

HW7: Floating point and real conversions

(CS220-02)

1) Show your work to calculate the binary real valued equivalent of 3.17 with 5 bits of precision in the fractional portion of the result.

$$17 = 10001$$

$$100 = 1100100 \rightarrow \text{convert to neg} = 0011011 + 1 = 0011100 \rightarrow$$

$$\begin{array}{r}
 0.00101 \\
 \hline
 1100100 \mid 10001.00000 \\
 + 0011100 \\
 \hline
 010010000
 \end{array}$$

$$3 = 11$$

$$3.17 = 11.00101$$

2) Show your work to calculate the binary real valued equivalent of 21.9 with 5 bits of precision in the fractional portion of the result.

$$9 = 01001$$

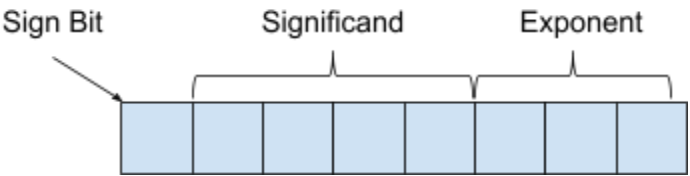
$$100 = 1100100 \rightarrow \text{convert to neg} = 0011011 + 1 = 0011100$$

$$\begin{array}{r}
 0.00010 \\
 \hline
 1100100 \mid 01001.00000 \\
 + 1100100 \\
 \hline
 1011000
 \end{array}$$

$$21 = 10101$$

$$21.9 = 10101.00010$$

For problems 3 through 11, assume a generic 8 bit floating point representation with the layout shown below...



3-6) Given the floating point binary pattern, 00110101₂, what is the decimal equivalent (fractions are preferred [e.g., $-4\frac{7}{8}$]) for each significand and exponent interpretation below?

		Significand	
		Denormal	Normal
Exponent	Unbiased	<div>+ 0.011 E -3</div> <div>101 -> 010+ 1 = 011 = 3</div> <div>+0.000011</div> <div>+3/64</div>	<div>+ 1.0011 E - 3</div> <div>+0.00010011</div> <div>+ 19/ 256</div>
	Bias = -3	<div>+ 0.011 E -6</div> <div>+0.000000011</div> <div>+3/512</div>	<div>+ 1.0011 E -6</div> <div>+0.000000011</div> <div>+3/512</div>

7-10) Given the floating point binary representation, determine the bit pattern used to store the binary value -11.01101_2 for each of the significand and exponent representations in the table below. $-11.01101 = -1.101101 E+ 1$

$11 = 3$
 $.01101 = 13/32$

		Significand	
		Denormal	Normal
Exponent	Unbiased	1 1101 001	1 1011 001
	Bias = -5	1 1101 110 E = exp + B 1 = exp + -5 exp = 6 = 110	1 1011 110

11) For the floating point representation provided using a denormalized significand and unbiased exponent. **SHOW WORK (or at least show all equivalent binary scientific notation)** to determine how many ways one can represent the exact value $+1 \frac{1}{2}$.

$$1 = 1$$

$$0.5 = 50/100$$

$$100 = 1100100 \rightarrow 0011011 + 1 = 0011100$$

$$50 = 110010$$

$$\begin{array}{r}
 00000.10000 \\
 \hline
 1100100 \mid 110010.00000 \\
 1100100 \\
 \hline
 00000
 \end{array}$$

$$0.5 = .100000 =$$

$$1.5 = 1.1 E0$$

$$0 = 000 \rightarrow 111 + 1 = 1000 = (\text{truncate}) 000$$

	denorm	norm
unb	1 1100 000	1 1000 000
b	1 1100	1 1000

(no bias so actually only 2 ways)

: 1 1100 000 and 1 1000 000