MATH1003 ASSIGNMENT 1

Suggested practice questions (the answers are in the back of the textbook):

1. Let
$$f(x) = \frac{x}{x+1}$$
. Find:

(i)
$$f(2+h)$$

(ii)
$$f(x+h)$$

(iii)
$$\frac{f(x+h)-f(x)}{h}$$
, where $h \neq 0$.

2. Find the domain of the function

$$f(x) = \frac{5x+4}{x^2+3x+2}.$$

3. Find the domain and sketch the graph of the following functions:

(i)
$$H(t) = \frac{4 - t^2}{2 - t}$$

(ii)
$$g(x) = \frac{|x|}{x^2}$$

(iii)
$$f(x) = \begin{cases} 2x + 3, & \text{when } x < -1; \\ 3 - x, & \text{when } x \ge -1. \end{cases}$$

4. Calculate the limit, if it exists, of the following:

(i)
$$\lim_{x\to 2} \frac{x^4 - 16}{x - 2}$$

(ii)
$$\lim_{x\to 5^-} \frac{6}{x-5}$$

(iii)
$$\lim_{x\to 0} \frac{x-1}{x^2(x+2)}$$
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