

DELTA SCORING FUNCTIONS REFERENCE

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1 Introduction

This document describes the set of functions and the way of their usage for obtaining the DELTA SCORING approach for test evaluations.

2 Instalation

To install the package download it from

<https://github.com/amitko/matlab-delta-scoring.git>.

Place the folder in the MATLAB path and rename it to +deltaScoring.

3 Ussage

Here is an example of a simple usage of the package.

Suppose the raw dichotomous item response is placed in variable `itemScore`.

To estimate the expected item difficulties ("deltas") the bootstrapping procedure

```
[ItemDelta, estimatedDeltaSE] = ...  
    deltaScoring.estimate.itemDeltaBootstrap(  
        itemScore);
```

is called. The resulted item deltas and the corresponding standard error of estimate are returned in variables `ItemDelta` and `estimatedDeltaSE`.

The classical person D-scores are calculated using the response patterns in itemScore and already calculated item deltas.

```
personDscores = ...
    deltaScoring.scoring.dScore(ItemDelta,
        itemScore, opt.Dscore_method);
```

Here `opt` is a structure containing the options for the considered delta scoring model. It can be generated by

```
opt = deltaScoring.scoring.Options;
```

Here and after the default will be the model RFM2. If a RFM3 model is required this can be stated in

```
opt.model = 3;
```

and the corresponding options should be passed to the functions.

The item parameters location b and shape s can be obtained by

```
[params, CI, ~, Results] = ...
deltaScoring.estimate.logitDeltaFit(itemScore,
    personDscores, opt);
```

where `params` contains the matrix with corresponding parameters for any item in the test $[b, s]$. The first column corresponds to the location parameter b while the second represents the shape s . If the model is RMF3, the guessing parameter is in the third column.

The matrix `CI` contains the 95% confidence interval of the estimated values. `Results` contains additional fitting parameters (for example MAD is available in `Results.MAD`).

The persons true scores can be calculated by

```
personTrueScores = ...
deltaScoring.scoring.trueScore(ItemDelta,
    ItemParameters, personDscores, opt);
```

and the SE

```
personTrueScoresSE = ...
deltaScoring.scoring.trueScoreSE(ItemDelta,
    ItemParameters, personDscores, opt);
```

A latent version of the location and shape parameters (together with their SE) can be obtained by

```
[LatentParams, LatentSE] = deltaScoring.estimate.
    ML_RFM_params( itemScore, personDscores, opt);
```

The corresponding MAD is obtained by

```
LatentMAD = deltaScoring.item.MAD(LatentParams,
    Results.observedLogitDelta, opt);
```

where `Results.observedLogitDelta` is calculated with `deltaScoring.estimate.logitDeltaFit` above and contains the proportion of observed correct answers for the values on the D-score scale.

The corresponding latent values of the person D-scores (and SE) can be obtained by

```
[latentScore, ~, latentScoreSE]= ...
deltaScoring.estimate.ML_RFM_scores( itemScore,
    LatentParams, opt)
```

The estimations of latent item parameters and person D-scores can be iterated until a convergence is reached

```
OldLatentParams = zeros(size(LatentParams));
while max(abs(OldLatentParams - LatentParams)) > eps
    OldLatentParams = LatentParams;
    [LatentParams, LatentSE] = ...
        deltaScoring.estimate.ML_RFM_params(
            itemScore, personDscores, opt);
    [latentScore, ~, latentScoreSE]= ...
        deltaScoring.estimate.ML_RFM_scores(
            itemScore, LatentParams, opt)
end
```

Equating of different tests can be performed by functions located in `deltaScoring.equating`. Here an example of equating of classical (non-latent) parameters of the test will be presented. The equating is based on calculation of two constants A and B which represent the change of scale for the test equating. These constants can be calculated on the base of item deltas of the target test `targetDeltas`, item deltas (already calculated above) and few common items between the two tests (stated in the variable `CommonItems`)

```
[A,B] = deltaScoring.equating.constants(
    targetDeltas, ItemDelta, CommonItems);
```

```

equatedItemDeltas = deltaScoring.equating.rescale
    (ItemDelta,A,B);
equatedDscores = deltaScoring.scoring.dScore(
    ItemDelta,itemScore,opt.Dscore_method);

```

4 Function reference

`deltaScoring.assembly.multipleTest`

```

multipleTest(nOfTest, nOfItems, itemDeltas,
    varargin)

```

Returnt the item idexes from the itemParams
which compose a number of tests test.

nOfTest
nOfItems - number of items in teh test.
itemDeltas - list (column) of estimated item deltas

Optional parameters: ['Name',value] pairs
The approach is based on Linear Optimal Test Design
Uses singleTest.

`deltaScoring.assembly.singleTest`

Returns the item idexes from the itemParams
which compose a test.

nOfItems - number of items in teh test.
itemDeltas - list (column) of estimated item deltas

Optional parameters: ['Name',value] pairs
The approach is based on Linear Optimal Test Design

deltaScoring.dif.conditionalDIF

conditionalDIF(focal_params,reference_params,o)

probabilities for correct item performance between focal and reference group, based on parameters of the items for the two groups.

o - deltaScoring.scoring.Options

deltaScoring.dif.ESonDIF

[onFocal, onReference] = EsonDIF(focal_params, reference_params,o)

Calculates the effect size on focal and reference group for DIF

INPUT:

 focal_params - item parameters,
 estimated on focal group
 reference_params - item parameters,
 estimated on reverence group
 o - options

deltaScoring.dif.functioning

Calculates different characteristics, corresponding to the DIF

deltaScoring.dif.Mantel_Haenszel

[a_MH,log_a_MH_SE,da_MH,z,p,MH,type,against]=
Mantel_Haenszel(response,score,groups,reference)

Calculates Mantel-Haenszel statistics

`deltaScoring.dif.MPDonDIF`

```
[onFocal, onReference] = MPDonDIF(dif)
dif = pcr_f - pcr_r;
```

`deltaScoring.dif.paramsForGroups`

```
[focal_params, reference_params, deltasF, deltasR] =
    paramsForGroups(itemResponse, group, latent, o)
Calculates the item parameters for the focal and
    reference group

group 0 - reference, 1 - focal
params by default are latent
```

`deltaScoring.dif.plotConditionalDIF`

```
plotConditionalDIF(dif, opt, visible)
Plots conditional DIF for the Focal and reference
    group
```

`deltaScoring.dif.plotICC`

```
plotICC(focal_params, reference_params, o, visible)
Plots ICC for the Focal and reference group
```

`deltaScoring.dif.plotTSC`

```
plotTSC(focal_params, reference_params, o, visible)
Plots test score for the Focal and reference group
```

`deltaScoring.dif.testing`

```
[DIF, DIFT, HA, HB, HAT, HBT, Results] = testing(
    focal_params, reference_params, o)
Tests DIF having estimated item parameters for
    focal
and reference group.
```

DIF - indicator for a specific item

0 - no DIF

1 - against focal

2 - against reference

DIFT - DIF on test level

HA - Hypothesis nder approach A. Cell array of
structures

HB - Hypothesis nder approach B. Cell array of
structures

HAT on test level

HBT on test level

Results - structure with detailed results

deltaScoring.equating.constants

```
[A,B] = constants(Base_test_deltas,New_test_deltas,
    common_items)
```

Y

X

Calculates the rescaling constants, based on common
items

between two test.

INPUT:

Base_test_deltas - item deltas of the base
test

New_test_deltas - item deltas of the new
test

common_items - twoo columns

[base_test_item_id
new_test_item_id]

OUTPUT:

A and B

deltaScoring.equating.dscore_common

NOT IN USE

deltaScoring.equating.dscore_rfm

```
[Dscore_equated] = dscore_rfm(X_params, X_rescaled,
                               Dscores, type, o)
Calculates equated latent D-Score based on the
latent parameters
```

INPUT:

```
          X_params    - latent parameters of
                        the test
X_rescaled - rescaled parameters of the test
after equating
          Dscores     - persons D-score
          type        - default value is m1
          o           - options
```

OUTPUT:

Dscore_equated - equated D-score

deltaScoring.equating.dscoreOnSubtest

NOT IN USE

deltaScoring.equating.rescale

```
res = rescale(deltas,A,B)
Rescales the item deltas of a test according
to rescaling constants A and B.
```

deltaScoring.equating.rescale_rfm

```
[X_params_rescaled, opts] = rescale_rfm(X_params,
    Y_params, common_items, method_type, o)
```

Calculates the rescaled latent item parameters of
test X on the scale of the base test Y.

INPUT:

```
X_params - parameters of test X
Y_params - parameters of test Y
common_items - common items; two
               columns
               [base_test_item_id
                 new_test_item_id]
method_type - Rescaling of the shape
               parameter s has two options
               direct
               [
               default
               ]
               |
               trough_a
```

OUTPUT:

```
X_params_rescaled
opts - Structure with
      bA, bB, sA, sB
```

deltaScoring.estimate.EM_RFM

```
Function [pars, ability] = irt.
    ItemParametersEstimate_EM_3PL( data, o)
```

estimates the parameters of the item
characteristic
curves under the IRT model using the EM
algorithm.

Input:

data - Dichotomous item response
o - scoring.Options (optional)

Output:

pars - Item parameters
[difficulty, discrimination, guessing]

deltaScoring.estimate.itemDeltaBootstrap

deltaScoring.estimate.latentLklh

latentLklh(xi,itemResponse,deltaScores,o)
Calculates person likelihood on a specific test
with a specific item response
For internal use in estimations

deltaScoring.estimate.logitDeltaFit

deltaScoring.estimate.logitDeltaPlot

h = logitDeltaPlot(GF,observedLogitDelta,o)
Plots the fit and the estimated logistics curve
Returns the figure object

INPUT:

GF - output from logitDeltaFit
observedLogitDelta - from Results of
logitDeltaFit

o - options
dScale

deltaScoring.estimate.ML_RFM_params

```
[pars,se] = ML_RFM_params( itemResponse,  
    deltaScores, o)  
Estimates the latent parameters of the items base  
on  
RFM model, using JML approach.
```

INPUT:

```
itemResponse - dichotomous item  
              response  
deltaScores  - person D-scores  
o            - oprions
```

OUTPUT:

```
pars          - estimated parameter  
              values  
se            - standard errors of  
              the estimates
```

deltaScoring.estimate.ML_RFM_scores

```
[scores,se, see]=ML_RFM_scores( itemResponse,  
    itemParams, o)  
Estimates the latent parameters for person  
abilities, based on  
RFM model, using JML approach.
```

INPUT:

```
itemResponse - dichotomous item  
              response  
itemParams   - person D-scores  
o            - oprions
```

OUTPUT:

```
      scores      - person latent D-
      scores
      se          - standard errors of
      the estimates
      see         - analitical solution for se
```

`deltaScoring.generate.guttman`

```
guttman(NofPersons,itemParams,options,reverse)
Generates a item response according Guttman concept
```

`deltaScoring.generate.itemResponse`

```
[res, out] = itemResponse(Persons,itemParams,
    options,env)
Generates an item response Persons over a set
of items, defined by their item Parameters.
```

```
env is a structure containing additional
information about cheating and guessing.
```

`deltaScoring.item.characteristicsFromParameters`

```
res = characteristicsFromParameters(item_params,o)
Calculates the item characteristics from item
parameters
```

INPUT:

```
    item_params - item parameters
    o           - options
```

OUTPUT

```
res - [location, discrimination]
```

deltaScoring.item.icc

```
res = icc(itemParameters,o)
Plots ICC curves under given item parameters
```

INPUT:

- itemParameters
- o - options

OUTPUT:

- res - figure handle

deltaScoring.item.MAD

```
res = MAD(params,observedLogitDelta,o)
Calculates the Mean Absolute Difference between
observed probability for correct response and
predicted probability obtained under the
selected RFM model.
```

INPUT:

- params - item parameters
- observedLogitDelta - observed PCR
- o - options

OUTPUT:

- res - MAD values

deltaScoring.item.parametersFromCharacteristics

```
res = parametersFromCharacteristics(location,
discrimination,o)
Calculates the item parameters from item
characteristics
```

INPUT:
 location
 discrimination
 o - options

OUTPUT
 res - [b,s]

deltaScoring.person.aberrant

res = aberrant(itemParams,itemDeltas,Dscores,
 itemResponse,options)
Finds aberrant person behaviour according
to the "quantile method" according to
An Examination of Different Methods of Setting
Cutoff Values in Person Fit Research
Amin Mousavi, Ying Cui & Todd Rogers

INPUT:
 itemParams - item parameters
 itemDeltas - item deltas
 Dscores - persons D-scores
 itemResponse - dichotomous item response

OUTPUT:
 res - aberrant indicator 0/1

deltaScoring.person.fitHStatistics

fitHStatistics(item_response)
Calculates the H statistics for the
dichotomous item response

deltaScoring.person.fitIndexZ

```
fitIndexZ(lklh,Elklh,Vlklk)
  Inputs are from person.likelihood
```

based on
D. Dimitrov, R. Smith. Adjusted Rasch Person-Fit
Statistics. J. of
Applied measurement. 2006

```
deltaScoring.person.fitMSE
```

```
[Outfit, Infit] = fitMSE(item_response,
  expected_item_score)
Calculates the Outfit and Infit of the MSE fit
```

```
deltaScoring.person.fitU
```

```
fitU( params, Dscore, responses, o)
Calculates U statistics
```

```
deltaScoring.person.fitUD1
```

```
fitUD1(deltas, Dscore, responses)
Calculates UD1 Statistics
```

```
deltaScoring.person.fitUD2
```

```
fitUD2( deltas, Dscore, responses, params, o)
Calculates UD2 statistics
```

```
deltaScoring.person.likelihood
```

```
[res, expected, variance] = likelihood(dScores,
  item_parameters,item_response,o)
```

Calculates the likelihood for a specific response pattern in item_response from a person with ability in dScores, over a set of items in item_parameters.

based on

D. Dimitrov, R. Smith. Adjusted Rasch Person-Fit Statistics. J. of Applied measurement. 2006

deltaScoring.person.plotConditionalSE

plotConditionalSE(dScores, SE)
Plots conditional standard error

deltaScoring.person.responseProbability

res = responseProbability(delta, item_parameters, o)
Calculates the probability for correct response from a person with ability delta over the set of items with parameters, defined in item_parameters.

INPUT

delta - Person ability
item_parameters - Item parameters [b,s,c]
o - Delta Scoring Options

deltaScoring.poly.ccr

ccr(itemParameters, observedLogitDelta, o)
Plots Category Characteristic Curves for the Polytomous items

INPUT:

itemParameters - row vector of values of the
difficulty parameter
for item grades.
observedLogitDelta - person ability value
o - options

deltaScoring.poly.itemPerformance

res = itemPerformance(itemParameters,delta,o)
Calculates the probability for correct performance
for the polytomous item

INPUT:

itemParameters - row vector of values of the
difficulty parameter
for item grades.
delta - person ability value
o - options

OUTPUT:

res - probability for correct performance

deltaScoring.poly.logitDeltaPlot

h = logitDeltaPlot(GF,observedLogitDelta,o)
Plots the fit and the estimated logistics curve
Returns the figure object

INPUT:

GF - output from logitDeltaFit
observedLogitDelta - from Results of
logitDeltaFit
o - options
dScale

OUTPUT:

h - figure haddle

deltaScoring.scoring.dScore

Returns the so called d-Score for a person
with a given response vector over a set
of items with precalculated deltas;

INPUT:

itemDeltas - item delta values
response - 0/1 item response
t - type
total / relative_to_n /
relative_to_d [default]

deltaScoring.scoring.dScoreSE_IRT

Returns the so called d-Score SE for a person
with a given ability theta (on a logit
scale)
over a set of items with IRT parameters [b,a,c];

left here only for convenience.

deltaScoring.scoring.itemPersonMap

deltaScoring.scoring.observedLogitDelta

observedLogitDelta(ItemResponse, Dscore,o)
Calculates the proportions of the correct scores
for different values of the dScale

INPUT:

ItemResponse - dichotomous item response 0/1
Dscore - estimated person's dScore
o - options

OUTPUT:

res - proportion of correct answers on
dScale

deltaScoring.scoring.Options

option = Options(varargin)

Defines the options for DELTA SCORING

Default Values

NofSamplesForBootstrapping: 1000
sampleProportionForBootstrapping: 0.1000
estTypeForBootstrapping: 'mode'
dScale: [21x1 double]
Models: {1x3 cell}
ModelNames: {'RFM1' 'RFM2'
'RFM3'}
ModelFixedParams: [1x1 struct]
Model_coefficients: {'b' 's' 'c'
'd'}
model: 2
type: 'raw'
skipObservedOnPlot: 2
aberrantQuantile: 0.7000
EM: [1x1 struct]
StartingPoint: [0.5000 1
0.1000]
Lower: [0.0100 0.2000
0]
Upper: [0.9900 5
0.5000]

```
RFM_params_method: 'constrained'
```

```
deltaScoring.scoring.PCR
```

```
res = PCR(params,delta,o)
Probability for correct response
```

```
INPUT:
  params - logistics parameres
  delta  - delta values
  o      - options
          mmodel
```

```
deltaScoring.scoring.poly2dih
```

```
[DIHscores,Poly,Org] = poly2dih(Response)
Converts polytomous to dihotomous item response
```

```
INPUT:
  Response - polytomous item response
```

```
OUTPUT:
  DIHscores - dihotomous ite response
  Poly      - indicator for polytomous items
  Org       - Labels, etc. for poly items
```

```
deltaScoring.scoring.scaledScore
```

```
res=scaledScore(scores,t)
Scales the score according to type t
t = 'range' scales in range 0..100
```

```
deltaScoring.scoring.trueScore
```

```
res = trueScore(itemDeltas, parameters, dScore, o)
Calculates the true-score measure for person's D-
score
on a set of items with delta scores in itemDeltas,
logistic parameters of the items and the person's D
-score
```

INPUT:

```
itemDeltas - item's delta scores
parameters - item's logistics parameters
dScore     - person's D-score
o          - Options (defaults scoring.Options)
```

deltaScoring.scoring.trueScoreSE

```
res = trueScoreSE(itemDeltas, parameters, dScore, o
)
Calculates the true-score SE measure for person's D
-score
on a set of items with delta scores in itemDeltas,
logistic parameters of the items and the person's D
-score
```

INPUT:

```
itemDeltas - item's delta scores
parameters - item's logistics parameters
dScore     - person's D-score
o          - Options (defaults scoring.Options)
```