Rule of thumb: Every material (solid, liquid, gas, plasma, intermedial phases) are made of atoms. They "may" attract or repel I form molecules of liquid or be restricted in definite shape of solid by huge cohesive force.

Experimental hints in favour of K.T.

1. Diffusion and Solution: John slowly poured to cozgas? Alcohol over water, it g diffusion spreads throughout.

- 2. Expansion of substance with heat: atoms tend to move away.
- 3. Phenomena of evaporation & vapour pressure.
- 4. Brownian motion. 1827 R. Brown + incessant motion of poleny on water.

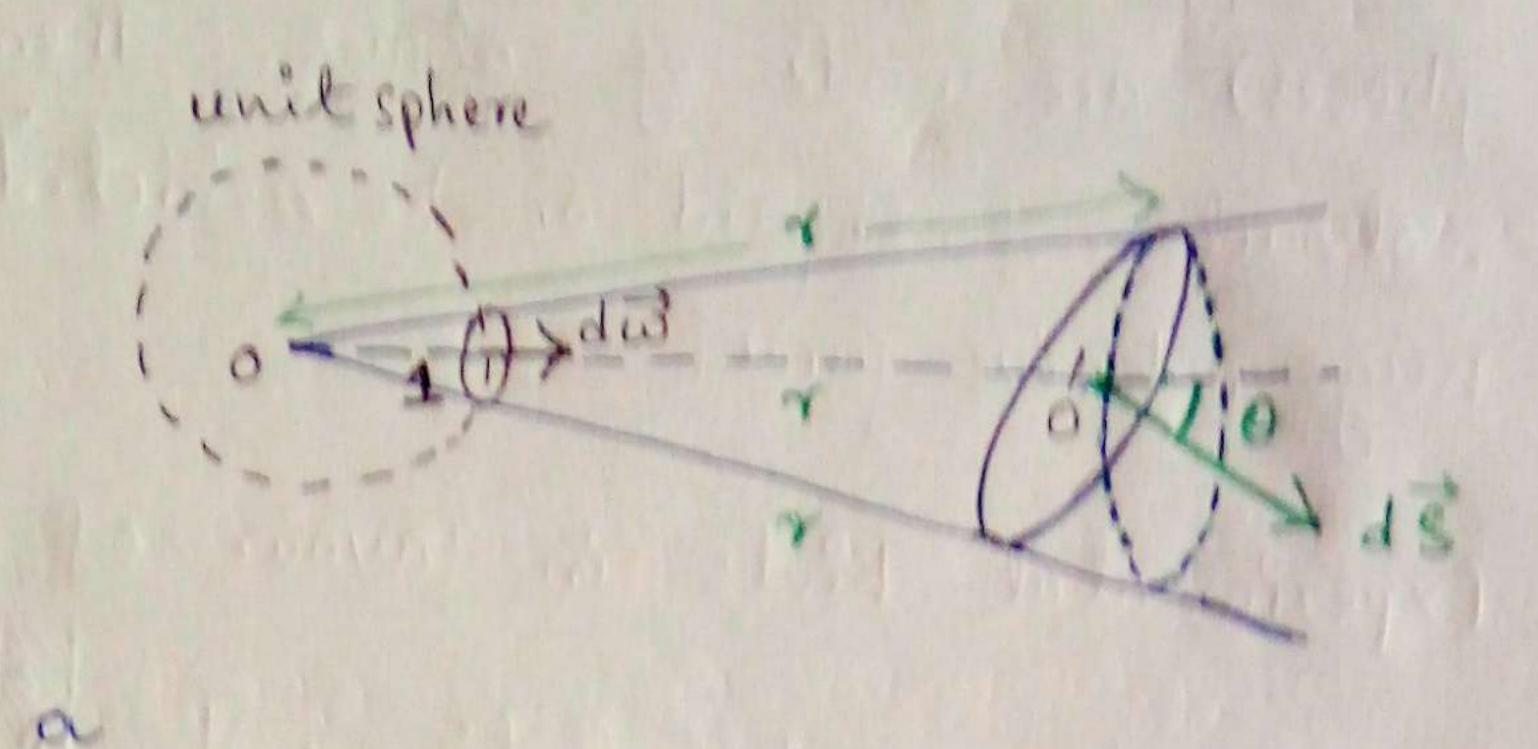
## Basic assumptions & postulates of K.T.

- 1. A gas consists of large number of identical atoms, which are rigid, elastic & equal mass objects.
- 2. Atoms are in chaos + motion is fully irregular & spans in all three directions.
- 3. Inevitably the gas molecules collide with each other & surface of container ( wall, sphere, cylinder). Total K.E. remains constant, but relocity of each atom continuously changes both in magnitude & direction. In evolving state Cintermediate) density in a volume element will change but in steady state, collicions do not affect the density
- 4. In between two successive collisions, molecules move in straight.
  Line following Newton's law.
- 5. Collisions are perfectly elastic i.e. no force of attraction repussion (P.E. =0), energy is fully kinetie.

6. Atoms are "point" mass meaning, their lotal volume Kake volume of the container.

## Concept of solid angle

Solid angle subtended by an area at a point is defined as the area Entercepted by the cone on a unit sphere Cravius = 1) with its centre at the apex of the

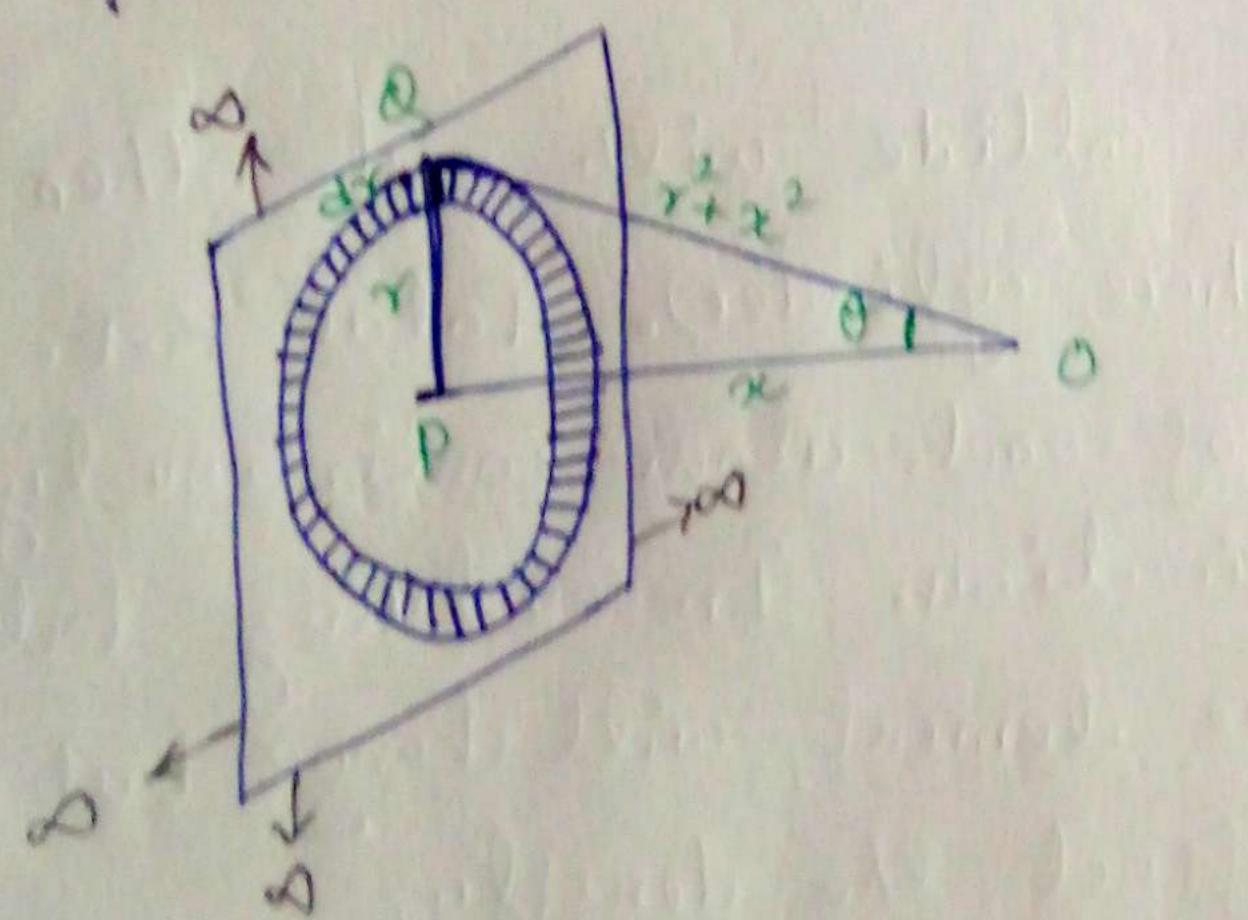


If ds is an area that makes a solid angle dw at origin 0 at a distance oo'= r, then from similar figures

$$\frac{d\omega}{r^2} = \frac{dS\cos\theta}{r^2} :: d\omega = \frac{dS\cos\theta}{r^2}$$

unit of solid angle = steradian.

1. Calculate the soled angle (a) subtended by an infinite plain at a point in front of it, (b) hemisphere and (c) Jull sphere at its center.

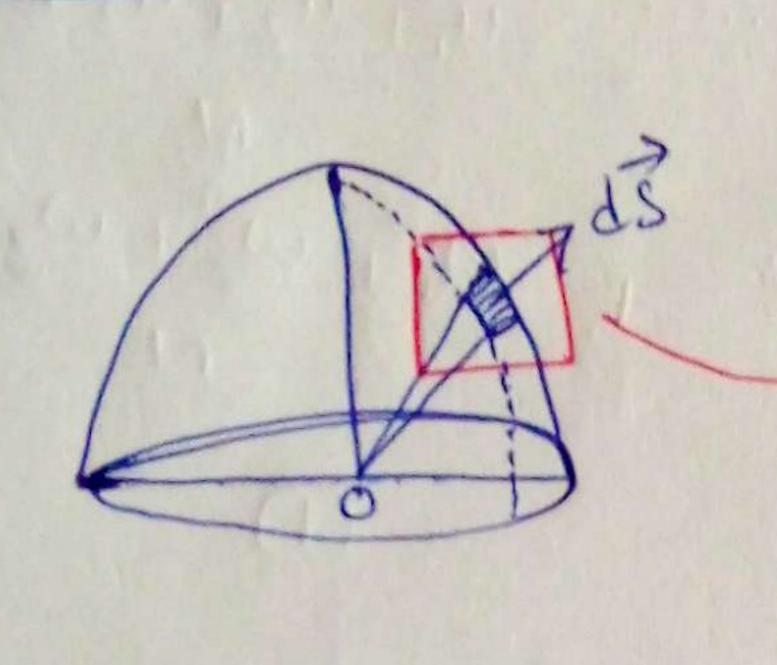


Consider the annular ring, or distance apart from P & thick do. Area of this ring = T(T+dT)^2-Tr = 2 Kodr (N.B. we throw o(dr) term in limit dr +0)

So solid angle subtended by that circular annulus  $d\omega = \frac{ds \cos \theta}{og^2} = \frac{2\pi r dr \cos \theta}{r^2 + x^2}$  Infinite plain meaning o going from 0 4 7/2.  $-i. \quad \omega = \int_{-\infty}^{\infty} \frac{2\pi r \, dr \, \cos \theta}{r^2 + n^2}$ [r=xland  $= 2\pi \int_{0}^{\pi/2} 2 \tan \theta \operatorname{asec}^{2} d\theta \operatorname{d} \theta \cos \theta$   $= 2\pi \int_{0}^{\pi/2} 2 \tan \theta \operatorname{asec}^{2} \theta \operatorname{d} \theta \cos \theta$ dr = x sectodo & 2+ x2 = 2 secto]

 $= 2\pi \int^{\pi/2} \sin \theta d\theta = 2\pi.$ 

Henrisphere



a = sino

= area PBRS = adø x rd0 = rzinododø.

Full sphere solid angle subtended =  $\int \int \int \sin \theta d\theta d\theta d\theta = 4\pi$ .

We will find out now pressure exerted by a perfect gas from K.T. (a) collisionless atoms in a box moving in 3 directions, (b) collisionless atoms coming from all directions.

collision will be dealt in mean free path!

Method 1 AB = AD = AE = 1 The gas is confined within this cube of volume 13. P (say) is a gas atom

PAR LE

with velocity "c" whose components in 3-direction is (u, v, w). N = total no. of atoms or molecules.

So each of them have different velocity c, c2, c3, c4, ... etc so different components (u,,v,,w,), (u2,v2,w2), (u3,v3,w3), ....

Mean square average  $c^2 = q^2 + q^2 + q^2 + \cdots = u_1^2 + u_2^2 + u_3^2 + \cdots$  $+\frac{v_1^2+v_2^2+v_3^2+\cdots}{N}$   $+\frac{w_1^2+w_2^2+w_3^2+\cdots}{N}$  $= \frac{12}{u^2} + \frac{1}{v^2} + \frac{1}{w^2}$ mean square velocity in Y-direction to-direction.

X-direction

Consider particle p with man un, relocaty == (u,v,w). It travels from ABCD to EFGH, makes collision to exert pressure, rebounds dastically, momentum gets changed, comes back to ABCD to make another collission.

Total distance traveled with velocity u is 21.

:. Time between collission = 21, meaning number of collission per second =  $\frac{u}{2l}$ .

Momentum imparted in +X direction of on EFGH = mu.

Momentum obtained in -X direction after collission = -mu.

: change of momentum = mu-(-mu) = 2mu.

Rate of change of momentum for one atom in X direction

= 2mux \( \frac{u}{2l} = \frac{mu^2}{l}.

Similarly in Y and Z direction, rate of change of momentum is most & must for one atom

:. Total rate of change of momentum for all outoms per unit area along x direction is

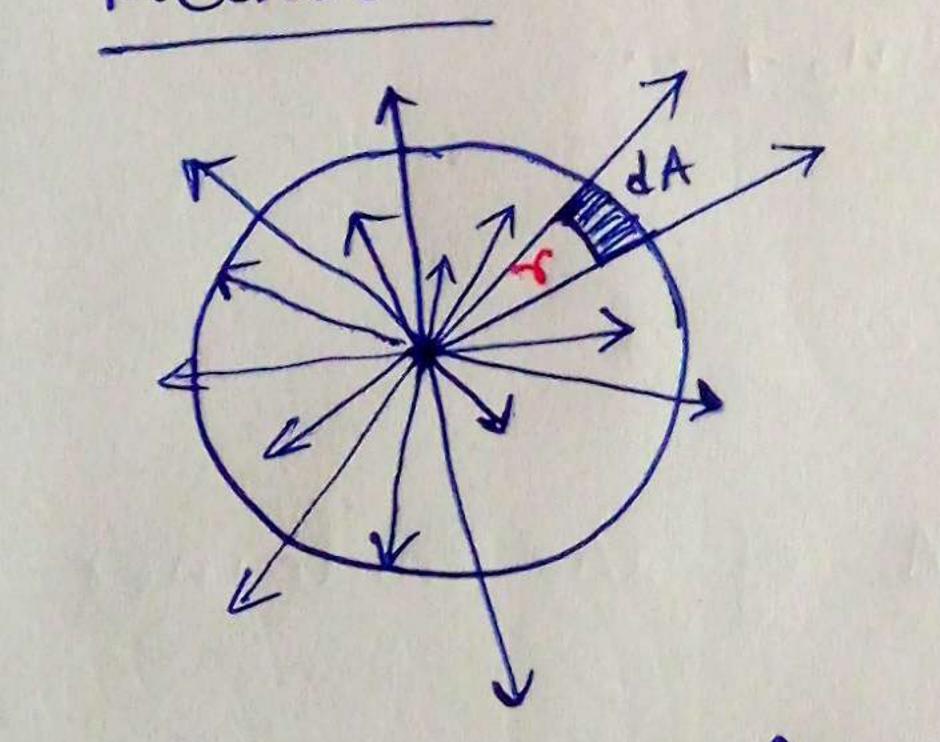
 $P_{x} = \frac{m(u_{1}^{2} + u_{2}^{2} + u_{3}^{2} + \cdots)}{l} \times \frac{1}{l^{2}} = \frac{mu^{2}N}{l^{3}} = \frac{mnu^{2}}{l}$  (see eq. 0) Similarly Py = mnv², Pz = mnw².

In steady state, molecules more in all directions, so no preference, meaning  $\bar{u}^2 = \bar{v}^2 = \bar{w}^2$ ,  $f P_x = P_y = P_z$ . meaing  $\bar{u}^2 = \bar{v}^2 = \bar{w}^2 = \frac{1}{3}\bar{c}^2$  (See eq. (1)

collecting all pieces together,

$$P_{\chi} = P_{y} = P_{z} = \frac{1}{3} \text{ mnc}^{2}$$

Method 2



N no. of molecules moving in all directions with all possible velocity. How many collide with vessel & insert pressure?

number of vectors per unit area =  $\frac{N}{4\pi r^2}$ 

: number of molecules at dA is  $\frac{NdA}{4\pi r^2}$ 

We already learned that dA = vsinddodd

 $\frac{1}{4\pi v^2} = \frac{N}{4\pi} \sin\theta d\theta d\phi$ 

:. number of molecules per unit volume within velocit range c 1 c+de [dne], within direction 010+d0 & \$\phi + d\phi
[dw = sinddod\$]

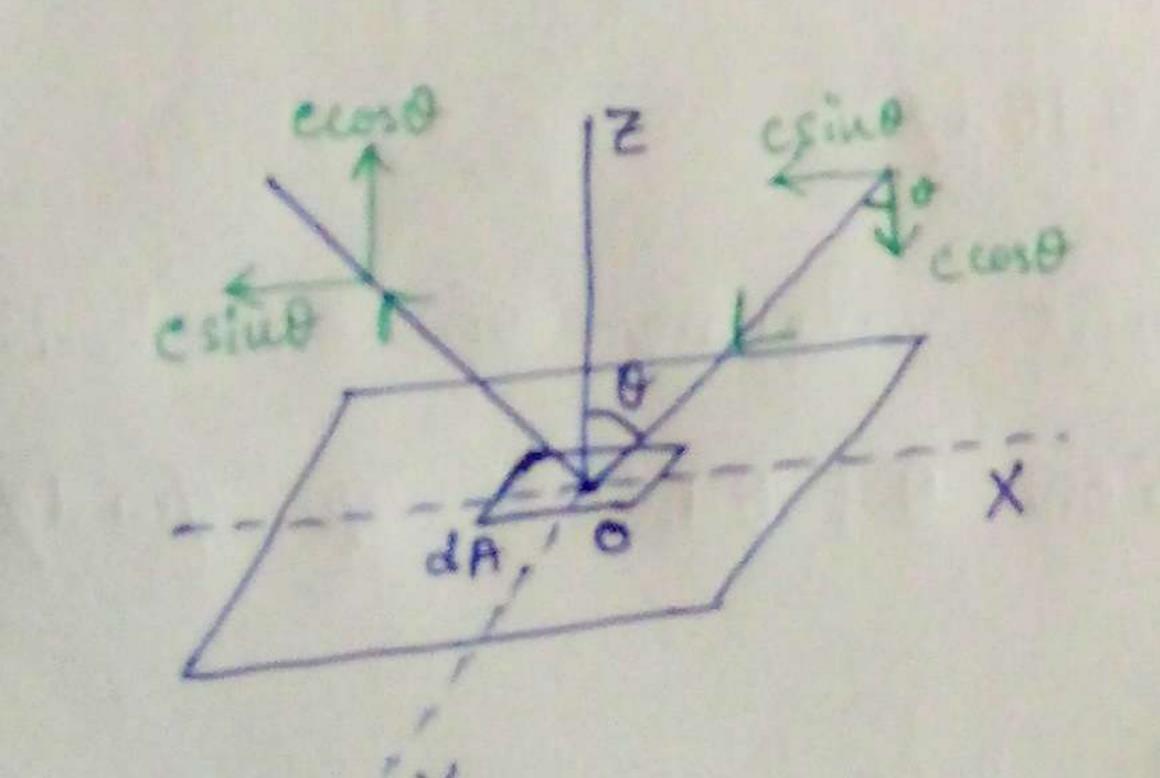
 $= \frac{dn_e}{4\pi} \sin \theta d\theta d\phi$ dnc,0,0

Let's find now, how many of them strike dA of the wall of container. Geometrically, this is the number of molecules within the slanted prism of length cdt with edges in the direction  $0 \neq \emptyset = \frac{dn_c}{4\pi} \sin\theta d\theta d\phi \times cdA\cos\theta dt$ « Total number of collisions at dA per unit time  $\int_{0}^{\infty} \int_{0}^{\infty} \int_{0}^{\infty} \frac{dn_{e}}{4\pi} \sin\theta d\theta d\phi \times cdA \cos\theta$ C=00=00=0 A7  $= \frac{dA}{4\pi} \int_{0}^{\infty} c du_{e} \int_{0}^{\infty} siu\theta \cos\theta d\theta \int_{0}^{\infty} d\phi = \frac{dA}{4} \int_{0}^{\infty} e du_{e}.$ 

of n, atoms per unit volume moves with relocity 9,

u, 9 + n2 c2 + n3 c3 + ... average velocily \( \bar{c} = W1+ N2+ N3+ -.. = Znici = inschue

.. Number of molecules colliding at dA of the container per unit time =  $\frac{dA}{4}$  nc



Now let's compute change in momentum by molecules striking area dt in unit time.

normal component of incident momentum is me cost 1 reflected momentum - me cost.

So each octour had a change in mamentum 2 mc cost. : Total change of momentum experienced by all gas atoms/molecules colliding to area dA, per unit time is  $\int_{0}^{\pi} \int_{0}^{\pi} \int$ c=0 0=0 Ø=0  $= \frac{m dA}{2\pi} \int_{C=0}^{\infty} c^2 dn_e \int_{C=0}^{7/2} \cos^2 \theta \sin \theta d\theta \int_{C=0}^{7/2} d\theta = \frac{1}{3} \operatorname{mdA} \int_{C=0}^{7/2} c^2 dn_e$ .. Force exerted by gas atoms on dA is F = \frac{1}{3} mdA nc Thus, pressure exerted  $p = \frac{F}{dA} = \frac{1}{3} \text{ mnc}^{-1}$ Corollary from above,  $P = \frac{1}{3}e^{\frac{2}{3}}$   $\overline{c} = \frac{3P}{J^2}$ for Hydrogen  $P = 8.9 \times 10^{-5}$  gm/ee. 1 atom pressure  $P = h g = 76 \times 13.6 \times 981$  dynes/cm<sup>2</sup>  $\therefore \ \, \overline{C} = \sqrt{\frac{3 \times 96 \times 13.6 \times 981}{8.9 \times 10^{-5}}} = \frac{\times 10^{5}}{1.85} \, \text{cm/sec}.$  $C_{1} = 3 \times 10^{8} \text{ m/s}, \quad C_{2} = 300 \text{ m/s}$   $C_{2} = 3 \times 10^{10} \text{ cm/s}, \quad C_{3} = 3 \times 10^{10} \text{ cm/s}.$ 

Kinetie interpretation of temperature From K.T.  $P = \frac{1}{3} \text{ mnc}^2 = \frac{1}{3} \text{m} \frac{N}{V} = \frac{1}{2}$ · PV = 1 mNc<sup>2</sup> = RT [Boyle's law] But we assume!  $\tilde{c} = \int \frac{3RT}{mN} = \int \frac{3RT}{M}$  where M = molecular weight RMS velocity of gas atom is proportional to square root of absolute temperature. As from T=0, \(\bar{e}=0\) ie. absolute zero temperature is where molecule cease to move. Now = 3RT = 3RT. divide by N, zmē = 3 KT, abs. temp. KB = Boltzmann's constant. mean K.E. for a given T, there is always a K.E. I molecular collission lead to uniform T. Boyle's law from K.T. PV = \frac{1}{3}M\tilde{c}^2 \times \text{ because } \tilde{c}^2 \tau T.

So if T is fixed \tilde{c}^2 is constant so PV = constant. Charle's law from Kit. Again État, so pvat. i.e. VdT when p = constant.

For same T & P, equal V of gases contain equal number of atoms.

P= \frac{1}{3} \m, \frac{N\_1}{V} \cdot \frac{1}{C\_1}^2
P= \frac{1}{3} \max \frac{N\_2}{V} \cdot \frac{1}{C\_2}^2 P.V. N. P.V. 2 · m, N, G= m2 N2 C2

so K.F. is equal. But Tis equal,

 $\frac{1}{2}m, \overline{c_1}^2 = \frac{1}{2}m_2\overline{c_2}^2 \Rightarrow m_1\overline{c_1}^2 = m_2\overline{c_2}^2$ 

.. N<sub>1</sub> = N<sub>2</sub>

Clapeyron's equation from K.T.

= 1/N x 3 MC  $P = \frac{1}{3} \text{ mne}^2 = \frac{1}{3} \frac{n}{N} \text{ mNe}^2$ 

 $= \frac{n}{N} RT = nK_BT \cdot \left[ K_B = \frac{R}{N} \right]$ 

N = 6.023 × 10<sup>23</sup> atoms/mole.

Universal gas constant R PV=RT.

 $R = \frac{PV}{T} = \frac{(76 \times 13.6 \times 981) \times 22.4 \times 10^3}{}$ 

= 8.31 × 107 dynes-cm/k/mole or erg/degk/mole.

in heat units, =  $\frac{8.31 \times 10^7}{4.18 \times 10^7}$  = 2 cal/degK/mole

 $\frac{8.31\times10^{7}}{6.023\times10^{23}}=\frac{1.38\times10^{-16}}{10^{23}}=\frac{1.38\times10^{-16}}{10^{23}}$ 1 KB = B =