Increasing/Occreasing Test:

f(x)>0 on (a,b) =>

f(x)>0 on $(a,b) \Rightarrow f$ is increasing on (a,b)f'(x)<0 on $(a,b) \Rightarrow f$ is decreasing on (a,b)

First Derivative Test

At a pointwhere f'(c)=0:

Show the state of the state of

5'(4) => local may

f'(x) + + + => => neither

f'(x) ____ => neither

2nd Derivative Last E.o: \(\begin{aligned} \(\epsi_c \end{aligned} = 0 \end{aligned} \) £"(c)>0 (and f"(x) continuous new c, so f"(x) > 0 new c) Since f''(4) > 0 new c, f'(4) 13 Movements new c. e only possibility it 56) - + fis incresis ad f'(c)=0. So: - + 1 => local min. Suppose f(x) has a continuous 2-d derivative new c and f'(c) = 0. Full test: a) If f"(c)>0, fachieves a local mon at c. b) If f"(c) <0, fachieves a local max ata (c) if f"(c) =0, the test is inconclusive.

flow to remember: f(v)=x2: 5'(o)=0, 5"(o)=2 local may $f(x) = -x^2$ f'(0) = 0 f''(0) = -2 local max Concavity: Regions where f'(b) is increased decreasing are easy to spot geometrically and are useful mathematically. e.g. $f(x) = \frac{1}{1 + x^2}$ f(x) = 0 Dof: We say a function is concave up on an interval
if I'm is increasing on the interval. [It is
concave up, in porticular, if I'm exists and I'm)>0
on the interval.

We say a function is concave down on an interval

We say a farction is concae down on an interval of f'(x) is decreased on the interval. [Inf
is concare down of f''(x) <0].

Rule of Thumb: Up "U" => concave up

Down "U" => concave down



A spot where concavity changes from up to down on vice wesa, is called a point of inflection. Look for f"(a) =0 but you need to see a Sign charge: not: 5" + + f"(4) + (- e.g. (no chase in concar, by. point of inflection. For fly = x4 f"(x) = 12x2 (4)=0 but not a point of inflection