

HW3: Standard bases and conversions

(CS220-02)

1) Convert the following decimal numbers using the iterative integer division (quotient-remainder) technique from lecture. Don't forget to print the final result with its base identified.

(a) 345 to base 2

Q	R
172	1
86	0
43	0
21	1
10	1
5	0
2	1
1	0
0	1

101011001
(base 2)

(b) 654 to base 6

Q	R
109	0
18	1
3	0
0	3

3010 (base 6)

2) Show the conversion from 0xBA5E to binary using the common base factor technique from class.

$$16 = 2^4 \leftrightarrow 2^1$$

0xBA5E : B= 1011, A= 1010, 5 = 0101, E=1110
put all together

1011101001011110

3) Show the conversion from the octal value 50267 to binary using the common base factor technique from class.

$$2^3 \leftrightarrow 2^1$$

$$5 = 101$$

$$0 = 000$$

$$2 = 010$$

$$6 = 110$$

$$7 = 111$$

put together: 101000010110111

4) Show the conversion from 0xC731 to base 4 using the common base factor technique from class.

$$16 = 2^4 \leftrightarrow 2^1 \leftrightarrow 2^2$$

0xC731 : C= 1100, 7= 0111, 3 = 0011, 1 = 0001

put all together = 1100011100110001 split into groups of 2: 11 00 01 11 00 11 00 01

-> convert each group to base 4

11 -> 3, 00 -> 0, 01 -> 1, 00 -> 0, 11 -> 3, 00 -> 0, 01 -> 1

= 3010301 (base 4)

5) Show the conversion from 2021013₄ to hexadecimal using the common base factor technique from class.

$$4 = 2^2 \leftrightarrow 2^1 \leftrightarrow 2^4 = 16$$

2021013: 2= 10, 0= 00, 2= 10, 1=01, 0=00, 1=01, 3=11

put all together = 10001001000111 split into groups of 4: 0010 0010 0100 0111

-> convert each group to base 16

0010= 2, 0010= 2, 0100= 4, 0111= 7

= 2247 (base 16)

6) Show the conversion from 0xD6B4A to octal using the common base factor technique from class.

$$16 = 2^4 \leftrightarrow 2^1 \leftrightarrow 2^3 = 8$$

0xD6B4A : D= 1101, 6= 0110, B = 1011, 4= 0100, A = 1010

put all together = 11010110101101001010 split into groups of 3: 011 010 110 101 101 001 010

-> convert each group to base 8

011 -> 3, 010 -> 2, 110 -> 6, 101 -> 5, 101 -> 5, 001 -> 1, 010 -> 2

= 3265512 (base 8)

7) Show the conversion from 311203_4 to octal using the common base factor technique from class.

$$4 = 2^2 \leftrightarrow 2^1 \leftrightarrow 2^3 = 8$$

311203 : $3=11$, $1=01$, $1=01$, $2=10$, $0=00$, $3=11$
put all together = 110101100011 split into groups of 3: $110\ 101\ 100\ 011$
-> convert each group to base 8
 $110=6$, $101=5$, $100=4$, $011=3$
= 6543 (base 8)

8) Show the conversion from the octal value 753721 to hexadecimal using the common base factor technique from class.

$$8 = 2^3 \leftrightarrow 2^1 \leftrightarrow 2^4 = 16$$

753721 : $7=111$, $5=101$, $3=011$, $7=111$, $2=010$, $1=001$
put all together = 11110101111010001 split into groups of 4: $0011\ 1101\ 0111\ 1101\ 0001$
-> convert each group to base 16
 $0011=3$, $1101=13=D$, $0111=7$, $1101=13=D$, $0001=1$
= $3D7D1$ (base 16)

9) Show the conversion from 4170348_9 to base 3 using the common base factor technique from class.

$9 = 3^2 \leftrightarrow 3^1 = 3$
 4170348_9 : $4=11$, $1=01$, $7=21$, $0=00$, $3=10$, $4=11$, $8=22$
combine:
 11012100101122 (base 3)

10) Show the conversion from $0x57AE$ to binary using the common base factor technique from class.

$$16 = 2^4 \leftrightarrow 2^1$$

$0x57AE$: $5=0101$, $7=0111$, $A=1010$, $E=1110$
put all together

0101011110101110

11) Show the conversion from 11010101101001111011_2 to octal using the common base factor technique from class. The number is rewritten below to prevent copy mistakes.

11010101101001111011

group by 3: 011 010 101 101 001 111 011 (added 0 to front for 3 digits per group)
convert each group to octal:
011=3, 010=2, 101=5, 101=5, 001=1, 111=7, 011=3
put all together: 3255173 (base 8)

12) What is the **character** (*not hex or decimal code... eg, 'a' is a character*) in the variable once this line of code completes?

```
char letter = 'f' - 'a' + 'A';
```

f = 102 , a = 97 , A = 65
 $102 - 97 + 65 = 70 = 'F'$

13) What is the **character** (*not hex or decimal code... eg, 'a' is a character*) in the variable once this line of code completes?

```
char letter = 'D' - 'A' + 'a';
```

D = 68, A = 65, a = 97
 $68 - 65 + 97 = 100$
100 = 'd'

14) Show the conversion to the BCD bitstring equivalent of the decimal number 174638?

1 = 0001, 7 = 0111, 4 = 0100, 6 = 0110, 3 = 0011, 8 = 1111
combine:
000101110100011000111111 (BCD)

15) Show the conversion to the decimal equivalent of the BCD bitstring 10101011000001001_{BCD}?

10101011000001001_{BCD}

split: 0001 0101 0110 0000 1001 , add 0's to beginning:
0001=1, 0101=5, 0110=6, 0000=0, 1001=9
combine:
15609 (base 10)

16) Show the conversion to the BCD bitstring equivalent of the number 103647₈?
Careful, this one requires more than one conversion step.

103647(base 8) -> decimal:
each digit * corresponding coeff: $7 \cdot 2^0 + 4 \cdot 2^1 + 6 \cdot 2^2 + 3 \cdot 2^3 + 0 \cdot 2^4 + 1 \cdot 2^5$
 $7 + 8 + 24 + 24 + 32 = 95$
9 = 1001 (binary)
5 = 0101 (binary)
combine:
10010101 (BCD)