta):
       x = X[0]; y = X[1];
       dxdt = mu*(x - x**3/3.0 - beta*y)
       dydt = x/mu
       return [dxdt, dydt]
   # main
   x0 = [1, 2]
                       # initial values
  mu, beta = 0.1, 0.2 \# Parameters of nonlinearity & Hookean Elasticity t0, tf = 0, 200 \# initial and final time
   t = np.linspace(t0,tf,1000) # create time interval with 1000 points
   sol = odeint(vanderpol, x0, t, args=(mu, beta))
   x, y = sol[:,0], sol[:,1]
   # plot
   plt.figure(4)
   plt.subplot(2,1,1); # dynamics
  plt.plot(t, x, 'kx-', label='x(t)', lw=.5, ms=2)
plt.plot(t, y, 'ro-', label='v(t)', lw=.5, ms=2)
plt.legend(loc='best', prop={'size':12})
  plt.grid()
  plt.title(r'Vanderpol Oscillator: \frac{d^2x}{dt^2}+\frac{1-x^2}{frac}d^2x}{dt^2}+\frac{x=0}{dt^2}
\mu'' + str(mu) + '$' + r'$, \beta'' + str(beta) + '$', fontsize = 12
  plt.xlabel('Time', fontsize = 12); plt.xticks(fontsize = 14)
   plt.ylabel('X(t),V(t)', fontsize = 12); plt.yticks(fontsize = 14)
   plt.subplot(2,1,2); # phase portrait
  plt.legend(loc='best', prop={'size':12})
   plt.xlabel('X(t)', fontsize = 12); plt.xticks(fontsize = 14)
   plt.ylabel('V(t)', fontsize = 12); plt.yticks(fontsize = 14)
   plt.grid()
   #plt.savefig('plot/01 vanderpol.pdf')
   plt.show()
if(duff):
   print ('--- 2ND ORDER NONLINEAR ODE : d2x/dt2 + lambda*dx/dt + kx + alpha x^3 =
acos(wt); dxdt = y, dydt = -kx-alpha x^3-lambda y + <math>acos(wt) \sim "")#
   # function definition
   def duffing(u,t,k,lam,alpha,a,omega):
       x = u[0]; y = u[1];
       dxdt = y
       dydt = -k*x - lam*y - a*np.cos(omega*t)
       return np.array([dxdt, dydt])
   # main
   u0 = [1, 0] # initial displacement and velocity
   k, lam, alpha, a, omega = 0.5, 0.1, 1.0, 0.2, 1.0 # Parameters
   t0, tf = 0, 50 # initial and final time
   t = np.linspace(t0,tf,1000) # create time interval with 100 points
```

```
sol = odeint(duffing, u0, t, args=(k,lam,alpha,a,omega)) # Forced
   x = sol[:,0]; y = sol[:,1]
   # plot
   plt.figure(5)
   plt.subplot(2,1,1)
   plt.plot(t, x, 'kx', label='x(t) [Duffing]', lw=2, ms=2)
plt.plot(t, y, 'ro', label='v(t) [Duffing]', lw=2, ms=2)
   plt.legend(loc='best', prop={'size':12})
   plt.grid()
   plt.axhline(lw=2, color='gray') # draw a horizontal line
   #plt.axis([0, 50, -1, 1])
   plt.text(15,-0.7, r'$\lambda='+str(lam)+', k='+str(k)+'$'+r' ,$\alpha='+str(alpha)
   ,a='+str(a)+' ,\omega='+str(omega)+'$', fontsize=12)
   plt.xlabel('Time', fontsize = 12); plt.xticks(fontsize = 12)
   plt.title(r'\$\frac{d^2x}{dt^2}+\lambda\frac{dx}{dt}+kx+\alpha x^3=a\cos(\alpha t)^{*},
fontsize = 12);
   plt.ylabel('X(t), V(t)', fontsize=12); plt.yticks(fontsize = 12)
   plt.subplot(2,1,2)
   plt.Bdsptot(2,1,2,7)
plt.plot(x, y, 'mo-.', label='Phase Diagram', lw=2, ms=2)
plt.plot(x[0], y[0], 'b*', label='Initial Value', lw=2, ms=12)
plt.legend(loc='best', prop={'size':10})
   plt.grid()
plt.axhline(lw=.5, color='coral') # draw a horizontal line
plt.axvline(lw=.5, color='coral') # draw a vertical line
plt.xlabel('X(t)', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('V(t)', fontsize = 12); plt.yticks(fontsize = 12)
   #plt.savefig('plot/01_dampshm.pdf')
   plt.show()
if(lorentz):
   print ('--- 2ND ORDER ODE : Lorentz Attractor --- ')
   print ('~~~ dx/dt=sigma*(y-x), dy/dt=x*(rho-z)-y, dz/dt=x*y-beta*z ~~~')
   print ('A 2D fluid-cell when heated from underneath and cooled from above (like earths
atmosphere) creates convection.')
   print ('x = rate of convective overturning, y = horizontal and z = vertical temperature
variations')
   # function definition
   def loratr(u, t, sig, rho, beta):
        x,y,z = u[0],u[1],u[2]
        dxdt = sig*(y-x)
        dydt = x*(rho-z)-y
        dzdt = x*y-beta*z
        return np.array([dxdt, dydt, dzdt])
   # alternatively, def loratr(u, t, sig, rho, beta):
   #
                            return [sig*(u[1]-u[0]), u[0]*(rho-u[2])-u[1], u[0]*u[1]-
beta*u[2]]
   # main
   u0 = [0, 1.0, 0]
                                               # initial x, y, z
   sig, rho, beta = 10.0, 26.0, 8.0/3 # parameters
   t0, tf = 0, 100
                                               # initial and final time
   t = np.linspace(t0, tf, 5000)
                                               # create time interval with 450 points
   sol = odeint(loratr, u0, t, args=(sig, rho, beta))
   x, y, z = sol[:,0], sol[:,1], sol[:,2]
   # plot X(t), Y(t), Z(t)
```

```
plt.figure(6)
    plt.subplot(3,1,1);
    plt.plot(t, x, 'r-', label='X(t)', lw=1, ms=2)
    plt.xticks(fontsize = 12); plt.ylabel('X', fontsize = 12); plt.yticks(fontsize = 12);
plt.grid();
    plt.subplot(3,1,2);
    plt.plot(t, y, 'g-', label='Y(t)', lw=1, ms=2)
    plt.xticks(fontsize = 12); plt.ylabel('Y', fontsize = 12); plt.yticks(fontsize = 12);
plt.grid();
    plt.subplot(3,1,3);
    plt.plot(t, z, 'b-', label='Z(t)', lw=1, ms=2)
plt.xlabel('t', fontsize=14); plt.xticks(fontsize = 12); plt.ylabel('Z', fontsize =
12); plt.yticks(fontsize = 12); plt.grid();
    # plot X-Y, Y-Z, Z-X
    plt.figure(7)
    plt.subplot(2,2,1)
   plt.subplot(x, z, 'r-', label='X-Z', lw=.5, ms=2)
plt.legend(loc='best', prop={'size':12})
plt.suptitle('Lorentz Attractor', fontsize=14)
    plt.xlabel('X', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('Z', fontsize = 12); plt.yticks(fontsize = 12)
    plt.subplot(2,2,2)
    plt.plot(x, y, 'k-', label='X-Y', lw=.5, ms=2)
plt.legend(loc='best', prop={'size':12})
    plt.xlabel('X', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('Y', fontsize = 12); plt.yticks(fontsize = 12)
    plt.subplot(2,2,3)
    plt.plot(y, z, 'g-.', label='Y-Z', lw=.5, ms=2)
plt.legend(loc='best', prop={'size':12})
    plt.xlabel('Y', fontsize = 12); plt.xticks(fontsize = 12)
plt.ylabel('Z', fontsize = 12); plt.yticks(fontsize = 12)
    plt.text(50, 35, r'\$\frac{dx}{dt}=\sigma(y-x)\$', fontsize=12)
    plt.text(50, 20, r'$\frac{dy}{dt}= x(\rho-z)-y$', fontsize=12)
    plt.text(50, 5, r'$\frac{dz}{dt}= xy-\beta z$', fontsize=12)
    #plt.savefig('plot/01_lorentz.pdf')
    plt.show()
```