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Course: GATE Computer Science Engineering(CS)

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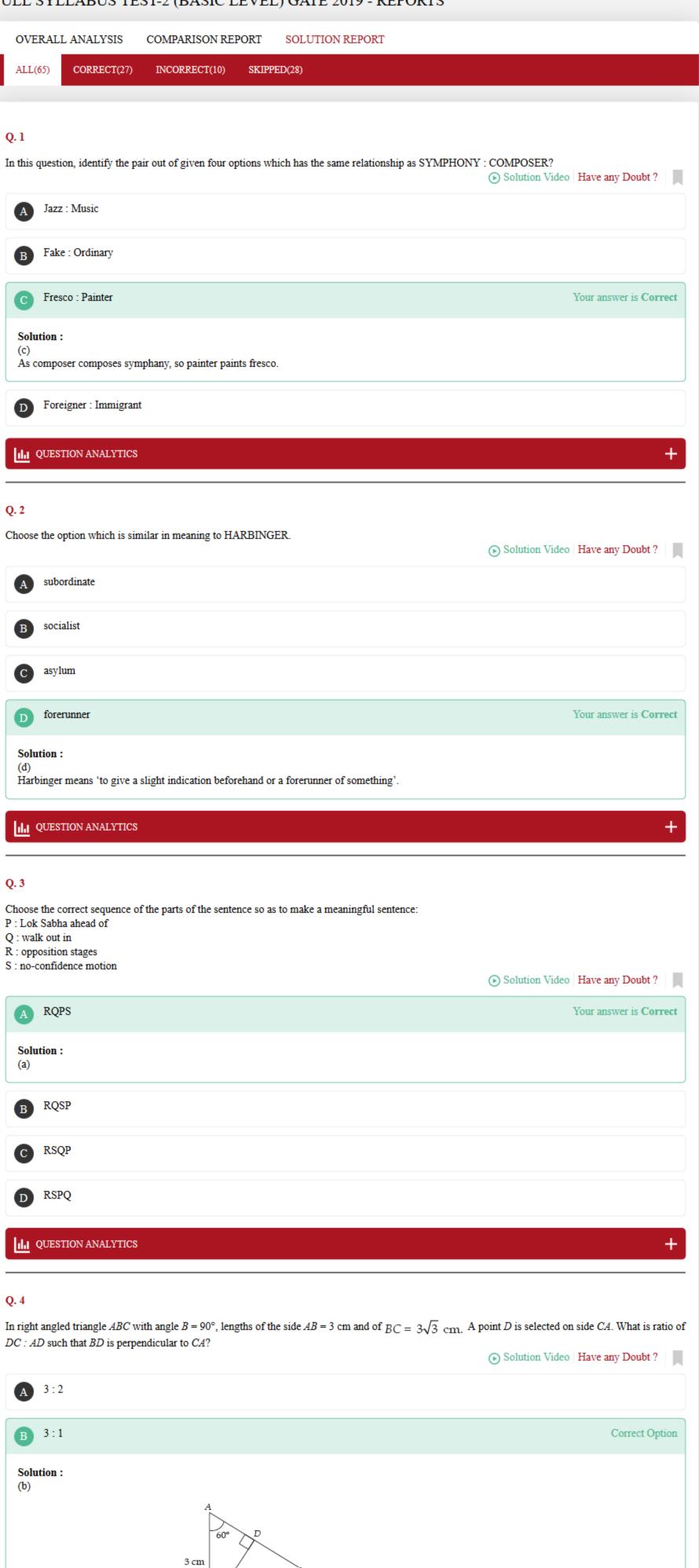
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### FULL SYLLABUS TEST-2 (BASIC LEVEL) GATE 2019 - REPORTS



In a right angled triangle if ratio of two perpendicular side is  $1:\sqrt{3}$ ,

then the triangle is a  $30^{\circ}$  –  $60^{\circ}$  –  $90^{\circ}$  triangle

 $\angle BAC = 60^{\circ}$ 

 $\angle BCA = 30^{\circ}$ Given:

 $BD \perp AC$  $\angle DBC = 60^{\circ}$  $\Rightarrow$ 

 $\angle DAB = 60^{\circ} \text{ and } \angle DBA = 30^{\circ}$ Right Δs BAD and CBD are also 30° - 60° - 90° triangles.

 $AD : BD : AB = 1 : \sqrt{3} : 2$ 

 $BD : DC : BC = 1 : \sqrt{3} : 2$ and

Which enables us to compute

$$AD = \frac{AB}{2} = \frac{3}{2}$$

$$CD = \frac{3\sqrt{3}}{2/\sqrt{3}} = \frac{9}{2}$$

$$DC:AD = \frac{9}{2}:\frac{3}{2}=3:1$$

C 5:2

D 2:1

### III QUESTION ANALYTICS

### Q. 5

If  $\left(x^2 + \frac{1}{x^2}\right) = 167$ , then what is the value of  $\left(x^3 + \frac{1}{x^3}\right)$ ? (Given x > 0)

Solution Video Have any Doubt?

2158

Correct Option

### Solution:

2158

$$\left(x^2 + \frac{1}{x^2}\right) = 167 \Rightarrow \left(x + \frac{1}{x}\right)^2 = \left(x^2 + \frac{1}{x^2} + 2\right) = 169$$

$$\left(x + \frac{1}{x}\right) = +\sqrt{169} = +13$$

$$\therefore \left(x^3 + \frac{1}{x^3}\right) = \left(x + \frac{1}{x}\right)\left(x^2 + \frac{1}{x^2} - 1\right) = 13 \times 166 = 2158$$

 $[:: a^3 + b^3 = (a + b) (a^2 - ab + b^2)]$ 

# III QUESTION ANALYTICS

# Q. 6

A group of boys and girls know either French or Spanish. The number of boys and girls are in the ratio 1: 4.30% of the girls know Spanish and the rest of them know French. On the other hand, 50% of the boys know Spanish and the rest of them know French. A student is chosen at random from the group of students who knows Spanish. What is the probability that the chosen student is a girl?

Solution Video Have any Doubt?



 $\frac{12}{17}$ 

Correct Option

# Solution:

Let the number of students be 100. Since ratio of number of boys : girls is 1 : 4; it means number of boys is 20 and number of girls is 80.

30% of girls know Spanish ⇒ number of girls who know Spanish = 30% of 80 = 24

50% of the boys know Spanish  $\Rightarrow$  number of boys who know Spanish = 50% of 20 = 10

Total number of students who know Spanish = 24 + 10 = 34

Hence probability that a girl is chosen from the group of students who know English =

 $\frac{24}{34} = \frac{12}{17}$  i.e. (b).





III QUESTION ANALYTICS

### Q. 7

Gatimaan express departed from Delhi for Agra which is 200 km away. However, in order to cope up with the delay due to rainy season, it departed 40 minutes earlier than the scheduled time of departure. With the speed of the train reduced by 50 km/hour as compared to the original speed, the train reached Agra as per original schedule. The original speed of the train will be

Solution Video Have any Doubt?

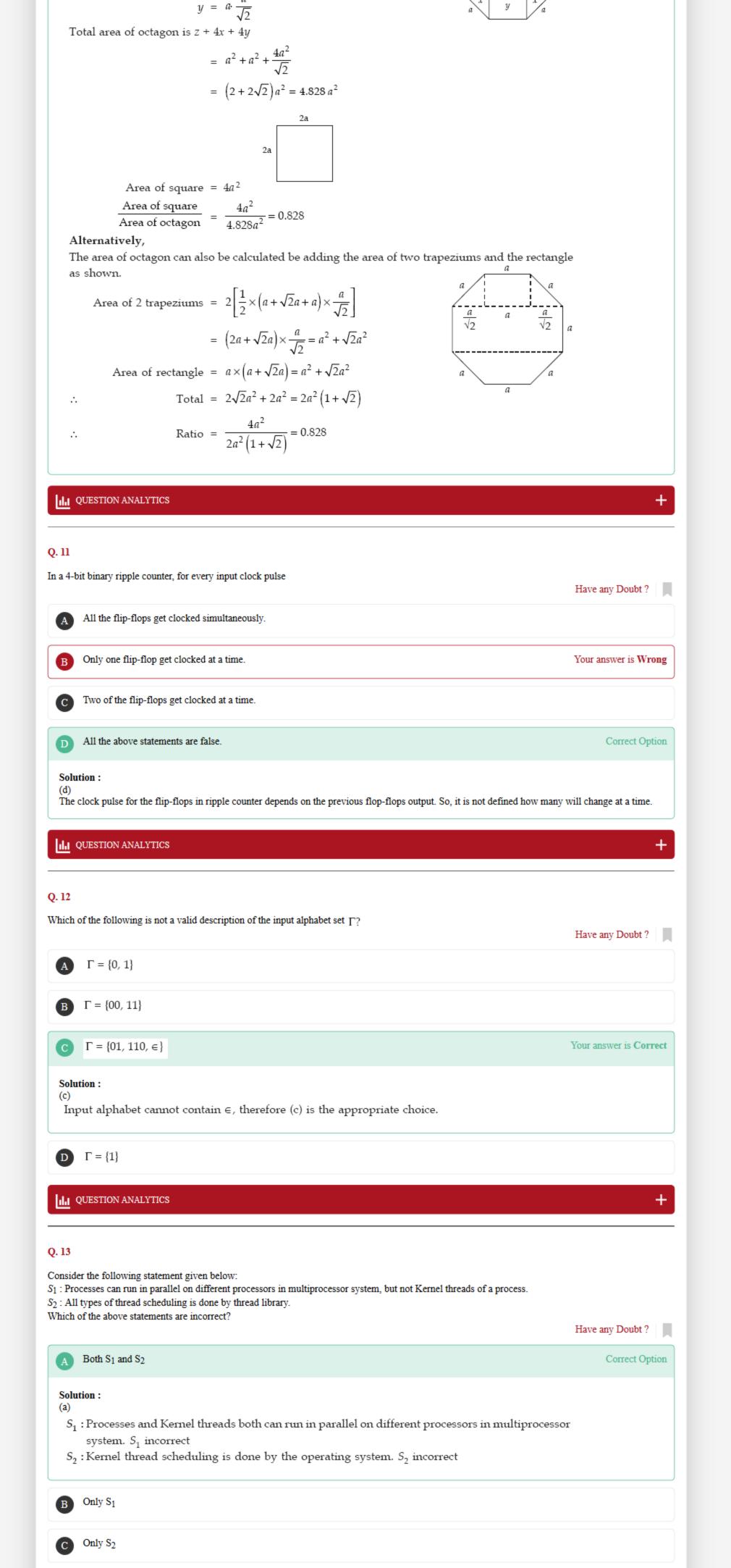


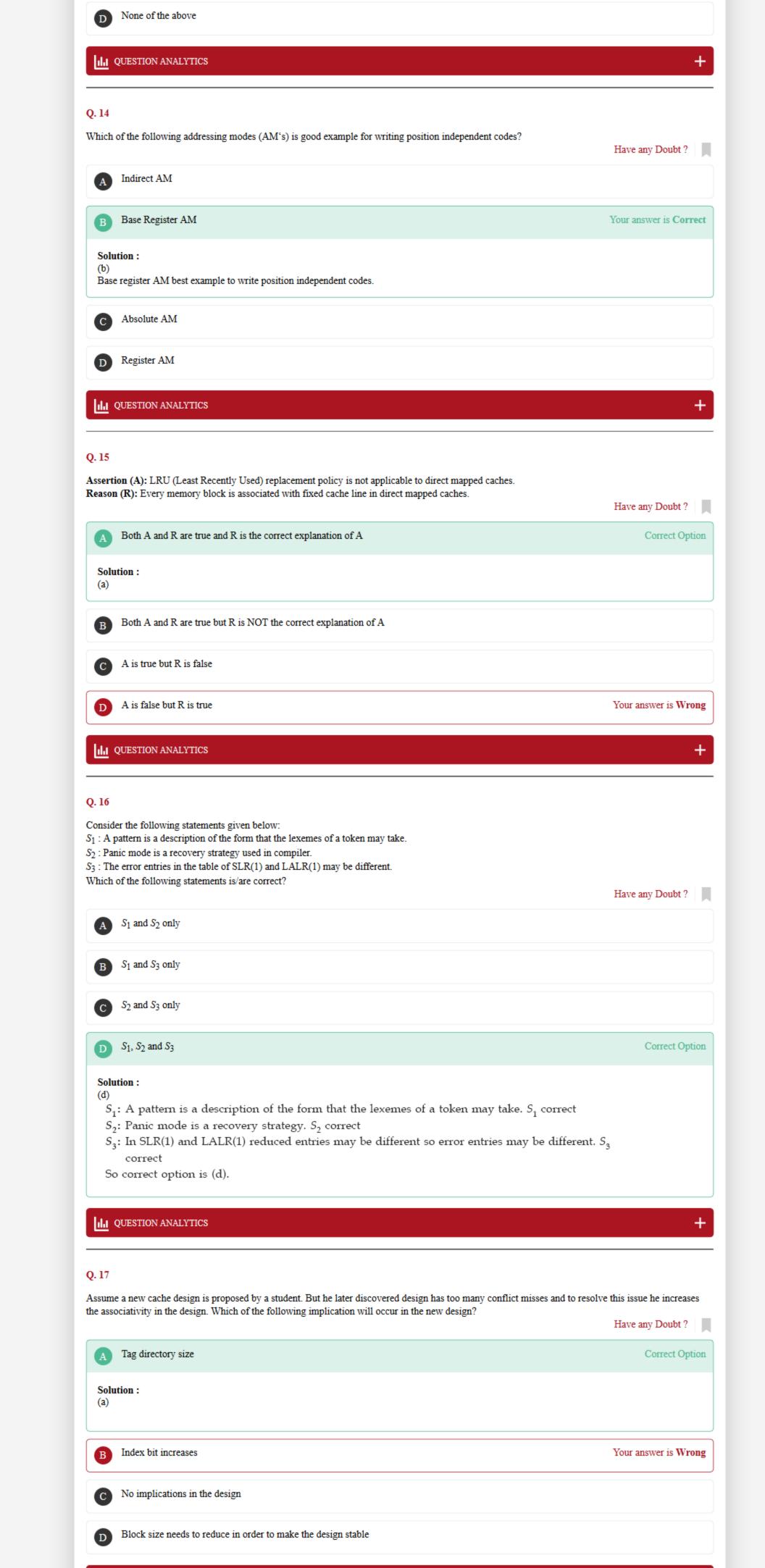
120 km/hr

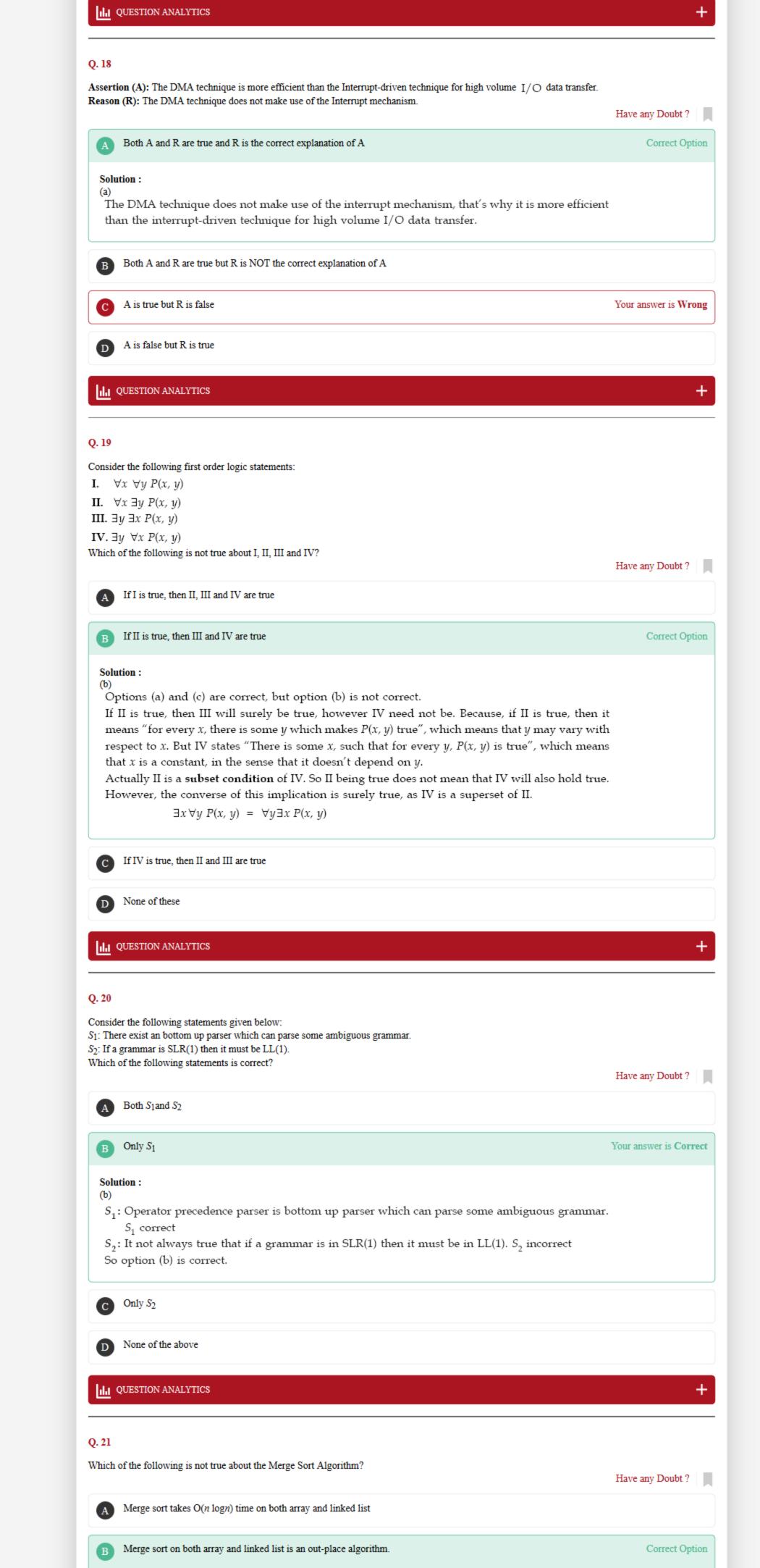


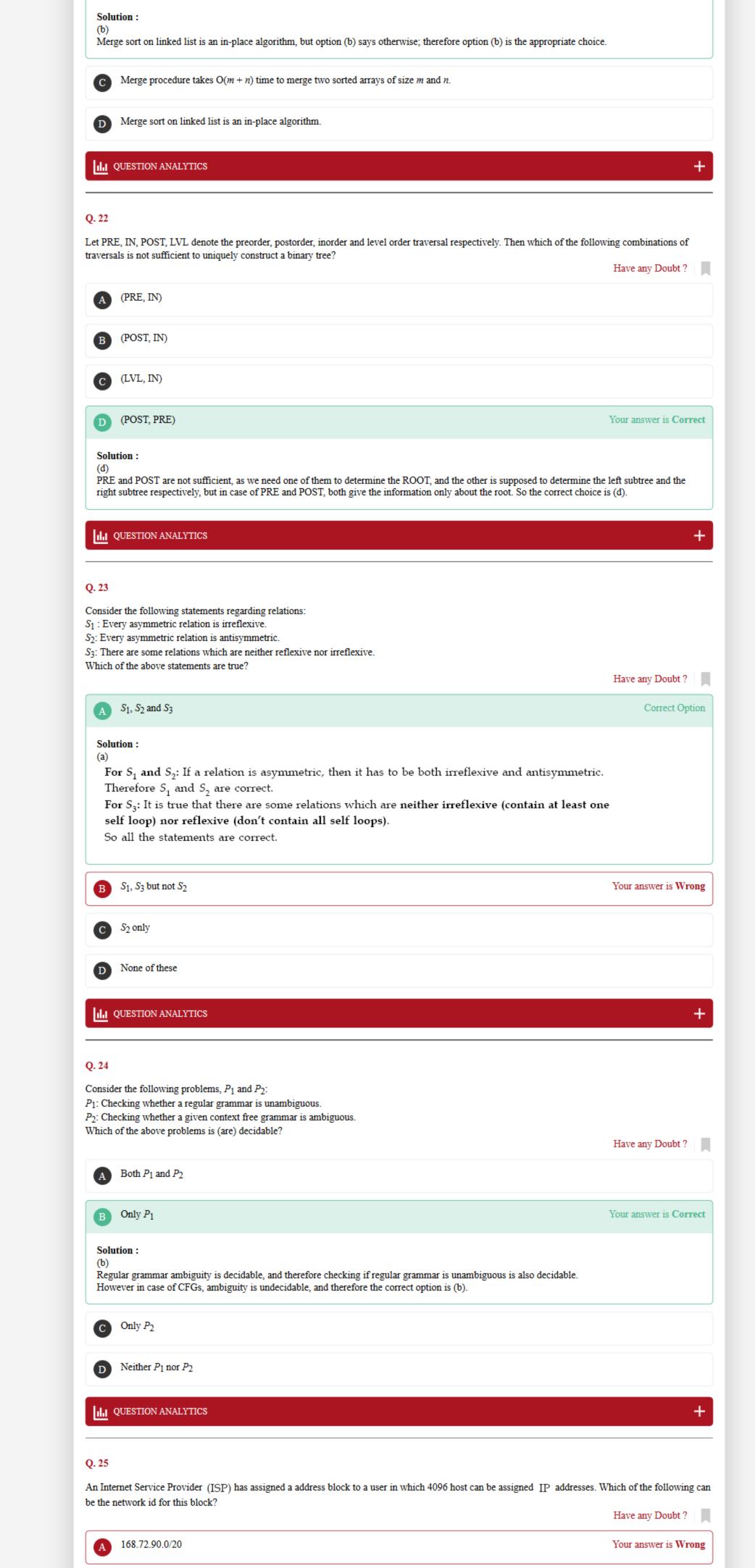
Correct Option

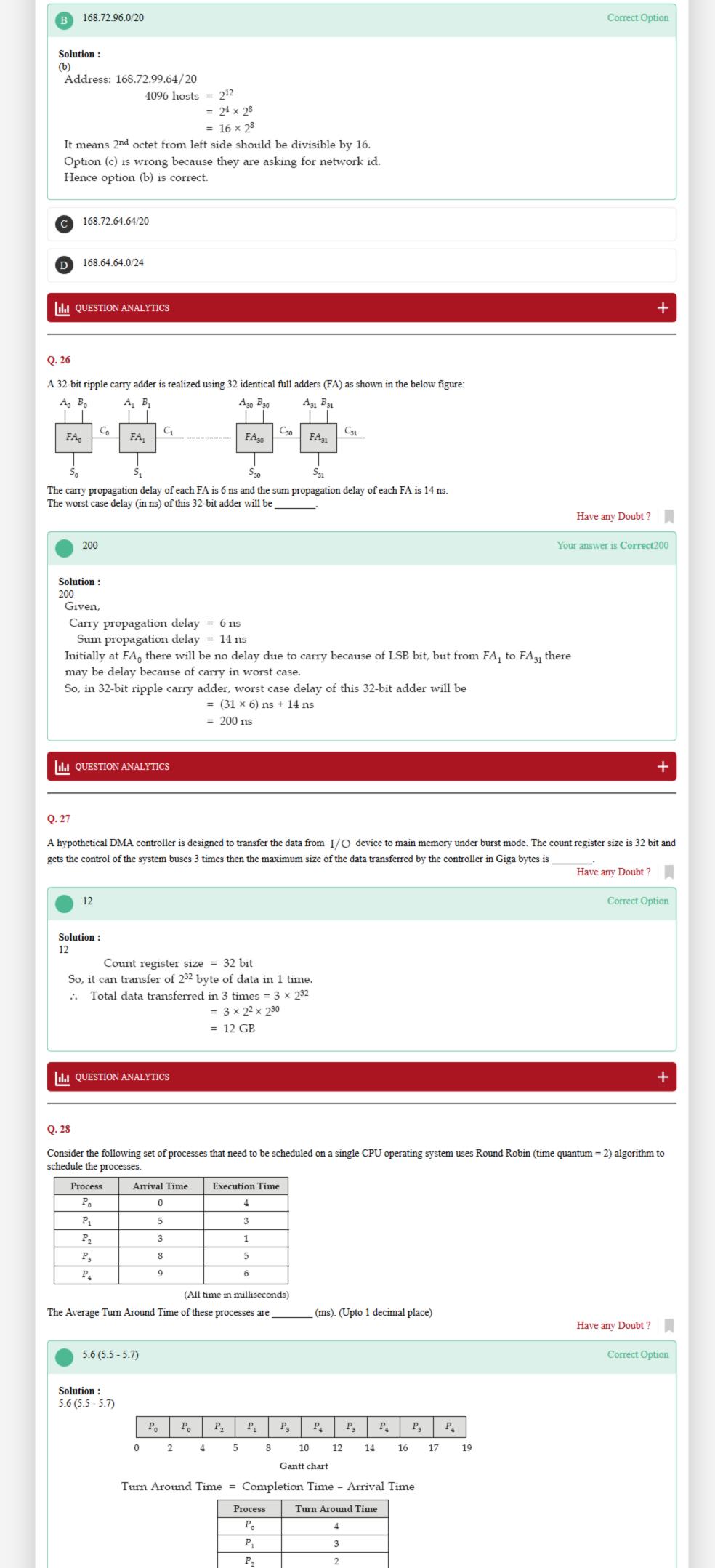
# Solution: Let the original speed of the train be 's' km/hour and the reduced speed will be (s - 50) km/hr. As per the question, a distance of 200 km is covered in 40 minutes more than the regular time taken to complete the journey. We can write the equation as $\frac{200}{s-50} - \frac{200}{s} = \frac{2}{3}$ or $300 \times 50 = s (s-50) = 150 \times 100$ which leads us to get s = 150 i.e. the original speed of the train is 150 km/hr i.e. option (b). 170 km/hr 210 km/hr III QUESTION ANALYTICS Q. 8 f(x) is a polynomial function of second degree such that f(-4) = 8, f(1) = 8 and f(3) = 15. What is the point at which the graph of this function intersects a line drawn parallel to y axis through x = 2? Solution Video Have any Doubt? (2, 8)(2, 10)(2, -11)D (2, 11) Correct Option Solution: Let, $f(x) = ax^2 + bx + c$ f(-4) = 16a - 4b + c = 8f(1) = a + b + c = 8 f(3) = 9a + 3b + c = 15Solving, we get $a = \frac{1}{2}$ , $b = \frac{3}{2}$ , c = 6This gives $f(x) = \frac{x^2}{2} + \frac{3x}{2} + 6$ . We have to find the value of f(x) at x = 2We can compute it as $f(2) = \frac{4}{2} + \frac{6}{2} + 6 = 11$ which leads us to get the desired point as (2, 11)i.e. (d). QUESTION ANALYTICS Q. 9 Sanjay and Mahesh are playing a game of bowling. Probability of Sanjay hitting the strike is 0.5 whereas Mahesh hitting the strike is 0.4. Sanjay wins if he hits the strike and Mahesh does not whereas Mahesh wins if he hits the strike and Sanjay does not. In the absence of these two happenings, the game ends in a tie. What is the probability on the tie? Solution Video | Have any Doubt? 0.40 0.45 0.50 Correct Option Solution: (c) Probability of Sanjay hitting the strike, P(S) = 0.5 gives probability of Sanjay NOT hitting the strike = $P(\overline{S}) = 1 - P(S) = 0.5$ . Similarly, Probability of Mahesh hitting the strike, P(M) = 0.4 gives probability of Mahesh NOT hitting the strike = $P(\overline{M}) = 1 - P(M) = 0.6$ In case of tie, Sanjay as well as Mahesh hit the strike OR both DO NOT hit the strike. Required probability = $P(S) \times P(M) + P(\overline{S}) \times P(\overline{M}) = 0.5 \times 0.4 + 0.5 \times 0.6 = 0.5$ D 0.55 III QUESTION ANALYTICS Q. 10 A square and a regular octagon have identical perimeter. The ratio of the areas of the square and the octagon is Solution Video Have any Doubt? 0.828 (0.827 - 0.829) Correct Option Solution: 0.828 (0.827 - 0.829) Sum of all of the interior angles of a polygon = $(n - 2)180^{\circ} = (8 - 2)180^{\circ} = 1080^{\circ}$ Therefore, Interior angle of a regular octagon = $\frac{1080}{8}$ = 135° $z = a \times a = a^2$ $x = \frac{1}{2} \frac{a}{\sqrt{2}} \cdot \frac{a}{\sqrt{2}} = \frac{a^2}{4}$

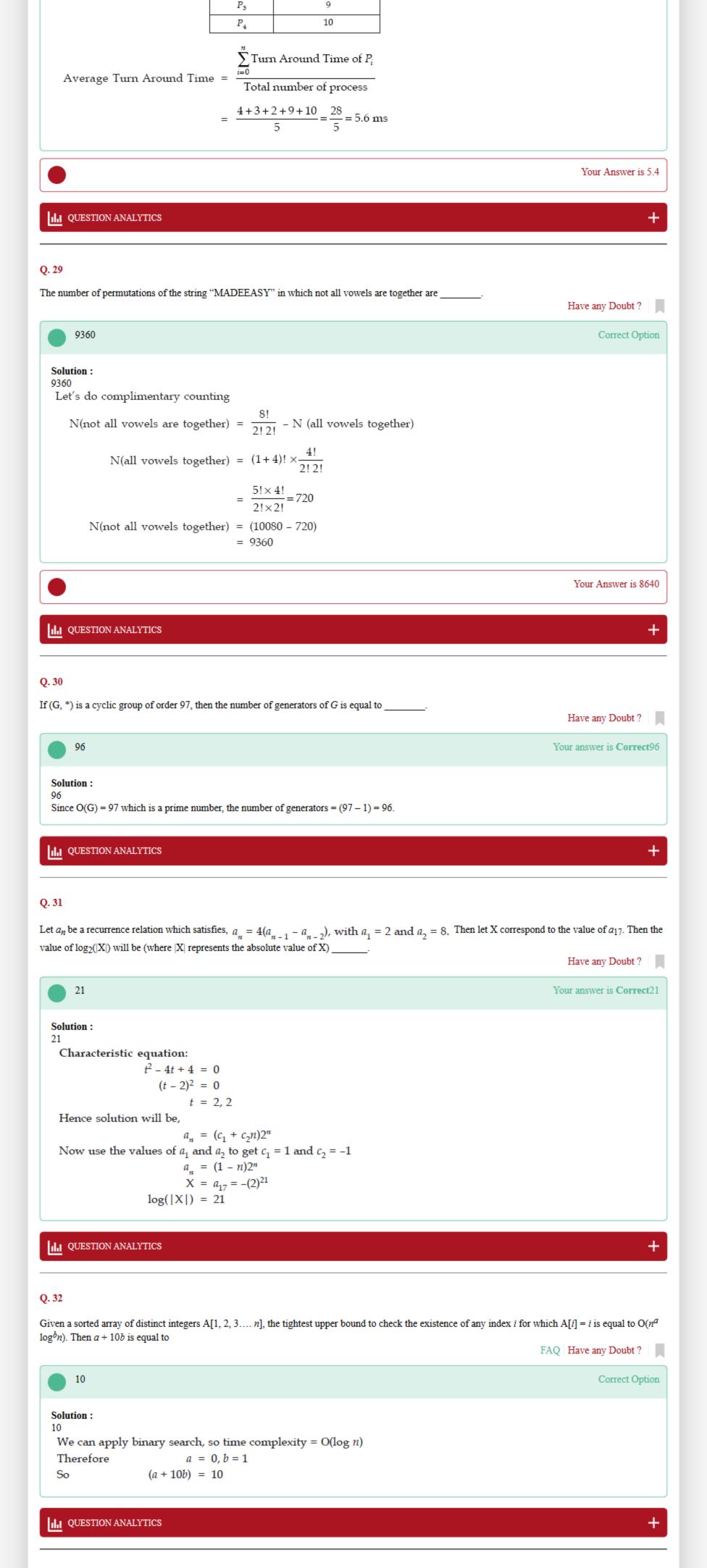




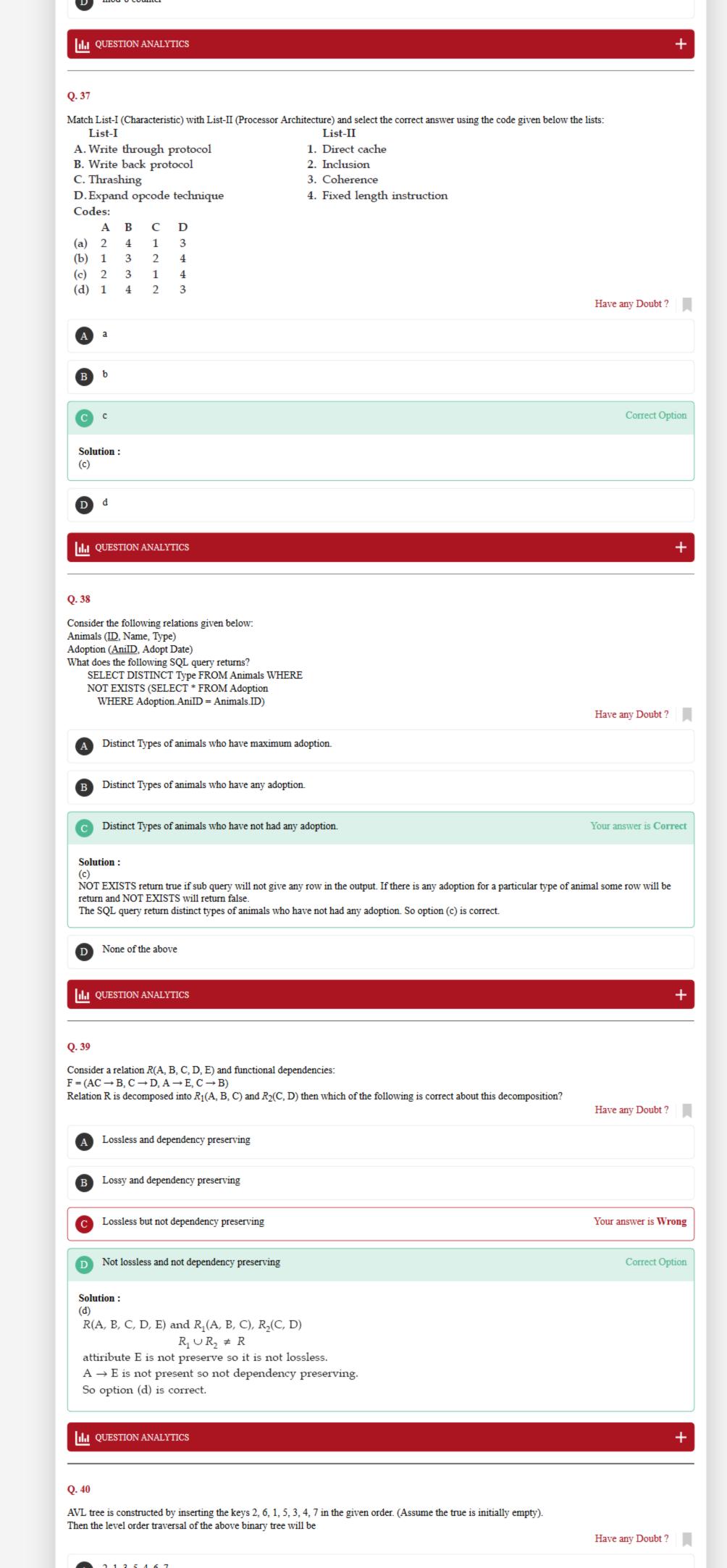


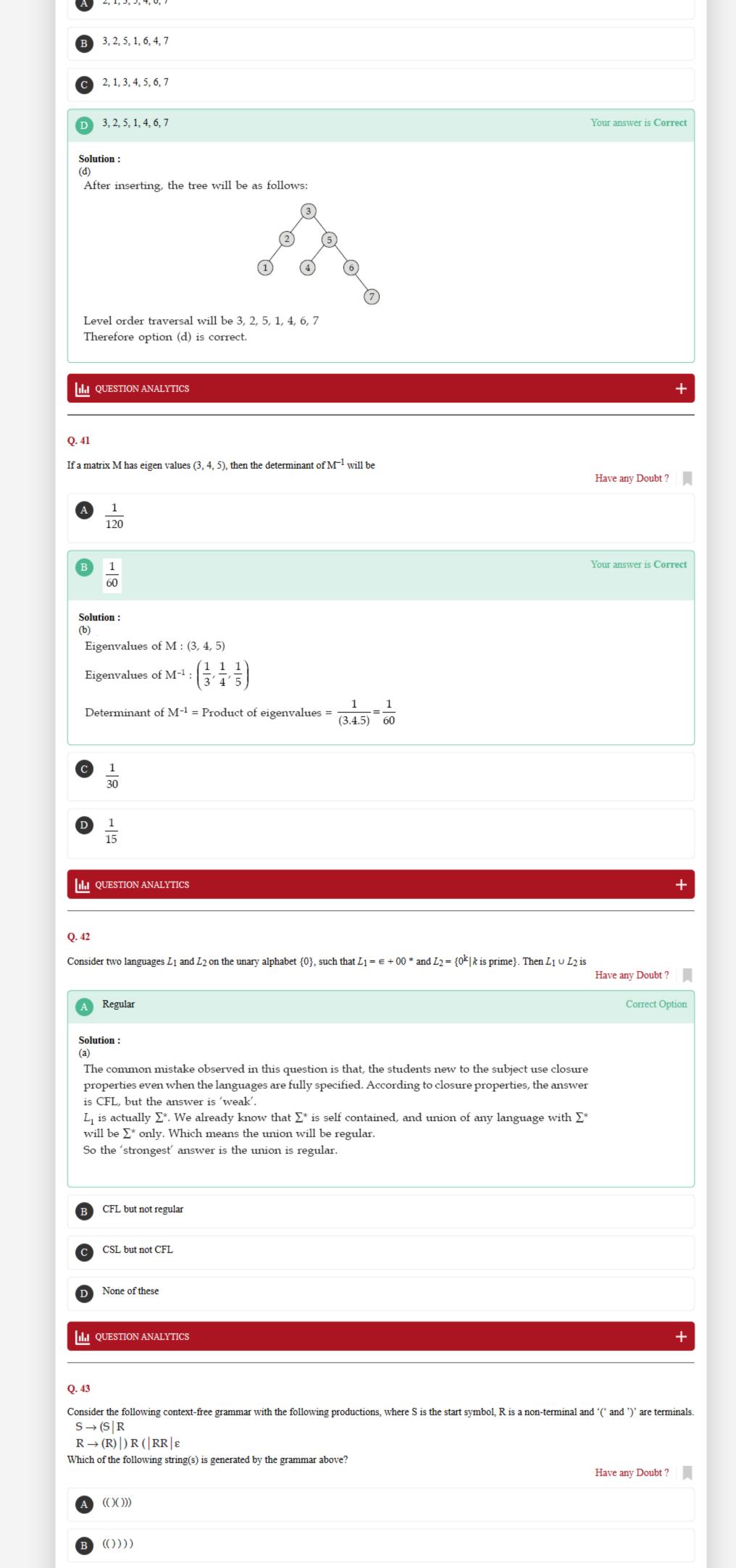


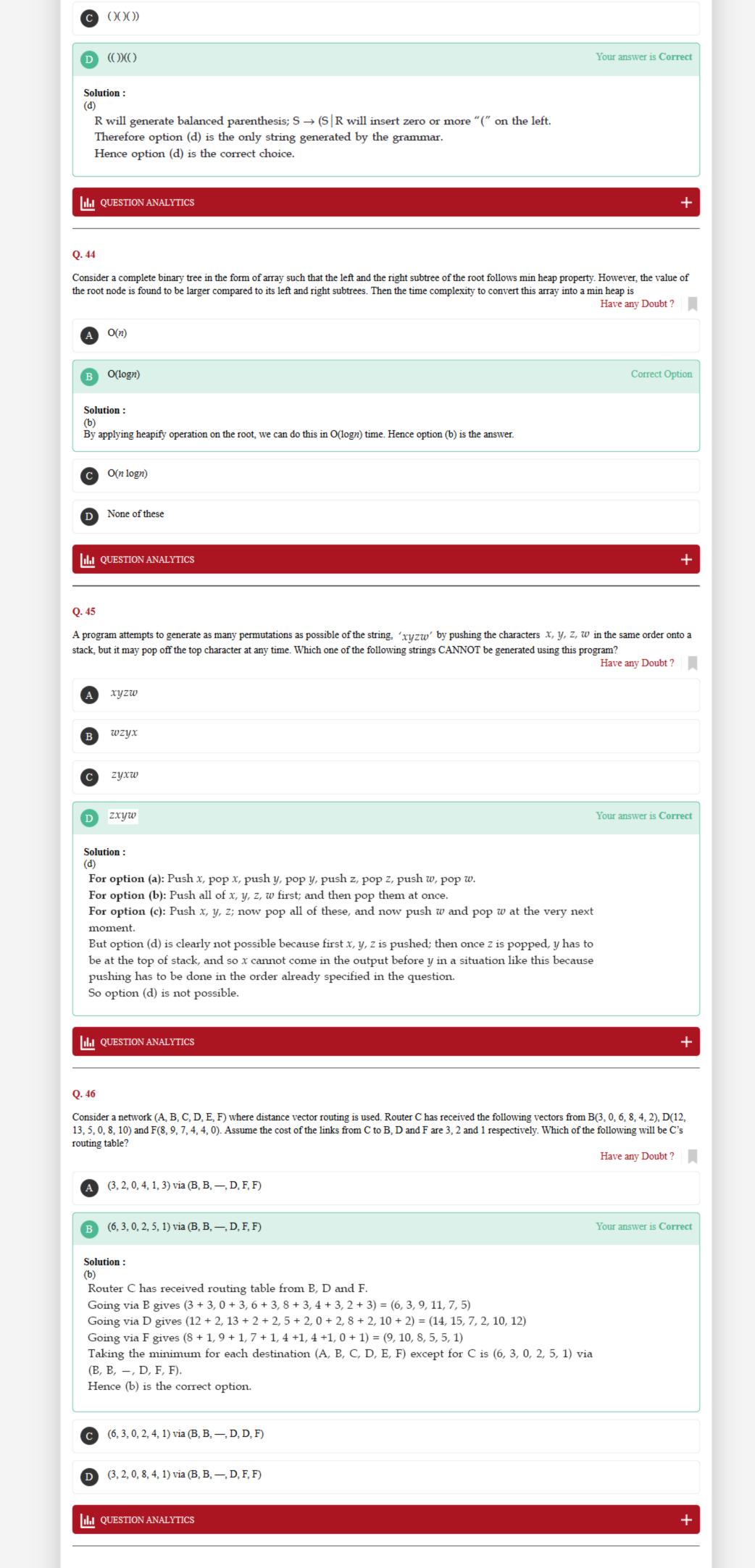




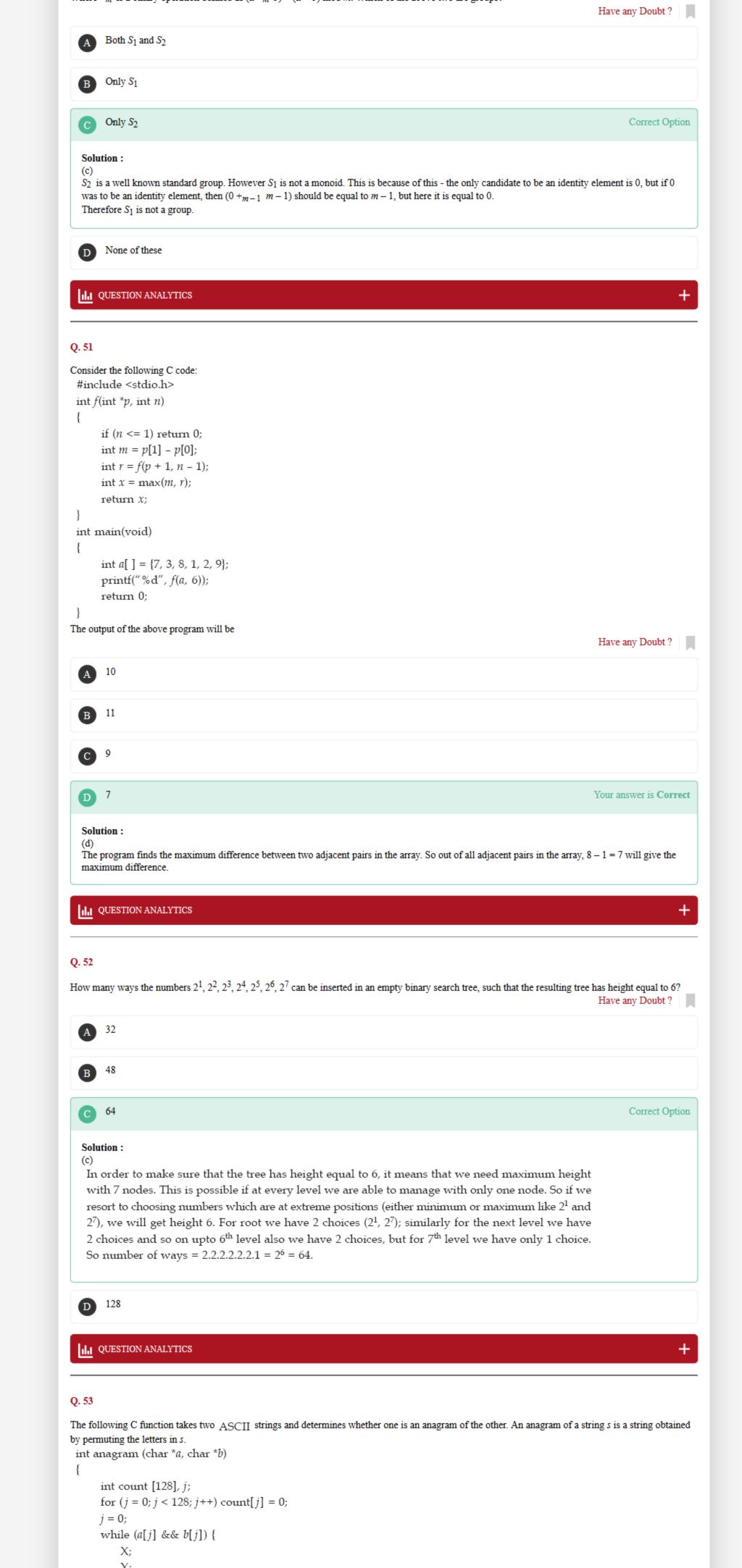
Q. 33 The number of perfect matchings in  $K_{1023}$ , where  $K_n$  denotes the complete graph with n vertices is equal to Have any Doubt? 0 Correct Option Solution: When n is odd,  $K_n$  does not have any perfect matching. So the number of perfect matchings will be equal to 0. QUESTION ANALYTICS Q. 34 The value of  $\lim_{x\to 0} \left(\frac{1-\cos x}{x^2}\right)$  will be \_\_\_\_\_\_. (Upto 2 decimal value) Have any Doubt? 0.50 (0.50 - 0.50) Your answer is Correct Solution: 0.50 (0.50 - 0.50)  $\lim_{x \to 0} \left( \frac{1 - \cos x}{x^2} \right) \left[ \frac{0}{0} \text{ form} \right]$ Applying L'Hospital rule,  $\lim_{x\to 0} \left(\frac{\sin x}{2x}\right)$  $= \frac{1}{2} \lim_{x \to 0} \left( \frac{\sin x}{x} \right)$  $= \frac{1}{2}(1)\left(\because \lim_{x\to 0}\frac{\sin x}{x} = 1\right) = \frac{1}{2}$ ILI QUESTION ANALYTICS Q. 35 Consider the following statements given below: S<sub>1</sub>: B trees are for primary index and B<sup>+</sup> trees are for secondary indexes. S<sub>2</sub>: An SQL query will not work if there are no index on the relation. The number of statements false are \_ Have any Doubt? Correct Option Solution:  $S_1$ : B trees are for primary index and  $B^+$  trees are for secondary indexes that is not true.  $S_1$  false  $S_2$ : It is not necessary to have a index on relation. SQL query will work without index on relation.  $S_2$  false III QUESTION ANALYTICS Q. 36 Consider the below circuit:  $Q_0$  (LSB) 3-bit  $Q_1$ synchronous up counter CLK - $Q_2$  (MSB) Reset The delay of NAND, NOT gate is 3 ns, 1 ns respectively and that of the counter is assumed to be zero. If the clock frequency is 500 MHz, then the counter behaves as a Have any Doubt? mod-5 counter mod-6 counter mod-7 counter Correct Option Solution: The counter will reset whenever  $(Q_2Q_1Q_0) = 101$ If the propagation delay of the gates were 0 ns, then circuit would have behaved as mod-5 counter as shown below: -000 -- 001 -- 010 -- 011 -- 100 -- 101 --3 4 Clock frequency = 500 MHz Clock time period = 2 ns However, the delay of NAND + NOT gate is 4 ns. During this time, two more clock pulses would reach the counter before reset the counter and it would count two more states. Hence it act as mod 7 counter.







```
Q. 47
In a RSA cryptosystem, a participant uses two prime numbers p and q is 19 and 13 respectively. If the public key is 7 then what is the private key in this
                                                                                                                        Have any Doubt?
  A
       29
  B 31
                                                                                                                       Your answer is Correct
  Solution:
         p = 19
         q = 13
        n = p \times q
           = 19 \times 13 = 247
     \phi(n) = (p-1) \times (q-1)
           = 18 \times 12 = 216
         e = 7
         d = e^{-1} \bmod \phi(n)
           = 7^{-1} \bmod \phi(n)
            = 31
  C 37
  D
       41
  QUESTION ANALYTICS
Q. 48
We are given log m sorted lists, each of size \log n/\log m. The time complexity of merging the lists into a single sorted list using merge sort is equal to
                                                                                                                        Have any Doubt?
        O(\log n.\log\log m)
                                                                                                                               Correct Option
  Solution:
   First let's find the height of the tree (say h).
                                h = O(\log \log m)
   The time to merge from level i to level i + 1 = O(\log n)
    So the total time to merge log m sorted lists into a single list of log n elements
                                    = O(\log n.\log \log m)
        O(\log m.\log \log n)
        O(\log m.\log n)
        O(m\log\log n)
  ILI QUESTION ANALYTICS
Q. 49
Let A[1 .... n] be an boolean array of 0's and 1's. Let f(m) be a function whose time complexity is \Theta(m). Consider the following piece of code written in C
 counter = 0;
 for (i = 1; i \le n; i++)
       if (a[i] == 1) counter++;
       else
           f(counter); counter = 0;
The complexity of this program fragment is
                                                                                                                        Have any Doubt?
       \Omega(n^2)
  \Omega(n\log n) and O(n^2)
        \Theta(n)
                                                                                                                               Correct Option
  Solution:
  The answer to this will be option (c), as irrespective of the arrangement of the numbers in the array, the time spent will always be proportional to n.
  D O(n)
  QUESTION ANALYTICS
Q. 50
Let S_1 and S_2 be two algebraic structures as described below:
S_1: (\{0, 1, 2, 3, 4, ..., m-1\}, +_{m-1})
S_2: (\{0, 1, 2, 3, 4, ..., m-2\}, +_{m-1})
Where + \dots is a binary operation defined as (a + \dots b) = (a + b) \mod m Which of the above two are groups?
```



```
for (j = 0; j < 128; j++) if (count [j]) return 0;
       return 1;
Choose the correct alternative for statements X and Y.
                                                                                                                    Have any Doubt?
       X: count [a[j]]++ and Y: count[b[j]]--
       X: count [a[j]]++ and Y: count[b[j]]++
       X: count [a[j++]]++ and Y: count[b[j]]--
  \square X: count [a[j]]++ and Y: count[b[j++]]--
                                                                                                                           Correct Option
  Solution:
  III QUESTION ANALYTICS
Q. 54
Consider the following two function P and Q which share two common variable A and B:
           P()
                                                  Q()
                                                  A = B + 6;
           A = A + 5;
                                                  B = A - 2;
           B = A - 3;
If P and Q executing concurrently, initial value of A = 2 and B = 3 than sum of all different final values B can take _____. (Do not count B = 3)
                                                                                                                    Have any Doubt?
                                                                                                                           Correct Option
  Solution:
   If P and Q execute serially
                               A = A + 5 (7)
                                                    A = B + 6 (9)
                               B = A - 3(4)
                                                        B = A - 2(7)
                                                     A = A + 5 (14)
                               A = B + 6 (10)
                               B = A - 2(8)
                                                        B = A - 3 (11)
                          B can take values 8
                                                        B can take values 11
   If P and Q executing concurrently.
         A = A + 5 (7) A = A + 5 (7)
                                                                                          A = B + 6 (9)
                                                             A = B + 6 (9)
         A = B + 6 (9)
                             A = B + 6 (9)
                                                                 A = A + 5 (14)
                                                                                              A = A + 5 (14)
          B = A - 2(7)
                             B = A - 3(6)
                                                                 B = A - 3 (11)
                                                                                               B = A - 2(12)
          B = A - 3(6)
                               B = A - 2(7)
                                                                  B = A - 2 (12)
                                                                                               B = A - 3 (11)
                                                            B can take values 12
   B can take values 6
                                B can take values 7
                                                                                             B can take values 11
    B can takes values 6, 7, 8, 11, 12.
                            Sum = 6 + 7 + 8 + 11 + 12 = 44
                                                                                                                        Your Answer is 30
  ILI QUESTION ANALYTICS
Q. 55
Consider the following page reference string:
1, 2, 3, 4, 5, 1, 3, 2, 5, 1, 4, 2, 1, 6
How many page faults would occur for Least Recently Used (LRU) page replacement algorithm with 3 available frame in main memory
                                                                                                                    Have any Doubt?
       13
                                                                                                                 Your answer is Correct13
  Solution:
    LRU replace the page which is least recently used.
                                            1 3 2 5 1 4 2
                                 4 5
                                             6
                                                  7
                                                        8
                                                              9
                                                                                            (13)
                                                                    10
    Total 13 page fault.
  III QUESTION ANALYTICS
Q. 56
Consider the following program codes:
                                 Meaning
  \begin{split} I_1 &: \text{LOAD } r_1, \ (r_0) & r_1 \leftarrow \text{M}[[r_0]] \\ I_2 &: \text{ADD } r_1, \ r_2 & r_1 \leftarrow r_1 + r_2 \\ I_3 &: \text{ADD } r_3, \ r_4 & r_3 \leftarrow r_3 + r_4 \end{split}
   \begin{split} I_4 \colon \text{LOAD } (r_0) \ r_3 & \text{M}[[r_0]] \leftarrow r_3 \\ I_5 \colon \text{SUB } r_1, \ r_3 & r_1 \leftarrow r_1 - r_3 \end{split}
   I_6: HALT
                                 Halts
   I_7: ADD r_2, r_1
                                 r_2 \leftarrow r_1 + r_2
```

The data transfer instruction size is 64 bit, ALU operation instruction size is 32 bit and branch instructions size is 16 bit.

If an interrupt occurs during the execution of  $I_{6'}$  the return address pushed on to the stack is \_ Have any Doubt? 3028 Correct Option Solution: 3028  $I_1: 3000 - 3007$  $I_2$ : 3008 - 3011  $I_3$ : 3012 – 3015 I<sub>4</sub>: 3016 - 3023  $I_5:3024-3027$  $\rightarrow$   $I_6$ : 3028 - 3029  $\rightarrow$  interrupt  $I_7:3030-3033$ Return address 3028 pushed on to the stack due to HALT instructions. **ILI** QUESTION ANALYTICS Q. 57 Consider a system with 48 bit virtual address and page size is 16 KB. Operating system uses multi level paging. Page table entry size is 4B. What is number of entries in last level page table such that last level page table will fit into one page Have any Doubt? 1024 1024 Your answer is Correct Solution: Virtual address = 48 bit  $1^{\text{st}}$  level page table size =  $\frac{\text{Virtual address}}{\text{Page size}} \times e$  $= \frac{2^{48}}{2^{14}} \times 4B = 2^{36}B$  $2^{\text{nd}}$  level page table size =  $\frac{2^{36}}{2^{14}} \times 4B = 2^{24}B$  $3^{\text{rd}}$  level page table size =  $\frac{2^{24}}{2^{14}} \times 4B = 2^{12}B$ It will fit in one page so total 3 levels of paging.  $3^{\text{rd}}$  level page table entries =  $\frac{2^{24}}{2^{14}} = 2^{10} = 1024$ QUESTION ANALYTICS Q. 58 Consider the following CFG:  $S \rightarrow Aa \mid ca$  $A \rightarrow c \mid d$ (Where S, A are nonterminal and a, c, d are terminals) How many conflict occur (both shift reduce and reduce-reduce) in CLR(1) parsing construction \_ Have any Doubt? Correct Option 1 Solution: S' →S.,\$  $S' \rightarrow .S, \$$  $S \rightarrow Aa$ , \$  $S \rightarrow A.a, $$  $5 \rightarrow .ca, $$  $A \rightarrow .c$ , a  $A \rightarrow .d$ , a 5 → Aa., \$ A → d., a  $S \rightarrow c.a, $$  $S \rightarrow c., a$  $S \rightarrow ca., $$ 1 shift reduce conflict There is one shift reduce conflict. ILI QUESTION ANALYTICS Q. 59 Consider the following three concurrent processes: Process 0 Process 1 Process 2 while (1) while (1) while (1) P(B); P(A); P(A); printf("1"); printf("0"); printf("2"); V(A); V(A); P(A); A and B are two counting semaphore variable and P and V are usual semaphore operation if A = 0, B = 4 what is the minimum number of 0's printed by the execution of the above processes \_ Have any Doubt? 0 Your answer is Correct0

Solution:

Assume program has been loaded in the memory starting from the location 5000 decimal onwards.

(i) A = 0, B = 4Process 0 execute 4 times and blocked, now value of A = 4. (ii) A = 4, B = 0Process  $P_2$  execute 4 time and blocked, now value of A = 0, B = 0. (iii) Process 1 execute P(A) and blocked, number of times 0 is printed is 0. ILI QUESTION ANALYTICS Q. 60 Consider the basic block given below:  $a \rightarrow a * b$  $c \rightarrow a + c$  $e \rightarrow c/e$  $a \rightarrow c + e$ Minimum number of nodes and edges present in DAG representation of the above block is x and y respectively value of x + y is \_\_\_\_\_. Have any Doubt? 16 Your answer is Correct16 Solution: 16 a = a \* b c = a + c e = c/e a = c + e c = a \* b = c c = (a \* b) + c c = c/e a = c + (c/e)DAG representation Total 8 nodes and 8 edge x + y = 8 + 8 = 16QUESTION ANALYTICS Q. 61 Consider a relation R(A, B, C, D, E, F, G) and set of functional dependencies F.  $F = \{BCD \rightarrow A, BC \rightarrow E, A \rightarrow F, F \rightarrow G, C \rightarrow D, A \rightarrow G\}$ Number of tables required to decompose R into BCNF is \_\_\_\_ Have any Doubt? Solution: R(A, B, C, D, E, F, G) Closure of  $(BC)^+$  = BCEDAFG {BC} is a key of R Minimal cover of F is F'  $F' = \{BC \rightarrow A, BC \rightarrow E, A \rightarrow F, F \rightarrow G, C \rightarrow D\}$ Now decompose into BCNF.  $R_1(B, C, A, E), R_2(A, F), R_3(F, G), R_4(C, D)$ So total 4 tables required. ILI QUESTION ANALYTICS Q. 62 A channel has a bit rate of 8 Kbps and a propagation delay of 15 msec. The minimum frame size in stop and wait protocol that gives an efficiency of atleast 50% is \_\_\_\_\_. (in bits) Have any Doubt? 240 Your answer is Correct240 Solution: 240 Propagation time = 15 msec Round Trip Time (R.T.T.) = 2 × 15 msec = 30 msec 8 KB ...... 1 sec ? ...... 1 msec 1 msec =  $\frac{8 \times 10^3 \text{ bits}}{10^3}$  = 8 bits Ιn So, in 1 RTT,  $30 \text{ msec} = 30 \times 8 \text{ bit} = 240 \text{ bit}$ To get efficiency of atleast 50%, user should transmit data atleast of 240 bit. ILI QUESTION ANALYTICS Q. 63 Given,  $A(x) = \frac{1+x}{(1-x)^3}$ ; and  $A(x) = \sum_{r=0}^{\infty} a_r x^r$ .

The value of  $(a_3 - a_0)$  will be \_\_\_\_\_.

Have any Doubt?

Your answer is Correct15

15

Solution:

Rewriting, 
$$\frac{1+x}{(1-x)^3} = \frac{1}{(1-x)^3} + \frac{x}{(1-x)^3}$$

We know,  $\left(\frac{1}{(1-x)^3}\right)$  corresponds to  $a_r = {}^{3-1+r}C_r$   $= {}^{2+r}C_r = {}^{2+r}C_2$ 

$$a_r = 3 - 1 + rC_r$$
  
=  $2 + rC_r = 2 + rC_2$ 

Now

$$\frac{1}{(1-x)^3} + x \cdot \frac{1}{(1-x)^3}$$

$$\downarrow \qquad \qquad \downarrow$$

# ILI QUESTION ANALYTICS

### Q. 64

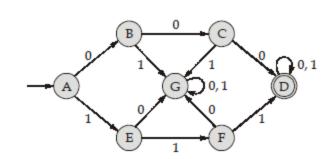
The number of states in the minimal DFA of the set of strings over {0, 1} which start with 000 or 111 is \_\_\_\_\_

Have any Doubt?

Your answer is Correct7

Solution:

7



The minimal DFA has 7 states, so 7 is the answer.

QUESTION ANALYTICS

### Q. 65

Recall that a list of elements is called a binary min-heap if in its tree representation, the root is the smallest in magnitude compared to its left and right subtrees. Out of all the possible permutations of {1, 2, 3, 4, 5, 6, 7}, a permutation is picked at random. The probability that the permutation satisfies the min-heap property is \_\_\_\_\_\_. (Upto 3 decimal places)

Have any Doubt?

0.015 (0.015 - 0.016)

Correct Option

### Solution:

0.015 (0.015 - 0.016)

In order to find the required probability, let's find the number of minheaps possible with {1, 2, 3,

Number of min heaps =  $1 \times {}^6C_3 \times 2! \times {}^3C_3 \times 2! = 80$ 

Total number of permutations = 7! = 5040

Therefore the required probability =  $\frac{80}{5040}$  = 0.0158 (can be rounded to 0.016 or 0.015 whichever

**ILL** QUESTION ANALYTICS

suits the user).