## Sem-IV - Special Relativity

(Instructor: AKB, Department of Physics, Asutosh College)
Assignment I: Length-contraction, time-dilation, velocity addition
Submission due date: 13/03/2020

Q.1) (a) Two rods of proper length  $l_0$  move lengthwise towards each other parallel to the common axis with the same velocity v relative to the Laboratory frame. Show that the length of each rod in the reference frame fixed to the other rod is

$$l = l_0 \frac{1 - \beta^2}{1 + \beta^2}, \beta = \frac{v}{c}.$$

(b) In a frame S the following two events occur

Event 1: 
$$x_1=x_0,\; t_1=\frac{x_0}{c}$$
 and  $y_1=z_1=0,$  Event 2:  $x_2=2x_0,\; t_2=\frac{x_0}{2c}$  and  $y_2=z_2=0.$ 

Find the velocity of the frame S' (w.r.t. S) at which these two events occur simultaneously. What is the value of t in S' at which these events are simultaneous?  $x_0$  is a constant and c is speed of light in free space.

Q.2) (a) An observer in a reference frame S' sees an objective travelling at a velocity 0.8c at right angle to x' axis of S'. An observer in a reference frame S whose x-axis is oriented parallel to x' axis of S' observes that S' has a velocity 0.8c along the x-axis of S. What is the magnitude of velocity of the object as observed by the observer in S? What is the angle made by the velocity of the object with the x-axis as observed by the observer in S? (b) Two events occur at the same place in an inertial frame and are separated by a time interval of 4sec. What is the spatial separation between these two events in an inertial frame in which events are separated by a time interval of 6sec?

Q.3) (a) In a certain inertial frame light pulses are emitted by two sources 5km apart. Time interval between two pulses is  $5\mu s$ . An observer moving at a speed v along the line joining these sources notes that the pulses are simultaneous. Find the speed v of the observer. (b) Two rockets of rest length  $l_0$  are approaching each other from opposite directions at same speed  $\frac{c}{2}$ . How long does one of them appear to the other?

Q.4) (a) Calculate the velocity at which the relative increase in the mass of relativistic particle is f%. (b) According to an observer on Earth, a certain star is d light years away. A spaceship travel from the Earth to the star at a uniform speed and takes a years to get there according to the pilot's measure of time. Show that the speed of the spaceship relative to Earth is  $\frac{c}{\sqrt{2}}$  where c is the speed of light.

Q.5) (a) A muon at rest has lifetime  $2 \times 10^{-6}s$ . What is its lifetime when it travels with a velocity  $\frac{3}{5}c$ ? (b) Half life of pions at rest is  $1.77 \times 10^{-8}sec$ . A collimated pion beam, leaving the accelerator target at a velocity of 0.99c, is found to drop to half its original intensity. Find the distance travelled by the pions in the laboratory.

Q.6) (a) Suppose that a meter stick pointing in the x-direction moves with the speed 0.8c along the x-axis of the reference frame of an observer situated at x = 0, y = 1m. The midpoint of the stick passes through the origin at t = 0. When does the observer see the mid point pass the origin? (b) Two particles move in opposite directions, each with a speed of 0.6c. What is the speed of one particle as seen by the other? (c) Show that a circle  $x^2 + y^2 = a^2$  in frame S appears to be an ellipse with eccentricity  $\frac{v}{c}$  in the frame S' which is moving with velocity v along the x-axis relative to S.

Q.7) (a) At the time a spaceship moving with speed v = 0.5c passes a space station located near Mars, a radio signal is sent from the station to Earth. This signal is received on Earth 1125s later. How long does the spaceship take to reach the Earth according to the observers on Earth? What is the duration according to the crew of the spaceship? (b) Two trains A and B each have proper length L and move in the same direction. A's speed is 4c/5 and B's speed is 3c/5. A starts behind B. How long, as viewed by a person on the ground, does it take for A to overtake B?