

### Sem-IV - Special Relativity

(Instructor: AKB, Department of Physics, Asutosh College)

#### Assignment II: Relativistic Dynamics

Submission due date: 05/04/2020

**Q.1)** (a) A rocket propels itself rectilinearly through the empty space by emitting radiation, whose recoil provides the necessary thrust. If  $v$  is the final velocity relative to its initial rest frame, prove that the ratio of the initial and final rest mass of the rocket is

$$\frac{m_i}{m_f} = \sqrt{\frac{1+\beta}{1-\beta}}; \beta = \frac{v}{c}.$$

(b) The density of a stationary body is  $\rho_0$ . Find the velocity (relative to the body) of the reference frame in which the density is 25% greater than  $\rho_0$ . (c) Two lumps of clay each of rest mass  $m_0$  move towards each other with equal speed  $\frac{3}{5}c$  and stick together. What is the mass of the composite lump?

**Q.2)** (a) In an accelerator, a particle of mass  $1\text{GeV}$  is accelerated to a total energy  $5\text{GeV}$ . Find out the velocity of the particle in the rest frame of the accelerator.

(b) Find the velocity of the electron whose KE is  $0.25\text{MeV}$ . Rest mass of electron is  $0.51\text{MeV}$ .

(c) A pion of mass  $m_\pi$  at rest decays into a muon of mass  $m_\mu$  and a neutrino of zero mass. Find the energy of the outgoing muon in terms of the two masses,  $m_\pi$  and  $m_\mu$  (assume  $m_\nu = 0$ ).

(d) A kaon decays at rest via  $K^+ \rightarrow e^+ + \pi^0 + \nu_e$ . Calculate the maximum energy of the positron emitted. Given, mass of kaon =  $494\text{MeV}/c^2$ , mass of pion =  $135\text{MeV}/c^2$  and mass of electron neutrino =  $0.5\text{MeV}/c^2$ .

**Q.3)** (a) A neutral pion of rest mass  $m$  and relativistic momentum  $P = \frac{3}{4}mc$  decays into two photons. One of the photons is emitted in the same direction as the original pion, and the other in the opposite direction. Find the relativistic energy of each photon.

(b) A  $\pi^+$  meson is created at a height  $120\text{km}$  above sea level with a total energy  $1.35 \times 10^5\text{MeV}$  and travels vertically downward. In its proper frame it disintegrates in  $2 \times 10^{-8}\text{sec}$  after its creation. At what altitude does the disintegration occur? Rest energy of  $\pi^+$  meson is  $135\text{MeV}$ .

(c) Show that a particle of rest mass zero has to travel with the velocity of light.

**Q.4)** (a) If the total energy of a particle of mass  $m$  is equal to twice its rest energy, then what will be the magnitude of its relativistic momentum?

(b) A body of mass  $m$  at rest breaks up spontaneously into two parts with masses  $m_1$  and  $m_2$  and speeds  $v_1$  and  $v_2$  respectively. Show that  $m > m_1 + m_2$  using conservation of mass-energy.

**Q.5)** (a) A particle of rest mass  $m_0$  moving with speed  $v$  collides and sticks with a stationary particle of rest mass  $M_0$ . Show that the speed of the composite particle is given by  $\gamma m_0 v / (M_0 + \gamma m_0)$ .

(b) A particle moving at speed  $0.8c$  collides with another of the same rest mass and they stick together. What is the rest mass and speed of the composite particle?