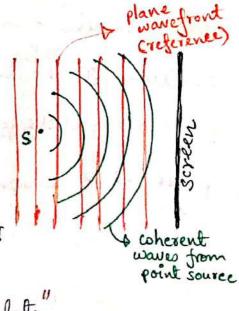
HOLOGRAPHY

In Breek, holography means whole writing. A regular shotograph is a two dimensional snapshot of a 3D object whose intensity distribution projected on a plane is recorded. Denis Gabor invented in 1947 a technique in which the last phase as well as the 3D nature of intensity is recorded. It is a two step procen by which (1) an object illuminated by whereat light makes interference fringes in a photographic envelopment light of same wavelength to produce 3D image. Coherent source (Laver) was developed in 1960 & Gabor received Nobel phize is Physics in 1971 for 3D lenslen method of photography.

Bask Principles of Holography

Consider the interference pattern caused by coherent monochromatic plane waves incident on a point scatterer S. Concentric bright of dark circles will be formed by superposition of scattered light I reference beam. The developed screen (plate) cotain light of dark partially absorbing fringe pattern, called "Gabor zone plate".

Since the reference beam is assumed to be in contant place across the hologram plate fringes at any point P will be separated by At that emespond to path difference of A.

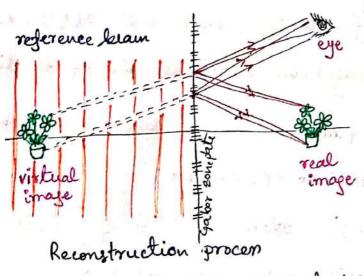


R

D -d

d = R - D $d = N\lambda = \frac{q^2}{2R - D}$ This plate is then illuminated by plane coherent waves in the absence of scatterer S. Light formed by interference between light and dark bands will now produce first order interference maxima at 0 that corresponds to Arsino = 2. This light will appear to diverge from S, so a virtual image can be seen from the right side of hologram.

Suppose now two scattering center S, S2 are present on left I each will record a Gabor zone plate on plate. The reconstruction well produce a virtual image of both scatterers. Extending this argument le continuum of scattering centres, hologram will consist of superposed Gabor zone plates. Upon reconstruction,



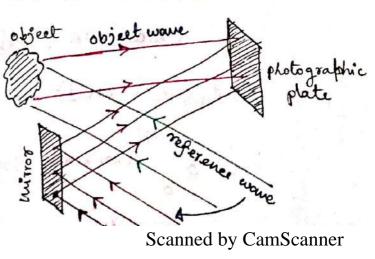
A scattered beam were separated Municated from either side & not necesarily the reference beam is plain.

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the distributed virtual image eye appears like the real image. This is called the on-axis hologrouphy.

In 1962, Leith L Upatneiks image developed off-axis hologram Duto increased wherence length of the laser beam, the reference so that hologram could be



Point Holography - Basic Theory

Recording of the phase distribution of an object wave which is a point scatterer of form $\frac{A}{r}$ cos(kr_wt+ ϕ) if the basic problem.

Recording process: Euppose object wave is $O(x,y) = a(x,y) \times [\phi(x,y) - \omega t]$

du to all point scatterers at the object in plane of photographic plate at 2=0. Suppose reference wome is plane wave propagating in XZ plane inclined at O with Z axis. So,

 $7(x,y,z) = A \cos(\overline{k}.\overline{r} - \omega t) = A \cos(kx \sin\theta + kz \cos\theta - \omega t)$ 80 this field at z = 0 is $y(x,y) = A \cos(kx \sin\theta - \omega t)$ $z = A \cos(2\pi dx - \omega t)$

where $\alpha = \frac{\sin \theta}{\lambda} = \text{spatial frequency. Note that } \tau(x,y) = \tau(x)$ no y dependence because its propagation vector was in XZ direction.

: Total field at photographic plate = object wave + reference wave u(x, y, t) = a(x, y) cos[d(x, y) - wt] + A cos(27dx - wt)

 $= \langle (x,y) = \langle (x,y),t) | u(x,y),t \rangle$ where $\langle \rangle = \langle [a(x,y) | u(x,y),t) \rangle + A | (ux) (2\pi dx - wt)]^2 \rangle$ $= \langle [a(x,y) | ux) [\phi(x,y) - wt] + A | (ux) (2\pi dx - wt)]^2 \rangle$

= $a^2(x,y) \langle \cos^2(\phi(x,y) - \omega t) \rangle + A^2 \langle \cos^2(2\pi dx - \omega t) \rangle$

+ 2 a(1,4) A < LOS[\$(x,4)-wt] LOS (27dx-wt)>

[Now $\langle \cos^2(\phi(x)) - \omega t \rangle$] = $\frac{1}{2\pi} \int_{0}^{2\pi} (\cos^2(\omega t - \phi(x,y))) d(\omega t)$ = $\frac{1}{2\pi} \frac{1}{2} \int_{0}^{2\pi} 2 \cos^2 x dx = \frac{1}{4\pi} \int_{0}^{2\pi} (1 + \cos 2x) dx = \frac{1}{2}$.]

Scanned by CamScanner

 $\langle \omega_{S}[\phi(a,y)-\omega_{t}]\omega_{S}(2\pi dx-\omega_{t})\rangle$ = { (ws[\$(7,4) -2wt+2x2x]> + { (ws[\$(x,4) - 2xdx]> = $\frac{1}{2} < \cos \left[\phi(\alpha, y) - 2\pi dx \right] > = \frac{1}{2} \cos \left[\phi(\alpha, y) - 2\pi dx \right]$ So $I(x,y) = \frac{1}{2}a^{2}(x,y) + \frac{1}{2}A^{2} + Aa(x,y) cos[\phi(x,y) - 2\pi dx]$ Ly phase of object wave

Reconstruction process: By suitable process, the photo plate is developed to obtain hologram such that transmittance is linearly related to I(2,4). So of R(2,4) represents the reconstruction

wave (identical to the reference wave r(x,y), then $\frac{R(x,y)}{2} = R(x,y) \Gamma(x,y) = \left[\frac{1}{2}a^{2}(x,y) + \frac{1}{2}A^{2}\right]R(x,y) + \frac{1}{2}A^{2}$ transmitted recombracted $A a(x,y)R(x,y) \cos \left[\phi(x,y) - 2\pi dx\right]$ field wave

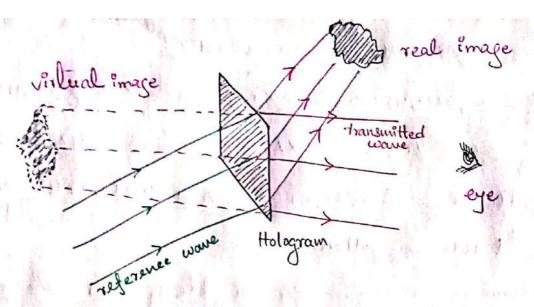
= $\left[\frac{1}{2}a^{2}(x,y) + \frac{1}{2}A^{2}\right]A\omega_{3}(2\pi dx - \omega t) + A^{2}a(x,y) \omega_{3}[2\pi dx - \omega t][\varphi(x,y) - 2\pi dx]$

= $\left[\frac{1}{2}a^{2}(x,y) + \frac{1}{2}A^{2}\right]A\omega_{3}(2\pi dx - \omega t) + \frac{1}{2}A^{2}a(x,y) \left[\omega_{3}\left[\beta(x,y) - \omega t\right]\right]$ + $\frac{1}{2}A^{2}a(x,y) \cos\left[4\pi dx - \beta(x,y)\right]$ + 1 A a (2,4) ws [4xd x - \$(21,4) - wt]

(1) = Reconstruction wave with modulated amplifude due to aca, 1) So this part of total field is travelling in the direction of reconstructed wave.

2) => Object wave O(1,4) that gives a virtual image. The secondmuted object wave travels in same direction as original object wave.

(3) =) Notice that identical to O(X,N) in addition to 4 xdx term place term of (x, v) las a negative sign, meaning this wave has opposite curvature than the object wave, so if object wave is diverging out then this wave is converging in sphrerical wave.



Effect of $4\pi dx$ is understood as follows. If we consider object wave is plane wave propagating along 2 direction then p(x,y)=0 so $\frac{1}{2}$ A a(x,y) cos $[4\pi dx - wt] \sim cos(k'x - wt)$ where previously ksind = $2\pi d$. So that

2/Ksin0 = 47x = K'= Ksin0'

or 0'= sin'(25ino)

So 3 => represents a plane propagating wave along direction of, so $4\pi dx$ rotates the wave direction. so the represents the conjugate of object wave propagating along a different direction from reconstruction wave & object wave. All O, O, 3 propagate in three different directions, they separate after travelling a distance so that observer can view the virtual image without any disturbance.