1. Compute the linearization of f(x) = 1/x at x = 2.

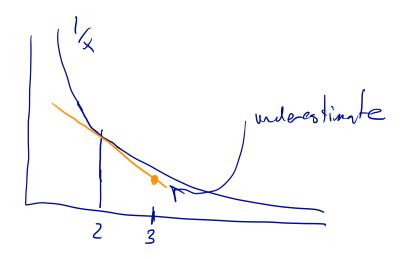
$$f(z) = \frac{1}{2}$$

 $f'(z) = \frac{1}{4}$
 $L(x) = \frac{1}{2} - \frac{1}{4} (x-2)$

2. Use your linearization to estimate 1/3.

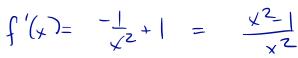
$$\frac{1}{3} = f(3) \approx L(3) = \frac{1}{2} - \frac{1}{4}(3-2) = \frac{1}{4}$$

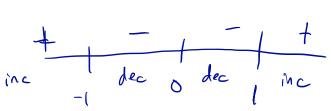
3. Draw a graph that illustrates the computation you just did. Then use the graph to determine if your estimate for 1/3 is an underestimate or an overestimate.

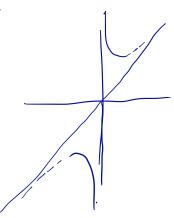


The problems on this page refer to the function $f(x) = \frac{1}{x} + x$.

4. On what intervals is the function increasing? Decreasing?



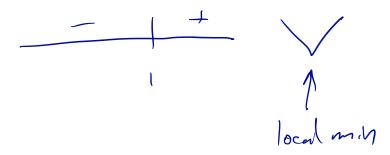




5. Find the critical points of f(x).

$$x = \pm 1$$

6. Use the first derivative test to classify the only positive critical point as a local min/max/neither.



7. Use the second derivative test to classify the only positive critical point as a local min/max if this is possible

$$f''(x) = \frac{2}{x^3}$$

$$f''(1) = 2$$
 local my

8. A circular metal plate is being heated in an oven. The radius of the plate is increasing at a rate of 0.01 cm/min when the radius is 50cm. How fast is the area of the plate increasing?

$$A = \pi r^{2}$$

$$\frac{dA}{dt} = 2\pi r \frac{dr}{dt}$$

$$= 2\pi \cdot 50 \cdot \frac{1}{100} = \pi \cdot \frac{2}{m \cdot h}$$

9. A Norman window is has a rectangular base and a semi-circle on top. What dimensions of the window minimize the perimeter if the area of the window is to be 4 ft².

$$A = 2rh + \frac{\pi r^2}{2} \qquad A = 4 \Rightarrow h = \frac{4 - \frac{\pi r^2}{2}}{2r} = \frac{8 - \pi r^2}{4r}$$

$$P = 2h + 2r + \pi r$$

$$P = \frac{8 - \pi r^2}{2r} + 2r + \pi r$$

$$P = \frac{4 + \frac{\pi}{2}r}{2r} + 2r$$

$$P = \frac{4 + \frac{\pi}{2}r}{r} + 2r$$

$$P' = -\frac{4}{r^2} + \left(2 + \frac{\pi}{2}\right)$$

$$P' = 0 \Rightarrow r = \frac{4}{2 + \pi r^2}$$

$$P' = 0 \Rightarrow r = \frac{4}{2 + \pi r^2}$$

10. The volume of a cone is given by $V = \frac{1}{3}\pi r^2 h$ where r is the radius of the base of the cone and h is the height of the cone. Use a differential to estimate the change in volume of the cone if the height is fixed at 9 feet and the radius changes from 5 feet to 5.5 feet.

11. Compute $\lim_{x\to 0} \frac{\sec(x)-1}{x^2}$

$$\lim_{\lambda \to 0} \frac{\sec(\lambda) - 1}{x^2} = \lim_{\lambda \to 0} \frac{\sec(\lambda) + a(\lambda)}{2x}$$

$$= \lim_{\lambda \to 0} \frac{\sec(\lambda) + a(\lambda)}{2} + \sec^2(\lambda)$$

$$= \lim_{\lambda \to 0} \frac{\sec(\lambda) + a(\lambda)}{2}$$

$$= 0 + 1$$