

Bipartite Matching/Network Flows Worksheet'

Large companies like Yahoo! and Google have enormous advertising potential due to the simple fact that million of users look at their websites everyday. By convincing people to provide some personal data or even by obtaining a user's location from their IP address, a company like Yahoo! or Google can show a user a targeted advertisement. For example, a Computer Science major from the Colorado School of Mines may see a banner ad for apartments in Golden while an investment banker in Connecticut may see a banner ad for Lincoln Town Cars instead.

Deciding which ads to show which people involves some behind-the-scenes computation. Suppose a popular website has identified k distinct demographic groups G_1, G_2, \dots, G_k . Note that these groups may overlap; for example G_i can be equal to all residents of Colorado, and G_j can be equal to all people with a computer science degree. Suppose the site has contracts with m different advertisers A_1, A_2, \dots, A_m to show exactly two copies of each ad to a subset of the n users U_1, \dots, U_n of the website. Advertiser A_i wants its ads shown only to users who belong to at least one of the demographic groups in the set $X_i \subseteq \{G_1, G_2, \dots, G_k\}$.

Describe how to use Bipartite Matching/Network Flows to design a good advertising policy - a way to show each of the m ads to 2 users of the site so that total of $2m$ ads are shown to $2m$ distinct users.

