



S = rectangular slit, XY = wire with thickness d. At point & outside the

geométrical shadow intensity distribution à same as straight edge at X and so diffraction bands of unequal width is formed above M & below N. These bands are independent of thickness of wire and effect on other side à negligible (because wire stops the important half-period strips).

within geometric shadow, interference fringes appears. Effect due to Ax of cylindrical wave-front at p in geometrical shadow is entirely due to few half-period strips at X, so a small luminous source an be thought at X. Similarly for BY partien, Y is a luminous source. If $PY-PX = n\lambda$, point P will be bright and = $(2n+1)\frac{1}{2}$, P will

Equal interference fringe width $\beta = \frac{D}{d}A$.

D = distance of screen from obstackle (wire)
d = tickness of obstackle (wire) diameter).

point c will be always bright as waves from X & Y always meet in phase. for moderate value of d pattern is shown, while as d is increased, & decreases finally to disappear, so only diffraction band above M & below N & seen.

plane waves of monochromatic light. The diffracted light is received on a distant screen which is gradually moved towards the aperture. If the centre of the circular patch of light first becomes dark, when the screen is 30 cm from the aperture, find the wavelength of light used.

Aperture diameter $2r = 1.2 \text{ mm} = 1.2 \times 10^{-3} \text{ m}$ So radius $r = 0.6 \times 10^{-3} \text{ m}$, a = 30 cm = 0.3 m.

for the first minimum on the axial point, the aperture must have 2 half-period 20nes. So $n = \frac{\pi r^2}{\pi a n} = 2$.

$$\alpha A = \frac{x^2}{2a} = \frac{(0.6 \times 10^{-3})^2}{2 \times 0.3} = 6 \times 10^{-7} \text{m} = 6000 \text{ Å}.$$

Cyl light of wavelength 6000 Å passes through a narrow circular aperture of radius 0.9 × 10 m. At what distance along the axis will the first maximum intensity be observed?

$$a = 6000 \times 10^{-10} \text{ m}, \quad r = 0.9 \times 10^{-3} \text{ m}. \quad \alpha = ?$$

for first maximum intensity
$$a^2+r^2=\left(a+\frac{\lambda}{2}\right)^2$$

$$\alpha = \frac{\pi^2}{\lambda} = \frac{(0.9 \times 10^{-3})^2}{6000 \times 10^{-10}} = 1.35 \text{ m}.$$

Fresnel Diffraction Integral

Omitting the time dependent factor e-int disturbance received at & from a source S trat emit monochromatic spherical wave, is A eikto According to Fresnel Huygen's theory we consider each element on the source of secondary

wavelet, so that wibribution est screen at P due to elimentary area ds at & b

elet, so that contribution at strain at the desired at
$$\frac{e^{ikr}}{du(r)} = \frac{e^{ikr}}{r_0} + \frac{e^{ik$$

For a plane wave of amplitude 3 A incident normally on aperture duce) = Ae'E' ds.

So total contribution at P due to whole wavefront is ucp) = c SS A e iki d5d7.

In principle A = A(5,7) but in absence of aperture A = constant. and $c = -\frac{i\kappa}{2\pi} = \frac{1}{i\lambda}$, so that $u(p) = \frac{A}{i\lambda} \iint \frac{e^{ik\tau}}{\tau} ds d\tau$ Two assuptions that are made is (i) screen does not affect the field at P, so dimension of apesture >> wavelength, (ii) C(x)

$$= 0 \quad \text{so that} \quad C(x) = C(1 + \omega_5 x) \approx 0.$$

$$Now \quad \alpha = \sqrt{(x - 5)^2 + (y - n)^2 + 2^2} = 2\sqrt{1 + \frac{(x - 5)^2 + (y - n)^2}{2^2}} = 2\sqrt{1 + 4}$$

$$\approx 2(1 + \frac{4}{2} - \frac{4}{8}^2 + \cdots) = 2 + \frac{(x - 5)^2}{22} + \frac{(y - n)^2}{22}$$

$$\therefore u(p) = \frac{1}{(n + 2)^2} e^{ikz} \iint A(5, n) e^{\frac{ik}{2}[(x - 5)^2 + (y - n)^2]} d5dn$$

where we have replaced & by 2 in denominator safely.

" u(ρ) ~ 1 eikz e ikz e ik (x²+y³) [A(S, η) e ik (s²+η²) e i(ug+ν²) dsdη where $u = \frac{2\pi x}{\lambda t}$ and $v = \frac{2\pi y}{\lambda t}$ (Spatial frequencies) This is called "Fresnel diffraction integral" with "fresnel approximation" or <4 neglected, so maximum place change is less than T, so I KZX << T (2 >> { \frac{1}{42} [(x-5)^2 + (y-7)^2]_{max}^2 \} - 0 7>> \[\frac{1}{4\pi}(\pi^2+\yi)^2\right]^3 \] for circular aperture with radius a when observed in region of dimension/a So if a=0.1 cm & observed region is radius 1 cm then x+y= x=10in then for $\lambda = 5 \times 10^{-5} \text{ cm}$, 2 >> 17 cm. In "Fraunhofer approximation", Z>> large so that e 2 (5+2) &1 which means maximum place change is way less than T. So in addition to 2 << neglected (or condition O), Z>> [5+2] max > so Z>> 2/2 (circular apesture) mis is called "Fraunhofer diffraction integral." So fresnel number $N_F = \frac{a^2}{22} <<1$ for fraunkofer approximation. Fresnel Integral => c(r) = 5 cos(\frac{\tau^2}{2}) du, s(\ta) = \int \sin(\frac{\tau^2}{2}) du property: c(-rc) = -c(r) c(A) = s(A) = 0.5S(T) C(0) = S(0) = 0. (r)2 - = (r-)2" Cornu's "