1. The average BAC of eight male subjects was measured after consumption of 15 mL of ethanol. The resulting data were modeled by the concentration function

$$C(t) = 0.0225te^{-0.0467t}$$

where t is measured in minutes after consumption and C is measured in mg/mL.

(a) How rapidly was BAC increasing after 10 minutes?

a) How rapidly was BAC increasing after to infinites:
$$C(t) = ate^{bt}$$

$$C'(t) = ae^{-bt} - abte^{-bt}$$

$$= ae^{-bt} (1-bt)$$

$$c = ae^{-bt} (1-bt)$$

$$c = ae^{-bt} (1-bt)$$

(b) How rapidly was BAC decreasing half an hour later?

$$((30) = -0.0022 \frac{m_0}{mL} \frac{1}{m_1 de} = -0.133 \frac{m_0}{mL} \frac{1}{hor}$$

**2.** The brightness of a star in units of  $m_V$  (apparent magnitude) is given by

$$B(t) = 4.0 + 0.35 \sin\left(\frac{2\pi t}{5.4}\right)$$

where t is measured in days. Find the rate of change of brightness after one day and interpret your answer. Include units.

$$\beta'(t) = 6.35 \frac{2\pi}{5.4} \cos\left(\frac{2\pi t}{5.4}\right)$$

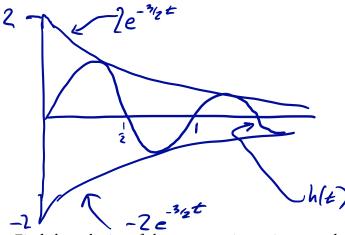
$$\beta'(1) = 0.35 \frac{247}{5.4} \cos \left(\frac{247}{5.4}\right)$$

**3.** A mass on a spring is oscillating. Its height at time t is

$$h(t) = 2e^{-\frac{3}{2}t}\sin(2\pi t)$$

where t is measured in seconds and h is measured in centimeters.

1. Make a sketch of  $y = 2e^{-\frac{3}{2}t}$ ,  $y = -2e^{-\frac{3}{2}t}$  and y = h(t).



2. Find the velocity of the mass at time t in general and at time t = 1 second in particular.

$$h'(t) = -3e^{-3/2t} \sin(2\pi t) + 4\pi e^{-3/2t} \cos(2\pi t)$$

$$h'(1) = 0 + 4\pi e^{-3/2}$$

$$= 2.80... \cos(5)$$

3. Compute  $\lim_{t\to\infty} h(t)$  and interpret what this means.

Since I'm 
$$\pm 2e^{-3t_2t} = 0$$
 $t = \infty$ 

and since  $-2e^{-3t_2t} \le h(t) \le 2e^{-3t_2t}$ 

I'm  $h(t) = 0$ . As  $t = \infty$ , the oscillations decay

and the mass approaches a constant

height  $h = 0$ .

**4.** Find all the locations where the tangent to the curve  $y = 2\cos(x) + \cos^2(x)$  is horizontal.

$$y'=2\sin y$$
 1  $2\sin x$   $\cos x$   
 $y'=0$  if  $\sin x$   $(1+\cos x)=0$  so  
 $\sin(y)=6$   $(x=\pi k, keZ)$  or  
 $\cos(x)=-1$   $(x=\pi+2\pi k keZ)$ .  
Continue these conditions the tensent is hunizontal at  $x=\pi k$ ,  
5. Compute  $f'(t)$  if  $f(t)=e^{at}\sin(bt)$ , where  $a$  and  $b$  are constants.

5. Compute f'(t) if  $f(t) = e^{at} \sin(bt)$ , where a and b are constants.

$$f'(t) = \int_{t}^{t} e^{at} \int_{s}^{t} \int_{s}^{t}$$

**6.** Find y'' if  $y = \cos(\sin(3x))$ .

$$\gamma' = -5 \cdot y \left( \sin(3x) \right) \frac{1}{Jx} \sin(3x)$$

$$= -5 i n \left( 5 \cdot h (3x) \right) \frac{3}{3} \cos(3x)$$