1. Estimate

$$\lim_{h\to 0}\frac{\sqrt{2+h}-\sqrt{2}}{h}$$

to 5 decimal digits.

$$f(h) = \sqrt{2+h} - \sqrt{2}$$

$$\lim_{x\to 0} \frac{x^2}{\cos(x) - 1}$$

to 5 decimal digits.

$$f(y) = \frac{y^2}{\cos^2(x) - 1}$$

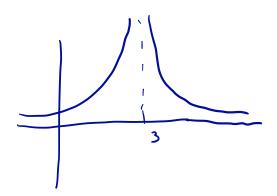
$$\frac{x}{0.1}$$
 = 2.0016.... $\frac{1}{2}$ = 2.0006.... $\frac{1}{2}$ = 2.00000016..... $\frac{1}{2}$ = 2.00000016..... $\frac{1}{2}$ = 2.000000016.....

3. Sketch the graph of

$$f(x)=\frac{1}{(3-x)^2}.$$

Then determine

$$\lim_{x\to 3} f(x).$$



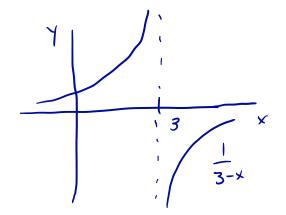
4. Determine

$$\lim_{x\to 3^+} \frac{1}{3-x}$$

and

$$\lim_{x\to 3^-}\frac{1}{3-x}$$

A sketch of the graph might be helpful.



$$\frac{1}{1} = \frac{1}{0} = -00$$

$$\lim_{x \to 3^{-}} \frac{1}{3-x} = \frac{1}{0^{+}} = +00$$

5. Determine exactly

$$\lim_{x \to 2} \frac{x^2 - 7x + 10}{x - 2}$$

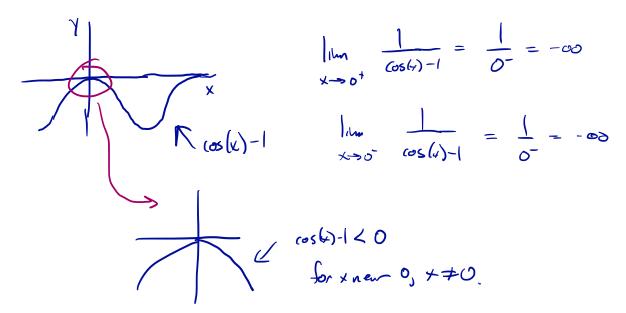
$$\lim_{x\to 2} \frac{x^2 - 7x + 10}{x - 2} = \lim_{x\to 2} \frac{(x - 5)(x - 2)}{x - 2}$$

$$= \lim_{x\to 2} x - 5 = -3.$$

6. Determine if

$$\lim_{x\to 0}\frac{1}{\cos(x)-1}$$

exists. If not, determine if the left- and right-hand limits exist.



7. Determine the left- and right-hand limits at 0 of f(x) = x/|x|.

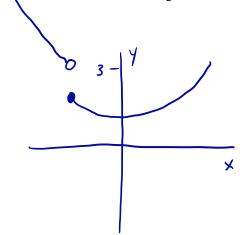
$$\lim_{x \to 0^+} f(x) = \lim_{x \to 0^+} \frac{x}{|x|} = \lim_{x \to 0^$$

$$l_{1}l_{1}l_{2}l_{3}l_{4} = l_{1}l_{1}l_{2} = l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3} = l_{2}l_{3}l_{4} = -1$$
 $l_{1}l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = -1$
 $l_{1}l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = -1$
 $l_{1}l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = -1$
 $l_{2}l_{3}l_{4} = l_{1}l_{2}l_{3}l_{4} = -1$
 $l_{2}l_{3}l_{4} = l_{1}l_{2}l_{4} = -1$

8. Suppose

$$g(x) = \begin{cases} x^2 + 1 & x \ge -1 \\ 2 - x & x < -1. \end{cases}$$

Sketch the graph. Then determine if $\lim_{x\to -1} g(x)$ exists. If not, determine if the left-and right-hand limits exist.



$$| \lim_{x \to -1^+} g(x) = \lim_{x \to -1^+} x^2 + 1 = | + | = 2$$

9. Determine

and

$$\lim_{x \to 0^+} 10^{-\frac{1}{x}}$$

$$\lim_{x\to 0^{-}} 10^{-\frac{1}{x}}.$$

As
$$x \rightarrow 0^{\dagger}$$
, $-\frac{1}{x} \rightarrow \frac{-1}{0^{+}} = -\infty$ and $10^{-\frac{1}{x}} \rightarrow 0$.