Velocity component distribution What is the number of molecules within velocity u 4 u+du but any value in ŷ or 2 direction.  $dN_{u,v,w} = N\left(\frac{m}{2\pi \kappa_0 T}\right)^{3/2} e^{-\frac{m}{2\kappa_0 T}\left(u^2 + v^2 + \omega^2\right)} du dv d\omega$  $oldsymbol{o}$   $oldsymbol{o}$  olds $= N \left( \frac{m}{2\pi K_B T} \right)^2 du \int e^{-\frac{3}{2}} d$ Now  $\int_{-\infty}^{\infty} e^{-\frac{mv}{2KBT}} dv = 2 \int_{-\infty}^{\infty} e^{-\frac{mv}{2KBT}} dv$  $= 2\sqrt{K_0T} \left( e^{-\frac{7}{2}} + \frac{\sqrt{2}}{2} dz \right)$ KBT d2 Jm . MJ2KBT JZ.  $= \sqrt{\frac{2k_BT}{m}} \times \sqrt{n} = \sqrt{\frac{2nk_BT}{m}}$  $\therefore dN_{u} = N\left(\frac{m}{2\pi k_{B}T}\right)^{3/2} \left(\frac{2\pi k_{B}T}{m}\right)^{3/2}$  $dN_u = N\left(\frac{u}{2\pi k_BT}\right)^2 e^{-\frac{uu^2}{2k_BT}} du$ Sluilarly, dNo = N(\frac{m}{2\tau KBT})^2 e^{-\frac{mv}{2KBT}} dv  $dN_{\omega} = N\left(\frac{m}{2\pi K_{B}T}\right)^{\gamma_{2}} e^{-\frac{m\omega^{2}}{2K_{B}T}} d\omega$ 

## Average velocity, RMS velocity, Most probable velocity

Ava. velocity 
$$\langle c \rangle = \frac{M_1C_1 + N_2C_2 + \cdots}{N_1 + N_2 + \cdots} = \frac{\sum N_1 \cdot c_1}{\sum N_1}$$

$$= \int_{0}^{\infty} \frac{cdN_c}{N} = \frac{N_1C_1}{N_1 + N_2 + \cdots} = \frac{\sum N_1 \cdot c_1}{\sum N_1}$$

$$= \int_{0}^{\infty} \frac{cdN_c}{N} = \frac{N_1C_1}{N_1 + N_2 + \cdots} = \frac{\sum N_1 \cdot c_1}{\sum N_1}$$

$$= \int_{0}^{\infty} \frac{cdN_c}{N} = \frac{N_1C_1}{N_1 + N_2C_2 + \cdots} = \frac{\sum N_1 \cdot c_1}{\sum N_1}$$

$$= \int_{0}^{\infty} \frac{cdN_c}{N} = \frac{N_1C_1}{N_1 + N_2C_2 + \cdots} = \frac{N_1C_1}{\sum N_1} = \frac{N_1C_1}{N_1 + N_2C_2 + \cdots} = \frac{N_1C_1}{\sum N_1} = \frac{N_1C_1}{N_1 + N_2C_2 + \cdots} = \frac{N_1C_1}{\sum N_1} = \frac{N_1C_1}{N_1 + N_2C_2 + \cdots} = \frac{N_1C_1}{\sum N_1C_1} = \frac{N_1C_1}{N_1C_1} = \frac{N_1C_1}{N_1C_$$

RMS velocity 
$$c_{rms}^2 = \frac{\sum N_1 c_1^2}{\sum N_1} = \frac{1}{N} \int_0^{\infty} c^2 dNe$$

$$= 4\pi \Lambda^3 \int_0^{\infty} c^4 e^{-bc^4} dc$$

$$= 4\pi \Lambda^3 \int_0^{\infty} \frac{e^2}{b^2} e^{-\frac{b}{2}} \frac{d^4 \sqrt{b}}{2b\sqrt{2}}$$

$$= \frac{4\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{2/2}}{2^{5/2}} dt = \frac{4\pi \Lambda^3}{2b^{5/2}} \Gamma(\frac{5/2}{2})$$

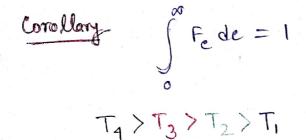
$$= \frac{4\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{2/2}}{2^{5/2}} dt = \frac{4\pi \Lambda^3}{2b^{5/2}} \Gamma(\frac{5/2}{2})$$

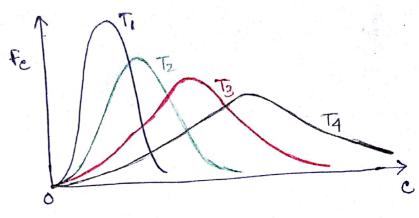
$$= \frac{4\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{2/2}}{2^{5/2}} dt = \frac{4\pi \Lambda^3}{2b^{5/2}} \Gamma(\frac{5/2}{2})$$

$$= \frac{3\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{2/2}}{2^{5/2}} dt = \frac{4\pi \Lambda^3}{2b^{5/2}} \Gamma(\frac{5/2}{2})$$

$$= \frac{3\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{2/2}}{2^{5/2}} dt = \frac{4\pi \Lambda^3}{2b^{5/2}} \Gamma(\frac{5/2}{2})$$

$$= \frac{3\pi \Lambda^3}{2b^{5/2}} \int_0^{\infty} e^{-\frac{b}{2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \frac{e^{-\frac{b}{2}}}{2^{5/2}} \int_0^{\infty} \frac{e^{-\frac{b}{2}}}{2$$





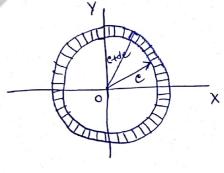
Also, no. of molecules colliding per unit area per unit time  $dn = \frac{1}{4} n\bar{c} = \frac{1}{4} n \sqrt{\frac{8k_BT}{m\pi}} = \frac{1}{4} \frac{\rho}{k_BT} \sqrt{\frac{8k_BT}{m\pi}} \quad (as \ \rho = nk_BT)$ 

$$du = \frac{P}{\sqrt{2m\pi K_BT}}$$

In the velocity distribution in two dimension is  $\frac{m(u+v)}{2\kappa_B T}$  and  $\frac{m}{2\kappa_B T}$  e  $\frac{m(u+v)}{2\kappa_B T}$  duche. From this, find the distribution of molecular speed. Using that, find  $\frac{1}{2\kappa_B T}$  cu,  $\frac{1}{2\kappa_B T}$  of  $\frac{1}{2\kappa_B T}$  and  $\frac{1}{2\kappa_B T}$  duckers.

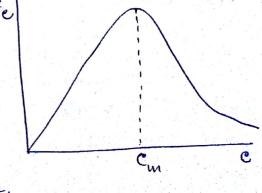
2 = 2 2

Take two woncentric circles between velocity C & C+de, area dudy =  $\pi(c+de)^2 - \pi e^2 = 2\pi e de$ .



$$e^{-\frac{m^2}{2\kappa_BT}} = n\left(\frac{m}{2\kappa_BT}\right) = \frac{m^2}{2\kappa_BT} = \frac{1}{2\kappa_BT} =$$

 $\frac{df_c}{dc}\Big|_{c=cm} = 0$   $\frac{d}{dc}\Big|_{c=cm} = \frac{m^2/2k_BT}{m^2}\Big|_{c=cm} = 0$ or  $1-\frac{2}{cm} = 0$  or  $c_m = \sqrt{\frac{k_BT}{m}}$ 



please also calculate in seduc & inseduc.

convince yourself that 
$$c_{rms} = \sqrt{\frac{2k_BT}{m}}$$
 and  $\overline{c} = \sqrt{\frac{7k_BT}{2m}}$ .

2. Using naxwell velocity distribution, calculate the probability that the velocity of 02 molecule lies between 100 m/s &

$$dM_c = 4\pi N \left(\frac{m}{2\pi k_B T}\right)^{3/2} e^{-\frac{mc}{2k_B T}} c^2 dc.$$

:. Probability 
$$P = \frac{dN_c}{N} = 4\pi \left(\frac{m}{2\pi k_B T}\right)^2 e^{-mc/2k_B T} e^{2c} - 1$$

Now 
$$M = \frac{M}{N} = \frac{32 \text{ gm}}{6.023 \times 10^{23}} = 5.31 \times 10^{-26} \text{ kg}$$
.

$$T = -73e = 200K$$
,  $C = 100 \text{ m/s}$ ,  $de = 101-100 = 1\text{ m/s}$ .

$$P = 4\pi \left[ \frac{5.31 \times 10^{-26}}{2\pi \times 1.38 \times 10^{-23} \times 200} \right]^{\frac{3}{2}} \times \exp \left[ -\frac{5.31 \times 10^{-26} \times 10^{4}}{2\times 1.38 \times 10^{-23} \times 200} \right] \times 10^{4} \times 10^{4}$$

$$= 4\pi \times 5.36 \times 10^{-9} \times 0.9 \times 10^{4} = 6.06 \times 10^{-4} = 0.06\%$$

3. Compute the fraction of molecules of a gas possessing speeds within 1% of the most probable speed.

$$C_{\rm m} = \sqrt{\frac{2\kappa_{\rm B}T}{m}}$$

fraction = probability P in equation ( above with c=cm

den is 1% of Cu As Chin

As c varies within 1% of Cm = [0.99 Cm, 1.01 Cm]

$$P = \frac{4}{\sqrt{N}} \left( \frac{M}{2K_{B}T} \right)^{\frac{3}{2}} e^{-\frac{1}{2}} \frac{2K_{B}T}{M} \sqrt{\frac{2K_{B}T}{M}} \times 0.02$$

- 1. At what value of speed c will the Maxwell's distribution Fe yield same magnitude for a mixture of hydrogen f helium gases at 27°c?
  - 2. Find (c) using fc.
  - 3. Molecular mass of an ideal gas of 02 % 32. Calculate Cm, c, cms of the gas at 27c. (Given R=8.3 J/c/mol)
  - 4. Convince yourself that  $\frac{RT}{M} = \frac{l}{l}$ . Using that, calculate Cm, c, Coms of the molecules of gas at densily 1.293 × 10<sup>-3</sup> gm/ce at 76 cm of Hg pressure.
    - 5. The quantity  $(c-\bar{c}) = c^2 2c\bar{c} + \bar{c}^2$  is squared diviation of atomie speed from average speed. Calculate the average value of this using Maxwell distribution I obtain the rms deviation.

Maxwell's distribution in reduced formal

dNe = 4 TN ( m 3/2 e me/2kBT c2de with respect to  $C_{\rm m} = \sqrt{\frac{2\kappa_{\rm B}T}{\rm m}}$ , non dimensionalized  $U = \frac{c}{C_{\rm m}}$ Substitute C = J2KBT U,

dNc = 4 TN ( m )3/2 2KBT U2 \( \frac{2KBT}{m} dU \end{array} \)

 $dN_{U} = \frac{4N}{\sqrt{\pi}} U^{2} e^{-U^{2}} dU.$ 

This distribution is independent of temperature.