We need some rules.

$$f(x) = 1$$

$$f'(x) = 0$$

$$\frac{d}{dx} \times = 1$$

e.g.
$$f(y) = x^{2}$$

 $f'(y) = \lim_{h \to 0} \frac{(x+h)^{2} - x^{2}}{h}$

On worksheet:
$$\frac{1}{4}x^3 = 3x^2$$

Rules for combining:
$$\frac{d}{dx} 7x^2 = 7 \frac{d}{dx}x^2 = 7 \cdot (2x) = 14x.$$

$$\frac{1_{14}}{h_{2}} \frac{7(x+h)^{2}-7x^{2}}{h_{2}} = \frac{1_{14}}{h_{2}} \frac{7(x+h)^{2}-x^{2}}{h_{2}}$$

$$= 7 \lim_{h \to 0} \frac{(xh)^2 \cdot 2}{h} - 7.2x$$

In fact:
$$\frac{1}{dx}x^n = nx^{n-1}$$
 $n = 1, 2, 3, \dots$ (Nat class)

In fact
$$\frac{d}{dx} \times a = a \times a^{-1}$$
 if $x > 0$, $a \in \mathbb{R}$ (Much later)

flow about
$$f(x) = 2x^2 - 5x + 9$$
?

$$\frac{d}{dx} \left[2x^2 - 6x + 9 \right] = \frac{d}{dx} \left[2x^2 \right] + \frac{d}{dy} \left[-6x \right] + \frac{d}{dx} \left[9 \right]$$

$$= 2 \frac{d}{dx} \left[x^2 \right] - 5 \frac{d}{dx} \left[x \right] + 7 \frac{d}{dx} \left[y \right]$$

$$= 2 \left[2 \times 7 - 5 \cdot 1 + 9 \cdot 0\right]$$
$$= 4 \times -5$$

In general
$$\frac{d}{dx} \left[f(x) + g(x) \right] = \frac{d}{dx} \left[f(x) \right] + \frac{d}{dx} \left[g(x) \right]$$

Comes from the sum rule for limits.

$$\int '(x) = \lim_{h \to 0} \frac{2^{x+h} - 2^{x}}{h} = \lim_{h \to 0} 2^{x} \frac{(2^{h} - 1)}{h}$$

$$= 2^{x} \lim_{h \to 0} \frac{2^{h} - 1}{h}$$

There

$$f'(x) = 10^{x} f'(0)$$