PHYSICAL OPTICS

(Diffraction and Holography)

Books*: 1. Opticks + Ghatak (6th Edition, Tata Mc Graw Hill)

> Standard textbook, Good for first line readers.

- 2. Introduction to Geometrical and Physical Optics >
 B.K. Mathur (Old Book) = Good for concept building and
 thony learning.
- 3. Fundamental of Optics (Tata McGrowttill) + Jenkins & while > Concise book, good for Problem solving.
- 4. Principles of Optics (Pergamon Press) -> Born & Wolf

 > Very good book for thony learning.
- 5. Feynman leetures on Physics Vol-1 -> Feynman/Leighton/ Bands (Narosa) -> Short and concise for concept building.
- 6. Optics as Hecht (Addison Wesley) => Good for problem solving and first time readers.
- 7. Introduction to Holography -> Toal (CRC Press) => New age book for basic holography principles.

Opticks optics.

Geometrical Opties deals with refraction and reflection at surfaces, lenses, Natrix method, dispersion through prism, Aberrations and eyepicees and it terms on the particle C corpuscular) theory of lightuing Fermat's principle. Physical opties on the other hand deals with wowe there of light as Fresnel-Hugen's principle and discusses on Interference and Coherence, Diffraction, Polarisation (crystal optics), fiber optics and Holography.

DIFFRACTION

fer mat's principle says that when a ray of light goes from one point to another through a set of media, it always follow a grath along which the time taken is minimum.

\frac{dt}{dx} = 0 yields the "law of reflection"

i = r. and the "Snell's -

reflection

refraction

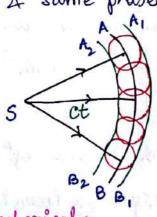
law of refraction vicini = vacint

by conservation of the horizontal component of momentum.

The corpuscular model of light establish the reetilinear (straight line) propagation of light and propagation of light through vacuum.

Wave thony and Huggens-Fresnel principle

A source of light transmit wave that contain energy in all directions. A "wave front is defined as the locus of all points which are in the same state of vibration (same phose). For example, circular ripples spreading out if a pond is a peoble is dropped, each circumferential point oscillating at same amplitude A same phase. Similarly for a light source, at a A2 AA,



spherical

nearby location x=ct where AB is a spherical wavefront, while at large distance, AB is a plane wavefront. Surface AB is called "primary wavefront", The direction in which the wave is propagated is known as "ray" which is perpendicular to the wavefront.

B₂ B B₁
plane
unvertical

Hygen-fresnel principle dells that all points on the primary wavefront are considered to be the centres of disturbance and they

transmit secondary waves in all direction with the same velocity on the primary. So A,B, surface that touch the spheres after ct, distance is the "secondary wavefront"

Using Huygen-fresned principle, law of reflection (i=r), law of refraction (v_1 sini = v_2 sin r), refraction of spherical wave at coneave spherical surface ($\frac{\mu}{v} - \frac{1}{u} = \frac{\mu-1}{R}$) and convex sphereval surface ($\frac{\mu-1}{R} = \frac{1}{v} - \frac{1}{u}$), lens formula for thin convex/coneave lens ($\frac{1}{f} = (\mu-1)(\frac{1}{f_1} - \frac{1}{f_2})$) can be obtained.

Why Diffraction ? Wave-particle duality as in deBroglie's matter wave though $\lambda = \frac{h}{p}$ gives rise to Heisenberg's uncertainty principle $\Delta \times \Delta P_{\chi} > h$.

opening) and if light propagation is rectilinear then there is no bending of light in the geometrical shadow.

But if a light quanta (photon) or electron pass through slit, then $\Delta x \sim b$, so $\Delta P_x \sim \frac{h}{b}$. As $P_x = p \sin \theta$, so $\sin \theta \sim \frac{h}{a} \sim \frac{h}{a}$

So sing $\sim \frac{h}{pb} \sim \frac{\lambda}{b}$.

When $b >> \lambda$, sing $\rightarrow 0$ or al

When $b >> \lambda$, sind $\rightarrow 0$ or almost no bending in geometrical shadow, while for $b \cap \lambda$ then there will be significant bending. The bending of light round corners and spreading of light waves into the geometrical shadow of an object is called Diffraction.

Difference between Interference & Diffraction

Interference

- 1. Result due to superposition of light from two different wavefront emanating from the same source.
- 2. fringes may/may-not be of same width.
- 3. All bright bands are of uniform intensity
- 4. Points of minimum intensity are perfectly dark.

Diffraction At wo

- 1. Result due to superposition of light from different parts of the same wavefront.
- 2. Fringes are never of same width
- 3. All bright bands are of different intensity
- 4. Points of minimum intensily are not perfectly dark.

Classification of Diffraction

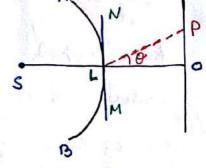
Diffraction phenomena are divided into two distinct classes, as fresnel's diffraction (near field) and fraunhofes diffraction

(far field).

In Fresnel diffraction, source of light & screen are all finite distance from aperture. No concave/convex lenses are used so that incident wavefront is either spherical/cylindical but not planar. So phose of secondary wavefront isn't same in the plane of aperture.

Fresnel's assumptions

(a) A wavefront is divided into a large number of small area (Fresnel's zone). Secondary waves originating from various



zones will interfere and the resultant effect can be noted at point P on the screen.

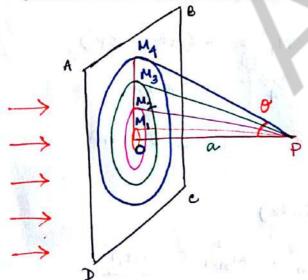
(b) Resultant at P due to a particular zone will depend on the distance of the point from the zone.

(c) he sultant at ρ will also dopend on obliquity factor, which is propositional to $(1+\cos\theta)$. So for a wavefront at L, maximum at O occurs for O=0, while in LN or LM direction, intensity is half of O, as $O=\frac{\pi}{2}$. Along LS, $O=\pi$, so no intensity is reverse direction. (Zone plate)

Fraunhofer diffraction occur when source of light/screen case effectively infinite distances from aperture. Two convex lenses are used I incident wavefront is plain. Secondary wavelet from exposed portion of the wavefront at aperture are in the same phase at all points in plane of the aperture.

(plane transmission grating, concave reflection grating)

Fresnel's half-period zone of a plain wave-front



- o first half period tone a+ 1/2
- O Second half period fone a + 2
- O Third half period zone a+ 37/2
- o fourth half period tone a+ 22

Let us consider a plane wavefront of a monochromatic light at any particular instant. We want to find out the resultant amplitude at P due to all the wavelets coming from this wavefront.

According to Huygen's principle, every point on the plane wavefront may be regarded as the origin of the secondary wavelets I therefore the resultant effect at P due to the whole wavefront will be equal to the resultant of all these secondary wavelets.

The wavefront is divided into a number of Fresnel's half period zones - from P drop a perpendicular on ABCD at O (pole of the wave). Let of= a and of as centre of radius (a+ 1/2), draw a sphere () cutting the wavefront in a circle at MI,

PM, = a + 3/2 so that the secondary wavelets from Of from the points on the circumference of M, on reaching p will differ in phase by $\frac{2\pi}{\lambda}(pM_1-op)=\frac{2\pi}{\lambda}\times\frac{\lambda}{a}=\pi=\frac{\pi}{a}(halfperiod)$

Generally other sphere of radii (a+ 22), (a+ 32), (a+ 42), ... can be drown that intersect at M2, M3, M4, ... so that the

whole wavefront can be divided into several half period zones.

Amplitude due to wavelets produced by each tone is

(i) Directly proportional to the area of the zone which is approximately equal.

(ii) Varies inversely with the distance of zone from P. (iii) Varies with the obliquity factor (1+ 000).

Area of 1st half period zone = TOM; = T(PM; - OP) $= \pi \left[(a + \frac{3}{2})^2 - a^2 \right] = \pi \left[a\lambda + \frac{3}{4} \right] \simeq \pi a\lambda.$

Similarly $\theta M_n^2 = \rho M_n^2 - o\rho^2 = \left(a + \frac{n\lambda}{2}\right)^2 - a^2 = an\lambda$ (nth circle)

OMN-1 = a(n-1) A ((n-1)th circle).

So Area of nth zone = Tr(OMn - OMn-1) = Taz.

So radii of zone & In.

area of zone independent of n

For visible light, a = small & so area of zone = Tax but if a & not very small then the area of half period zones of higher order decreases gradually. If the phase of the wavelets coming from B & zero then the plane of wavelets from intermediate points between O and M, will vary from 0 to T (because $\frac{2\pi}{A}(PM_1-OP)=\pi$).

 $_{\circ}$ Average phase of all wavelets from 1^{st} tone = $\frac{0+x}{2} = \frac{x}{2}$ Dimilarly phase différence of wavelets from M, & M2 will be butween To and 2T, so that average phose of all wavelets from 2rd zone = $\frac{\overline{\Lambda} + 2\overline{\Lambda}}{2} = \frac{3\overline{\Lambda}}{2}$, from 3^{rd} zone $\frac{5\overline{\Lambda}}{2}$, from 4^{th} zone $\frac{7\overline{\Lambda}}{2}$ & so on...

Resultant phose-différence between two consecutive zones = $\bar{\Lambda}$. Resultant phose-différence between two alternate zones = $2\bar{\Lambda}$. So if resultant from 1st half period zone is positive then 2nd half period zone is negative.

Amplitude decreoses du to obliquités factor (1+ 6050), so resultant amplitude di da do da

D = d1-d2+d3-d4+d5-... ±dn.

(i) If n = odd, to a first approximation $d_2 = \frac{d_1 + d_3}{2}$, $d_4 = \frac{d_3 + d_5}{2}$

So that $D = \frac{d_1}{2} + \left(\frac{d_1 + d_3}{2} - d_2\right) + \left(\frac{d_3 + d_5}{2} - d_4\right) + \cdots + \frac{d_n}{2}$

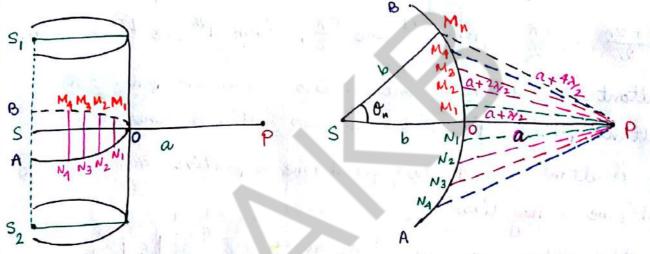
 $= \frac{d_1}{2} + \frac{d_n}{2}.$

(") If n = even, $D = \frac{d_1}{g} + \frac{d_{n-1}}{g} - dn$

If his very large, then effect from nt zone is negligible l

resultant amplitude due to whole wave is $D = \frac{di}{2}$ and $D = \frac{di}{2}$ and $D = \frac{di}{2}$ intensity $I = D^2 = \frac{di^2}{4}$. If an obstacle is placed at 0 then the resultant disturbance at P is P = P the disturbance due to wavelets from the 1ct half-period tone with one-fourth the intensity. If obstackle at 0 blocks a considerable number of half-period tones, effect is negligible if no light is received at P = P or light travels approximately in a straight line.

Fresnel's half-period strip of a cylindrical wave-front

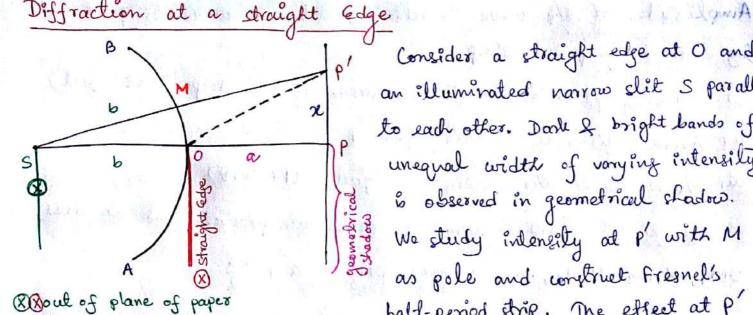


consider a long and narrow slit S_1S_2 , when illuminated by monothromatic light of wavelength λ , produces cylindrical wavefront. To find the resultant amplitude, the wavefront can be divided into half period strips, with 0 as pole. Consider an equational section AOB through 0 in plane of paper. With P as centre I radius $(a+\frac{\lambda}{2})$, $(a+\frac{2\lambda}{2})$, ... etc, draw arcs that cut AOB at point

M, N, M2N2, etc. Through these points, draw lines parallel to length of slit (axis of wavefront) and the area of the wavefront is the N3N2N1O M. M2 N2N1O M2

Amplitude of the waves reaching P due to wavelets produced loy each talf-period strip in (i) Directly proportional to the area of the strip (not equal) (ii) Average distance of strip from P (iii) Varies with the obliquity factor (1+ 650) As length of strip is same, so areas are proportional to are OM, M, M2, M2H3, ... where $pM_n = a + \frac{n\lambda}{2}$ from triangle PM,S, we have PM, = SM, + PS - 2SM, PS coson $\omega(a + \frac{n\lambda}{2}) = b^2 + (a+b)^2 - 2b(a+b)\cos\theta_n$ $\alpha \alpha^{2} + \alpha n \lambda + \frac{n^{2} \lambda^{2}}{4} = 26 + \alpha^{2} + 206 - 306 - 26 + 6(\alpha + 6) \delta_{n}^{2}$ or an $\lambda = b(a+b) O_n^2$ or $O_n =$ Now OMn = bon = bkIn. OM, = bk, OM2 = bk52, OM3 = bk53. So MIM2 = 6K (52-1) = 0.414 6K M2M3 = bk (J3-52) = 0.318 bk M3 M4 = bKCJA-J3) = 0.268 bK, M4M5 = 0.236 bK, ... Le area of strip initially decreases rapidly & then for increasing order more slowly. and because of opposite sign they caned out each other. So the resultant at P is only due to first few half period etrips. (from half wavefront) $D = d_1 - d_2 + d_3 - d_4 + \cdots$ (from right side half wavefront le resultant due la whole wavefront = \frac{d1}{2} \pm \frac{d1}{2} = d_1 (n odd) (n even)

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Consider a straight edge at O and an illuminated narrow slit S parallel to each other. Don't & bright bands of unequal width of varying intensity is observed in geometrical shadow. We study intensity at p' with M as pole and construct Fresnel's half-period strip. The effect at P'

depends upon the number of half-period strips contoured in OM I

Due to straight edge, the effect at P is due to the upper half of the wavefront only, so displacement at P is $\frac{1}{2}$ of the displacement for whole wavefront or & of the full wavelet intensity.

of half-period strips contained in &M depends on the path difference of-MP Now OP = $\int \alpha^2 + \chi^2 = \alpha \left(1 + \frac{\chi^2}{\alpha^2}\right)^2$

$$SP' = \sqrt{(a+b)^2 + x^2} = a+b + \frac{x^2}{2(a+b)}$$

$$80 \text{ Mp}' = \text{Sp}' - \text{MAP}' \text{SM} = \alpha + \frac{\chi^2}{2(\alpha + b)}$$

: Path difference op_mp' = a+ \frac{2^2}{2a} for the displacement tobe maximum,

$$\frac{bx^2}{2a(a+b)} = \frac{(2n+1)\frac{\lambda}{2}}{2} \quad \text{for } x = \left[\frac{a(a+b)(2n+1)\lambda}{b}\right]^{\frac{1}{2}}, n=0,1,2,...$$

$$x \propto \sqrt{2n+1} \quad \text{(bright band)}$$

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For the displacement to be minimum, $\frac{bx^2}{2a(a+b)} = n\lambda$ as $x = \left[\frac{2a(a+b)n\lambda}{b}, n=1, 2, 3, x < \sqrt{n}\right]$ (dark band) Using these, wavelength of light can be found.

CW A narrow slit illuminated by light of $\lambda = 5890 \text{Å}$ is located at a distance of 0.1m from a straight edge. If the measurements are made at a distance of 0.5 m from the edge, calculate the distance between 1th 1 2nd dark band.

For nth dark band
$$x = \sqrt{\frac{2a(a+b)n\lambda}{b}}$$
 $0 = 0.5m$
 $b = 0.1m$
 $3 = 5890 \times 10^{-10}$
 $3 = 5890 \times 10^{-10}$
 $3 = 5890 \times 10^{-10}$

Read about diffraction of light by a thin wire. fringe width $\beta = \frac{DA}{d}$, D = distance between obstacle 4 crosswire of Eyepiece, A = wavelength of light.

Fresnel's diffraction at a circular aperture

B

Geometrical
Shadow

P

geometrical
Shadow

from a point source S a wavefront (spherical) touches a circular aperture MN. To calculate the amplitude at screen P, we need to devide the wavefront MON into Fresnel's half-period zones about the pole O.