

Assignment 4

b. we want to prove that $(\text{pipe } f_1 \dots f_n \text{ } c)$ is equivalent to $(c (\text{pipe } f_1 \dots f_n))$

base case- $n=1$

$$(\text{pipe } f_1 \text{ } c_1) = (c_1 (\lambda (x \text{ } c_2) (f_1 \text{ } x \text{ } c_2))) = c_1(f_1 \text{ } x \text{ } c_2) = (c_1(f_1 \text{ }))$$

$$(c_1(\text{pipe } (f_1))) = (c_1 (f_1))$$

While f_1 is the cps of f

induction hypothesis- $n = k$

$$(\text{pipe } f_1 \dots f_k \text{ } c) = (c (\text{pipe } f_1 \dots f_k))$$

inductive step - $n = k+1$

need to prove - $(\text{pipe } f_1 \dots f_{k+1} \text{ } c) = (c (\text{pipe } f_1 \dots f_{k+1}))$

$\text{lst-fun} = f_1 \dots f_{k+1}$

$$\Rightarrow (\text{pipe } \text{lst-fun } c_1) =$$

$$(\text{pipe } (\text{cdr } \text{lst-fun}) (\lambda (\text{res}) (\text{compose } (\text{car } \text{lst-fun}) \text{ res } c_1)))) =$$

$$((\lambda (\text{res}) (\text{compose } (\text{car } \text{lst-fun}) \text{ res } c_1))(\text{pipe } (\text{cdr } \text{lst-fun } c_1)))) =$$

$$((\lambda (\text{res}) (\text{compose } (\text{car } \text{lst-fun}) \text{ res } c_1))c_1(\text{pipe } (\text{cdr } \text{lst-fun}))) = \text{//induction}$$

$$C_1(\text{compose } (\text{car } \text{lst-fun}) (\text{pipe } (\text{cdr } \text{lst-fun}))) = \text{// induction}$$

$$\Rightarrow (c_1 (\text{pipe } \text{lst-fun})) =$$

$$(c_1 (\text{compose } (\text{car } \text{lst-fun}) (\text{pipe } (\text{cdr } \text{lst-fun}))))$$

we will prove that $(\text{compose } f \text{ } g \text{ } c)$ is equivalent to $(c (\text{compose } f \text{ } g))$:

$$c(\text{Compose } f \text{ } g) = c(g(f \text{ } x))$$

we assume that $f \text{ } x \text{ } c = c(f \text{ } x)$, $g \text{ } y \text{ } c = c(g \text{ } y)$.

$$(\text{compose } f \text{ } g \text{ } c_1) = c_1(\lambda (x \text{ } c_2) (f \text{ } x \text{ } \lambda (\text{res}) (g \text{ } \text{res } c_2))) =$$

$$c_1(\lambda (\text{res}) (g \text{ } \text{res } c_2) (f \text{ } x)) = c_1(c_2(g(f \text{ } x))) = c(g(f \text{ } x)) \text{ as needed.}$$

Question 2-

d. we will use each of the following procedures for a different purpose-

reduce1-lzl – when we need to reduce all the elements of the lazy list into a single value when the lazy list are -

Examples : calculating the sum or product of all elements in a lazy list, finding the maximum or minimum element in a lazy list.

Reduce2-lzl- when you only need to reduce the first n elements of the lazy list or when dealing with large or infinite lazy lists where processing the entire list isn't feasible. Examples - Calculating the sum of the first n elements in a lazy list , finding the average of the first n elements in a lazy list.

Reduce3-lzl- when you need to process and potentially consume the lazy list incrementally while producing a lazy list of results.

Examples- Generating a lazy list where each element is the cumulative sum up to that point. producing a lazy list of running averages as elements are processed.

G.

Advantages for 'generate-pi-approximations' implementation w.r.t. the pi-sum implementation taught in class are:

1. **Lazy evaluation** : generate-pi-approximations uses lazy lists, which means it generates approximations on demand. This is memory efficient because it doesn't compute more terms than necessary.
2. **Intermediate Results** : It allows access to intermediate results of the approximation. You can get the first few terms without computing the entire sum.
3. **Memory use**: generate-pi-approximations uses lazy lists which means it computes the next element only when needed and don't waste valuable memory space.

Disadvantages:

1. **Complex**: The implementation is more complex, involving multiple higher-order functions and lazy list manipulations. This can make the code harder to understand and maintain.
2. **Direct calculation**: This implementation directly sums the terms without the additional overhead of lazy evaluation, which can make it faster for small inputs.

Question 3-

3.1

1. `unify[x(y(y), T, y, z, k(K), y), x(y(T), T, y, z, k(K), L)]`

a. `[=x(y(y), T, y, z, k(K), y) x(y(T), T, y, z, k(K), L)]`

`sub: {}`

b. picking one equation: `[=x(y(y), T, y, z, k(K), y) x(y(T), T, y, z, k(K), L)]`

c. **case 3-**

d. `[y(y) = y(T), T=T, y=y, z=z, k(K)=k(K), y=L]`

`sub: {}`

e. picking one equation: `y(y) = y(T)`

`[T=T, y=y, z=z k(K)=k(K), y=L]`

`sub: {}`

f. **case 3 -**

g. `[y= T]`

h. picking one equation: `y= T`

i. `[T=T, y=y, z=z, k(K)=k(K), y=L]`

`sub: {} * {y= T} = {y= T}`

j. picking one equation: `T=T`

`[y=y, z=z, k(K)=k(K), y=L]`

k. `sub: {y= T}`

l. picking one equation: `y=y`

`[z=z, k(K)=k(K), y=L]`

m. `{y=T} * {y=y} = {y = T}`

picking one equation: `z=z`

`{y=T}`

n. picking one equation: `k(K)=k(K)`

`[y=L]`

`{y =T}`

case 3 -

o. $[K = K]$

p. $\{y = T\} * \{K = K\} = \{y = T\}$

q. picking one equation: $[y = L]$

$[]$

Sub: $\{y = T\}$

r. sub: $\{y = T\} * \{y = L\} = \{y = T, L = T\}$

2. $\text{unify}[f(a, M, f, F, Z, f, x(M)), f(a, x(Z), f, x(M), x(F), f, x(M))]$

a. $[=f(a, M, f, F, Z, f, x(M)), f(a, x(Z), f, x(M), x(F), f, x(M))]$

sub: $\{\}$

b. picking one equation: $[=f(a, M, f, F, Z, f, x(M)), f(a, x(Z), f, x(M), x(F), f, x(M))]$

c. case 3-

d. $[a = a, M = x(Z), f = f, F = x(M), Z = x(F), f = f, x(M) = x(M)]$

sub: $\{\}$

e. picking one equation: $a = a$

$[M = x(Z), f = f, F = x(M), Z = x(F), f = f, x(M) = x(M)]$

sub: $\{\}$

f. case 1-

g. picking one equation: $M = x(Z)$

$[f = f, F = x(M), Z = x(F), f = f, x(M) = x(M)]$

sub: $\{\}$

h. case 3 - **FAIL NOT THE SAME STRUCTURE**

3. unify[t(A, B, C, n(A, B, C), x, y), t(a, b, c, m(A, B, C), X, Y)]
- a) [=t(A, B, C, n(A, B, C), x, y), t(a, b, c, m(A, B, C), X, Y)]
sub: {}
 - b) picking one equation: [=t(A, B, C, n(A, B, C), x, y), t(a, b, c, m(A, B, C), X, Y)]
 - c) case 3-
 - d) [A=a, B=b, C=c, n(A, B, C) =m(A, B, C), X=X, Y=Y]
 - e) picking one equation: A=a
 - f) case 2
 - g) [B=b, C=c, n(A, B, C) =m(A, B, C), X=X, Y=Y]
 - h) sub: {A=a}
 - i) picking one equation: B=b
 - j) case 2
 - k) [C=c, n(A, B, C) =m(A, B, C), X=X, Y=Y]
 - l) sub: {A=a} * {B=b} = {A=a, B=b}
 - m) picking one equation: C=c
 - n) case 2
 - o) [n(A, B, C) =m(A, B, C), X=X, Y=Y]
 - p) sub: {A=a, B=b} * {C=c} = {A=a, B=b, C=c}
 - q) picking one equation: n(A, B, C) =m(A, B, C)
n could not be m because those are actual values and not generic variables.

4. unify[z(a(A, x, Y), D, g), z(a(d, x, g), g, Y)]
- a) [= z(a(A, x, Y), D, g), z(a(d, x, g), g, Y)]
 - b) picking one equation: [= z(a(A, x, Y), D, g), z(a(d, x, g), g, Y)]
sub: {}
 - c) case 3-
 - d) [a(A, x, Y) = a(d, x, g), D=g, g=Y]
sub: {}
 - e) picking one equation: a(A, x, Y) = a(d, x, g)

- f) case 3
- g) $[A=d, x=x, Y=g]$
- h) Sub: $\{A=d, Y=g\}$
- i) picking one equation: $D=g$
- j) case 2
- k) $[g=Y]$
- l) Sub: $\{A=d, Y=g\} * \{D=g\} = (A=d, Y=g, D=g)$
- m) picking one equation: $g=Y$
- n) case 2-
- o) Sub: $\{A=d, Y=g\} * \{g=g\} = (A=d, Y=g, D=g)$

3.3

The proof tree of the query $?- \text{path}(a,b, P)$ is infinite because the tree contains the circle (a,c,a) and contains the edge (a,b) so the algorithm can perform the circle in infinite number of times before taking the edge (a,b) .

In addition the tree is a success tree because there is at least One branch that leads to success.(example: (a,b) is a branch that leads to success).

