

HW5: Truncation, Sign Extension, and Arithmetic (CS220-02)

- 1) What is the resulting bit pattern when the unsigned 10 bit binary value 1101001101 is stored in an 8 bit container?

1101001101 -> chop off first 2 bits: 01001101

- 2) What is the resulting bit pattern when the signed 10 bit binary value 1100101110 is stored in an 8 bit container?

1100101110 -> chop off first 2 bits: 00101110
truncation doesn't matter signed or unsigned

- 3) What is the resulting bit pattern when the unsigned 8 bit binary value 11001101 is stored in a 10 bit container?

11001101 -> add 2 0s : 0011001101
extension if unsigned add 0's

- 4) What is the resulting bit pattern when the signed 8 bit binary value 01001101 is stored in a 10 bit container?

01001101 -> add 2 0s : 0001001101
extension if signed add whatever 1st digit is before

- 5) What is the resulting bit pattern when the signed 8 bit binary value 10110010 is stored in a 10 bit container?

10110010 -> add 2 1s : 1110110010

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**For problems 6 through 22, assume a 6 bit machine and that
A = 000111, B = 111100, C = 011010, D = 110101 and E = 111101**

- 6) (a) Show work to find unsigned A + C. (b) What is the decimal equivalent of the answer?

$$A = 7, C = 26$$

$$000111$$

$$+ 011010$$

$$= 100001$$

$$= 2^5 + 1 = 33$$

- 7) (a) Show work to find unsigned D + E. (b) What is the decimal equivalent of the answer?

$$110101$$

$$+ 111101$$

$$= 1110010 \rightarrow \text{extra bit added chop off} = 110010$$

$$= 114 \text{ before chop off, } 50 \text{ after}$$

$$D = 53, E = 61 \text{ total should be } 114 \text{ total}$$

- 8) (a) Show work to find signed 2s complement A + D. (b) What is the decimal equivalent of the answer?

Signed addition: binary add then find 2's complement to find real value

$$000111 : 7$$

$$+ 110101 : +53$$

$$= 111100 : 60$$

$$2's \text{ complement: } 111100 \rightarrow 000011 + 1 = 000100$$

so the answer 60 was originally a -4

- 9) (a) Show work to find signed 2s complement -B + C. (b) What is the decimal equivalent of the answer?

$$-111100 : 60 \text{ convert to pos} \rightarrow = 000011 + 1 = 000100$$

$$+011010 : 26$$

=

$$000100 : -60$$

$$+011010 : 26$$

$$=011110 : 30. \rightarrow 2's \text{ complement} = 100001 + 1 = 100010 = 34$$

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10) (a) Show work to find signed 2s complement $A + -B$. (b) What is the decimal equivalent of the answer?

$A = 000111 : 7$, $B = 111100 : 60$, convert $-B$ to pos: $= 000100$

$$\begin{array}{r} 000111 \\ + 000100 \\ \hline = 001011 : 11 \end{array} \rightarrow 2\text{'s complement} = 110100 + 1 = 110101 = 53$$

11) (a) Show work to find signed 2s complement $C + E$. (b) What is the decimal equivalent of the answer?

$c = 011010$, $e = 111101$

$$\begin{array}{r} 011010 : 26 \\ + 111101 : 61 \\ \hline 1010111 \text{ truncate} \rightarrow 010111 = 23 \end{array}$$

2's complement: $010111 \rightarrow 101000 + 1 = 101001 = 41$

*not sure if to truncate excess 7th bit before or after 2's complement...

12) (a) Show work to find signed 2s complement $B + D$. (b) What is the decimal equivalent of the answer?

$b = 111100$ $D = 110101$

$$\begin{array}{r} 111100 : 60 \\ + 110101 : 53 \\ \hline 1110001 : 113 \text{ (truncate)} = 110001 = 49 \end{array}$$

2's complement: $110001 \rightarrow 001110 + 1 = 001111 = 15$

13) (a) Show work to find signed 2s complement $C - A$. (b) What is the decimal equivalent of the answer?

$c = 011010$, $a = 000111$

$-A \rightarrow 2\text{'s complement} = 111000 + 1 = 111001$

$C + A:$

$$\begin{array}{r} 011010 : 26 \\ + 111001 : 7 \\ \hline = 1010011 : \text{(truncate)} = 010011 = 19 \end{array}$$

2's complement $010011 = 101100 + 1 = 101101 = 45$

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- 14) (a) Show work to find signed 2s complement A - D. (b) What is the decimal equivalent of the answer?

$$a = 000111, d = 110101$$

$$-D \rightarrow 2\text{'s complement} = 001010 + 1 = 001011$$

A+D

$$000111 : 7$$

$$+001011 : 53$$

$$=010010 = 18 \rightarrow 2\text{'s complement} = 101101 + 1 = 101110 = 46$$

- 15) (a) Show work to find signed 2s complement E - C. (b) What is the decimal equivalent of the answer?

$$c=011010, e = 111101$$

$$-C \rightarrow 2\text{'s complement} = 100101 + 1 = 100110$$

E+C

$$111101 : 61$$

$$+100110 : 26$$

$$1100011 \text{ (truncate)} = 100011 \rightarrow 2\text{'s complement} = 011100 + 1 = 100011 = 35$$

- 16) (a) Show work to find signed 2s complement -B - C. (b) What is the decimal equivalent of the answer?

$$c=011010, b = 111100$$

$$-C \rightarrow 2\text{'s complement} = 100101 + 1 = 100110$$

$$-B \rightarrow 2\text{'s complement} = 000011 + 1 = 000100$$

B + C

$$000100 : 60$$

$$+100110 : 26$$

$$101010 \rightarrow 2\text{'s complement} = 010101 + 1 = 010110 = 22$$

- 17) (a) Show work to find signed 2s complement C - D. (b) What is the decimal equivalent of the answer?

$$c=011010, d = 110101$$

$$-D \rightarrow 2\text{'s complement} = 001010 + 1 = 001011$$

C + D

$$100110 : 26$$

$$+001011 : 53$$

$$110001 \rightarrow 2\text{'s complement} = 001110 + 1 = 001111 = 15$$

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- 18) (a) Show work to find unsigned $E * C$. For this, restrict the result to 6 bits. (b) What is the decimal equivalent of the answer?

$c=011010$, $e = 111101$

$$\begin{array}{r} 111101 \\ 1*011010 \\ \hline = \quad 111101 \\ \quad 111101 \\ \quad 111101 \\ \quad 1110010 \quad = 50 \end{array}$$

- 19) (a) Show work to find signed 2s complement $B * E$. For this, restrict the result to 6 bits. (b) What is the decimal equivalent of the answer?

$b = 111100$, $e = 111101$

$$\begin{array}{r} 111100 \\ 1*111101 \\ \hline = \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 1110100 \quad = 52 \end{array}$$

- 20) (a) Show work to find signed 2s complement $A * -B$. For this, restrict the result to 6 bits. (b) What is the decimal equivalent of the answer?

$b = 111100$, $a = 000111$

$-B \rightarrow 2\text{'s complement} = 000011 + 1 = 000100$

$$\begin{array}{r} 1000111 \\ 1*000100 \\ \hline = \quad 000111 \\ \quad 1000111 \quad = 7 \end{array}$$

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- 21) (a) Show work to find signed 2s complement $-E * A$. For this, restrict the result to 6 bits.
(b) What is the decimal equivalent of the answer?

$$e = 111101, a = 000111$$

$$-E \rightarrow 2\text{'s complement} = 111101 + 1 = 111110$$

$$\begin{array}{r} 111110 \\ 1*000111 \\ \hline = \quad 111110 \\ \quad 111110 \\ \quad 111110 \\ \quad 111010 = 58 \end{array}$$

- 22) (a) Show work to find signed 2s complement $B * -D$. For this, restrict the result to 6 bits.
(b) What is the decimal equivalent of the answer?

$$b = 111100, d = 110101$$

$$-D \rightarrow 2\text{'s complement} = 001010 + 1 = 001011$$

$$\begin{array}{r} 111100 \\ 1*110101 \\ \hline = \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 111100 \\ \quad 1101100 = 44 \end{array}$$