

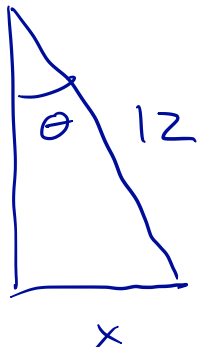
1. Find dy/dx if $y = \arcsin(3x)$.

$$\begin{aligned}\frac{d}{dx} \arcsin(3x) &= \frac{1}{\sqrt{1-(3x)^2}} \cdot \frac{d}{dx} 3x \\ &= \frac{3}{\sqrt{1-(3x)^2}}\end{aligned}$$

2. Find dy/dx if $y = \arctan(\sqrt{4-x^2})$.

$$\begin{aligned}\frac{dy}{dx} &= \frac{1}{1+(\sqrt{4-x^2})^2} \cdot \frac{d}{dx} \sqrt{4-x^2} \\ &= \frac{1}{1+4-x^2} \cdot \frac{1}{2} \frac{1}{\sqrt{4-x^2}} \cdot \frac{d}{dx} (4-x^2) \\ &= \frac{-x}{(5-x^2)\sqrt{4-x^2}}\end{aligned}$$

3. A 12-foot ladder is leaning against a wall. Let x denote the distance of the base of the ladder from the wall, and let θ be the angle between the ladder and the wall. How fast does the angle θ change with respect to x ?



$$\sin \theta = \frac{x}{12}$$

$$\theta = \arcsin\left(\frac{x}{12}\right)$$

$$\begin{aligned} \frac{d\theta}{dx} &= \frac{1}{\sqrt{1 - \left(\frac{x}{12}\right)^2}} \cdot \frac{1}{12} \\ &= \frac{1}{\sqrt{12^2 - x^2}} \end{aligned}$$

4. I compute that $d\theta/dx \approx 0.1$ when $x = 7$. What does this mean in language your parents can understand? Feel free to express your answer in terms of degrees instead of radians.

When the ladder is 7 ft from the wall,
the angle between the ladder and the wall
increases at a rate of 0.1 rad/foot as
the base of the ladder is shifted away from the wall.

$$\text{Note: } 0.1 \frac{\text{rad}}{\text{ft}} = 0.1 \frac{\text{rad}}{\text{ft}} \cdot \frac{360^\circ}{2\pi \text{ rad}} \approx \text{degrees/ft}$$