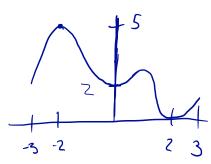
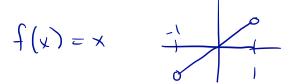
1. Sketch the graph of a function with domain [-3, 3] that has an absolute maximum of 5 at x = -2, an absolute minimum of 0 at x = 2 and a local minimum of 2 at x = 0.

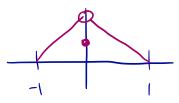


2. Give an example of a function with domain (-1,1) that does not attain either an absolute minimum or an absolute maximum value. Why doesn't your example violate the Extreme Value Theorem?



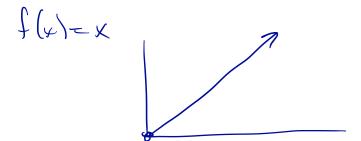
No violation: interal not closed.

3. Sketch a discontinuous function with domain [-1,1] that attains a minimum but does not attain a maximum value. Why doesn't your example violate the Extreme Value Theorem?



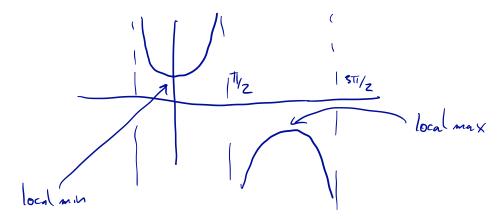
No violation: function not continuous

**4.** Give an example of a continuous function with domain  $[0, \infty)$  that attains a minimum but does not attain a maximum value. Why doesn't your example violate the Extreme Value Theorem?



No viblation: interval not bounded

**5.** Consider the function sec(x). Sketch this function. From the sketch answer the following. Does this function have any absolute maximums? Absolute minimums? Local maximums? Local minimums?



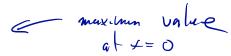
no absolute mox/ming

**6.** Find all critical points of the function  $f(x) = \sin(x)^{1/3}$ .

$$\int_{-\infty}^{\infty} (x) = 0 \quad \text{if } \cos(x) = 0 \quad \left( x = \frac{\pi}{2} + k\pi, \left( k \in \mathbb{Z} \right) \right)$$

Sall critical points

7. Find the absolute maximum and minimum values of  $f(x) = e^{-x^2}$  on the interval [-2,3], and the locations where those values are attained.





8. Find the maximum and minimum values of  $f(x) = x + \frac{1}{x}$  on the interval [1/5,4]. Determine where those maximum and minimum values occur.

$$S = (1)^2$$

$$f(1)=2$$
 emin value at  $x=1$ 

endpoint 
$$\pm = \frac{1}{5}$$
  $f(15) = 5 + \frac{1}{5}$ 

$$f(1/5) = 5 + \frac{1}{5}$$

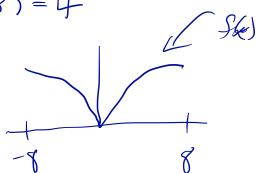
$$f(4) = 4 + \frac{1}{4}$$
 maxualve at  $x = 4$ 



9. Find the maximum and minimum values of  $f(x) = x^{2/3}$  on the interval [-8,8]. Determine where those maximum and minimum values occur.

end point 
$$x=8$$
  $f(8)=4$ 

3



**10.** A ball thrown in the air at time t = 0 has a height given by

$$h(t) = h_0 + v_0 t - \frac{1}{2} g_0 t^2$$

meters where t is measured in seconds,  $h_0$  is the height at time 0,  $v_0$  is the velocity (in meters per second) at time 0 and  $g_0$  is the constant acceleration due to gravity (in m/s²). Assuming  $v_0 > 0$ , find the time that the ball attains its maximum height. Then find the maximum hight.

$$h'(t) = v_0 - g_0 t$$
 $h'(t) = 0 \implies t = v_0 \iff time of max height$ 

$$h\left(\frac{v_0}{g_0}\right) = h_0 + v_0 \left(\frac{v_0}{g_0}\right) - \frac{1}{2} g_0 \left(\frac{v_0^2}{g_0^2}\right)$$

$$= h_0 + \frac{1}{2} \frac{v_0^2}{g_0} \qquad m_1 \times h_{eight}$$