

1. Compute $\int_1^2 \frac{t^3 - 3t^2}{t^4} dt$.

2. Compute $\frac{d}{dx} \int_5^x \cos(\sqrt{s}) ds$.

3. Compute $\int x^2(3 - x) dx$

4. Compute $\int 9\sqrt{x} - 3 \sec(x) \tan(x) dx$

5. Snow is falling on my garden at a rate of

$$A(t) = 10e^{-2t}$$

kilograms per hour for $0 \leq t \leq 2$, where t is measured in hours.

- a. If $m(t)$ is the total mass of snow on my garden, how are $m(t)$ and $A(t)$ related to each other?
- b. What does $m(2) - m(0)$ represent?
- c. Find an antiderivative of $A(t)$.
- d. Compute the total amount of snow accumulation from $t = 0$ to $t = 1$.
- e. Compute the total amount of snow accumulation from $t = 0$ to $t = 2$.
- f. From the information given so far, can you compute $m(2)$?
- g. Suppose $m(0) = 9$. Compute $m(1)$ and $m(2)$.

6. A airplane is descending. Its rate of change of height is $r(t) = -4t + \frac{t^2}{10}$ meters per second.

a. if $A(t)$ is the altitude of the airplane in meters, how are $A(t)$ and $r(t)$ related?

b. What physical quantity does $\int_1^3 r(t) dt$ represent?

c. Compute $A(3) - A(1)$.

7. Gravel is being added to a pile at a rate of rate of $1 + t^2$ tons per minute for $0 \leq t \leq 10$ minutes. If $G(t)$ is the amount of gravel (in tons) in the pile at time t , compute $G(10) - G(0)$.

8. Challenge! Compute

$$\frac{d}{dx} \int_5^{x^3} \cos(\sqrt{s}) \, ds.$$

Hint: Let $H(x) = \int_5^x \cos(\sqrt{s}) \, ds$. You're interested in $H(x^3)$. Apply the Chain Rule!

9. Challenge! Compute

$$\frac{d}{dx} \int_x^{x+1} \sqrt{s^2 + 1} \, ds.$$