Rule of thumb: Every material (solid, liquid, gas, plasma, intermedial phases) are made of atoms. They "may" attract or repel I form molecules of liquid or be restricted in definite shape of solid by huge cohesive force.

Experimental hints in favour of K.T.

1. Diffusion and Solution: John slowly poured to cozgas? Alcohol over water, it g diffusion spreads throughout.

- 2. Expansion of substance with heat: atoms tend to move away.
- 3. Phenomena of evaporation & vapour pressure.
- 4. Brownian motion. 1827 R. Brown + incessant motion of poleny on water.

## Basic assumptions & postulates of K.T.

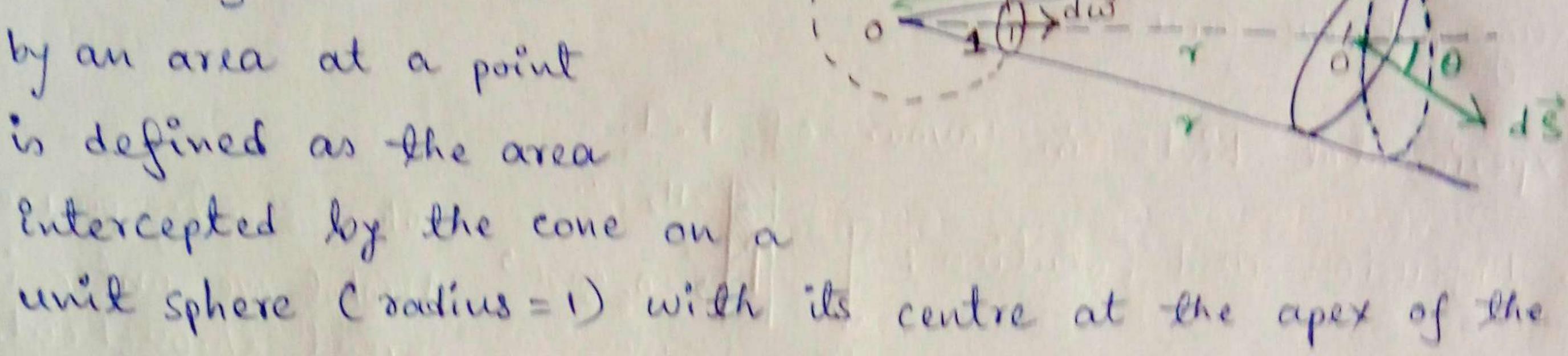
- 1. A gas consists of large number of identical atoms, which are rigid, elastic & equal mass objects.
- 2. Atoms are in chaos + motion is fully irregular & spans in all three directions.
- 3. Inevitably the gas molecules collide with each other & surface of container ( wall, sphere, cylinder). Total K.E. remains constant, but relocity of each atom continuously changes both in magnitude & direction. In evolving state Cintermediate) density in a volume element will change but in steady state, collicions do not affect the density
- 4. In between two successive collisions, molecules move in straight.
  Line following Newton's law.
- 5. Collisions are perfectly elastic i.e. no force of attraction repussion (P.E. =0), energy is fully kinetie.

6. Atoms are "point" mass meaning, their lotal volume Kake volume of the container.

unit sphere

## Concept of solid angle

Solid angle subtended by an area at a point is defined as the area

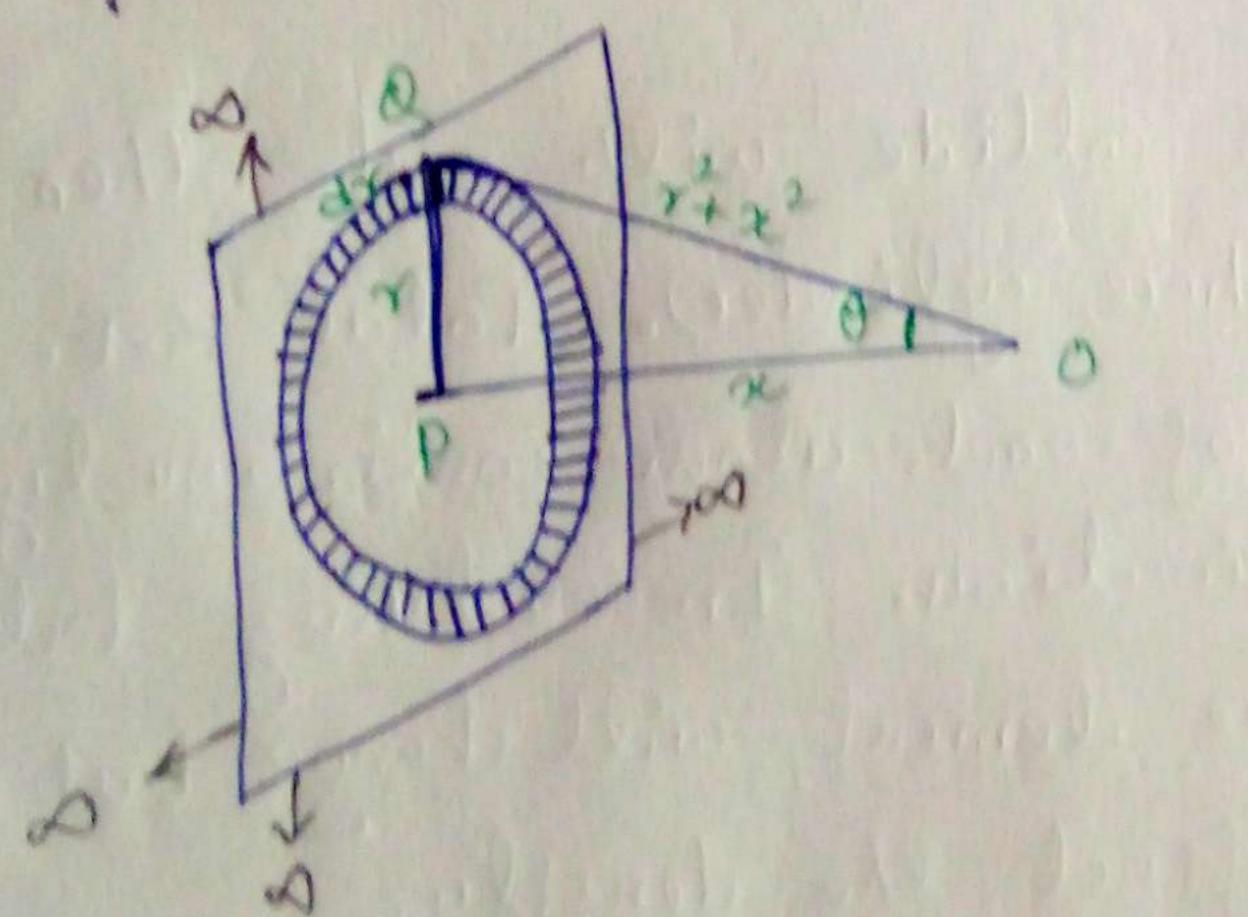


If ds is an area that makes a solid angle dw at origin 0 at a distance oo'= x, then from similar figures

$$\frac{d\omega}{t^2} = \frac{dS\cos\theta}{\tau^2} :: d\omega = \frac{dS\cos\theta}{\tau^2}$$

unit of solid angle = steradian.

1. Calculate the soled angle (a) subtended by an infinite plain at a point in front of it, (b) hemisphere and (c) Jull sphere at its center.



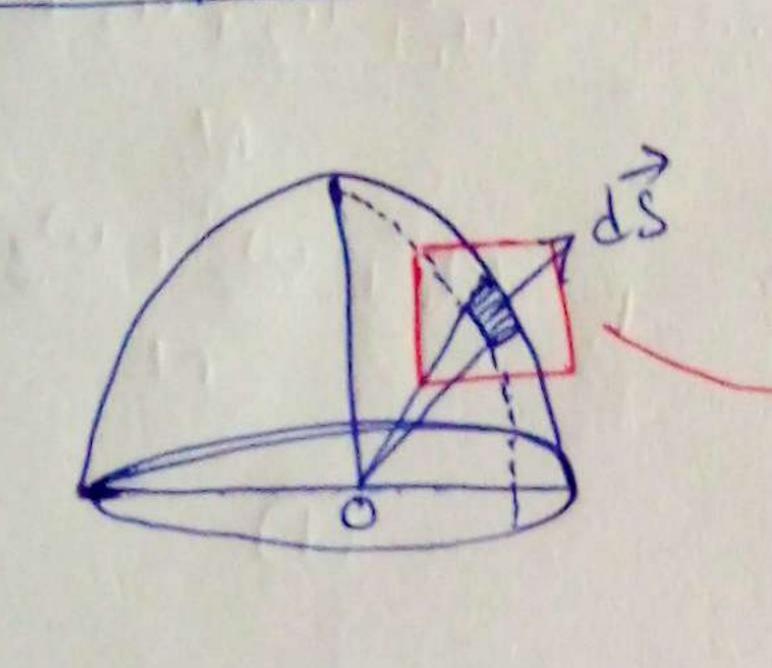
Consider the annular ring, or distance apart from P & thick do. Area of this ring = T(T+dT)^2-Tr = 2 Kodr (N.B. we throw o(dr) term in limit dr +0)

So solid angle subtended by that circular annulus  $d\omega = \frac{ds \cos \theta}{og^2} = \frac{2\pi r dr \cos \theta}{r^2 + x^2}$  Infinite plain meaning o going from 0 4 7/2.  $-i. \quad \omega = \int_{-\infty}^{\infty} \frac{2\pi r \, dr \, \cos \theta}{r^2 + n^2}$ [r=xland  $= 2\pi \int_{0}^{\pi/2} 2 \tan \theta \operatorname{asec}^{2} d\theta \operatorname{d} \theta \cos \theta$   $= 2\pi \int_{0}^{\pi/2} 2 \tan \theta \operatorname{asec}^{2} \theta \operatorname{d} \theta \cos \theta$ 

 $= 2\pi \int^{\pi/2} \sin \theta d\theta = 2\pi.$ 

dr = x sectodo & 2+ x2 = 2 secto]

Henrisphere



a = sino

= area PBRS = adø x rd0 = rzinododø.

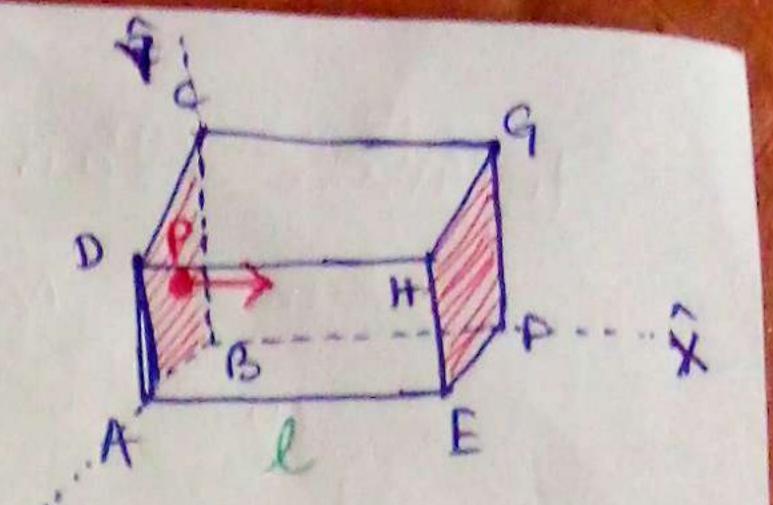
So de at point  $0 = \frac{\sqrt[3]{\sin \theta d \theta d \phi}}{\sqrt[3]{\pi}} \times \cos \theta = \frac{\sin \theta d \theta d \phi}{\sqrt[3]{\pi}}$ . So solid angle subtended =  $\int d\omega = \int \int \int \int \sin \theta d \theta d \phi = 2\pi$ .

Full sphere solid angle subtended =  $\int \int \int \sin \theta d\theta d\theta d\theta = 4\pi$ .

We will find out now pressure exerted by a perfect gas from K.T. (a) collisionless atoms in a box moving in 3 directions, (b) collisionless atoms coming from all directions.

collision will be dealt in mean free path!

Method 1 AB = AD = AE = 1 The gas is confined within this cube of volume 13. P (say) is a gas atom



with velocity "c" whose components in 3-direction is (u, v, w).

N = total no. of atoms or molecules.

So each of them have different velocity c, c2, c3, c4, ... etc so different components (u,,v,,w,), (u2,v2,w2), (u3,v3,w3), ....

Mean square average  $c^2 = q^2 + q^2 + q^2 + \cdots = u_1^2 + u_2^2 + u_3^2 + \cdots$  $+\frac{v_1^2+v_2^2+v_3^2+\cdots}{N}$   $+\frac{w_1^2+w_2^2+w_3^2+\cdots}{N}$  $= \frac{12}{u^2} + \frac{1}{v^2} + \frac{1}{w^2}$ mean square velocity in Y-direction to-direction.

X-direction

Consider particle p with man un, relocaty == (u,v,w). It travels from ABCD to EFGH, makes collision to exert pressure, rebounds dastically, momentum gets changed, comes back to ABCD to make another collission.

Total distance traveled with velocity u is 21.

:. Time between collission = 21, meaning number of collission per second =  $\frac{u}{2l}$ .

Momentum imparted in +X direction of on EFGH = mu.

Momentum obtained in -X direction after collission = -mu.

: change of momentum = mu-(-mu) = 2mu.

Rate of change of momentum for one atom in X direction

= 2mux \( \frac{u}{2l} = \frac{mu^2}{l}.

Similarly in Y and Z direction, rate of change of momentum is most & must for one atom

:. Total rate of change of momentum for all outoms per unit area along x direction is

 $P_{x} = \frac{m(u_{1}^{2} + u_{2}^{2} + u_{3}^{2} + \cdots)}{l} \times \frac{1}{l^{2}} = \frac{mu^{2}N}{l^{3}} = \frac{mnu^{2}}{l}$  (see eq. 0) Similarly Py = mnv², Pz = mnw².

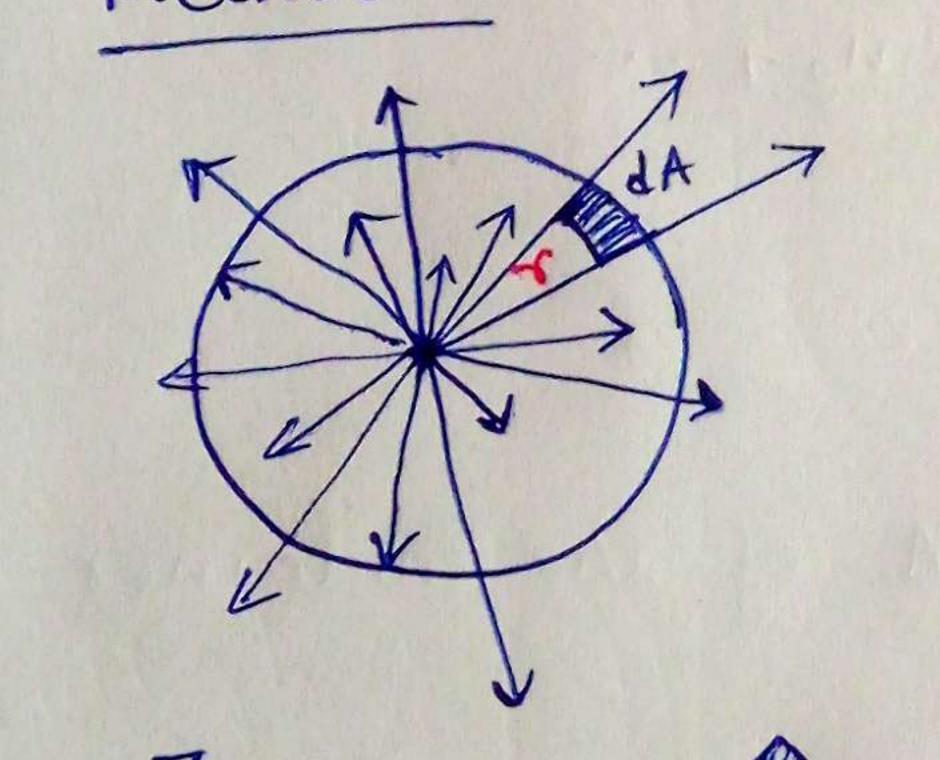
In steady state, molecules more in all directions, so no preference, meaning  $\bar{u}^2 = \bar{v}^2 = \bar{w}^2$ ,  $f P_x = P_y = P_z$ . meaing  $\bar{u}^2 = \bar{v}^2 = \bar{w}^2 = \frac{1}{3}\bar{c}^2$  (See eq. (1)

collecting all pieces together,

$$P_{\chi} = P_{\gamma} = P_{Z} = \frac{1}{3} \text{ mnc}^{2}$$

$$P = \frac{1}{3} mnc^2$$

Method 2



N no. of molecules moving in all directions with all possible velocity. How many collide with vessel & insert pressure?

number of vectors per unit area =  $\frac{N}{4\pi r^2}$ 

: number of molecules at dA is  $\frac{NdA}{4\pi r^2}$ 

We already learned that dA = vsinddodd

 $\frac{1}{4\pi v^2} = \frac{N}{4\pi} \sin\theta d\theta d\phi$ 

:. number of molecules per unit volume within velocit range c 1 c+de [dne], within direction 010+d0 & \$\phi + d\phi
[dw = sinddod\$]

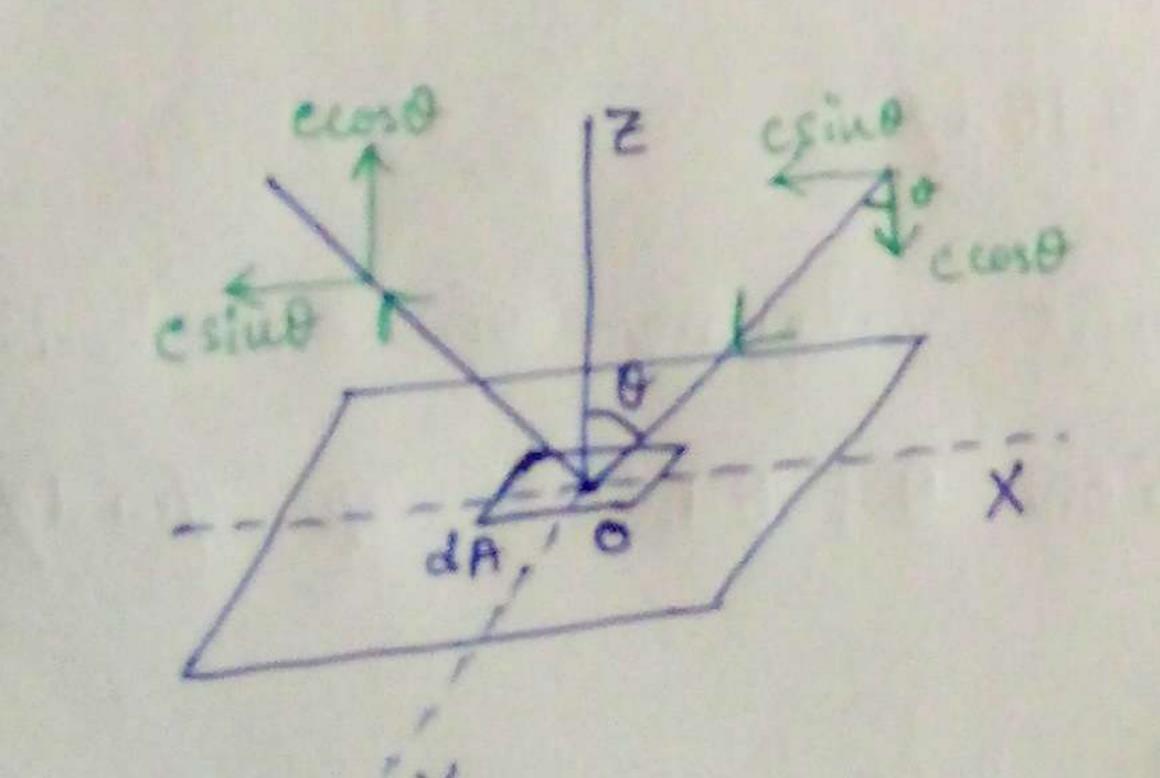
 $= \frac{dn_e}{4\pi} \sin\theta d\theta d\phi$ dnc,0,0

Let's find now, how many of them strike dA of the wall of container. Geometrically, this is the number of molecules within the slanted prism of length cdt with edges in the direction  $0 \neq \emptyset = \frac{dn_c}{4\pi} \sin\theta d\theta d\phi \times cdA\cos\theta dt$ « Total number of collisions at dA per unit time  $\int_{0}^{\infty} \int_{0}^{\infty} \int_{0}^{\infty} \frac{dn_{e}}{4\pi} \sin\theta d\theta d\phi \times cdA \cos\theta$ C=00=00=0 4=0  $= \frac{dA}{4\pi} \int_{0}^{\infty} c du_{e} \int_{0}^{\infty} siu\theta \cos\theta d\theta \int_{0}^{\infty} d\phi = \frac{dA}{4} \int_{0}^{\infty} e du_{e}.$ 

of n, atoms per unit volume moves with relocity 9,

u, 9 + n2 c2 + n3 c3 + ... average velocily \( \bar{c} = W1+ N2+ N3+ -.. = Znici = inschue

.. Number of molecules colliding at dA of the container per unit time =  $\frac{dA}{4}$  nc



Now let's compute change in momentum by molecules striking area dt in unit time.

normal component of incident momentum is me cost 4 reflected momentum - me cost.